



CS3005: DIGITAL MEDIA AND GAMES

3D Graphics for Games

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Gaming

VFX

VR

Animated
Movies

Architectural
Visualisations

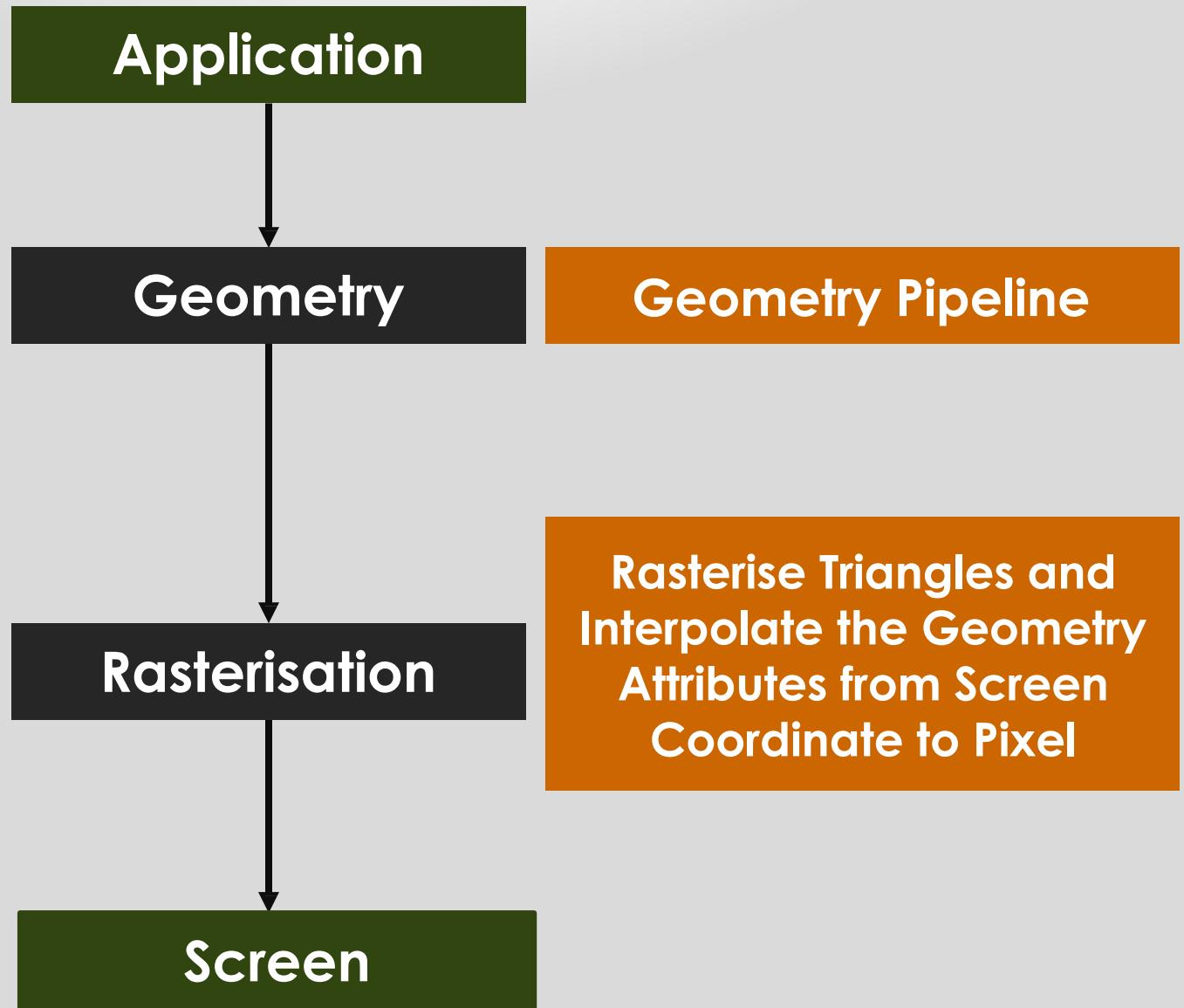
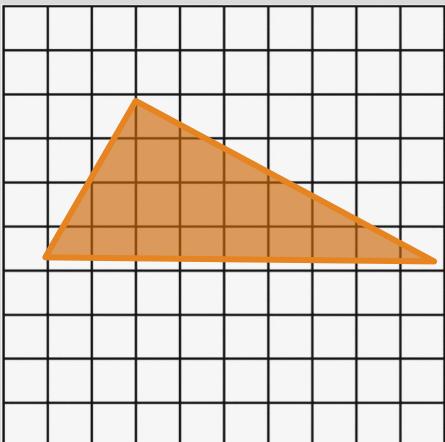
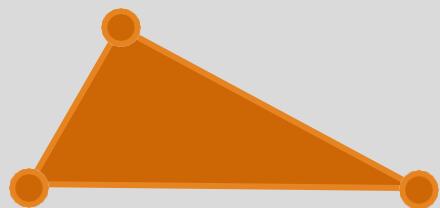
3D Printing

