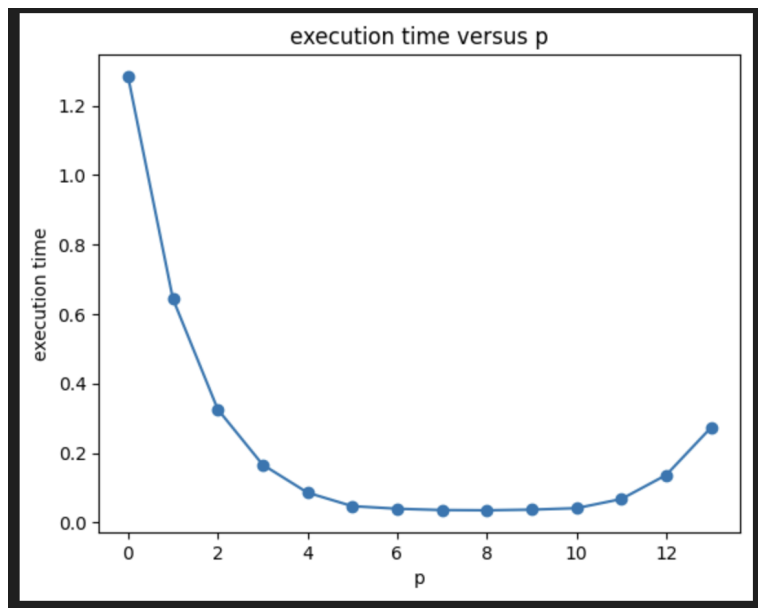


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CSCE-735  
DUE: 9-11-2023  
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1. Execute the code for  $n=108$  with  $p$  chosen to be  $2^k$ , for  $k = 0, 1, \dots, 13$ . Using the experimental data obtained from these experiments, answer the following questions. For plots, use a logarithmic scale for the x-axis.

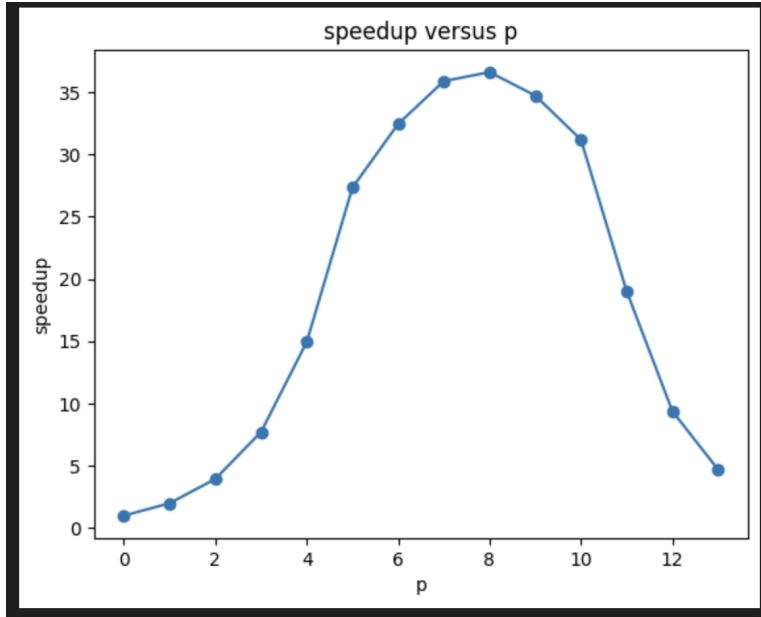
```
Trials = 100000000, Threads = 1, pi = 3.1416149600, error = 7.10e-06, time (sec) = 1.2843
Trials = 100000000, Threads = 2, pi = 3.1417022800, error = 3.49e-05, time (sec) = 0.6440
Trials = 100000000, Threads = 4, pi = 3.1415910800, error = 5.01e-07, time (sec) = 0.3258
Trials = 100000000, Threads = 8, pi = 3.1415947600, error = 6.70e-07, time (sec) = 0.1666
Trials = 100000000, Threads = 16, pi = 3.1415291200, error = 2.02e-05, time (sec) = 0.0860
Trials = 100000000, Threads = 32, pi = 3.1415901200, error = 8.06e-07, time (sec) = 0.0470
Trials = 100000000, Threads = 64, pi = 3.1413512400, error = 7.68e-05, time (sec) = 0.0396
Trials = 100000000, Threads = 128, pi = 3.1429299200, error = 4.26e-04, time (sec) = 0.0358
Trials = 100000000, Threads = 256, pi = 3.1412995200, error = 9.33e-05, time (sec) = 0.0351
Trials = 100000000, Threads = 512, pi = 3.1468450800, error = 1.67e-03, time (sec) = 0.0370
Trials = 100000000, Threads = 1024, pi = 3.1514026000, error = 3.12e-03, time (sec) = 0.0412
Trials = 100000000, Threads = 2048, pi = 3.1453611600, error = 1.20e-03, time (sec) = 0.0676
Trials = 100000000, Threads = 4096, pi = 3.1494162400, error = 2.49e-03, time (sec) = 0.1369
Trials = 100000000, Threads = 8192, pi = 3.1377031200, error = 1.24e-03, time (sec) = 0.2737
```

