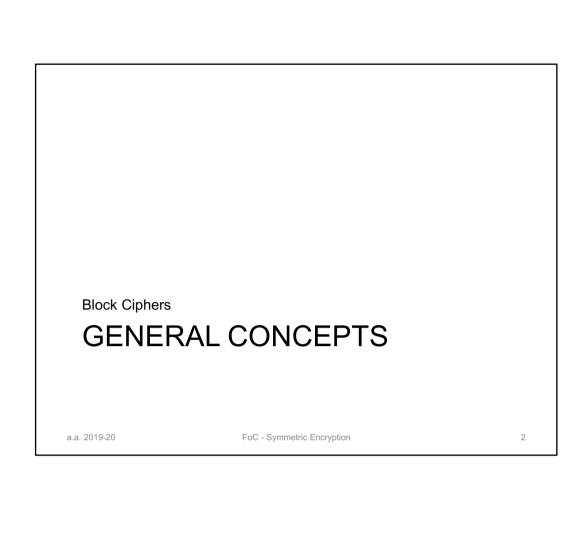
Block Ciphers

Gianluca Dini
Dept. of Ingegneria dell'Informazione
University of Pisa
gianluca.dini@unipi.it

Version: 2021-03-15



Possible Problem; @ cosa sicione se

pel Albumsose @ Au' BT 101 1

1 DETACH MALAKATATU DI SUE DI)

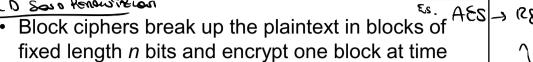
 $D_k: \{0,1\}^n \to \{0,1\}^n$

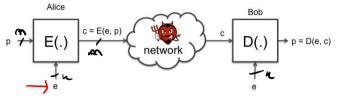
Block cipher

E e D Sous fenousières

CHAVI

a.a. 2019-20





- $E_k: \{0,1\}^n \to \{0,1\}^n$
- E is a keyed permutation: $E(k, m) = E_k(m)$
- $E_{\kappa}(\cdot)$ is a permutation

CRIPTO UN BLOCEO C BUT ALLY VOUSA _

CAUBY DI

ALCHOPTIGO +D 41400 vao

MON RO CONCER DURANTE UES

FoC - Symmetric Encryption

Permutation



- E_k is a permutation
 - E_K is efficiently computable → TEND POUNDUACE
 - Ek is bijective
 - Surjective (or onto)
 - Injective (or one-to-one)
 - E_k^{-1} is efficiently computable

a.a. 2019-20

FoC - Symmetric Encryption

Examples



NO POSSO CESSENE DENTATI

- · Block ciphers
 - DES n = 64 bits, k = 56 bits
 - -3DES n = 64 bits, k = 168 bits
 - AES n = 128 bits k = 128, 192, 256 bits
- Performance (AMD Opteron, 2.2 GHz)
 - RC4 126 MB/s
 - Salsa20/12 643 MB/s
 - Sosemanuk 727 MB/s
 - 3DES 13 MB/s
 - AES-128 109 MB/s → 874001

a.a. 2019-20

FoC - Symmetric Encryption

Random permutations



7150 (18518M OUTRT 11

TUTI 1 POSSIBLII WOUT

2" WAT 00 --- 00 00 --- 01 1 --- H TUTE CE ROSS Dec

ON JBU.

Penestation

 $N = 2^{n} - 1$

A random permutation π

• Let Perm_n be the set of all permutations π : $\{0,1\}^n \rightarrow \{0,1\}^n$

P_N • |Perm_n| = (2ⁿ!) = NILLED & RESIDEN PRILLED & MARIE OF M

A true random cipher

- implements all the permutations in Perm_n
- uniformly selects a permutation
 π ∈ Perm_n at random



a.a. 2019-20

FoC - Symmetric Encryption

Ю

True Random Cipher



- A True random cipher is perfect -> 5€ (2000 A DEFINITION OF DAKE)
- A true random cipher implements all possible Random permutations (2ⁿ!)

SERVEUNA CHIAVE Pin Beneviations

271

- Need a uniform random key for each permutation (naming) -> kiconscent una porcustazione DaniAutha
 - key size := log₂ (2n!) ≈ (n 1.44) 2n = NILLED & BUT CLET STUDIO F 6 (E CERMI)_ - Exponential in the block size!
 - The block size cannot be small in order to avoid a dictionary
- A true random cipher cannot be implemented

AL CHES LANG DEL BLOCKS LACHANG CLESSES ESPONENTALMENTE! NOS RESO VEALE CHIAN ALIAE.

a.a. 2019-20

, no Book 5176 h = 4548178

V = 4x24 = 4x6 - 64 Bits FATIBLE JERCOTE'NON USALS ME 4!

MA TOTACLETTE WELCOM

DICTIONARY ATTACK

DUENSION DEL DIRECHARDON RESENDRA:

COLE POSSO PREVENCE QUESTO TIPO (1) ATTAOOT

DEVO BENDONE U DIZIONALIO YOU CULLACIATIONA BLO W LEGEORIS

$$(N=32) = 32 \times 2^{82} = 2 \times 2^{82} \text{ bits}$$

$$(N=32) = 32 \times 2^{82} = 2 \times 2^{82} \text{ bits}$$

$$(N=32) = 32 \times 2^{82} = 2 \times 2^{82} \text{ bits}$$

BLOW DIFE , 64 BITS ACUSIO!