Requires Basic 3D

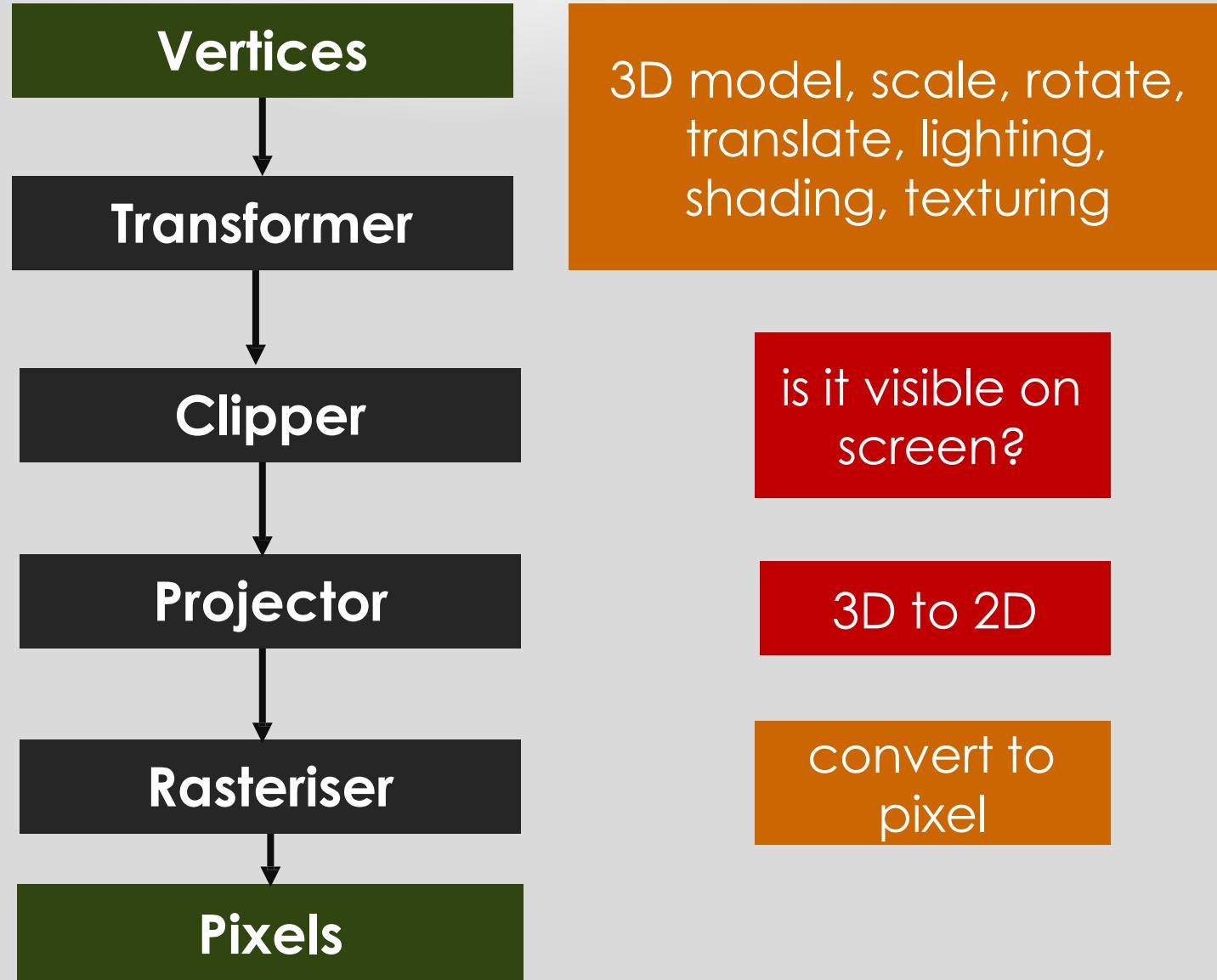


Requires Basic 3D

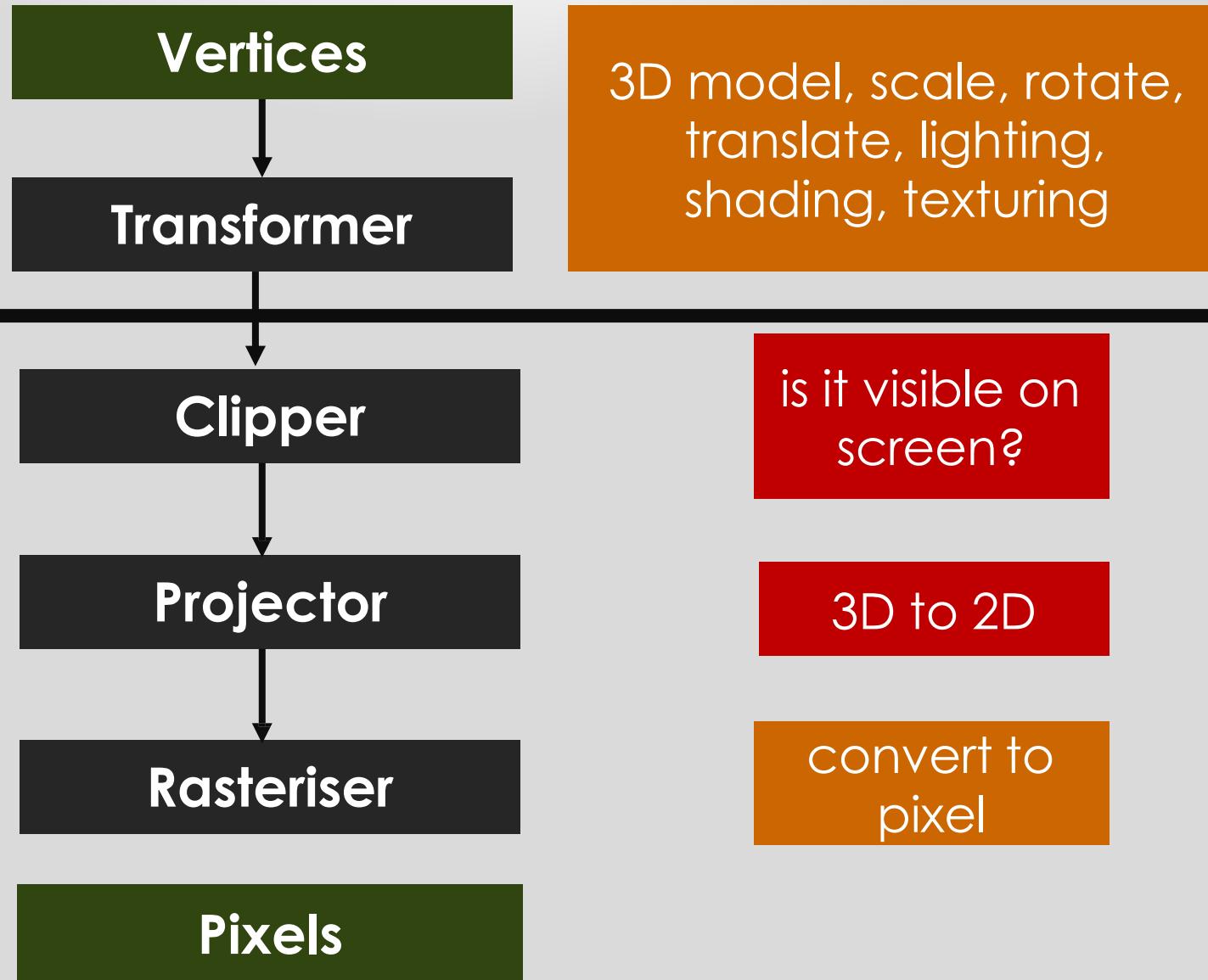
3D Graphics Pipeline



3D Graphics Pipeline



3D Graphics Pipeline

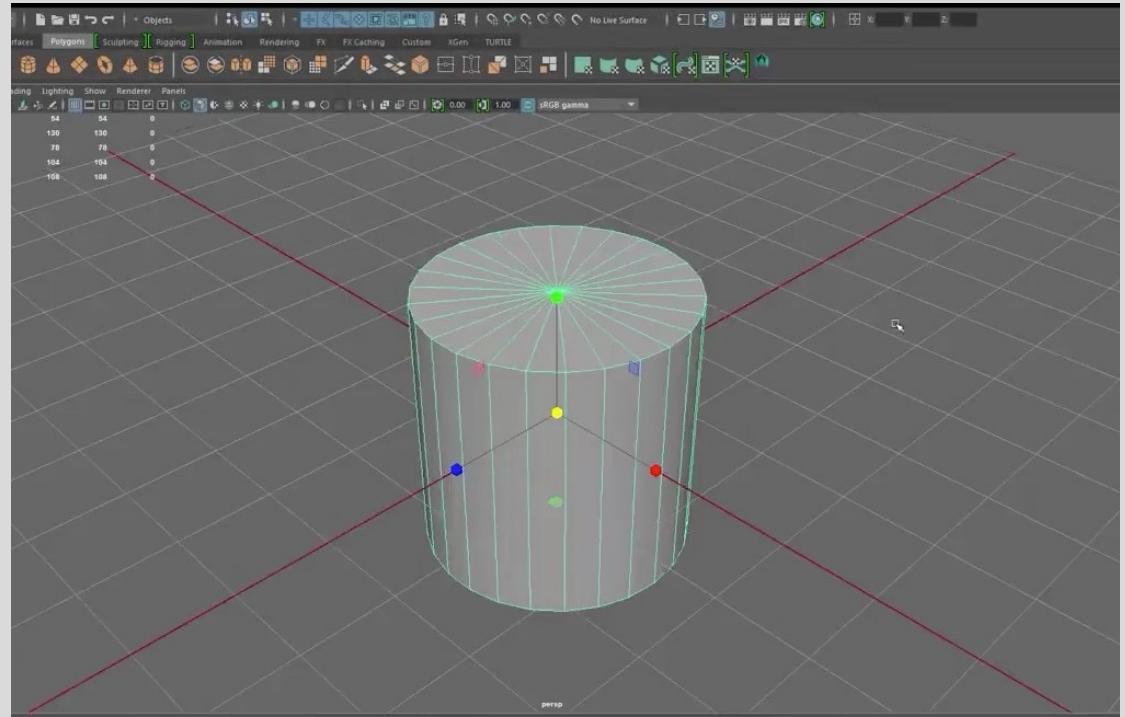


3 Building Blocks of 3D

Modelling

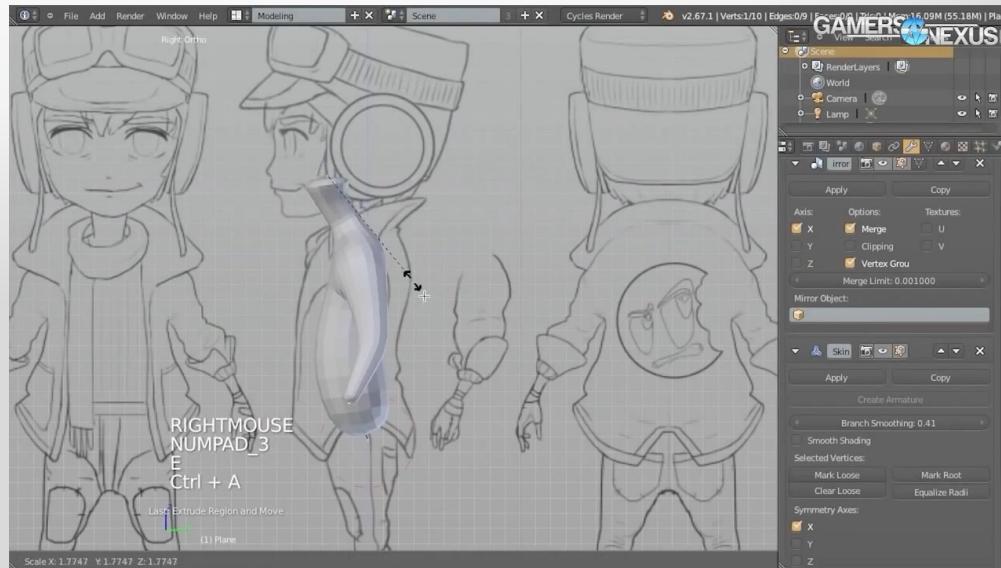
Lighting

Texturing



Modelling

3d Modeling design



3d Capture



3DGeometry

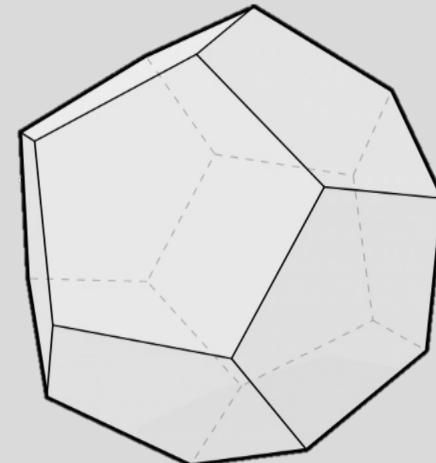
3DGeo met ry

earth measure

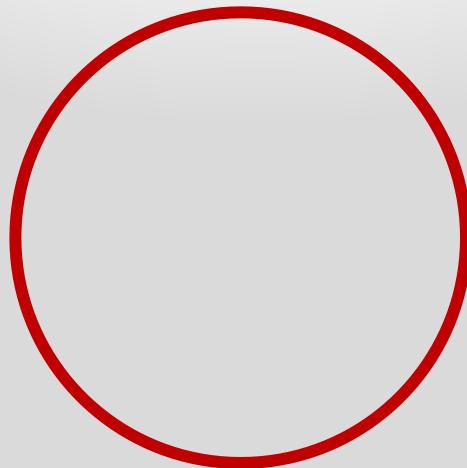
↓ ↓
geo • met ry :

🎮 The study of shapes,
sizes, patterns, and
positions.

🎮 The study of spaces
where some quantity
(lengths, angles, etc.) can
be measured.



How can we describe geometry?



Unit Circle

How can we describe geometry?

Implicit

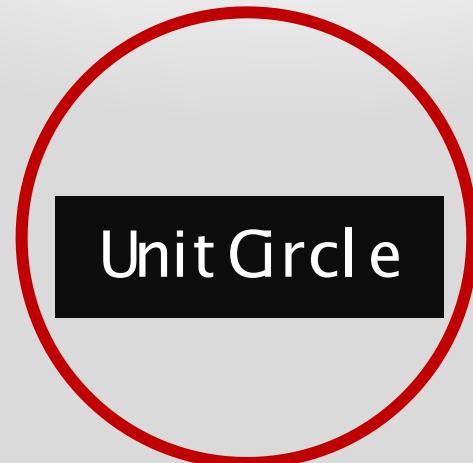
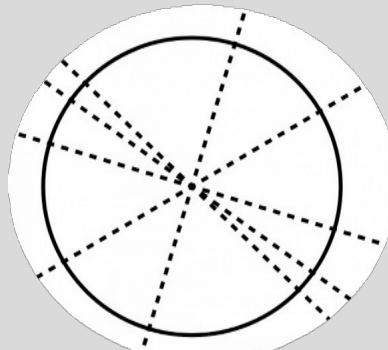
$$x^2 + y^2 = 0$$

Curvature

$$k = 1$$

Tomographic

constant
density

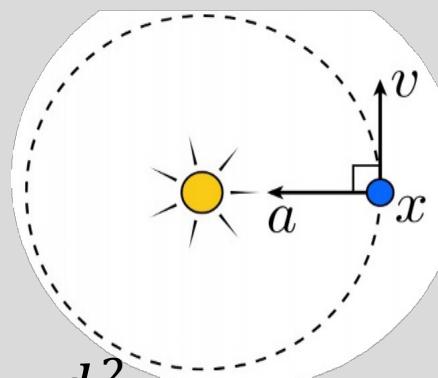


Explicit

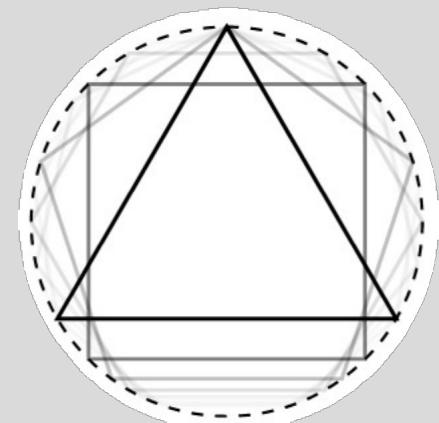
$$\left(\frac{\sin \theta}{x}, \frac{\cos \theta}{y} \right)$$

Discrete

Dynamic



$$\frac{d^2}{dt^2} x = -x$$

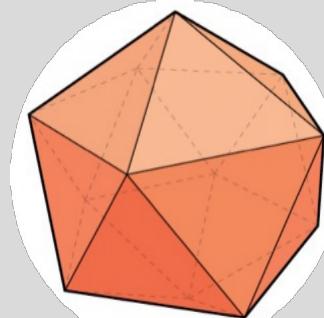
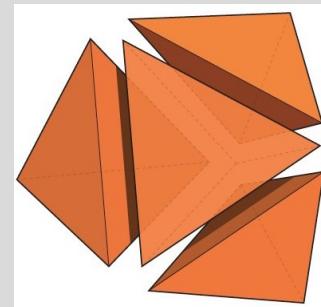
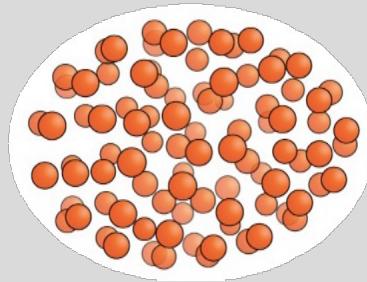


$$n \rightarrow \infty$$

Many ways to digitally encode geometry

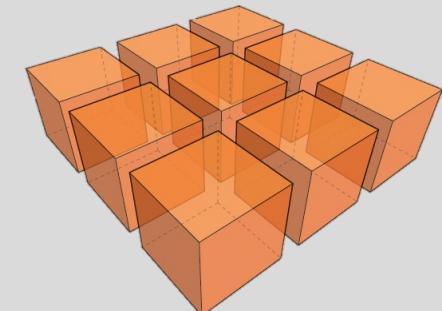
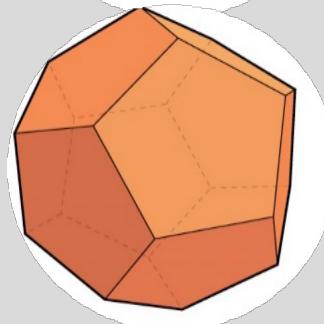
Explicit

