# Communication systems

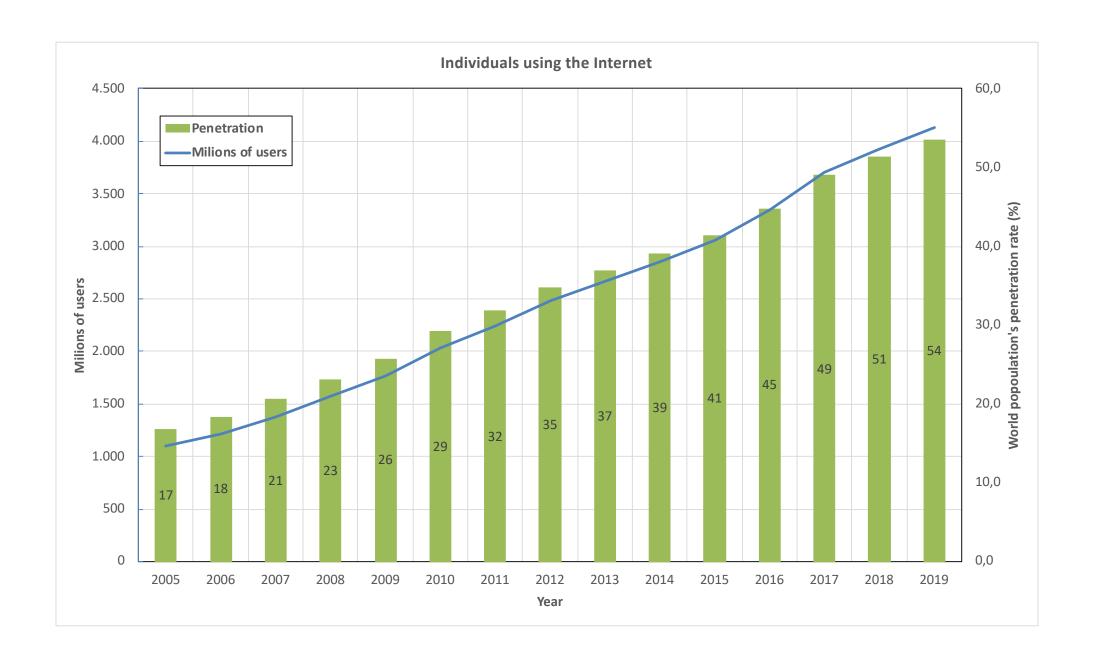
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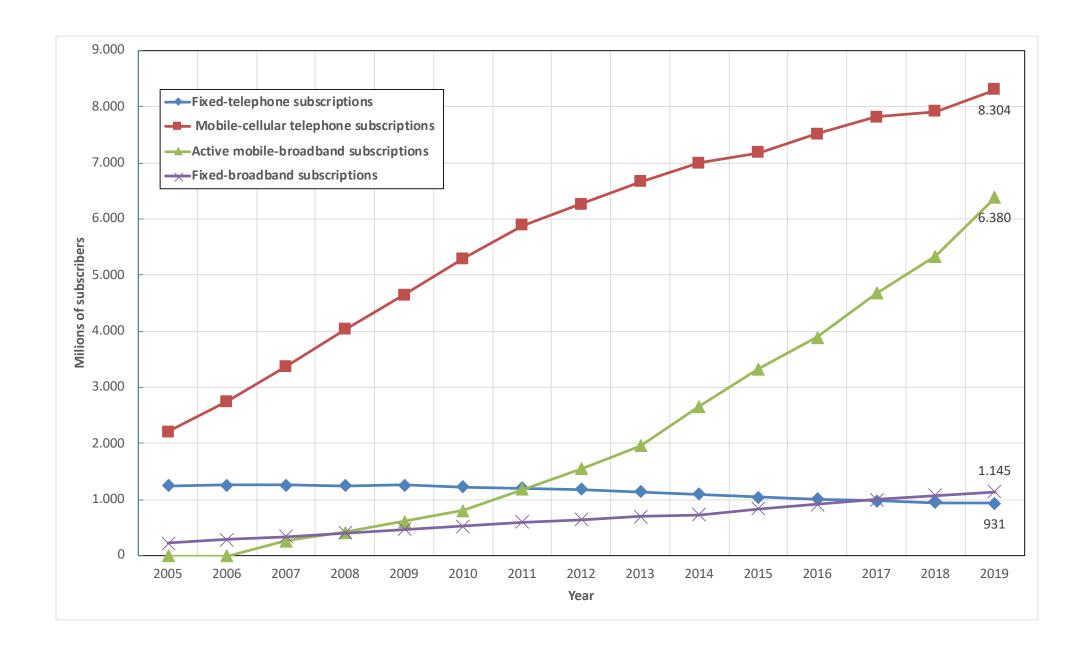
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**ELECTRONICS AND COMMUNICATIONS SYSTEMS** 