Known - PRINTERT ATTACK L'ATTACHNIE HA + DENSITUAL COME OI TESTO CUFRATO E MOS CUFATOL VAUDO POR UNA

descort 23

(= 8x(p)

CSTAN _

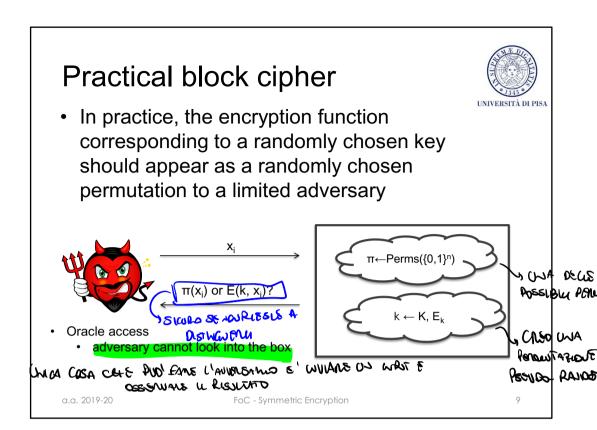
Pseudorandom permutations



- Consider a family of permutations parametrized by $k \in K = \{0, 1\}^k, E_k: \{0,1\}^n \to \{0,1\}^n$
- A E_κ is a pseudorandom permutation (PRP) if it is indistinguishable from a uniform random permutation by a limited adversary
- $|\{E_k\}| = 2^k \le |Perm_n|$, with |k| = k
- A block cipher is a practical instantiation of a PRP

a.a. 2019-20

FoC - Symmetric Encryption



Let's neglect how our block ciphers (DES, 3DES, AES,...) are implemented inside. Assume they are secure according to the above notion.

Exhaustive key search



- The attack
 - Given a pair (pt, ct), check whether ct == E_{ki} (pt), i = 0, 1, ..., $2^k 1$
 - Known-plaintext attack
 - Time complexity: O(2k)
- False positives
 - Do you expect that just one key k maps pt into ct?
 - How many keys (false positives) do we expect to map pt into ct?
 - How do you discriminate the good one?

a.a. 2019-20

FoC - Symmetric Encryption

Exhaustive key search



- False positives
 - Do you expect that just one key k maps pt into ct?
 - How many keys (false positives) do we expect to map pt into ct?

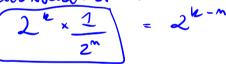
- How do you discriminate the good one?

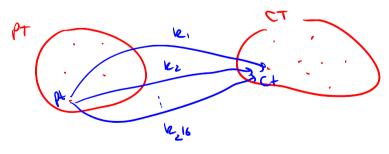
a.a. 2019-20

FoC - Symmetric Encryption

1

EXECTED NATION OF READ CHE CONDUMO OF IN C+)





(06S) W= 80 BIT

beeys cut collinate pt wet =

E, Entering and Color (be' C+)

PER FATE UN ATTACCO BRUTE-FORLE NO BISQUIO DI Z O PIÒ COPPLE (PI



- Problem: Given (ct, pt) s.t. ct = E_{k*}(pt) for a given k*, determine the number of keys that map pt into ct
- Solution.
 - Given a certain key k, $P(k) = Pr[E_{k*}(pt) == ct] = 1/2^n$
 - The *expected* number of keys that map pt into ct is $2^k \times 1/2^n = 2^{k-n}$

a.a. 2019-20

FoC - Symmetric Encryption



- Example 1 DES with n = 64 and k = 56
 - On average 2⁻⁸ keys map pt into ct
 - One pair (pt, ct) is sufficient for an exhaustive key search
- Example 2 Skipjack with n = 64 and k = 80
 - On average 2¹⁶ keys map pt into ct
 - Two or more plaintext-ciphertext pairs are necessary for an exhaustive key search

a.a. 2019-20

FoC - Symmetric Encryption



- Consider now t pairs (pt_i, ct_i), i = 1, 2,..., t
 - Given k*, $Pr[E_{k^*}(pt_i) = ct_i$, for all $i = 1, 2, ..., t] = 1/2^{tn}$
 - Expected number of keys that map pt_i into ct_i, for all i = 1, 2, ..., t, is 2^k/2^{tn} = 2^{k-tn}
- Example 3 Skypjack with k = 80, n = 64, t = 2
 - The expected number of keys is = $2^{80-2\times64} = 2^{-48}$
 - Two pairs are sufficient for an exhaustive key search

a.a. 2019-20

FoC - Symmetric Encryption



THEOREM

Given a block cipher with a key length of k bits and a block size of n bits, as well as t plaintext-ciphertext pairs, (pt₁, ct₁),..., (pt_t, ct_t), the expected number of false keys which encrypt all plaintexts to the corresponding ciphertexts is 2^{k-tn}

FACT

Two input-output pairs are generally enough for exhaustive key search

a.a. 2019-20

FoC - Symmetric Encryption

15

See exercise.