- 🕹 Point cloud
- 🕹 Polygon mesh
- 🕹 Subdivision, NURBS



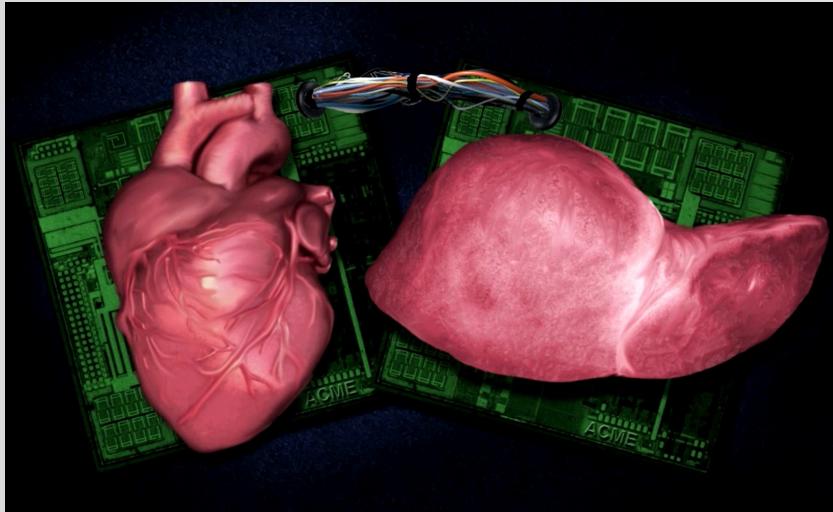
Implicit

- 🕹 Level set
- 🕹 Algebraic surface
- 🕹 L-systems



Given all these options, what is the best way to encode geometry on a computer?

Examples of geometry

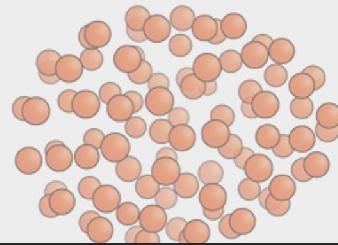


MANY WAYS TO DIGITALLY ENCODE GEOMETRY

EXPLICIT



Point cloud



Some representations work better than others—depends on the task

IMPLICIT



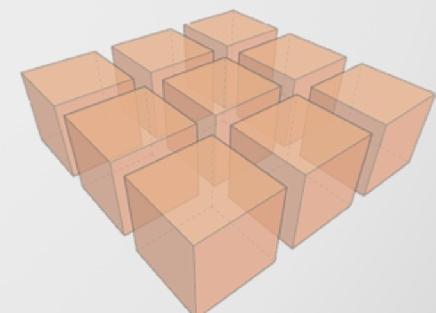
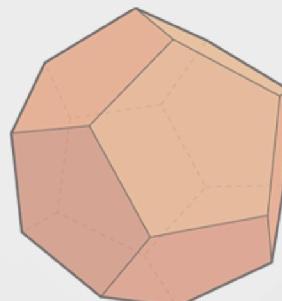
Level set



Algebraic surface

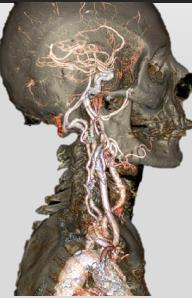


L-systems



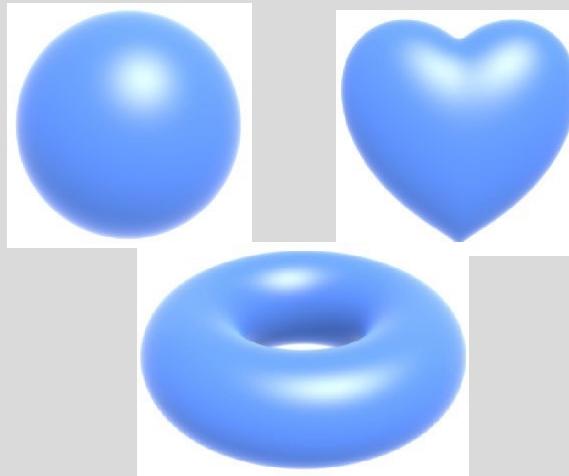
Some representations work better than others—depends on the task

Level set



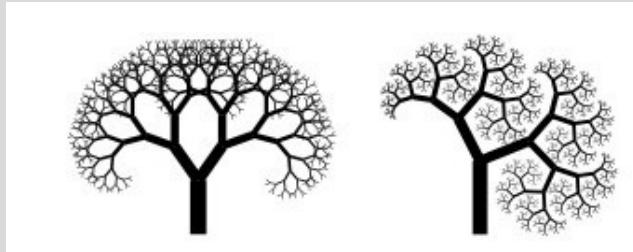
constant tissue density

Algebraic surface



polynomials

LSystem



natural patterns

Explicit representation in Graphics

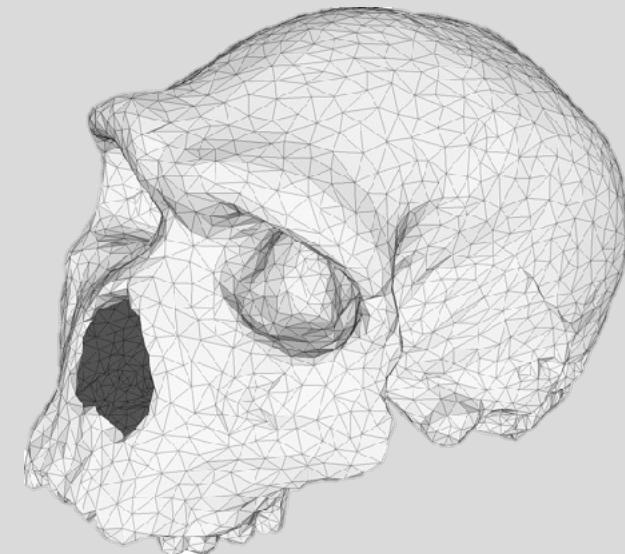
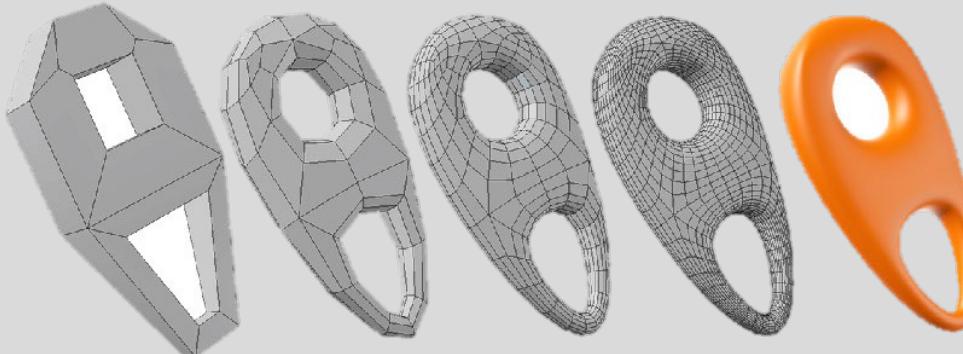
🕹 **Point cloud**

🕹 **Polygon mesh**

🕹 **Triangle mesh**

🕹 **Subdivision surfaces**

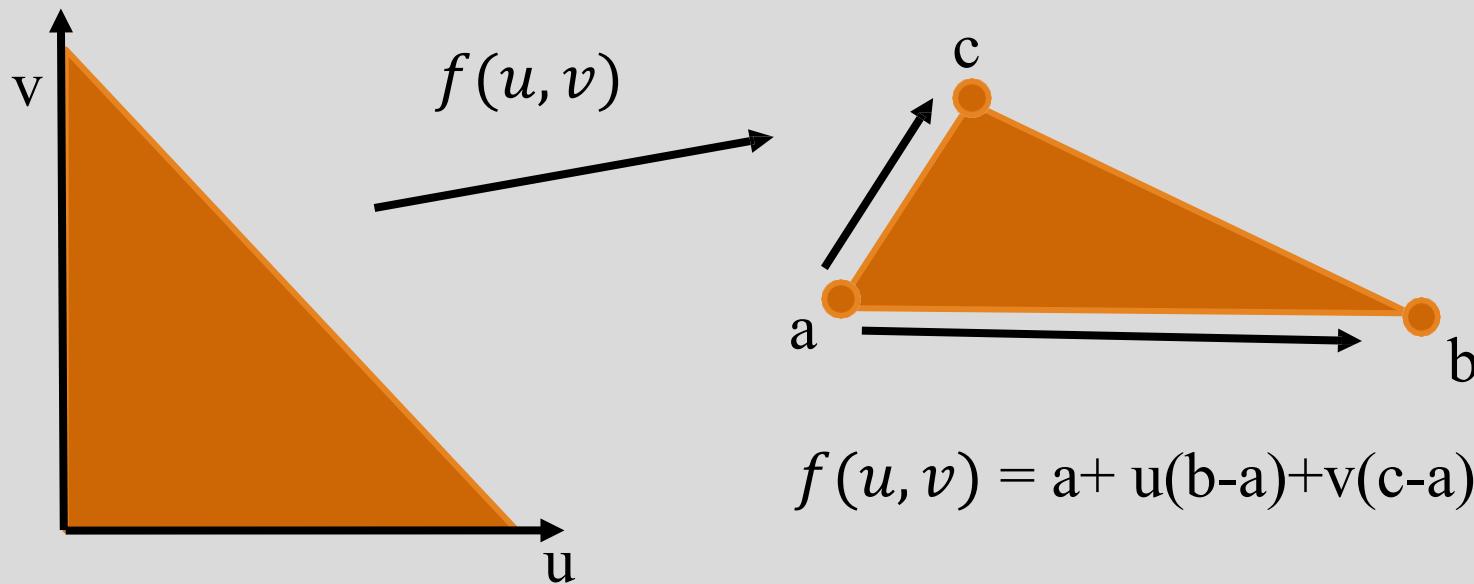
🕹 **NURBS**



Triangle Mesh

The reason why triangles are commonly used in practice is **simplicity**:

Three points in space unambiguously define a plane

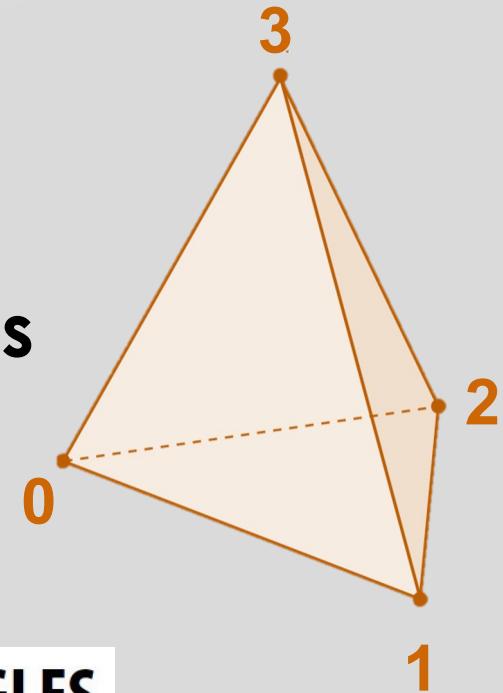


TriangleMesh

🎮 Store vertices as triples of coordinates (x,y,z)

🎮 Store triangles as triples of indices (i,j,k)