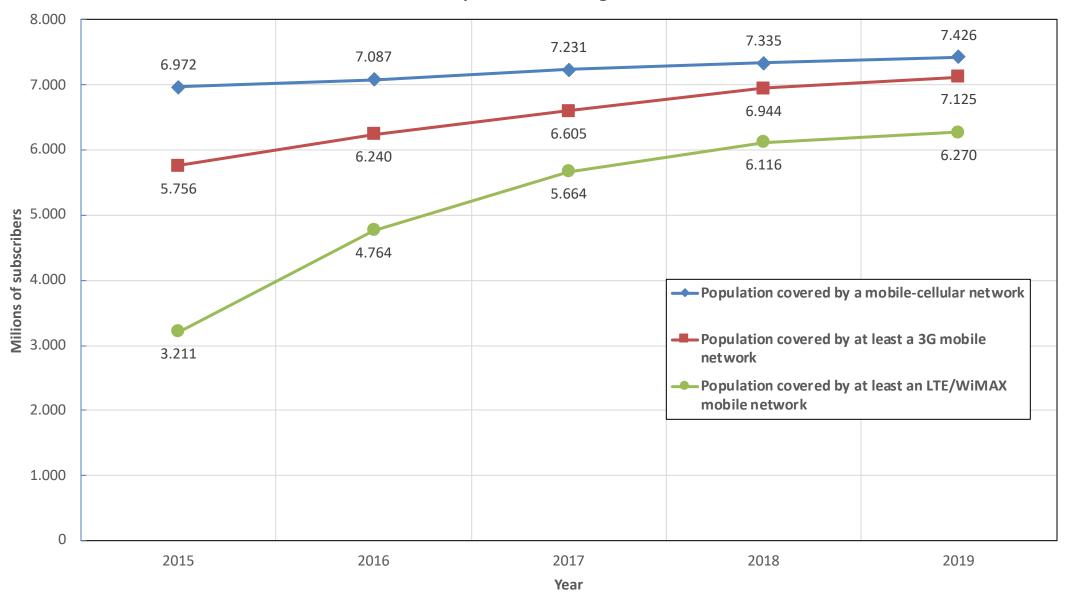
**COMPUTER ENGINEERING** 

- Some data from the International Telecommunication Union (ITU).....
- The number of people with access to mobile communications is higher than those with access to working toilets (around 4.5 billions).
- The number of people that owns a mobile phone is larger than the number of people that owns/uses a toothbrush (around 4 billion).