For example, let us consider DES, Skipjack and AES for t = 2

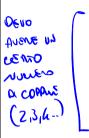
- **DES**: n = 64, k = 56, $2^{(56 128)} = 2^{(-72)}$
- Skipjack: n = 64, k = 80, $2^{(80 128)} = 2^{(-48)}$
- **AES**: n = 128, $k = 128 = 2^{(128 256)} = 2^{(-128)}$



Exercise 1 - Exhaustive key search



- Exhaustive key search is a known-plaintext attack
- However, the adversary can mount a cyphertextonly attack if (s)he has some knowledge on PT



```
(Pt. Ct) PLETILITIO COSE L'AMONSARIO CONSIE IL TESTOCIEMTO E

HA ACCINE NITORIAMONI SUL TESTO W

CENANO.

(Pt. Ct.)

(CASO PLOUTO COTUME
```

a.a. 2019-20

FoC - Symmetric Encryption

Exercise 1 – exhaustive key search



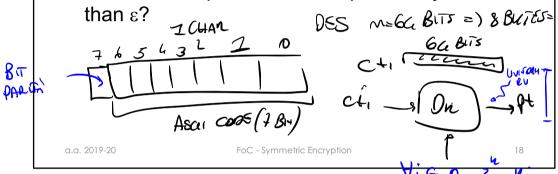
 Assume DES is used to encrypt 64-bit blocks of 8 ASCII chars, with one bit per char serving as parity bit

CO BOCE-DE WIAWON

8 CH

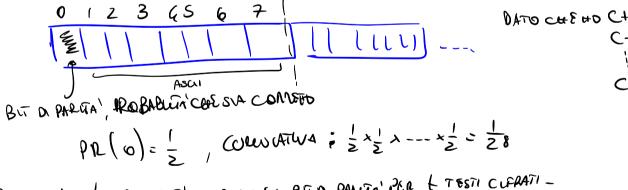
TUTICI

 How many CT blocks the adversary needs to remove false positives with a probability smaller



Let us consider a ciphertext block. Trial decryption of one ciphertext block with a given key k yields 8 correct parity bits with a probability $p(1) = 2^{-8}$. Actually, every bit is correct with a probability of 1/2. In the case of t blocks, the probability p(t) of 8t parity bits being correct is $p(t) = 2^{-8t}$. Thus, we can determine t by means of the following condition $2^{-8t} < \epsilon$. Consequently, the expected number of keys $r = 2^{k-8t}$.

In the DES case, $r = 2^{56-8t}$. For most practical purposes, t = 10 suffices to avoid false positives.



PROBABLIA' = 1 PROBABLIA' OI WOOWHANS IL BIT O PALIEN' IPER & TESTI CLERATI -

#KEUS =
$$2^{4} \times \frac{1}{28} = 2$$

Exercise 2 - dictionary attack



- Consider E with k and n.
- The adversary has collected D pairs (pt_i, ct_i), i = 1,..., D, with D << 2ⁿ
- Now the adversary reads C newly produced cyphertexts ct*_i, j = 1,..., C.
- Determine the value of C s.t. the Pr[Exists j, j = 1, 2,... C, s.t. c*_j is in the dictionary] = P

a.a. 2019-20

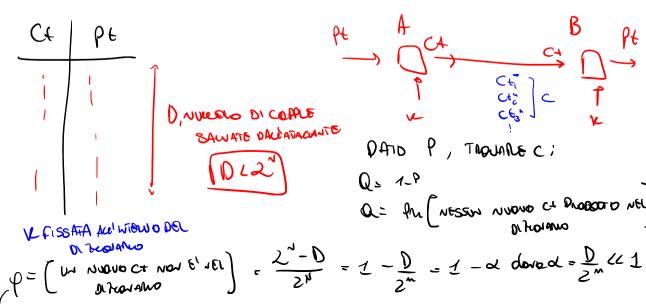
FoC - Symmetric Encryption

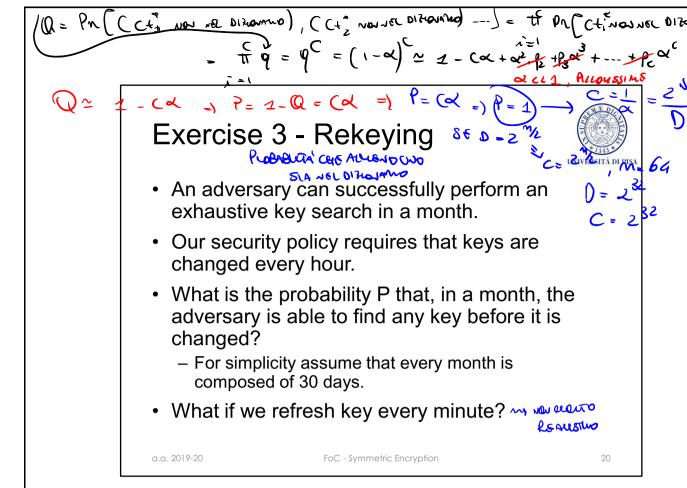
19

Let Q = 1 – P , where Q is the probability that none of the C newly produced ciphertexts are in the dictionary. Initially, we compute q = Pr[probability q that a ciphertext is *not* in the dictionary]. Probability q = (#favourable cases) / (#possible cases) = $(2^n - D) / 2n = 1 - \alpha$ with $\alpha = D / 2^n$. It follows that $\alpha << 1$. Then, we compute Q = Pr[none of the C ciphertexts is in the dictionary] = Pr[(ct*1 is not in the dictionary), (ct*2 is not in the dictionary, ...)] = Pr[(ct*1 is not in the dictionary)] × Pr[(ct*2 is not in the dictionary)] × ... = $q^C = (1 - \alpha)^C \approx 1 - C \times \alpha$. It follows that $P = C \times \alpha$.

