

# Synchronization of Physical Clocks

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## Outline

Getting  
Computer Clocks  
Synchronized

- Generalities
- Cristian's algorithm
- Berkeley algorithm
- Network Time Protocol

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# Generalities



## Time References



Every node has an internal clock, whose value has to be kept as close as possible to a reference time.

- **UTC** - coordinated universal time, primary reference for the scientific community, and based on International Atomic Time
- **UT1** - successor of GMT, “solar-based” reference time
- **Unix (POSIX) time** - nr. of seconds elapsed since 00:00:00 (UTC), Thursday, 1 January 1970, minus in-between *leap seconds*

# Leap Seconds?

Earth's rotation slowdown  
and irregularities make  
UT1 deviate from UTC.

Thus, corrections are needed.

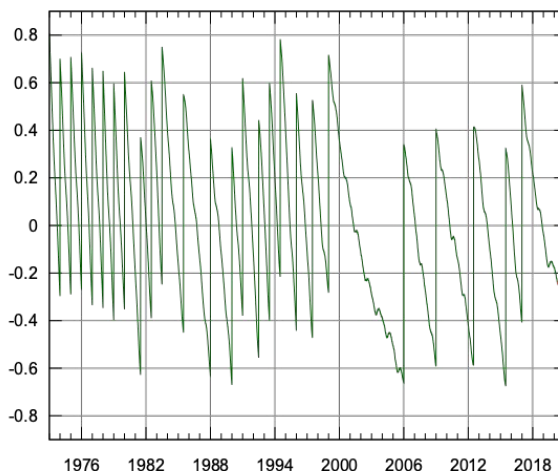


Chart aside: UT1-UTC vs UTC

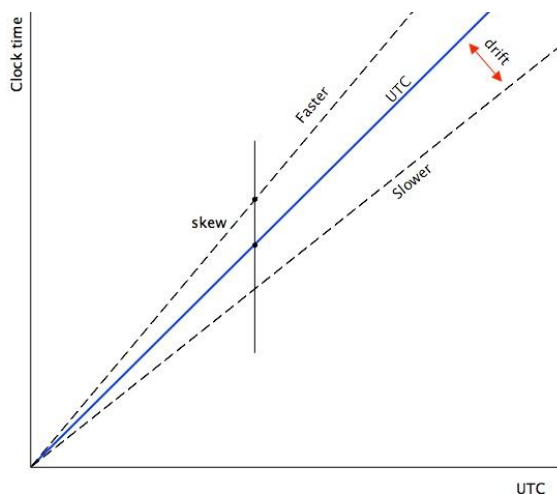
From Wikipedia

## Non-Aligned Clocks

**Skew** - difference in instantaneous  
reads of two clocks

**Drift** - difference in the rate  
of clocks.

Keeping two clocks synchronized  
means imposing an upper bound  $D$   
on any of their instantaneous reads.

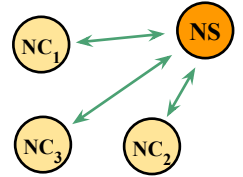




# External vs Internal Synchronization

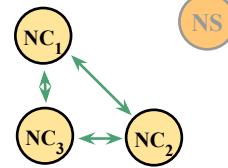
**External:** w.r.t. a trusted source of reference time  $S(t)$ , i.e.

$$|S(t) - C_i(t)| < D \quad \forall i$$



**Internal:** agreement within a group of nodes, i.e.

$$|C_i(t) - C_j(t)| < D \quad \forall i, j$$



If a system is externally synchronized with an accuracy  $D$ , then its internal clocks agree within a bound of  $2D$

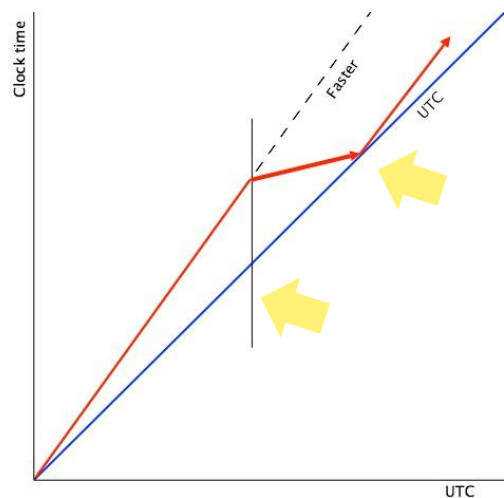
## Resetting a Clock



**Important:** clock *monotonicity* must be assured!

No way to set back a clock: instead, its pace should be slowed down up to the point the correct value is reached.