1.1. (10 points) Plot execution time versus  $p$  to demonstrate how time varies with the number of threads.



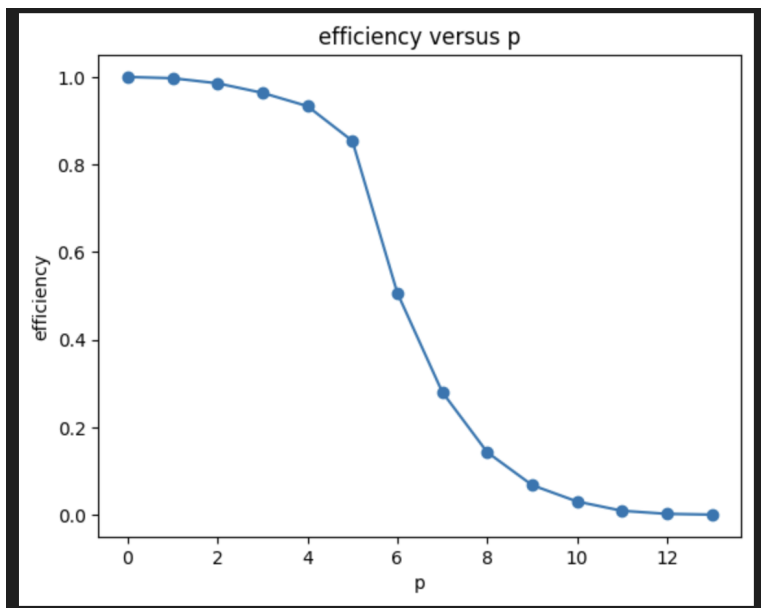
1.2. (10 points) Plot speedup versus  $p$  to demonstrate the change in speedup with  $p$ .

Speedup = [1.0, 1.994254658385093, 3.9419889502762433, 7.708883553421368, 14.933720930232559, 27.325531914893617, 32.43181818181818, 35.874301675977655, 36.58974358974359, 34.71081081081081, 31.17233009708738, 18.998520710059175, 9.381300219138057, 4.6923639020825725]



1.3. (5 points) Using the definition:  $\text{efficiency} = \text{speedup}/p$ , plot efficiency versus  $p$  to demonstrate how efficiency changes as the number of threads are increased.

Efficiency = [1.0, 0.9971273291925465, 0.9854972375690608, 0.963610444177671, 0.9333575581395349, 0.8539228723404255, 0.5067471590909091, 0.28026798184357543, 0.1429286858974359, 0.06779455236486487, 0.030441728610436893, 0.009276621440458582, 0.002290356498813002, 0.000572798327890939]



1.4. (5 points) In your experiments, what value of  $p$  minimizes the parallel runtime?

ANS: in my experiments, when  $p$  is 256 and  $k = 8$  minimizes the parallel runtime.