If we specify P = 1, then C \times α = 1, which implies that C \times D/2ⁿ = 1 and thus C = 2ⁿ/D. If D = 2^{n/2} then C = 2^{n/2}. Let n = 64, then D = 232 entries, each of 2 \times 8 = 16 bytes. It follows that the dictionary size in bytes is $2^4 \times 2^{32}$ = 16 Gbytes.

Of course the challenge for the adversary is to collect D pairs. For this reason, it is wise to change the encryption key periodically.





Let us assume that a month is composed of 30 days and thus of H = 720 hours.

As a key is found in one month by means of a brute force attack, we can reasonably assume that $p = Pr[a \text{ given key is guessed in a given hour before it is changed}] = 1/H = 1.4 \times 10-3$.

Let q = Pr[no key is guessed in a given hour before it is changed] = 1 - p = 1 - 1/H.

Let P = Pr[probability that, in a month, the adversary guesses at least one key before it is changed]. Furthermore, let Q = 1 – P be the probability of the complementary event, i.e., Pr[the adversary cannot find any key before it is changed in a month] = Pr[(no key is guessed in hour 1), (no key is guessed in hour 2),...] = Pr[no key is found in hour 1] × Pr[no key is found in hour 2] × ... × Pr[no key is found in hour H] = $q^H = (1 - p)^H = (1 - 1/H)^H$. Consequently, P = 1 – Q = 1 – $(1 - 1/H)^H$. With H =720, Q ≈ 0.37 and P ≈ 0.63.

Assume we increase the refresh frequency (e.g., every minute). This means that the value of H increases and becomes H = 720 × 60. When H becomes very large, H $\rightarrow \infty$, then Q \rightarrow 1/e \approx 0.37, and thus P \rightarrow (1 - 1/e) \approx 0.63. This means that increasing the frequency with which the key is changed does not meaningfully improve the value of P.

The only practical advantage of frequently changing the key mainly reside in the fact that a

$$= \Re\left(\left(\text{ANDESANONOU WOOMA } e_1\right), \left(\text{ANVORSANONOU WOOMAKE}\right) - \left(1\right) = \frac{1}{M} \Re\left(\text{ANVORSANONOU WOOMAKE}\right)$$

$$= \frac{1}{M} q = Q = \left(1 - Q\right) + \left(1 - \frac{1}{M}\right) + \left(1 - \frac{1}{$$

MULTIPLE ENCRYPTION AND KEY WHITENING

a.a. 2019-20

FoC - Symmetric Encryption

DES challenge (1981)



- Find $e \in \{0,1\}^{56}$ s.t. $c_i = DES(e, p_i)$, i = 1, 2, 3
 - 1997: Internet search 3 months
 - 1998: EFF machine (Deep Crack) 3 days (250K\$)
 - 1999: combined search 22 hours
 - 2006: COPACABANA (120 FPGAs) 7 days (10K\$)
- 56-bit ciphers should not be used

a.a. 2019-20

FoC - Symmetric Encryption

22

The **DES Challenges** were a series of <u>brute force attack</u> contests created by <u>RSA Security</u> to highlight the lack of security provided by the <u>Data Encryption Standard</u>.

Three plaintexts were provided. RSA would pay 10.000 dollars to whom who was able to find the key and thus break the system.

The plaintext is provided in order to discard false positives.

COPACABANA (Cost-Optimized Parallel Code-Breaker) – University of Bochum and University of Kiel, Germany

Increasing the Security of Block Ciphers



- DES is a secure cipher
 - No efficient cryptanalys is known who Butteract
- · DES key has become too short
- Can we improve the security of DES יים משני אינון באינולעני
- Yes, by means of two techniques
 - Multiple encryption
 - Key whitening

