

SECURITY IN NETWORKED COMPUTING SYSTEMS

Computer Engineering

22 July 2015

EXERCISE NO. 1

#MARKS: 10

With reference to a perfect cipher,

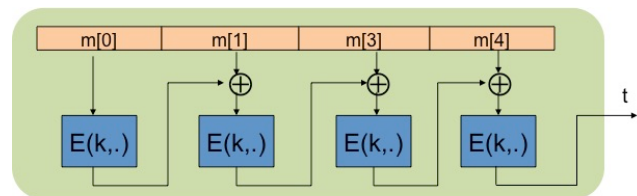
1. State the Shannon's formal definition of perfect cipher and give an intuitive explanation of the definition;
2. Prove that in a perfect cipher the number of keys cannot be smaller than the number of messages;
3. Argue whether an asymmetric cipher can be perfect or not.

EXERCISE NO. 2

#MARKS: 10

State the security definition of a Message Authentication Code (MAC).

List and briefly introduce the main methods of building a MAC out of other cryptographic primitives.



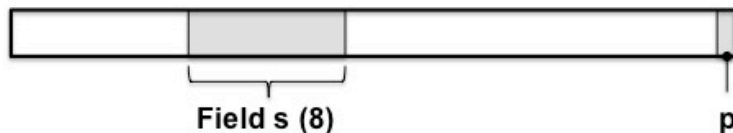
raw CBC

Show that the rawCBC-MAC (see figure) is insecure. Hint: compute the MAC  $t_1$  of the single block message  $m_1$  and the MAC  $t_2$  of the two-block message  $m_2 = (m_1, m_1 \oplus t_1)$ . Generalize the attack for an arbitrary number of blocks message.

EXERCISE NO. 3

#marks: 10

Let us assume that a plaintext  $P$  has the format specified in the figure where  $s$  is an 8-bit field that specifies an amount of money and  $p$  is a *parity bit* s.t.



$p$  is 0 if the number of 1s in the plaintext (bit  $p$  excluded) is even; it is 1 otherwise. The whole plaintext is encrypted by means of one-time-pad.

Q1. Does this encryption scheme suffer from malleability? Motivate the answer.

Q2. Assume that field  $s$  specifies the value 130. Argue whether and how, it is possible to modify the cipher-text so that the decrypted plaintext specifies 146 in the field  $s$  and such a modification goes undetected.

Q3. Propose a possible countermeasure.

**SECURITY IN NETWORKED COMPUTING SYSTEMS***Computer Engineering***22 July 2015****SOLUTION****Exercise n.1**

Q1, Q2, Q3. See theory.

**Exercise n.2**

Q1. See theory

Q2. See theory.

Q3. Compute  $t_1$  and  $t_2$  as hinted, and verify that  $t_1 = t_2$ . This means that a collision has arisen. One possible way to generalize is to consider a message having the following structure  $m = (m_1, m_1 \oplus t_1, \dots, m_1 \oplus t_1)$ , where  $m_1$  is a single block message and  $t_1$  is  $m_1$ 's tag.

**Exercise n. 3**

**Q1.** The encryption scheme is malleable. A simple way to prove it is the following. Let  $P[i]$ ,  $C[i]$ , and  $K[i]$  be the  $i$ -th bit of the plaintext, ciphertext and key, respectively, s.t.  $C[i] = P[i] \text{ xor } K[i]$ . Notice that  $P[0] = p$ . Finally let  $C'$  be the modified ciphertext and  $P'$  the resulting plaintext after decryption. Notice that an adversary can easily complement a bit of the plaintext by operating on the ciphertext. Assume that the adversary wishes to complement bit  $i$ . Then, (s)he computes  $C'[i] = C[i] \text{ xor } 1 = (P[i] \text{ xor } K[i]) \text{ xor } 1 = (P[i] \text{ xor } 1) \text{ xor } K[i] = P'[i] \text{ xor } K[i]$ . It follows that  $P'[i] = P[i] \text{ xor } 1$ , that is,  $P'[i]$  is the complement of  $P[i]$  ( $P'[i] = \sim P[i]$ ).

In order for the attack to go undetected, and the scheme to be malleable, the parity bit must be consistently modified as well. Notice that since  $P[i]$  is complemented the number of 1 either increment or decrement by one. In both cases the parity bit has to be complemented as well. This implies that  $C'[0] = C[0] \text{ xor } 1$ .

**Q2.** The attack consists in complementing  $C[0]$  and the 5-th most significant bit in  $s$ .

**Q3.** The problem can be solved by replacing the parity bit by a tag resulting from a secure hash function.