#### Population's coverage



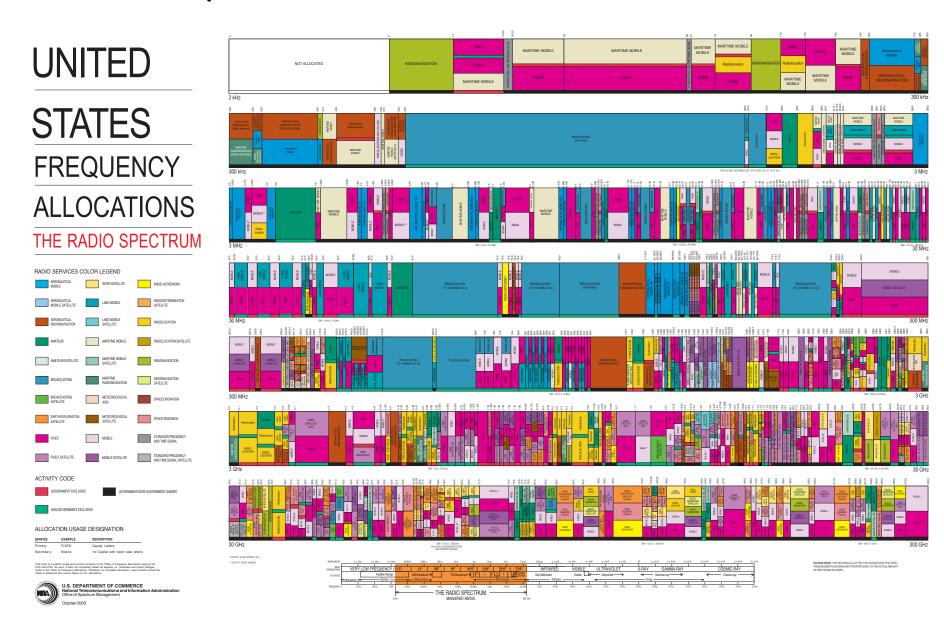
### Syllabus

- 1. Radio transmissions
- 2. The wireless propagation channel
- 3. Multi-user communications
- 4. Cellular systems
- 5. Mobile communications standards

#### 1. Radio transmissions

- Introduction to analog and digital wireless systems
- Analog systems: FM radio
- Software defined radio principles
- SDR exercitation: FM receiver implementation with SDR and Matlab
- Digital systems: PAM modulation

#### The radio spectrum



# **Analog Communications**



# 8(+)=m(+)~ cos(2ti fet) = 8(f)= H(f) E(=f(f-fc)+=f(f+fe))

# Analog communications: amplitude modulation dual side band (AM-DSB)

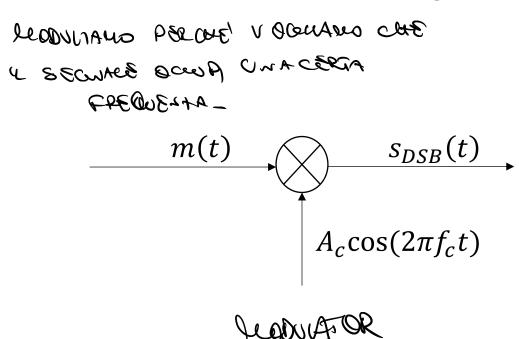
• The AM-DSB modulation is probably the simplest modulation

possible

$$S_{DSB}(t) = A_{c}m(t)\cos{(2\pi f_{c}t)}$$

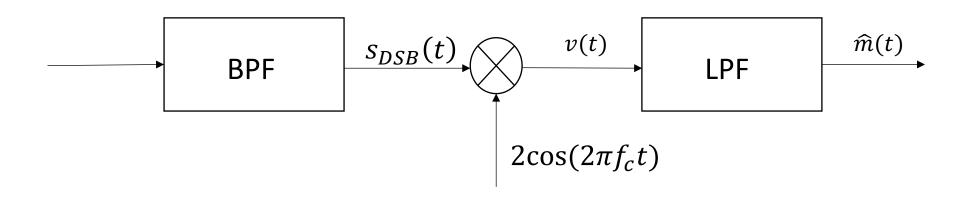
 $Cos(2\pi f_c t) \stackrel{f}{\rightleftharpoons} S(f - f_c)$ BASEBAND SIGNAC  $\frac{1}{2}A_cM(0)$ 

LOSUTOSAT COTALCOAL



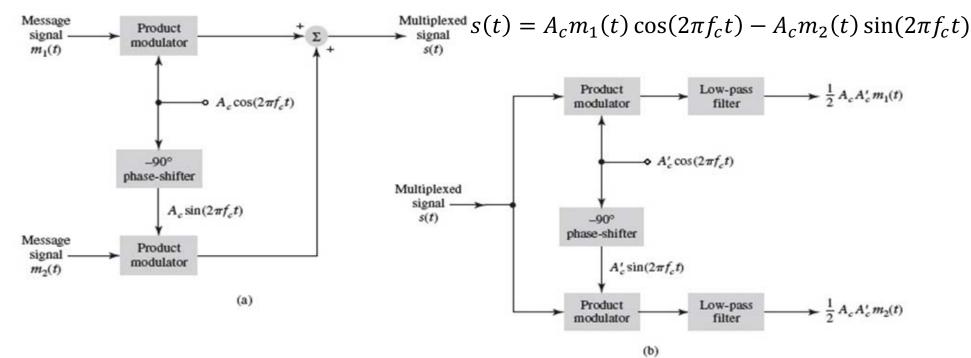
#### DSB coherent detection

• Neglecting for the moment the effect of the noise and of the propagation channel, recovery of m(t) from  $s_{DSB}(t)$  is possible with coherent detection.