2. Repeat the experiments with  $n=10^{10}$  to obtain the execution time for  $p=2k$ , for  $k = 0, 1, \dots, 13$ .

Trials = 10000000000	Threads = 1	pi = 1.4236202260	error = 5.47e-01	time (sec) = 127.5424
Trials = 10000000000	Threads = 2	pi = 3.1416070092	error = 4.57e-06	time (sec) = 63.9059
Trials = 10000000000	Threads = 4	pi = 3.1416060276	error = 4.26e-06	time (sec) = 31.9454
Trials = 10000000000	Threads = 8	pi = 3.1416118228	error = 6.10e-06	time (sec) = 15.9876
Trials = 10000000000	Threads = 16	pi = 3.1416066896	error = 4.47e-06	time (sec) = 8.0048
Trials = 10000000000	Threads = 32	pi = 3.1416332068	error = 1.29e-05	time (sec) = 4.0086
Trials = 10000000000	Threads = 64	pi = 3.1416139092	error = 6.77e-06	time (sec) = 3.2660
Trials = 10000000000	Threads = 128	pi = 3.1415943424	error = 5.38e-07	time (sec) = 2.8004
Trials = 10000000000	Threads = 256	pi = 3.1416473120	error = 1.74e-05	time (sec) = 2.7011
Trials = 10000000000	Threads = 512	pi = 3.1415762012	error = 5.24e-06	time (sec) = 2.6941
Trials = 10000000000	Threads = 1024	pi = 3.1414319268	error = 5.12e-05	time (sec) = 2.6863
Trials = 10000000000	Threads = 2048	pi = 3.1412588724	error = 1.06e-04	time (sec) = 2.7007
Trials = 10000000000	Threads = 4096	pi = 3.1407169720	error = 2.79e-04	time (sec) = 2.7164
Trials = 10000000000	Threads = 8192	pi = 3.1412633928	error = 1.05e-04	time (sec) = 2.7735

2.1. (5 points) In this case, what value of  $p$  minimizes the parallel runtime?

ANS: in my experiments, when  $p$  is 1024 minimizes the parallel runtime.

2.2. (5 points) Do you expect the runtime to increase as  $p$  is increased beyond a certain value? If so, why? And is this observed in your experiments.

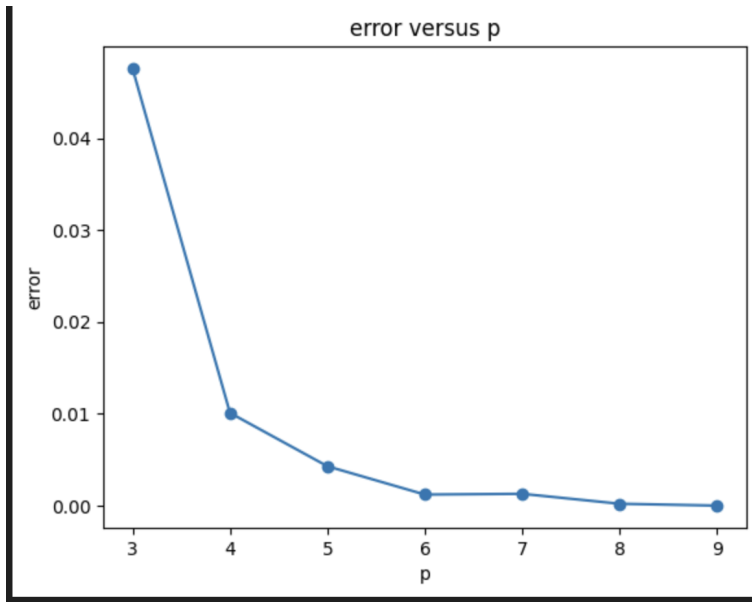
Yes, I expect the runtime to increase as  $p$  is increased beyond a certain value. There are two main issues will affect parallelism: partitioning and communication. Above two cases, we can see  $p = 256$  which is best for  $n = 10^8$ , and  $p = 1024$  which is best for  $n = 10^{10}$ . I think it will cause the issue because of limit number of tasks. Therefore, it will execute the task sequentially.

3. (5 points) Do you expect that there would be a difference in the number of threads needed to obtain the minimum execution time for two values of  $n$ ? Is this observed in your experiments.

Yes, I expect that there would be a difference in the number of threads needed to obtain the minimum execution time for two values of  $n$ . The different  $n$  value and thread  $p$  value will get the different execution time base on the problem 1 and problem 2 graph. When we increase threads, more tasks can be parallelized and can obtain the minimum execution time.

4. (5 points) Plot error versus  $n$  to illustrate accuracy of the algorithm as a function of  $n$ . You may have to run experiments with different values of  $n$ ; for example  $n$  could be chosen to be  $10^k$ , for  $k = 3, \dots, 9$ . Use  $p = 48$ .