a.a. 2019-20

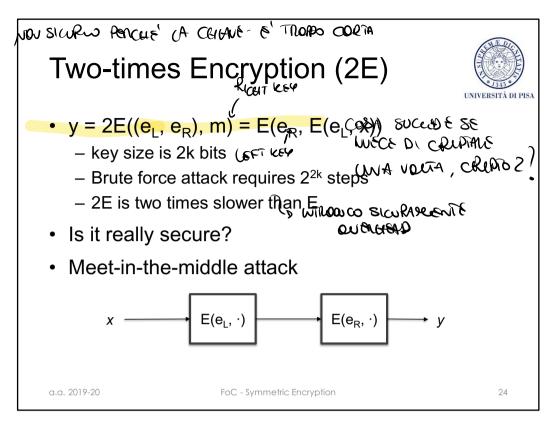
FoC - Symmetric Encryption

0e2

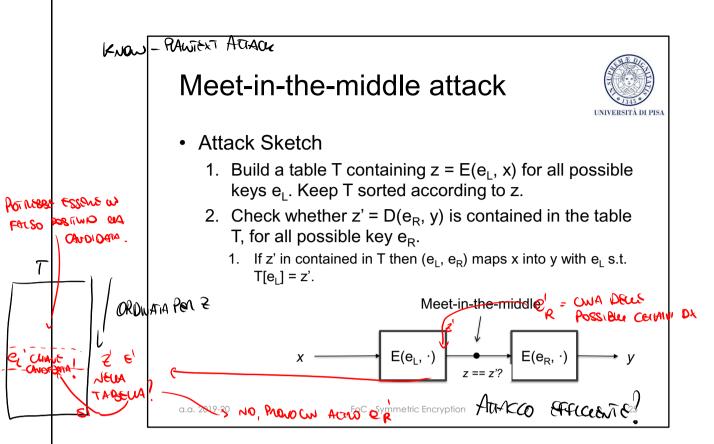
E, UNIDEANE CAE
NON OR ENENO
ELLI TORENIE
CAE

OR ORDERUIT

OR ORDERUI



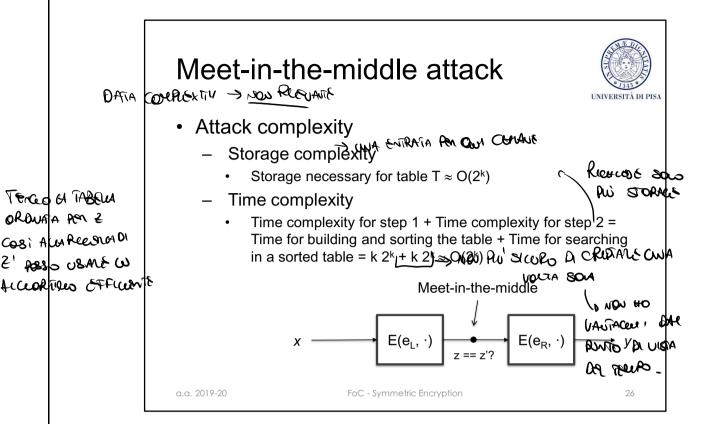
As to computing the number of false postives, you may consider L-subsequent encryptions as a cipher having a key large Lk-bits.



A naive brute-force attack would require us to search through all possible combinations of both keys, i.e., the effective key lengths would be 2^{2k} and an exhaustive key search would require $2^k \times 2^k = 2^{2k}$ encryptions (or decryptions). However, using the meet-in-the-middle attack, the key space is drastically reduced.

The Meet-in-the-middle Attack.

- 1. Build a table T containing z = E(eL, x) for all possible key left-keys eL and keep T sorted according to eL.
- 2. For all possible eR, check whether z' = D(eR, y) is contained in the table T. Assume that for a given eR*, exists eL* s.t. T[eL*] = z', the pair (eL*, eR*) maps p into c and thus it is a candidate key.
- 3. In order to get rid of false positives you may need two or more pairs (x, y).



Attack complexity

Data complexity (negligible): a few pairs.

Storage complexity := he storage necessary for T: O(2⁵⁶). Remarkable!

Time complexity := Time complexity for step 1 + Time complexity for step 2 = (Time for building the table + Time to sort) + (Time to perform all the searches in a sorted table) = $(56 \times 2^{56}) + (56 \times 2^{56}) = O(2^{56})$

Two-times DES



• 2DES

u CHAUF DES

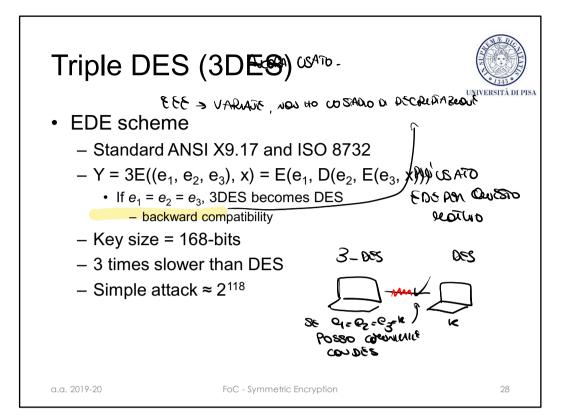
- Time complexity: 2⁵⁶ (doable nowadays!)
- Space complexity: 2⁵⁶ (lot of space!)
- 2DES brings no advantage

a.a. 2019-20

FoC - Symmetric Encryption

27

As to computing the number of false positives, you may consider L-subsequent encryptions as a cipher having a key large Lk-bits.

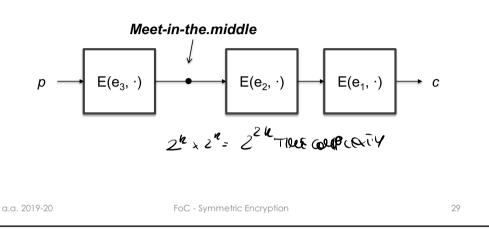


Nowadays anything that is larger than 290 is considered secure.

3DES – meet-in-the-middle attack



- Time = 2¹¹² (undoable!)
- Space = 2⁵⁶ (lot of space!)



The value for time complexity neglects the time for keeping the table sorted in the first phase and for searching in the table in the second phase.

