

ASSIGNMENT #1

Using k-Nearest Neighbours, predict if a student will Pass(1) or Fail(0) based on:

- x_1 = hours studied
- x_2 = sleep hours

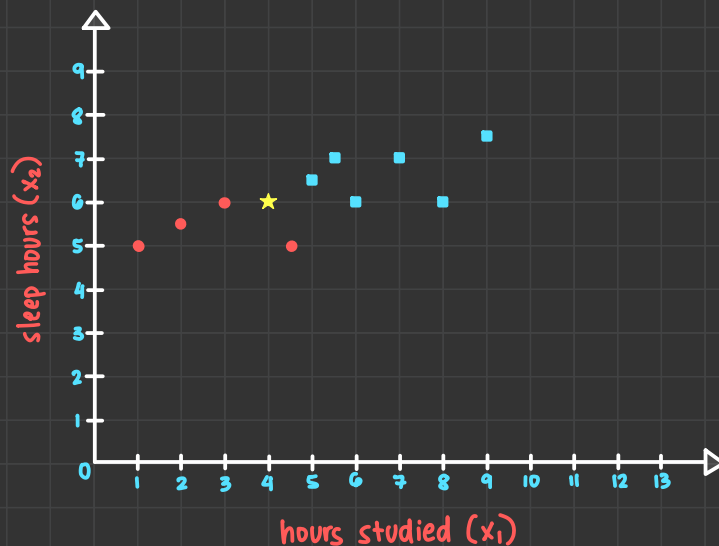
TRAINING DATA

STUDENT	HOURS STUDIED(x_1)	SLEEP HOURS(x_2)	PASS/FAIL(y)
1	1.0	5.0	0 (FAIL)
2	2.0	5.5	0 (FAIL)
3	3.0	6.0	0 (FAIL)
4	4.5	5.0	0 (FAIL)
5	5.0	6.5	1 (PASS)
6	5.5	7.0	1 (PASS)
7	6.0	6.0	1 (PASS)
8	7.0	7.0	1 (PASS)
9	8.0	6.0	1 (PASS)
10	9.0	7.5	1 (PASS)

TASK

A new student studied 4 hours and slept 6 hours. We want to predict whether they PASS or FAIL using KNN with $k=3$.

PLOT ALL DATA POINTS USING A SCATTER PLOT



COMPUTE DISTANCES

For the new student, compute the EUCLIDEAN DISTANCE from all data points

$$d = \sqrt{(x_1 - 4)^2 + (x_2 - 6)^2}$$

STUDENT	(X ₁)	(X ₂)	(Y)	EUCLIDEAN DISTANCE
1	1.0	5.0	0 (FAIL)	3.16
2	2.0	5.5	0 (FAIL)	2.06
3	3.0	6.0	0 (FAIL)	1.0
4	4.5	5.0	0 (FAIL)	1.12
5	5.0	6.5	1 (PASS)	1.12
6	5.5	7.0	1 (PASS)	1.80
7	6.0	6.0	1 (PASS)	2.0
8	7.0	7.0	1 (PASS)	3.16
9	8.0	6.0	1 (PASS)	4
10	9.0	7.5	1 (PASS)	5.22

SOLUTION:

$$d_1 = \sqrt{(1 - 4)^2 + (5 - 6)^2} = 3.16$$

$$d_2 = \sqrt{(2 - 4)^2 + (5.5 - 6)^2} = 2.06$$

$$d_3 = \sqrt{(3 - 4)^2 + (6 - 6)^2} = 1.0$$

$$d_4 = \sqrt{(4.5 - 4)^2 + (5 - 6)^2} = 1.12$$

$$d_5 = \sqrt{(5 - 4)^2 + (6.5 - 6)^2} = 1.12$$

$$d_6 = \sqrt{(5.5 - 4)^2 + (7 - 6)^2} = 1.80$$

$$d_7 = \sqrt{(6 - 4)^2 + (6 - 6)^2} = 2.0$$

$$d_8 = \sqrt{(7 - 4)^2 + (7 - 6)^2} = 3.16$$

$$d_9 = \sqrt{(8 - 4)^2 + (6 - 6)^2} = 4$$

$$d_{10} = \sqrt{(9 - 4)^2 + (7.5 - 6)^2} = 5.22$$

FIND THE 3 NEAREST NEIGHBORS

Highlight the rows with the 3 smallest distances

STUDENT	(X ₁)	(X ₂)	(Y)	EUCLIDEAN DISTANCE
1	1.0	5.0	0 (FAIL)	3.16
2	2.0	5.5	0 (FAIL)	2.06
3	3.0	6.0	0 (FAIL)	1.0
4	4.5	5.0	0 (FAIL)	1.12
5	5.0	6.5	1 (PASS)	1.12
6	5.5	7.0	1 (PASS)	1.80
7	6.0	6.0	1 (PASS)	2.0
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9	8.0	6.0	1 (PASS)	4
10	9.0	7.5	1 (PASS)	5.22

MAJORITY VOTE

- Count how many are PASS(1) and how many are FAIL(0)
 - PASS(1) = 1
 - FAIL(0) = 2
- Predict the outcome for the new student

A new student who studied 4 hours and slept 6 hours will **FAIL(0)** the exam

DISCUSSION QUESTION

1. What was your final prediction?

With $k=3$, my final prediction is that the new student who studied 4 hours and slept 6 hours will FAIL(0) the exam

2. How would the prediction change if we use $k=5$ instead of $k=3$

STUDENT	(x_1)	(x_2)	(y)	EUCLIDEAN DISTANCE
1	1.0	5.0	0 (FAIL)	3.16
2	2.0	5.5	0 (FAIL)	2.06
3	3.0	6.0	0 (FAIL)	1.0
4	4.5	5.0	0 (FAIL)	1.12
5	5.0	6.5	1 (PASS)	1.12
6	5.5	7.0	1 (PASS)	1.80
7	6.0	6.0	1 (PASS)	2.0
8	7.0	7.0	1 (PASS)	3.16
9	8.0	6.0	1 (PASS)	4
10	9.0	7.5	1 (PASS)	5.22

As you can see on the table, if we change the k value into $k=5$, the prediction will change. With $PASS(1)=3$ and $FAIL(0)=2$, the new student who studied 4 hours and slept 6 hours will PASS(1) the exam since the majority of nearest neighbors are PASS(1).