

# Phong Illumination Model

## Diffuse Reflection

- Diffuse reflection is based on Lambert's cosine law, which states that the intensity of light is proportional to the cosine of the angle between the light direction  $\mathbf{l}$  and the surface normal  $\mathbf{n}$ .
- The intensity of light is higher if the angle is sharper.
- The dot product  $\mathbf{n} \cdot \mathbf{l}$  represents this cosine value, and I use max to ensure it is non-negative.
- $\mathbf{p} \cdot \mathbf{L}_{\text{light}}$  represents the final color of the object with light.

$$\mathbf{diffuse} = r_{\text{view}} \cdot \mathbf{p} \cdot \mathbf{L}_{\text{light}} \cdot \max(\mathbf{n} \cdot \mathbf{l}, 0.0)$$

## Ambient Reflection

- Ambient reflection represents the constant illumination of the object by the environment.
- It is usually a small constant value added to ensure that objects are visible even when not directly lit.
- Higher ambient strength means the entire object brightens up more by the same amount.

$$\mathbf{ambient} = \frac{1}{\pi} \cdot \mathbf{ambientStrength} \cdot \mathbf{p} \cdot \mathbf{L}_{\text{light}}$$

## Specular Reflection

- Specular reflection represents the mirror-like reflection of light sources on shiny surfaces.
- It does not use the object color ( $\mathbf{p}$ ) because specular highlights are typically the color of the light source.
- Higher shininess ( $m$ ) means a smaller specular highlight.
- It is based on the dot product between the view direction  $\mathbf{v}$  and the reflection direction  $\mathbf{r}$ , raised to the power of the shininess factor ( $m$ ).
- $s$  is the specular strength. Smaller specular strength means less intensity.

$$\mathbf{specular} = \mathbf{L}_{\text{light}} \cdot s \cdot \max(\mathbf{n} \cdot \mathbf{l}, 0.0) \cdot (\max(\mathbf{r} \cdot \mathbf{v}, 0.0))^m$$

## Final Color

Combine the three components to get the final color:

$$\mathit{finalColor} = \mathit{diffuse} + \mathit{specular} + \mathit{ambient}$$