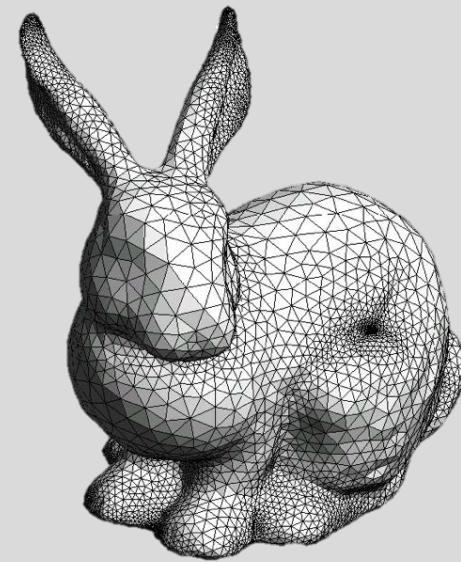
🎮 E.g., tetrahedron



VERTICES			TRIANGLES			
	x	y	z	i	j	
0:	-1	-1	-1	0	2	1
1:	1	-1	1	0	3	2
2:	1	1	-1	3	0	1
3:	-1	1	1	3	1	2

TriangleMesh

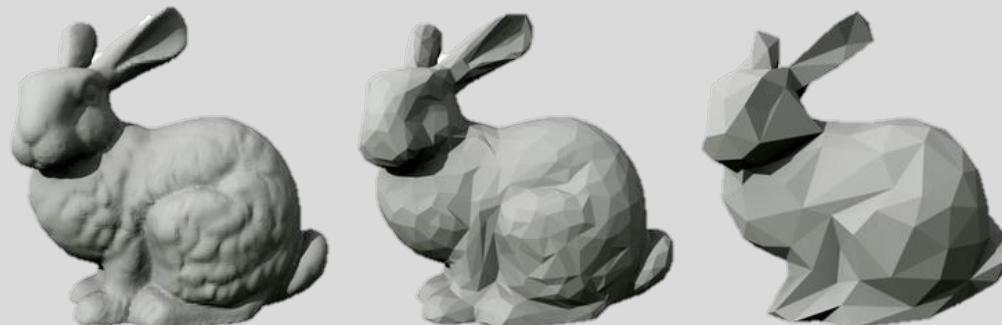
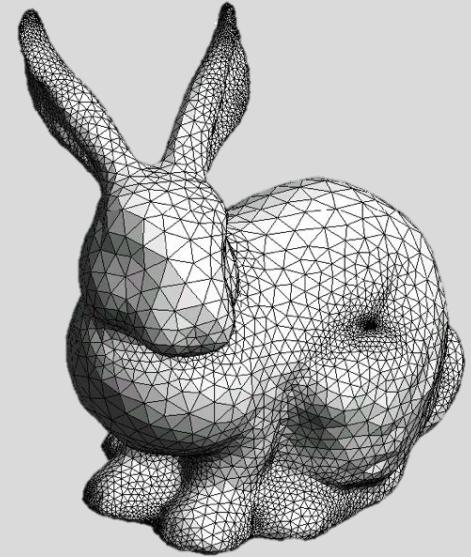
```
# vertex count = 2503
# face count = 4968
v -3.4101800e-003 1.3031957e-001 2.1754370e-002
v -8.1719160e-002 1.5250145e-001 2.9656090e-002
v -3.0543480e-002 1.2477885e-001 1.0983400e-003
v -2.4901590e-002 1.1211138e-001 3.7560240e-002
v -1.8405680e-002 1.7843055e-001 -2.4219580e-002
v 1.9067940e-002 1.2144925e-001 3.1968440e-002
v 6.0412000e-003 1.2494359e-001 3.2652890e-002
v -1.3469030e-002 1.6299355e-001 -1.2000020e-002
v -3.4393240e-002 1.7236688e-001 -9.8213000e-004
v -8.4314160e-002 1.0957263e-001 3.7097300e-003
v -4.2233540e-002 1.7211574e-001 -4.1799800e-003
v -6.3308390e-002 1.5660615e-001 -1.3838790e-002
v -7.6903950e-002 1.6708033e-001 -2.6931360e-002
v -7.2253920e-002 1.1539550e-001 5.1670300e-002
f 420 1071 1065
f 264 281 254
f 298 309 281
f 368 366 367
f 368 396 366
f 1639 1564 1139
f 560 48 47
f 82 471 212
f 25 38 37
f 202 1206 1080
f 264 298 281
f 298 331 309
f 309 331 366
```



OBJ File

TriangleMesh

Game designers have to carefully balance **model fidelity vs polygon count**, because if the count goes too high, the **framerate** of an animation drops below what users perceive as smooth.



3D Transformations

Translation

Position

Scaling

Size

Rotation

orientation

**represent 3D transformations as
matrices**

3D Transformations

Translation

$$T_b = \begin{bmatrix} b_x \\ b_y \\ b_z \end{bmatrix}$$



Homogeneous Coordinates

$$v = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$T_b = \begin{bmatrix} I & T_b \\ \mathbf{0}^T & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & b_x \\ 0 & 1 & 0 & b_y \\ 0 & 0 & 1 & b_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & b_x \\ 0 & 1 & 0 & b_y \\ 0 & 0 & 1 & b_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$v' = T_b v$$

3D Transformations

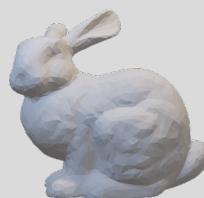
Scaling

$$S_s = \begin{bmatrix} S_x & 0 & 0 \\ 0 & S_y & 0 \\ 0 & 0 & S_z \end{bmatrix}$$



$$v = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$S_s = \begin{bmatrix} S_s & \mathbf{0} \\ \mathbf{0}^T & 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 & 0 \\ 0 & S_y & 0 & 0 \\ 0 & 0 & S_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Homogeneous Coordinates

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 & 0 \\ 0 & S_y & 0 & 0 \\ 0 & 0 & S_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

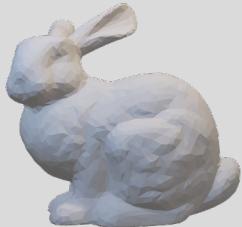
$$v' = S_s v$$

3D Transformations

Rotation

$R_{yz}(\theta)$: rotation about x axis by θ

$$R_x = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta \end{bmatrix}$$



$$v = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Homo geneous
Coordinates



$\theta = 90^\circ$

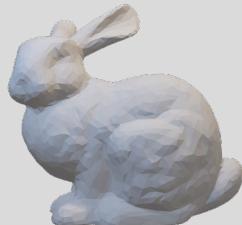
$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$
$$v' = R_x v$$

3D Transformations

Rotation

$R_{zx}(\theta)$: rotation about y axis by θ

$$R_y = \begin{bmatrix} \cos \theta & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin \theta & 0 & \cos \theta \end{bmatrix}$$



$$\mathbf{v} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Homo geneous
Coordinates



$$\theta = 90^\circ$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

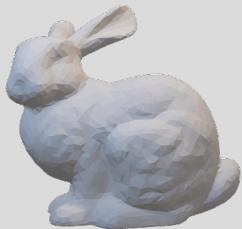
$$\mathbf{v}' = R_y \mathbf{v}$$

3D Transformations

Rotation

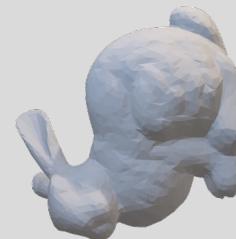
$R_{xy}(\theta)$: rotation about z axis by θ

$$R_z = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$



$$\begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Homo geneous
Coordinates



$\theta = 90^\circ$

$$v = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$v' = R_z v$$

why this is so beautiful ?

we can represent translation as a matrix, we can compose it with other transformations

Example: translate 10 units down
the Z then rotate 90° around X

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(90^\circ) & -\sin(90^\circ) & 0 \\ 0 & \sin(90^\circ) & \cos(90^\circ) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

why this is so beautiful ?

we can represent translation as a matrix, we can compose it with other transformations

Example: translate 10 units down the Z then rotate 90° around X

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

WHY THIS IS SO BEAUTIFUL ?

we can represent translation as a matrix, we can compose it with other transformations

Example: translate 10 units down
the Z then rotate 90° around X

Caution: matrix multiplication is NOT commutative!

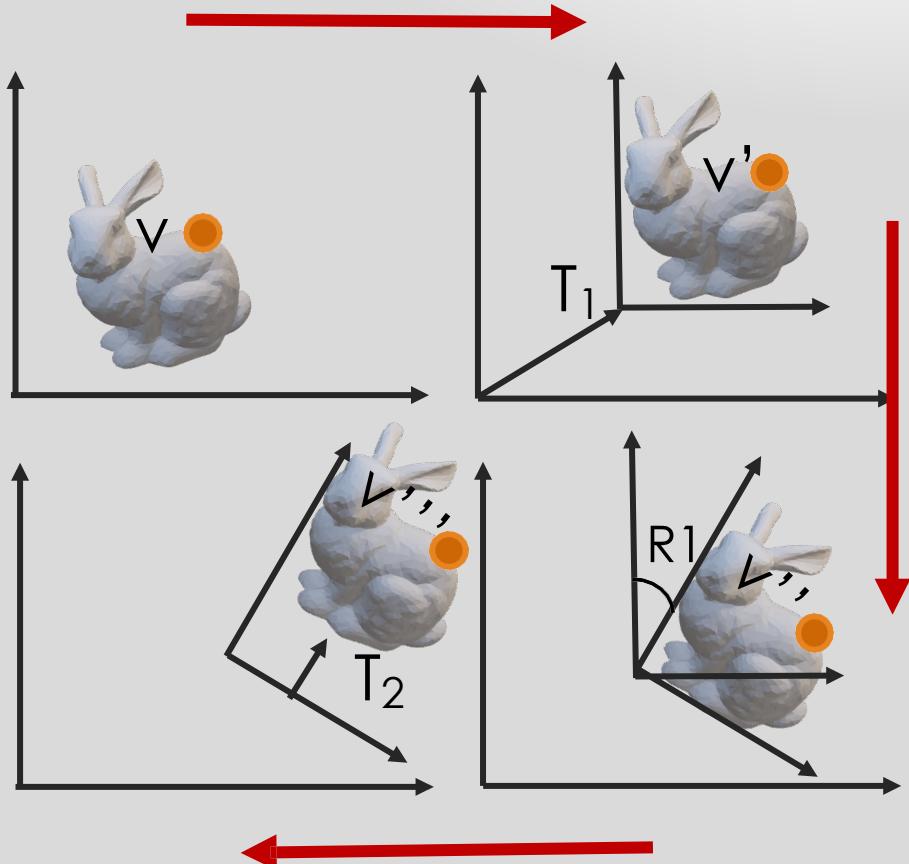
$$\begin{bmatrix} y \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} y \\ z \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

World Coordinates

- 🎮 We have been discussing transformations as transforming points.
- 🎮 Always need to think of the transformation in the world coordinate system.
- 🎮 Useful to think of them as a change in coordinate system.
- 🎮 Model objects in a local coordinate system, and transform into the world system.

World Coordinates



$$\begin{aligned}v'' &= T_1 v \\v''' &= T_1 R_1 v \\v'''' &= T_1 R_1 T_2 v\end{aligned}$$

- 🎮 Concatenate local transformation matrices from left to right
- 🎮 Can obtain the local world transformation matrix
- 🎮 v', v'', v''' are the world coordinates of p after each transformation

Transformations

Quiz

- 🎮 I sat in the car, and realized the side mirror is 0.4m on my right and 0.3m in my front
- 🎮 I started my car and drove 5m forward, turned 30 degrees to right, moved 5m forward again, and turned 45 degrees to the right, and stopped
- 🎮 What is the position of the side mirror now, relative to where I was sitting in the beginning?