False positives for multiple encryption



- THEOREM
 - Given there are r subsequent encyptions with a block cipher with a key lenght of k bits and a block size of n bits, as well as t plaintext-ciphertext pairs, (pt₁, ct₂),..., (pt_t, ct_t), the expected number of false keys which encrypt all plaintext to the corresponsig ciphertext is 2^{rk tn}

a.a. 2019-20

FoC - Symmetric Encryption

Limitations of 3DES



- 3DES resists brute force but 80 three ms
 - It is not efficient regarding software implementation
 - It has a short block size (64 bit)
 - A drawback if you want to make a hash function from 3DES, for example
 - Key lengths of 256+ are necessary to resist quantum computing attack

Busho Pen CRUTALL PREND PEN DEPLEMENTAL HASH FUNCTIONS.

a.a. 2019-20

FoC - Symmetric Encryption

Key whitening



- KW is not a "cure" for weak ciphers
- Applications
 - DESX: a variant of DES
 - AES: uses KW internally
- Performance
 - Negliglible overhead w.r.t. E (Just two XOR's!)

a.a. 2019-20

FoC - Symmetric Encryption

32

To some extent, Multiple Encryption makes the resulting cipher more resistant to linear and differential cryptoanalysis. In contrast, Key Whitening does not. So KW is not a "cure" for weak ciphers.

DEVE COEMONE
ESSONE SLUND
(= (

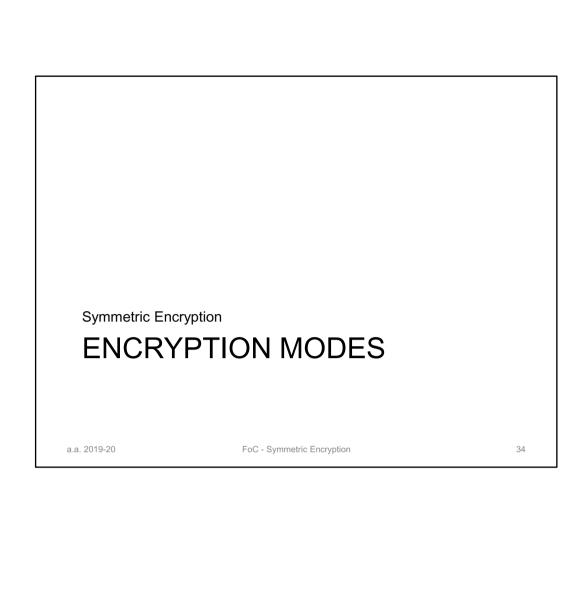
Key whitening



- Attacks
 - Brute-force attack
 - Time complexity: 2k+2n encryption ops
 - Meet-in-the-middle:
 - Time complexity 2k+n
 - Storage complexity: 2n data sets
 - The most efficient attack
 - If the adversary can collect 2^m pt-ct pairs, then time complexity becomes $2^{R^{\frac{1}{12}m}}$
 - The adversary cannot control m (rekeying)
 - Example: DES (m = 32)
 - Time complexity 288 encryptions (nowadays, out of reach)
 - Storage complexity 2³² pairs = 64 GBytes of data (!!!)

a.a. 2019-20

FoC - Symmetric Encryption



Other encryption modes



- Other encryption modes
 - To build a stream cipher out of a block cipher
 - Cipher Feedback mode (CFB)
 - Output Feedback mode (OFB)
 - Counter mode (CTR)
 - Authenticated encryption
 - Galois Counter mode (GCM, CCM, ...)
 - and many others (e.g., CTS, ...)
- · Block ciphers are very versatile components

a.a. 2019-20

FoC - Symmetric Encryption

Encryption Modes



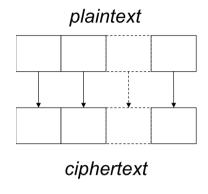
- A block cipher encrypts PT in fixed-size *n*-bit blocks
- When the PT len exceeds n bits, there are several modes to the block cipher
 - Electronic Codebook (ECB)
 - Cipher-block Chaining (CBC)
 - Cipher-feedback (CFB)
 - Output feedback (OFB)

a.a. 2019-20

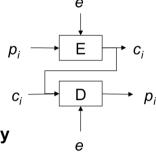
FoC - Symmetric Encryption

Electronic codebook





$$\forall 1 \le i \le t, c_i \leftarrow E(e, p_i)$$
$$\forall 1 \le i \le t, p_i \leftarrow D(e, c_i)$$



PT blocks are encrypted separately

a.a. 2019-20

FoC - Symmetric Encryption

ECB - properties



PROS

- No block synchronization is required
- No error propagation
 - One or more bits in a single CT block affects decipherment of that block only
- Can be parallelized

· CONS

- Identical PT results in identical CT
 - · ECB doesn't hide data pattern
 - · ECB allows traffic analysis
- Blocks are encrypted separately
 - · ECB allows block re-ordering and substitution

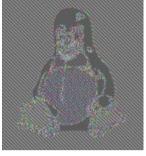
a.a. 2019-20

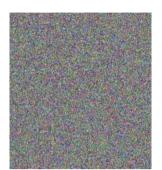
FoC - Symmetric Encryption

ECB doesn't hide data patterns









Plaintext

ECB encrypted

Non-ECB encrypted

a.a. 2019-20

FoC - Symmetric Encryption

39

ECB mode is used to encrypt a bitmap image with large areas of uniform colour. While the colour of each individual pixel is encrypted, the overall image may still be discerned as the pattern of identically coloured pixels in the original remains in the encrypted version.