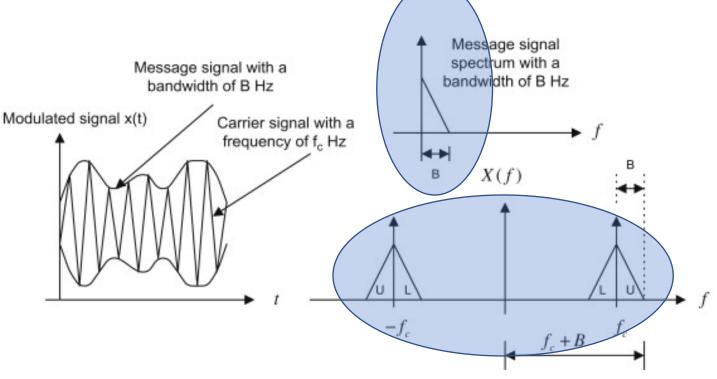
#### Analog Quadrature Amplitude Modulation

• To double the amount of information transmitted on a given bandwidth, it is possible to multiplex two DSB signal on the same channel exploiting the orthogonality of  $\sin(2\pi f_c t)$  and  $\cos(2\pi f_c t)$ 



Passband signals

- The vast majority of communication systems are passband systems.
- The transmitted signal s(t) has its energy concentrated in a bandwidth 2B centered around some nominal carrier frequency  $f_c$  and above and relatively far away from dc.
- For a passband signal it is  $f_c \gg 2B$



Passband signal spectrum

Baseband signal spectrum

### Complex envelope of a passband signal

- The passband modulator-demodulator can be drawn in a more compact form by using complex notation.
- Any passband signal s(t) can be represented as

$$s(t) = \operatorname{Re}\left\{\tilde{s}(t)e^{j2\pi f_{c}t}\right\} = s_{I}(t)\cos(2\pi f_{c}t) - s_{Q}(t)\sin(2\pi f_{c}t)$$

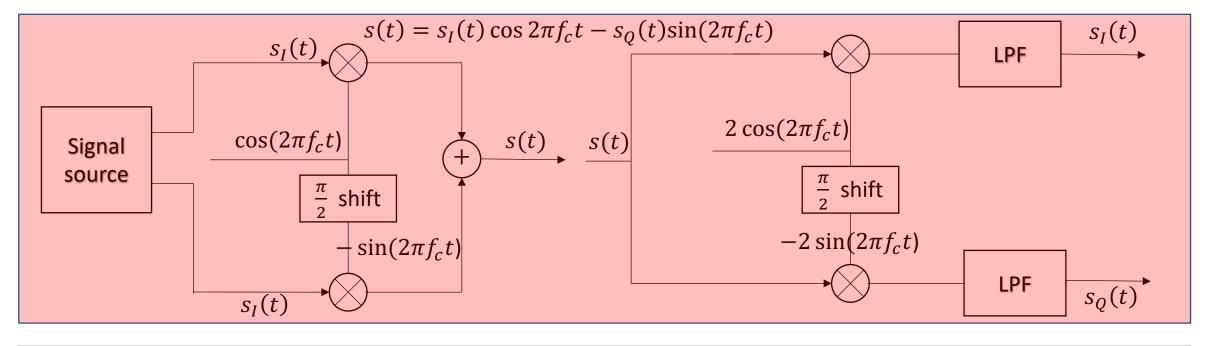
where  $\tilde{s}(t) = s_I(t) + js_Q(t)$  is the *complex envelope* of the signal with  $s_I(t)$  and  $s_Q(t)$  the in-phase and quadrature components.