The side mirror position
is locally (0.4,0.3)

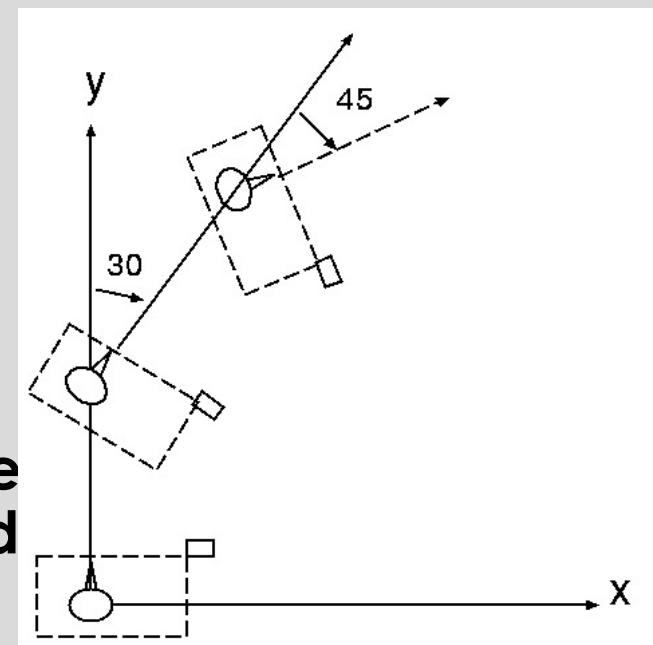
Transformations

Quiz

The local-to-global transformation matrix at the last configuration of the car is

$$TR_1TR_2 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 5 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} & 0 \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 5 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & 0 \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

The final position of the side mirror can be computed by $TR_1TR_2 p$ which is around (2.89331, 9.0214)



3 Building Blocks of 3D

Modelling

Lighting

Texturing

3 Building Blocks of 3D

Done

Lighting

Texturing

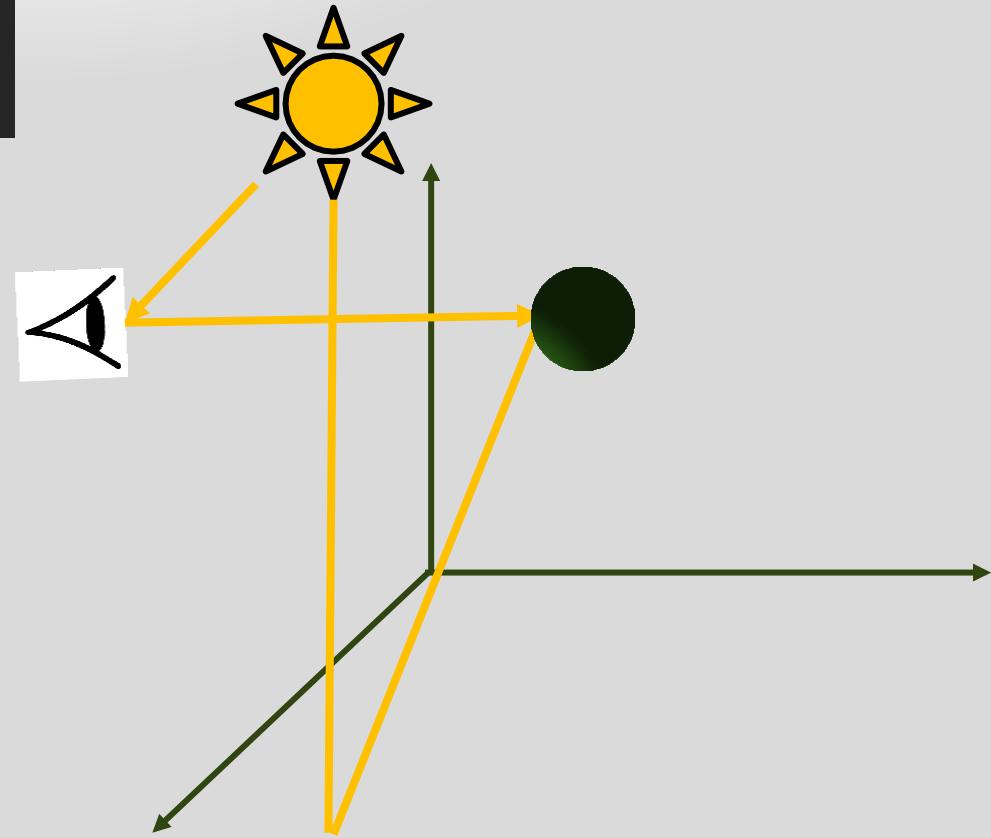
Lighting

Lighting and Shading

lighting equation

Emissive+
Ambient +
Diffuse +
Specular+

lighting Model

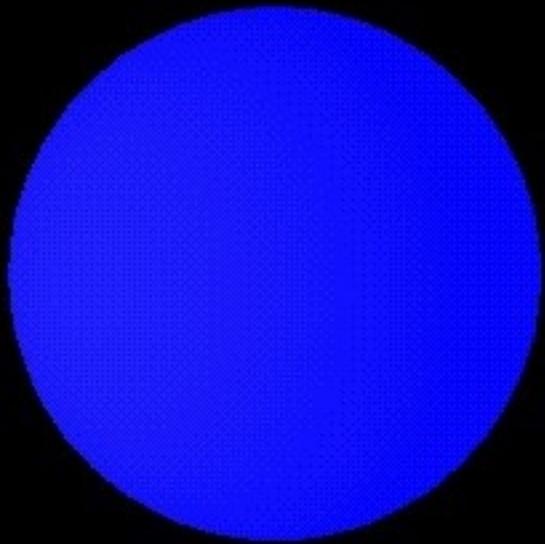


Lighting and Shading

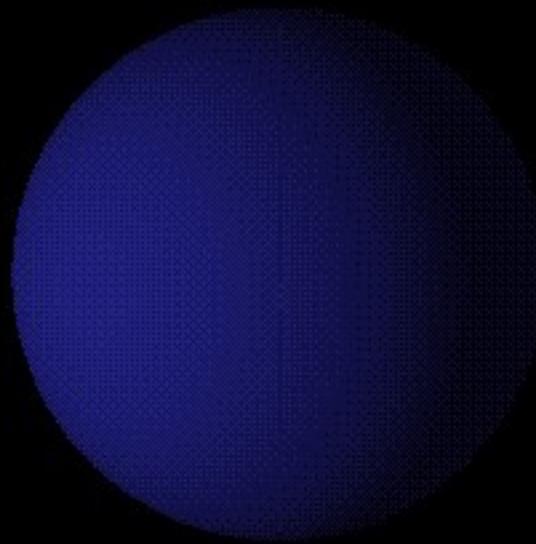


Emissive

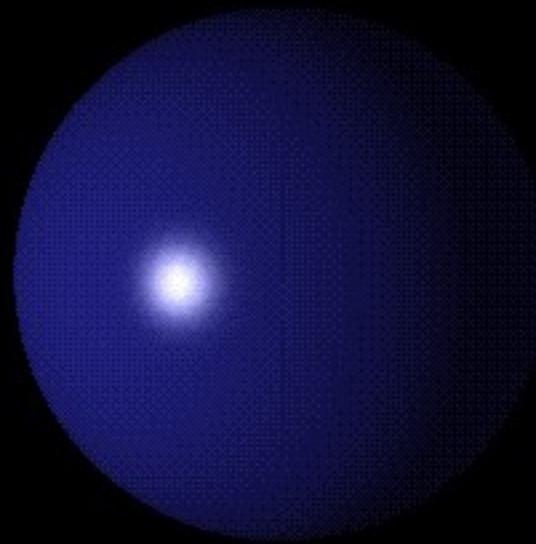
Lighting and Shading



Ambient

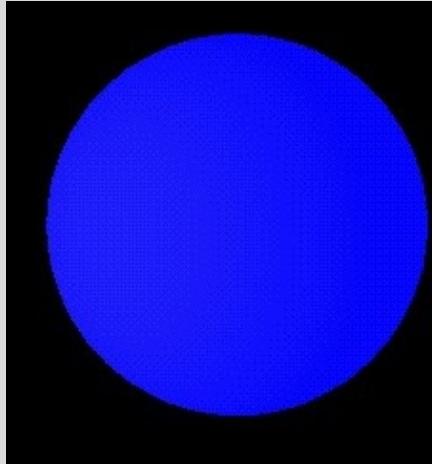


Diffuse

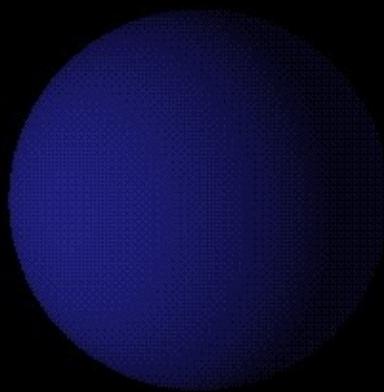


Specular

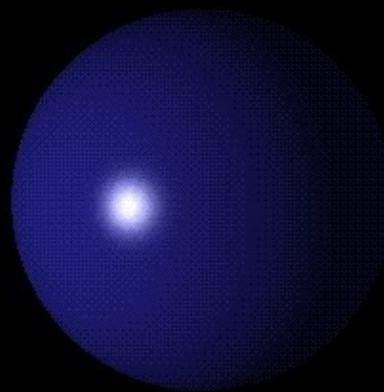
Lighting and Shading



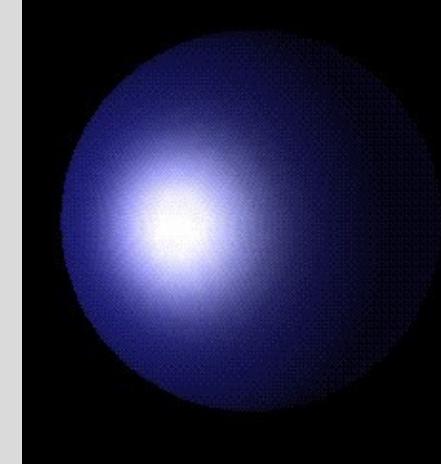
Ambient



Diffuse



Specular



Result

Lighting and Shading

lighting equation

The diffuse and specular components are computed based on the lights in the scene, while emissive and ambient are essentially independent.

The diffuse term can be thought of as a flat matte finish, and specular can be thought of as the shine finish of an object.

In terms of computation, the specular term is also affected by the camera angle.

Lighting and Shading

Types of light sources

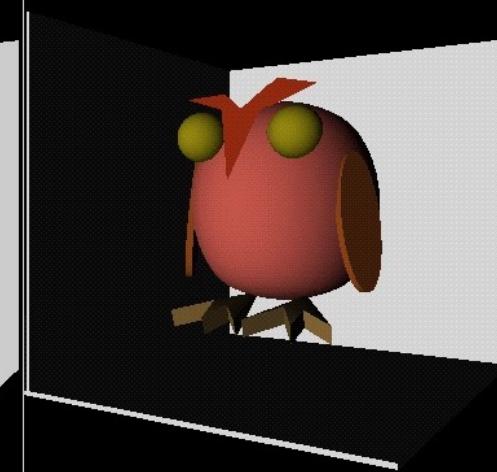
- 🎮 **Ambient light:** no identifiable source or direction.
- 🎮 **Point source:** given only by point.
- 🎮 **Directional light:** given only by direction.
- 🎮 **Spotlight:** from source in direction.
 - 🕹️ Cut-off angle defines a cone of light.
 - 🕹️ Attenuation function (brighter in centre).