ECB - block attack



- Bank transaction that transfers a client U's amount of money D from bank B1 to bank B2
 - Bank B1 debits D to U
 - Bank B1 sends the "credit D to U" message to bank B2
 - Upon receiving the message, Bank B2 credits D to U
- · Credit message format
 - Src bank: M (12 byte)Rcv banck: R (12 byte)
 - Client: C (48 byte)
 - Bank account: N (16 byte)Amount of money: D (8 byte)
- Cipher: n = 64 bit; ECB mode

a.a. 2019-20

FoC - Symmetric Encryption

ECB – block attack



- Mr. Lou Cipher is a client of the banks and wants to make a fraud
- Attack aim
 - To replay Bank B1's message "credit 100\$ to Lou Cipher" many times
- Attack strategy
 - Lou Cipher activates multiple transfers of 100\$ so that multiple messages "credit 100\$ to Lou Cipher" are sent from B1 to B2
 - The adversary identifies at least one of these messages
 - The adversary replies the message several times

a.a. 2019-20

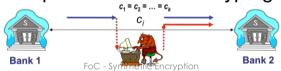
FoC - Symmetric Encryption

ECB - block attack



42

- Mr. Lou Cipher performs k equal transfers
 - credit 100\$ to Lou Cipher \rightarrow c1
 - credit 100\$ to Lou Cipher → c2
 - **–** ...
 - credit 100\$ to Lou Cipher → ck
- Then, he searches "his own" CT in the network
 - k equal CTs!
- Finally he replies one of these cryptograms



a.a. 2019-20

The number *k* is large enough to allow the adversary to identify the cryptograms corresponding to its transfers with high probability.

ECB - block attack



 An 8-byte timestamp field T (block #1) is added to the message to prevent replay attacks



- However, Mr Lou Cipher can
 - Identify "his own" CT by inspecting blocks #2-#13
 - Intercept any "fresh" CT
 - Substitute block #1 of "his own" CT with block #1 of the intercepted "fresh" block
 - Replay the resulting CT

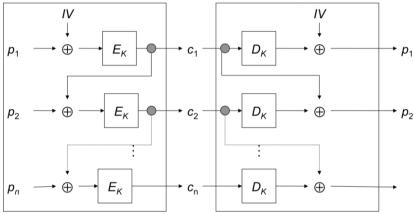
a.a. 2019-20

FoC - Symmetric Encryption

Cipher block chaining (CBC)



$$c_{0} \leftarrow IV.\forall 1 \leq i \leq t, c_{i} \leftarrow E_{k} (p_{i} \oplus c_{i-1})$$
$$c_{0} \leftarrow IV.\forall 1 \leq i \leq t, p_{i} \leftarrow c_{i-1} \oplus D_{k} (c_{i})$$



a.a. 2019-20

FoC - Symmetric Encryption

CBC - properties



- Chaining dependencies: c_i depends on p_i and all preceding PT blocks
- Encryption is randomized by using IV
 - CBC is non deterministic
 - Identical ciphertext results from the same PT under the same key and IV
 - IV is a nonce
- · CT-block reordering affects decryption
- IV can be sent in the clear but its integrity must be guaranteed
- CBC suffers from Error propagation
 - Bit errors in c_i affect decryption of c_i and c_{i+1} (error propagation)
 - CBC is self-synchronizing (error recovery)
 - CBC does not tolerate "lost" bits (framing errors)

a.a. 2019-20

FoC - Symmetric Encryption

CBC - block attack



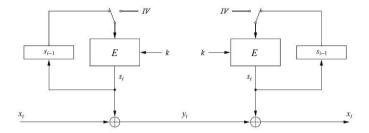
- If Bank A chooses a random IV for each wire transfer the attack will not work because LC
- However if LC substitutes blocks 5 10 and 13, bank B would decrypt account number and deposit amount to random numbers => this is highly undesirable
- Encryption itself is not sufficient, we need to protect integrity
 - We need additional mechanisms: MDC, MAC, dig sig

a.a. 2019-20

FoC - Symmetric Encryption

Output Feedback Mode (OFB)





Let e() be a block cipher of block size b; let x_i , y_i and s_i be bit strings of length b; and IV be a nonce of length b.