Typical example: the “make” compilation utility.



# Cristian's Algorithm

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## Idea: Exploit Round Trip Time

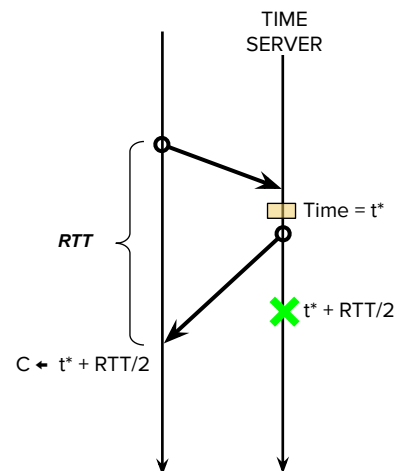
RTT can be measured by the client.

If  $RTT \ll 1$ , assuming req/reply latencies to be the same does not yield an excessive error, thus:

$$C \approx t^* + RTT/2$$



In practice, several tries can be done, so to possibly get lower RTTs.



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# Internal Synchronization: The Berkeley Algorithm, and Beyond

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## A Centralized Solution

Developed for groups of UNIX computers.

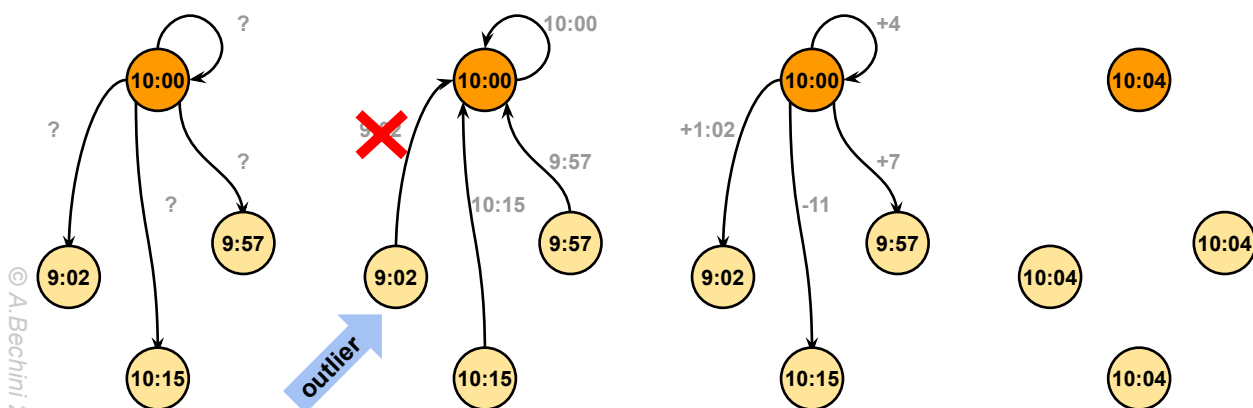


One process/node acts as master (*time daemon*); Successive steps:

- The time daemon asks all the others for their clock values.
- Each node answers back its actual time value;  
the master annotate each RTT as well.
- The time daemon computes a *proper* average.
- The time daemon sends each node the clock correction value  
(why not broadcasting the time?)

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# Berkeley Algorithm: an Illustration



## Decentralized Averaging Algorithm

Each node has a daemon, with approximated UTC.

- Periodically, each node broadcasts its own time.
- On each node, the new time value is obtained by averaging the local time and the received values.