Lighting and Shading

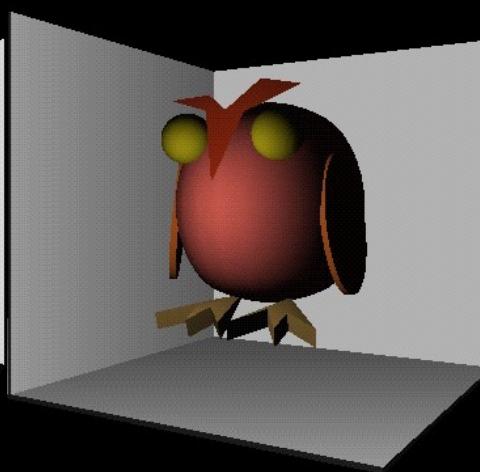
Types of light sources



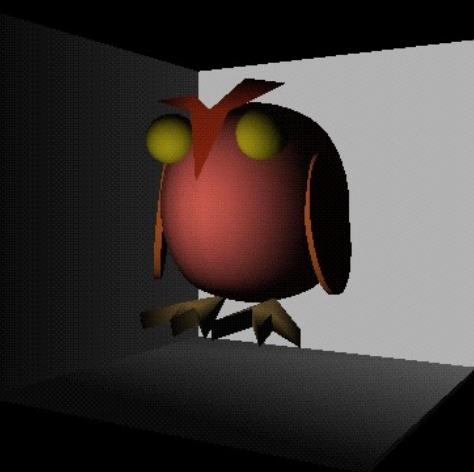
Ambient light



Directional light



Point source



Spotlight

Lighting and Shading

Shading Models

Flat Model

Gouraud Model

Phong Model

Lighting and Shading

Flat Model

We define a normal at each polygon (not at each vertex)

Lighting: Evaluate the lighting equation at the center of each polygon using the associated normal

Shading: Each sample point on the polygon is given the interpolated lighting value at the vertices (i.e., a total hack)



Lighting and Shading

Gouraud Model

Define a normal vector at each vertex

Lighting: Evaluate lighting equation at each vertex using associated normal vector

Shading: Each sample point's color on polygon is interpolated from color values at polygon's vertices



An issue with Gouraud shading is that specular highlights appear to “jump” as the object rotates.

Lighting and Shading

Phong Model

Each vertex has an associated normal vector

Lighting: Evaluate lighting equation at each vertex using associated normal vector

Shading:

For every sample point on the polygon we interpolate normals at vertices of the polygon and compute color using lighting equation with the interpolated normal at each interior pixel



Lighting and Shading



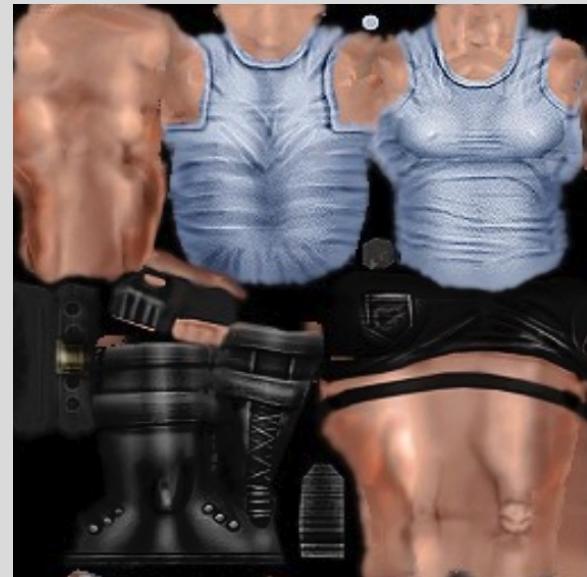
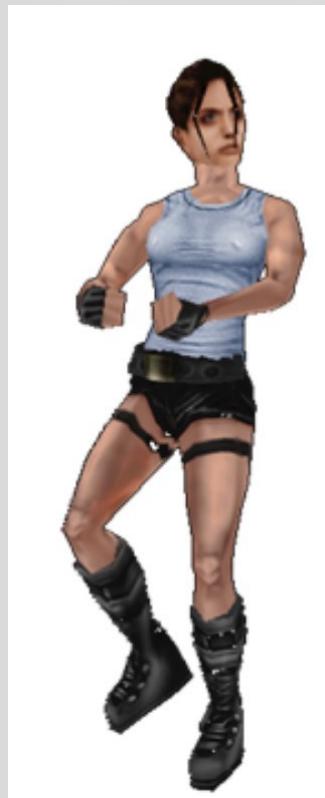
Flat
Model

Gouraud
Model

Phong
Model

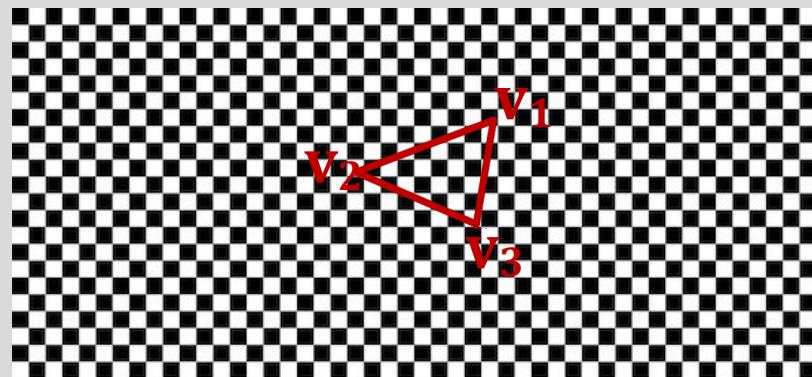
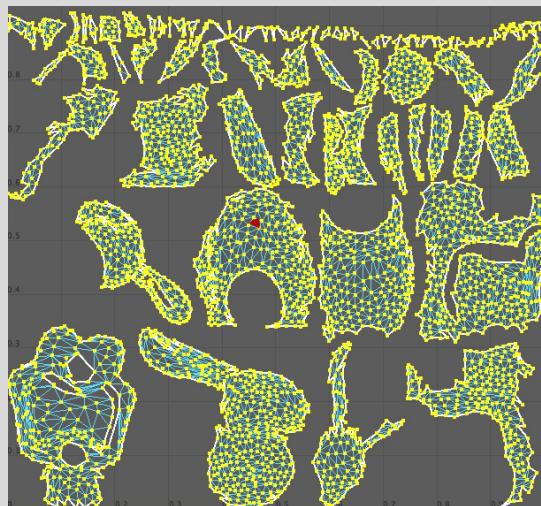
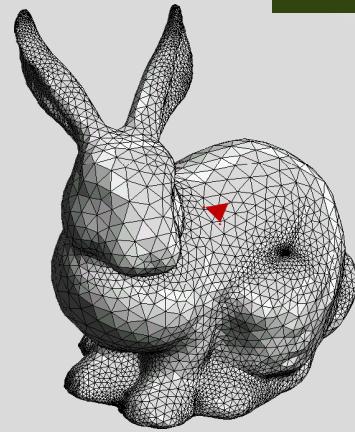
Texturing

Texturing



Texturing

- For each triangle in the model establish a corresponding region in the phototexture



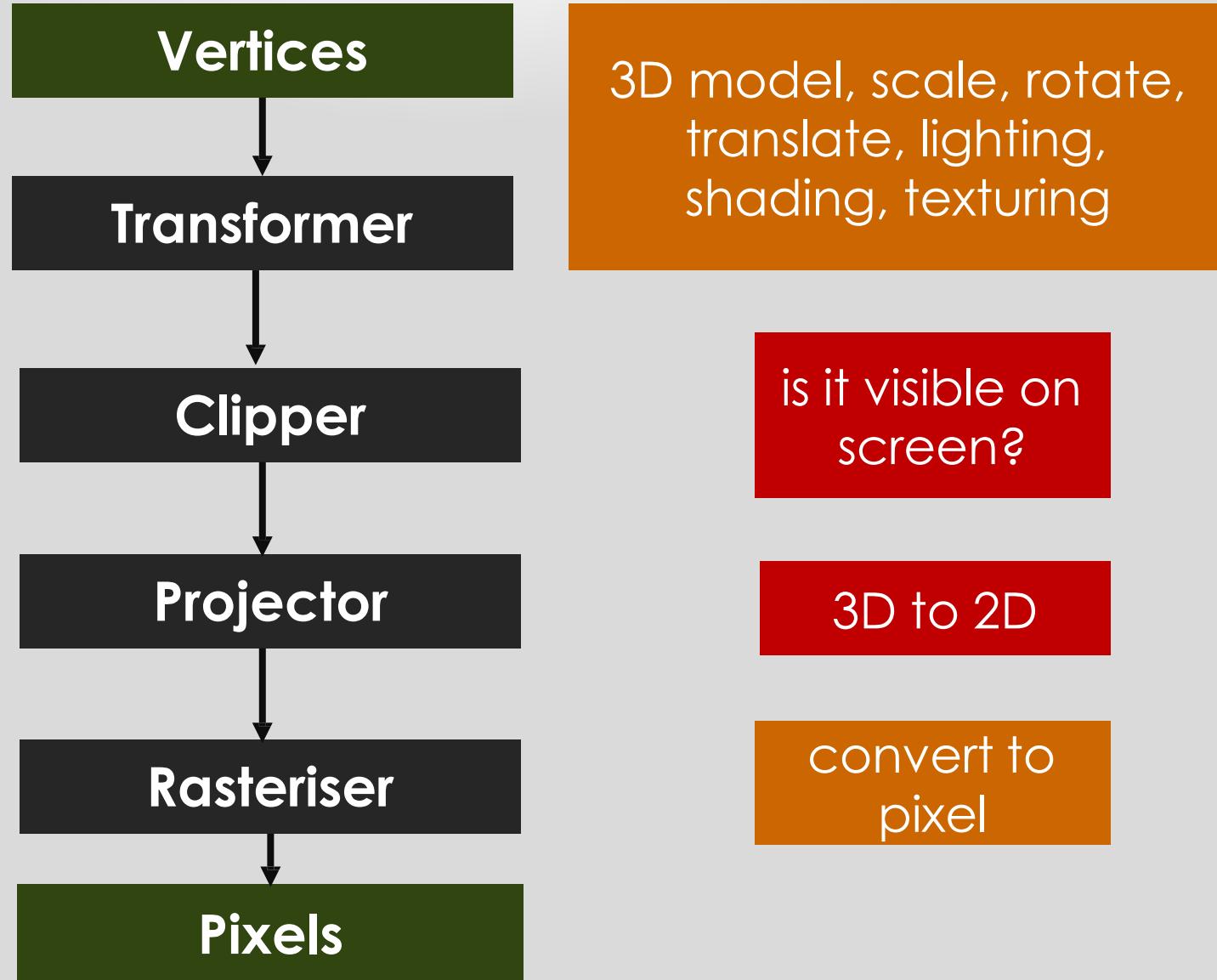
2D image

- During rasterization interpolate the coordinate indices into the texture map



Texture map

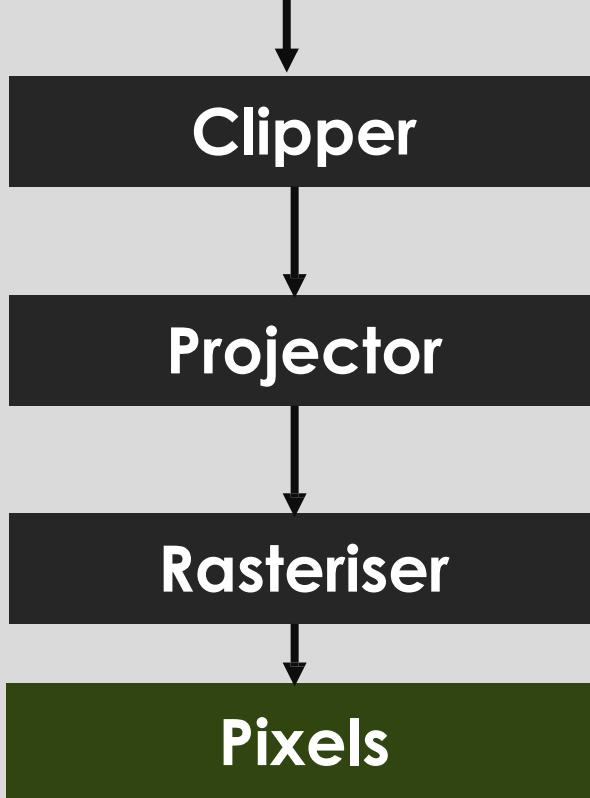
3D Graphics Pipeline



Viewing and Projection

Done

3D graphics
pipeline



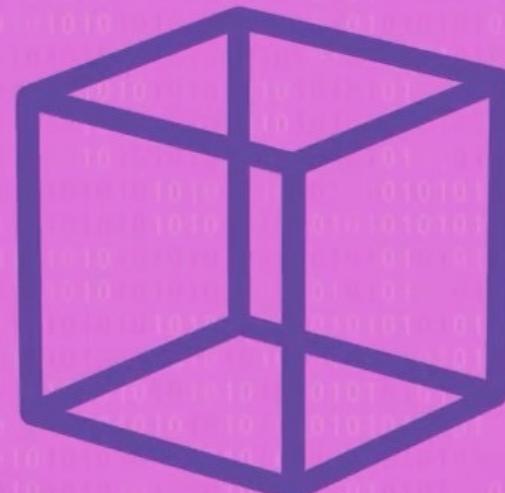
is it visible on
screen?