Encryption (first block): $s_1 = e_k(IV)$ and $y_1 = s_1 \oplus x_1$

Encryption (general block): $s_i = e_k(s_{i-1})$ and $y_i = s_i \oplus x_i$, $i \ge 2$

Decryption (first block): $s_1 = e_k(IV)$ and $x_1 = s_1 \oplus y_1$

Decryption (general block): $s_i = e_k(s_{i-1})$ and $x_i = s_i \oplus y_i$, $i \ge 2$

a.a. 2019-20

FoC - Symmetric Encryption

Output Feedback Mode (OFB)



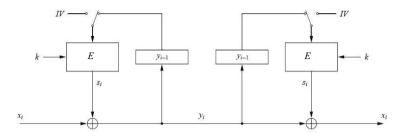
- OFB builds a stream cipher out of a block cipher
- The key stream is generated block-wise
- OFB is a synchronous stream cipher
- The receiver does not use decryption (E⁻¹)
- IV should be a nonce and make OFB nondeterministic
- Since OFB is synchronous, pre-computation of key stream blocks is possible

a.a. 2019-20

FoC - Symmetric Encryption

Cipher Feedback Mode (CFB)





Definition 5.1.4 Cipher feedback mode (CFB)

Let e() be a block cipher of block size b; let x_i and y_i be bit strings of length b; and IV be a nonce of length b.

Encryption (first block): $y_1 = e_k(IV) \oplus x_1$

Encryption (general block): $y_i = e_k(y_{i-1}) \oplus x_i, i \ge 2$

Decryption (first block): $x_1 = e_k(IV) \oplus y_1$

Decryption (general block): $x_i = e_k(y_{i-1}) \oplus y_i, i \ge 2$

a.a. 2019-20 FoC - Symmetric Encryption

Cipher Feedback Mode (CFB)



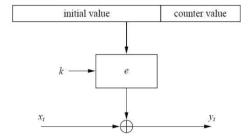
- OFB builds a stream cipher out of a block cipher
- CFB is an asynchronous stream cipher as the key stream is also a function of the CT
- · Key stream is generated block-wise
- IV is a nonce and makes CFB nondeterministic

a.a. 2019-20

FoC - Symmetric Encryption

Counter Mode (CTR)





Definition 5.1.5 Counter mode (CTR)

Let e() be a block cipher of block size b, and let x_i and y_i be bit strings of length b. The concatenation of the initialization value IV and the counter CTR_i is denoted by $(IV||CTR_i)$ and is a bit string of length b.

Encryption: $y_i = e_k(IV||CTR_i) \oplus x_i$, $i \ge 1$ **Decryption**: $x_i = e_k(IV||CTR_i) \oplus y_i$, $i \ge 1$

a.a. 2019-20

FoC - Symmetric Encryption

Counter Mode (CTR)



- CTR prevents 2TP
- · CTR can be parallelized
- IV || CTR_i does not have to be kept secret
 - It can be transmitted together with CT_i
- Counter can be a regular counter or a more complex functions, e.g., LFSR

a.a. 2019-20

FoC - Symmetric Encryption

52

2TP

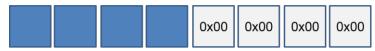
If we use the same input twice, then CT1 = PT1 xor S and CT2 = PT2 xor S. In case of KPA against one pt, e.g., against (CT1, PT1), then the adversary can determine S and then decrypt also the other pt.

Consider e = AES (b = 128 bit). Then, we can choose |IV| = 96 bit and |counter| = 32. Therefore, we can encrypt 2^{32} different pt's, each one being 128 bit (16 byte) long. Therefore, we can encrypt 2^{32} x 2^4 bytes = 64 Gbytes in total.

The need for a padding scheme



Naïve (wrong) solution: Pad the message with zeroes to the right, without ambiguous boundaries



Problem: What if the message was a NULL-terminated string?



At the receiving side: Was it a NULL-terminated string or a 7-bytes pt?

a.a. 2019-20

FoC - Symmetric Encryption

The PKCS#7 padding scheme



Padding is necessary when PT len is not a block multiple

If PT len is NOT a block multiple
Padding bytes ← #bytes to complete a
block

HELLO333

If PT is a block multiple
Padding = block
Each padding byte ← 8



Padding give rise to ciphertext expansion

a.a. 2019-20

FoC - Symmetric Encryption

54

Exercise:

Let us suppose that you decrypt a CT and get the last block as [..., 13, 06, 05].

Is this possible? Can CT be a valid ciphertext?

The answer is NO.

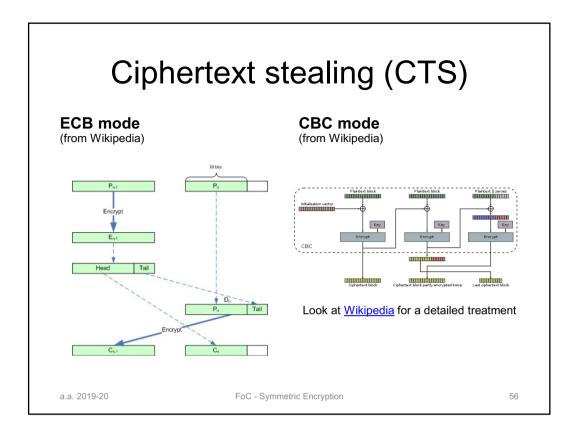
Ciphertext Stealing (CTS)



- CTS allows encrypting PT that is not evenly divisible into blocks without resulting in any ciphertext expansion
- sizeof(CT) = sizeof(PT)
- · CTS operates on the last two blocks
 - A portion of the 2nd-last CT block is stolen to pad the last PT block

a.a. 2019-20

FoC - Symmetric Encryption



To implement CTS encryption or decryption for data of unknown length, the implementation must delay processing (and buffer) the two most recent blocks of data, so that they can be properly processed at the end of the data stream.