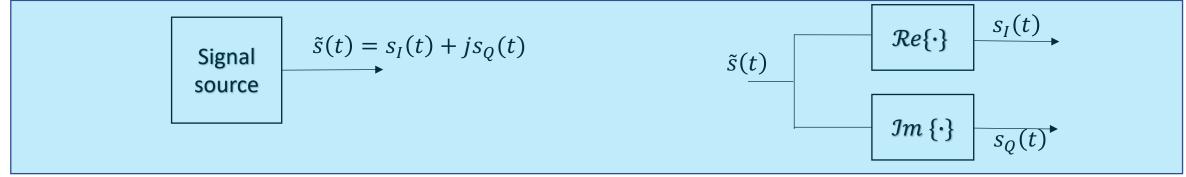
- Complex envelope for known modulated signals
  - $\tilde{s}_{DSB}(t) = A_c m(t); s_I(t) = A_c m(t), s_Q(t) = 0.$
  - $\tilde{s}_{QAM}(t) = A_c m_1(t) + j A_c m_2(t)$ ;  $s_I(t) = A_c m_1(t)$ ,  $s_Q(t) = A_c m_2(t)$ .

#### Complex envelope of a passband signal

- The complex envelope is an equivalent baseband representation of a passband signal.
- Employing the baseband equivalent has several benefits:
  - A baseband model is simpler to study, since it removes the effects of the carrier frequency from the signal model.
  - A baseband model can be numerically simulated with much lower computation than a passband model because the bandwidth and, as a consequence, the sampling rate is much lower.
  - A baseband model is often the basis for a digital implementation of a bandpass communications system.

#### Bandpass vs. equivalent baseband model

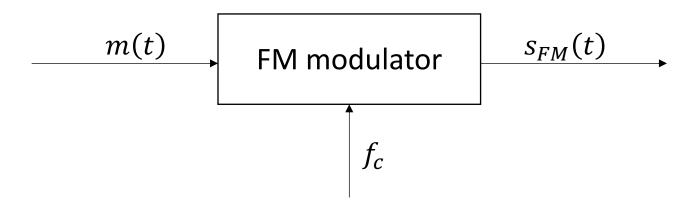




# Analog communications: frequency modulation (FM)

 In the FM modulation, the message is embedded in the signal phase

$$s_{FM}(t) = A_c \cos \left(2\pi f_c t + 2\pi k_f \int_{-\infty}^t m(\tau) d\tau\right)$$



#### FM radio

#### Advantages:

- Constant envelope modulation: greatly simplifies amplifier design
- By properly adjusting FM parameters, it is possible to trade spectral efficiency with energy efficiency
- Commercial FM transmits an audio signal with bandwidth  $B=15\,\mathrm{kHz}$  over a bandwidth of approx 200 kHz.

#### FM radio

• The complex envelope of a FM signal is Phase  $\phi(t)$  of the complex envelope

$$\tilde{S}_{FM}(t) = A_c e^{j2\pi k_f \int_{-\infty}^{t} m(\tau) d\tau}$$

Frequency deviation of an FM signal

$$f_d(t) = \frac{1}{2\pi} \frac{d}{dt} \phi(t)$$

- Maximum frequency deviation  $\Delta f = \max\{|f_d(t)|\} = k_f \max\{|m(t)|\}$
- Modulation index  $m_f = \frac{\Delta f}{B_m}$

# FM signal with a modulating sinusoid

• Let m(t) be a sinusoid

$$m(t) = V_m \cos(2\pi f_m t)$$

The FM signal is

Fivi signal is
$$s_{FM}(t) = A_c \cos \left( 2\pi f_c t + 2\pi k_f \int_{-\infty}^{t} V_m \cos(2\pi f_m \tau) d\tau \right)$$