3D to 2D

convert to
pixel

Viewing and Projection

Projection



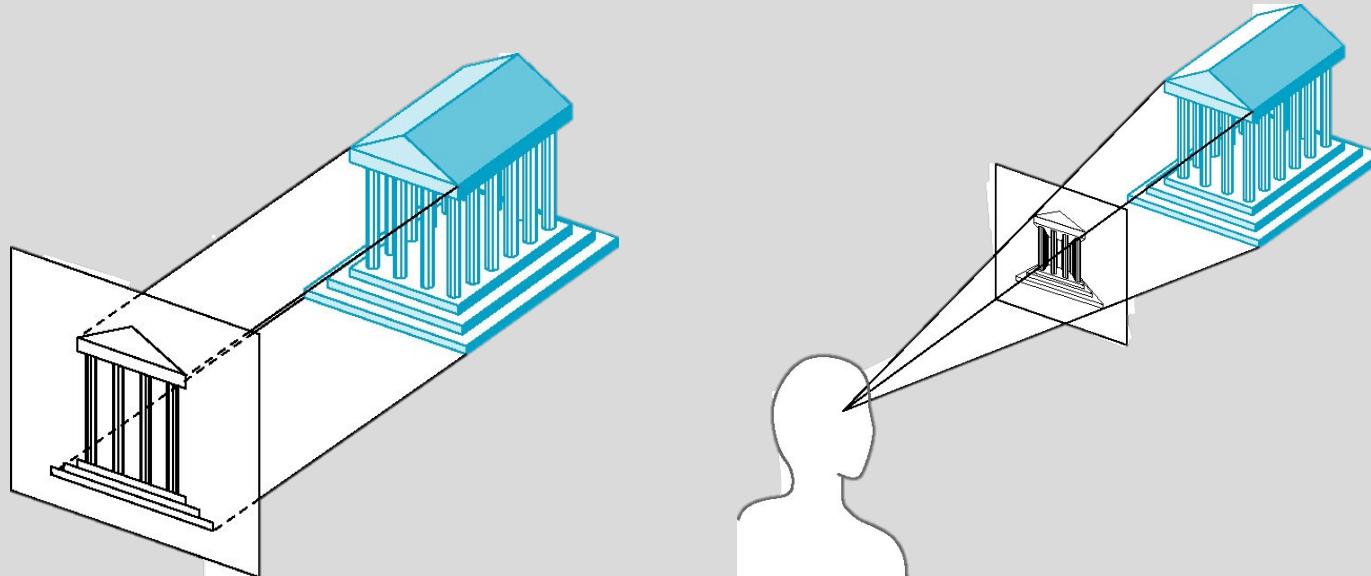
Viewing and Projection

Projection

Complex transformation [Angel Ch. 5]

Orthographic
Projection

Perspective
Projection

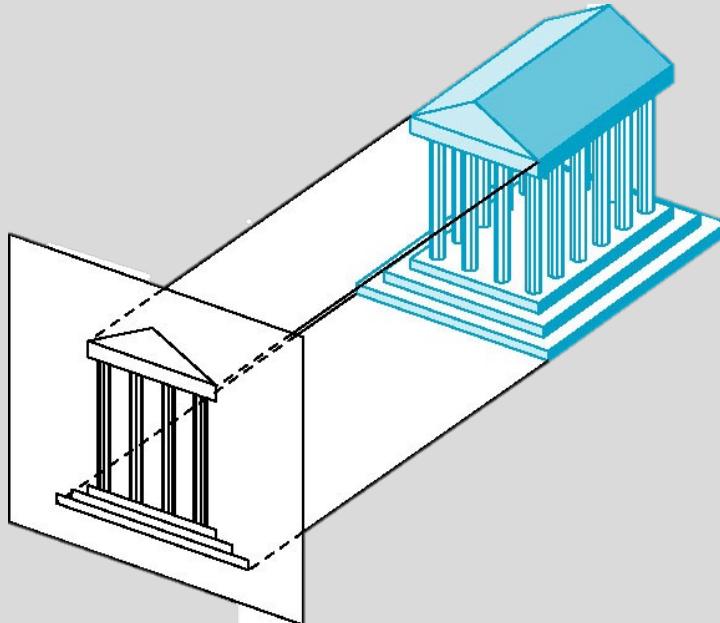


Viewing and Projection

Projection

Orthographic Projection

- **projection** that maintains parallel lines but provides no sense of depth.
- It is used in the engineering fields to create accurate renderings of models. They maintain parallel lines but provide no sense of depth. All vertices are projected straight onto a viewing window

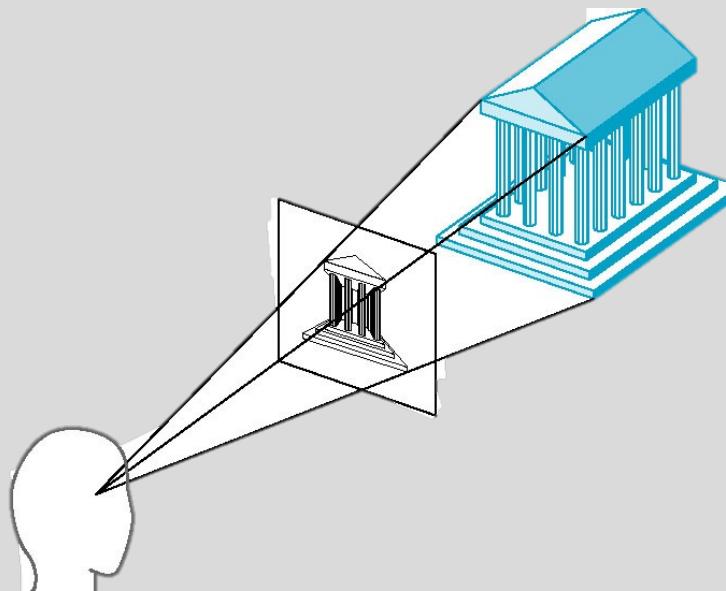


Viewing and Projection

Projection

Perspective Projection

- **projection** provides for a sense of depth, but parallel lines are skewed toward vanishing points
- a virtual scene to make it appear like a view from a real-world camera. Objects further from the camera appear to be smaller and all lines appear to project toward vanishing point which skew parallel lines. Perspective projections are almost always used in gaming, movie special effects, and visualizations of virtual worlds.

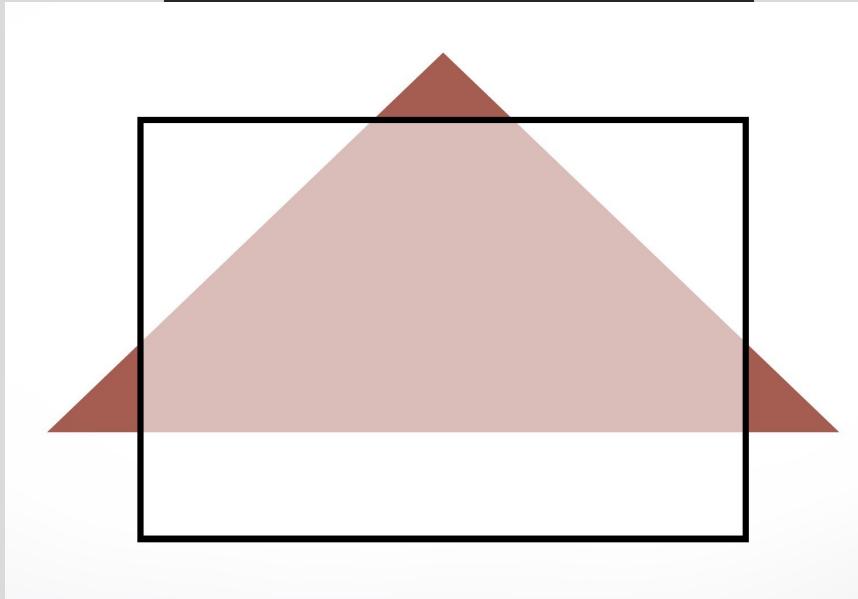


Viewing and Projection

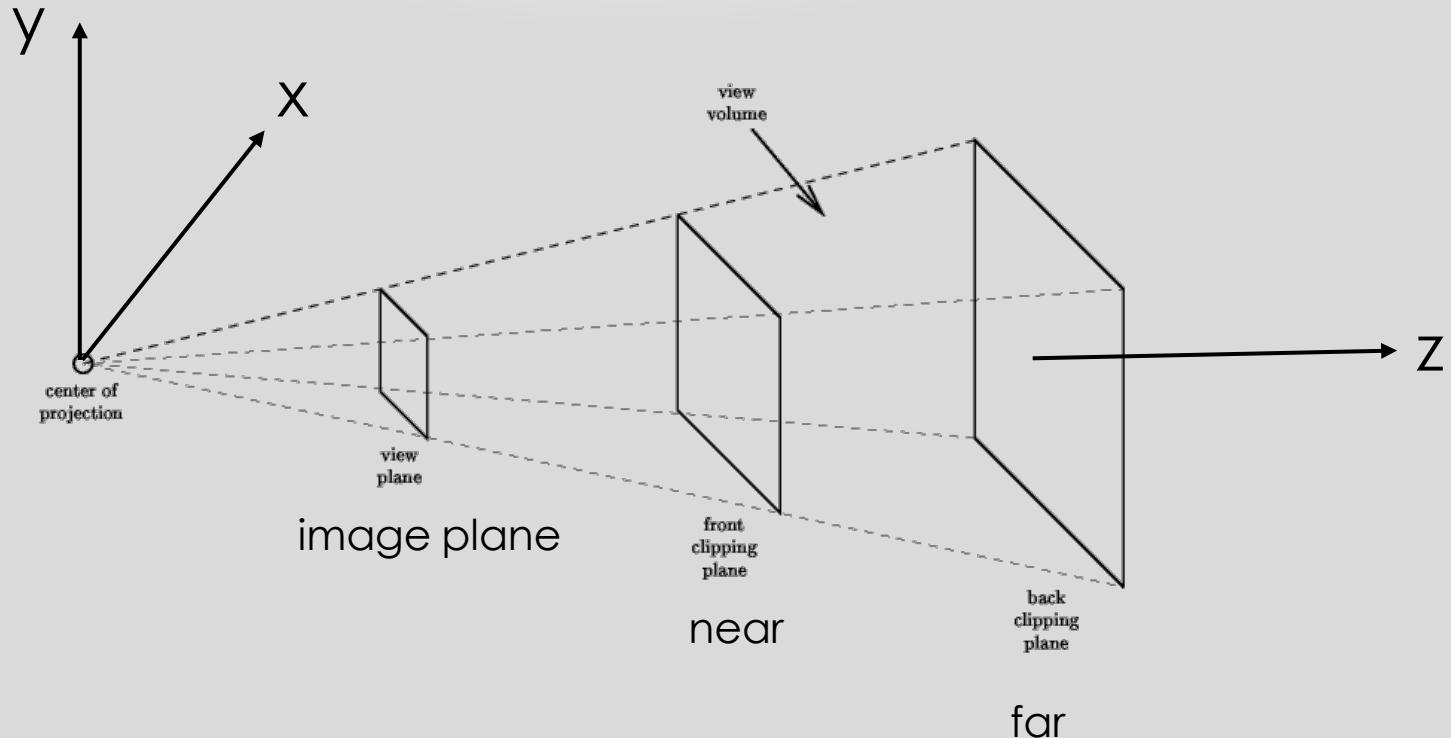
Clipping

Mostly automatic (must set viewport)