# NTP - Network Time Protocol



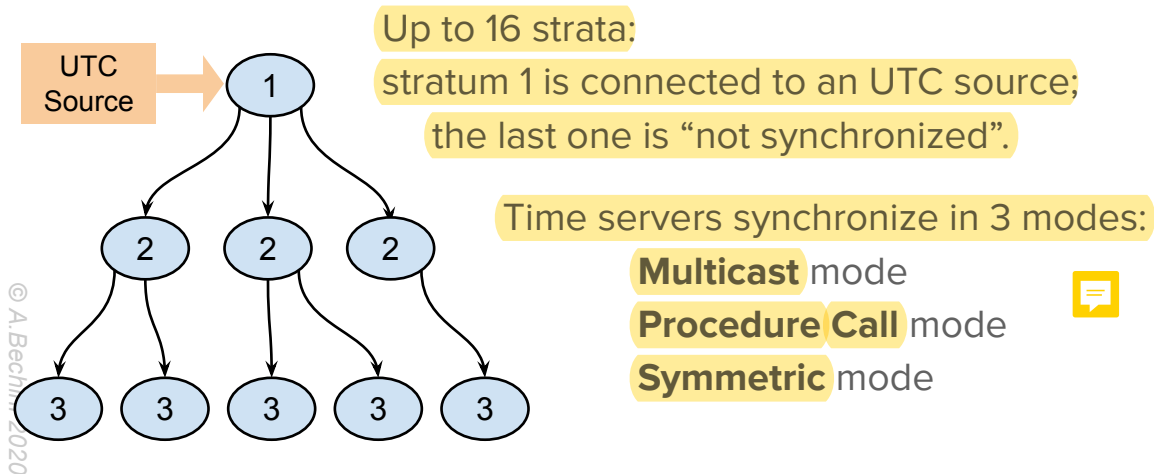
## NTP - Overview

To enable clients across Internet to get synchronized with UTC.

- Scalable to large networks
- Statistical techniques to filter data
- Authentication against interference
- Hierarchy of time servers, spread across the Internet
- Messages sent over UDP



# Time Servers' Hierarchy - Strata



## NTP Modes

- **Multicast:** 1+ servers multicast the time to the other nodes;  
suitable for LANs
- **Procedure Call:** more accurate because of latency compensation,  
using an approach based on Cristian's algorithm
- **Symmetric:** the most accurate and expensive,  
used between servers in the upper (most precise) strata;  
Pairs of servers exchange messages carrying the timestamp  
for the involved events



# Symmetric Mode

From the exchanged messages, a process must be able to get an estimate  $o_i$  of the actual offset  $o$  to fix its clock

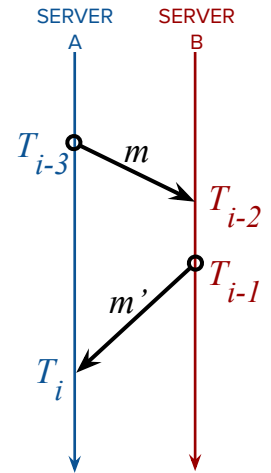
$$\begin{cases} T_{i-2} = T_{i-3} + t_m + o \\ T_i = T_{i-1} + t_{m'} - o \end{cases} \quad \begin{cases} o = T_{i-2} - T_{i-3} - t_m \\ o = T_i - T_{i-1} + t_{m'} \end{cases}$$



$$RTT = t_m + t_{m'} = \Delta T_A - \Delta T_B = (T_i - T_{i-3}) - (T_{i-1} - T_{i-2})$$

$$o = \frac{1}{2} (T_{i-2} - T_{i-3} + T_{i-1} - T_i - t_m + t_{m'}) = o_i + \frac{1}{2} (t_{m'} - t_m)$$

$$o_i - \frac{1}{2} RTT \leq o \leq o_i + \frac{1}{2} RTT$$



## Symmetric Mode: How to Fix Time

Estimated offset:



$$o_i = \frac{1}{2} (T_{i-2} - T_{i-3} + T_{i-1} - T_i)$$

Accuracy (upper bound):

$$RTT$$

- To fix the time, several pairs  $\langle o_i, RTT \rangle$  are collected, and the most accurate value is used.