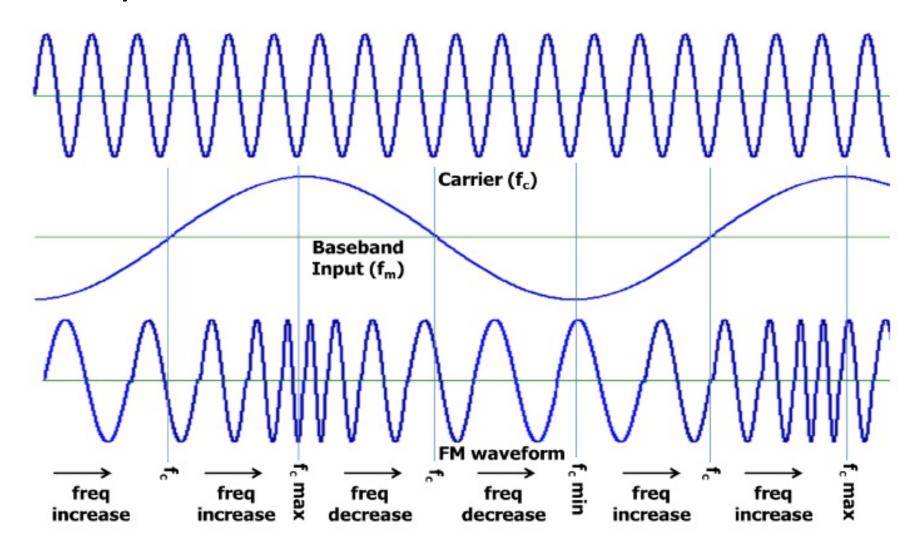
$$= A_c \cos \left( 2\pi f_c t + 2\pi k_f V_m \frac{\sin(2\pi f_m t)}{2\pi f_m} \right)$$

$$= A_c \cos \left( 2\pi f_c t + m_f \sin(2\pi f_m t) \right)$$
The polarization in the signal is a signal in the properties. The properties is a signal in the properties of the properties in the properties of the propert

Complex envelope is

$$\tilde{S}_{FM}(t) = A_c e^{jm_f \sin(2\pi f_m t)}$$

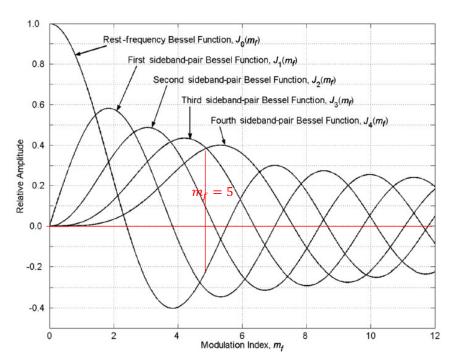
# Frequency modulation

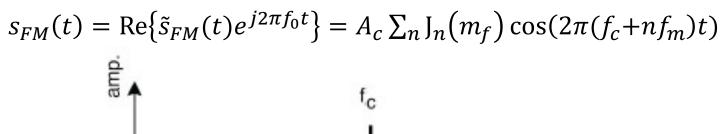


#### FM signal spectrum

• Expoliting the periodicity of  $\tilde{s}_{FM}(t) = A_c e^{jm_f \sin(2\pi f_m t)}$ , the complex envelope can be written as a sum of Fourier coefficients

$$\tilde{S}_{FM}(t) = A_c \sum_n (n(m_f)) e^{j2\pi n f_m t}$$
 Bessel function of the first type of order  $n$ 





#### FM signal spectrum

- It is is impossible to calculate a closed form expression for FM spectrum
- A good approximation is the Carson bandwidth rule

$$B_{FM} \approx 2(m_f + 1)B = 2(\Delta f + B)$$

- Any frequency modulated signal has an *infinite* number of sidebands and hence an infinite bandwidth but most of the energy (98% or more) is concentrated within the bandwidth defined by Carson's rule.
- In commercial mono FM we have  $B_{FM} \approx 180 \; \mathrm{kHz}$ 
  - B = 15 kHz (high quality audio)
  - $\Delta f = 75 \text{ kHz}$
  - $m_f = 5$

#### FM receiver

 Neglecting the effect of noise and channel, the complex envelope of the received signal is

$$\tilde{v}(t) = A_c e^{j2\pi k_f \int_{-\infty}^{t} m(\tau)d\tau}$$

• The modulating signal can be recovered by differentiating the phase of v(t)

$$\widehat{m}(t) = \frac{1}{2\pi k_f} \frac{d}{dt} \angle \widetilde{v}(t)$$

Conceptual FM baseband receiver