2D Clipping Problem



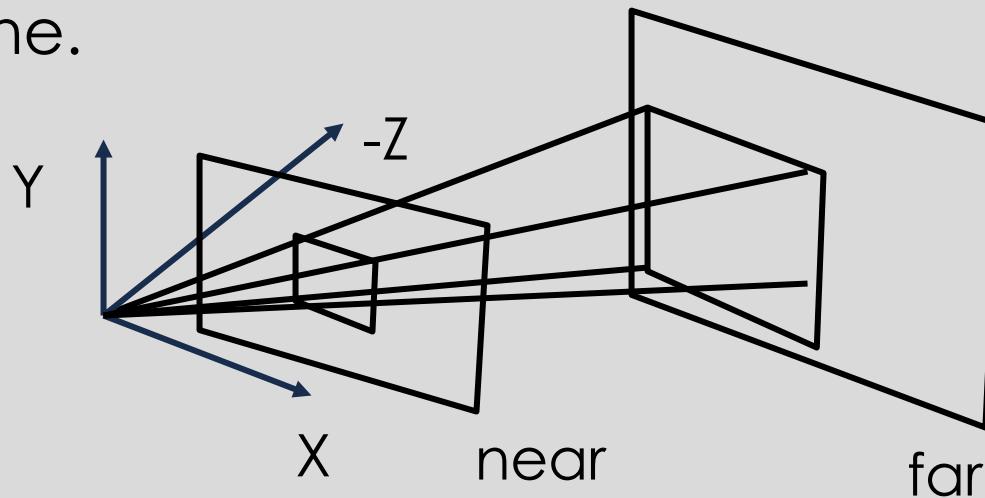
Viewing and Projection



Clipping is tricky because of frustum shape

Viewing and Projection

- 🎮 Define the “view frustum” (6 parameters).
- 🎮 Assume origin is the view point.
- 🎮 Near and far planes (planes parallel to XY plane in the negative Z axis).
- 🎮 Left, right, top, bottom rectangle defined on the near plane.



Rendering

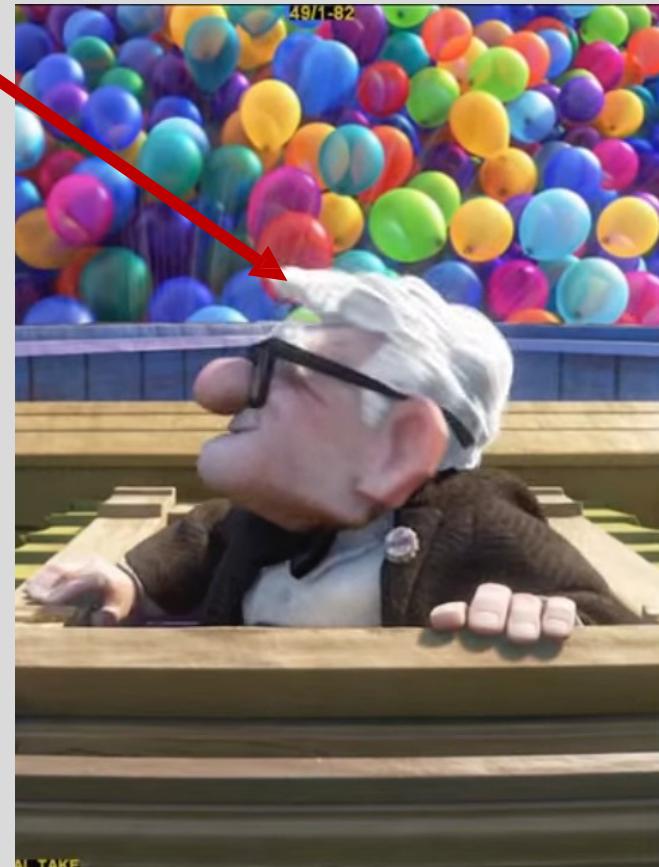
is the automatic process of generating a photorealistic or non-photorealistic image from a 2D or 3D model



Rendering

The rendering equation is an integral equation based on light and is very computationally demanding

Aliasing



Rendering

The rendering equation is an integral equation based on light and is very computationally demanding

Aliasing

Aliasing: the process by which smooth curves or lines become jagged due to the resolution of the graphics device or insufficient data to represent the curves

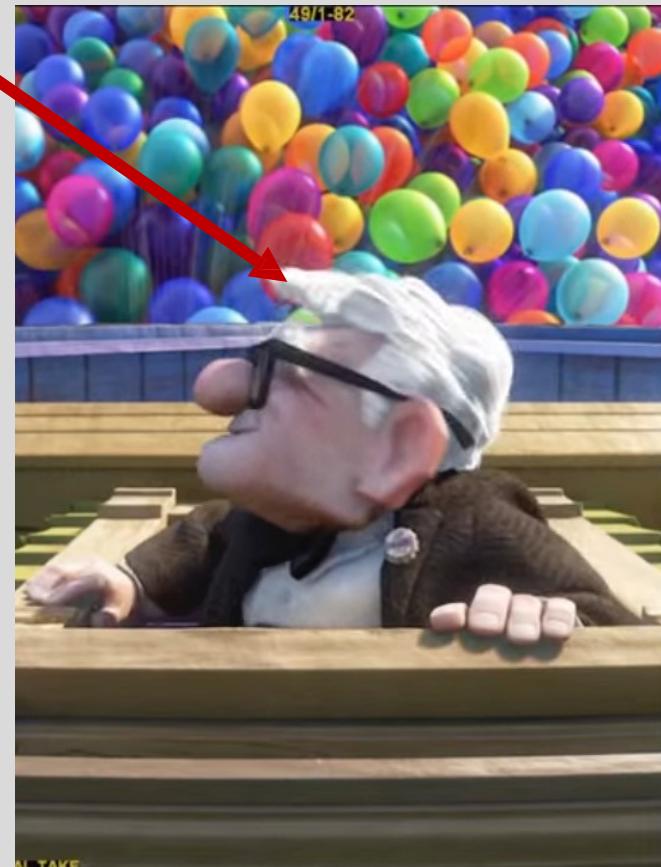


Rendering

The rendering equation is an integral equation based on light and is very computationally demanding

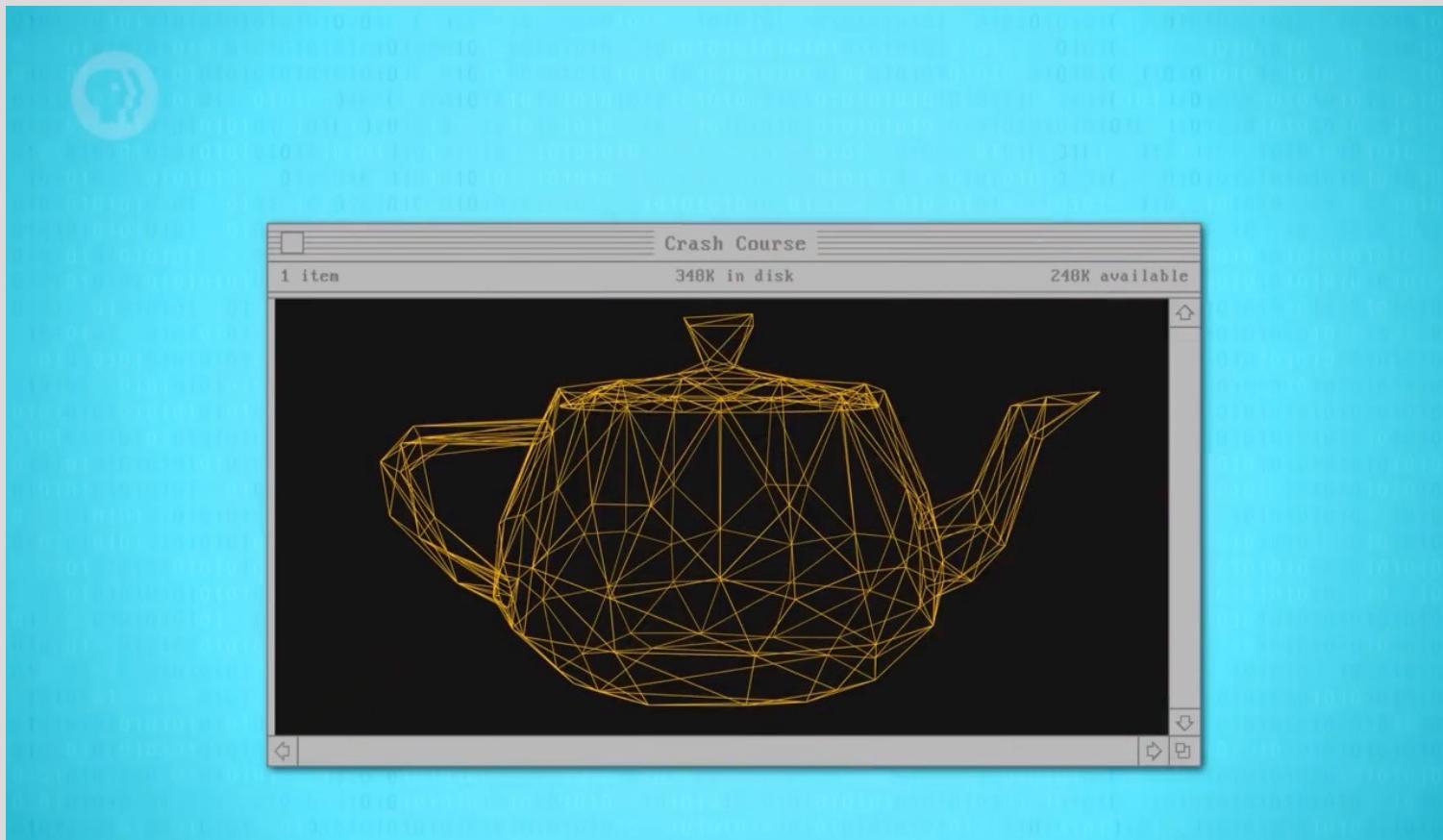
Aliasing

**Anti-aliasing is a technique
for minimizing the distortion
artefacts**



Rendering

The rendering equation is an integral equation based on light and is very computationally demanding



<https://www.youtube.com/watch?v=TEAtmCYYKZA>



CS3005: DIGITAL MEDIA AND GAMES

Questions?

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