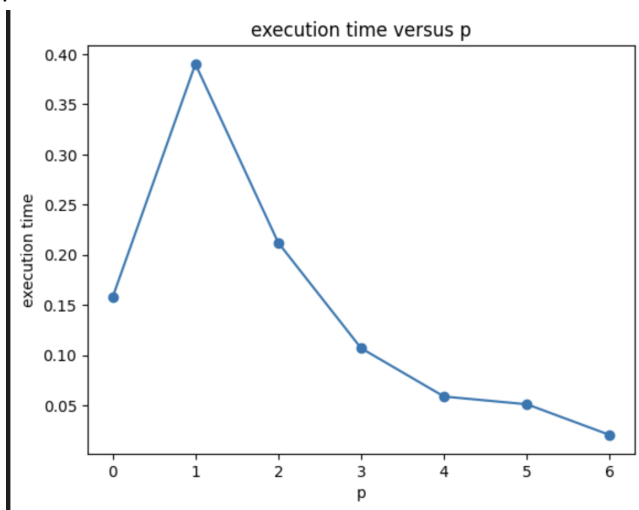
Trials = 1000	Threads = 48	pi = 2.9920000000	error = 4.76e-02	time (sec) = 0.0026
Trials = 10000	Threads = 48	pi = 3.1732000000	error = 1.01e-02	time (sec) = 0.0017
Trials = 100000	Threads = 48	pi = 3.1550800000	error = 4.29e-03	time (sec) = 0.0018
Trials = 1000000	Threads = 48	pi = 3.1453960000	error = 1.21e-03	time (sec) = 0.0020
Trials = 10000000	Threads = 48	pi = 3.1456372000	error = 1.29e-03	time (sec) = 0.0068
Trials = 100000000	Threads = 48	pi = 3.1409400400	error = 2.08e-04	time (sec) = 0.0325
Trials = 1000000000	Threads = 48	pi = 3.1416179080	error = 8.04e-06	time (sec) = 0.2802



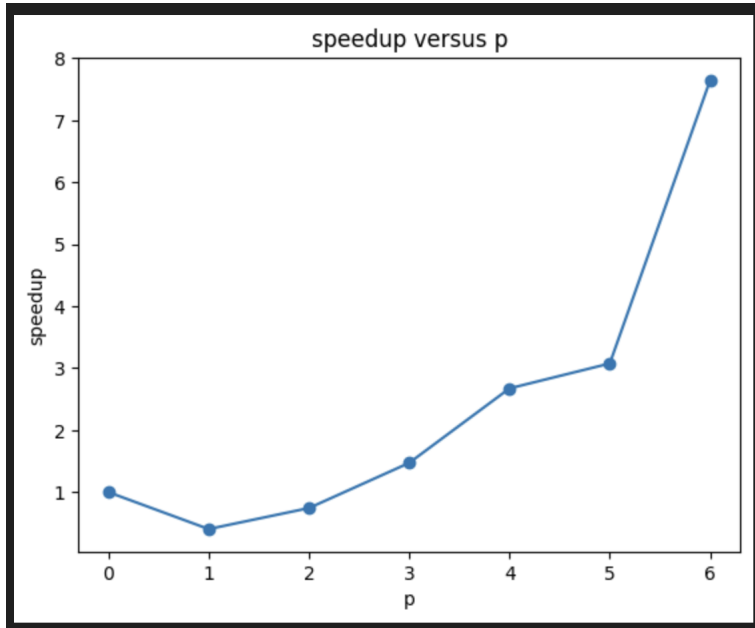
5. Execute the code for  $n=108$  with  $p$  chosen to be  $2k$ , for  $k = 0, 1, \dots, 6$ . Specify  $\text{ntasks-per-node}=4$  in the job file. Using the experimental data obtained from these experiments, answer the following questions. For plots, use a logarithmic scale for the x-axis.

```
Processes = 1
n = 100000000, p = 1, pi = 3.1415926535904264, relative error = 2.02e-13, time (sec) = 0.1575
Processes = 2
n = 100000000, p = 2, pi = 3.1415926535900223, relative error = 7.29e-14, time (sec) = 0.3901
Processes = 4
n = 100000000, p = 4, pi = 3.1415926535902168, relative error = 1.35e-13, time (sec) = 0.2121
Processes = 8
n = 100000000, p = 8, pi = 3.1415926535896137, relative error = 5.71e-14, time (sec) = 0.1070
Processes = 16
n = 100000000, p = 16, pi = 3.1415926535897754, relative error = 5.65e-15, time (sec) = 0.0589
Processes = 32
n = 100000000, p = 32, pi = 3.1415926535897736, relative error = 6.22e-15, time (sec) = 0.0512
Processes = 64
n = 100000000, p = 64, pi = 3.1415926535897940, relative error = 2.83e-16, time (sec) = 0.0206
```

5.1. (10 points) Plot execution time versus  $p$  to demonstrate how time varies with the number of processes.

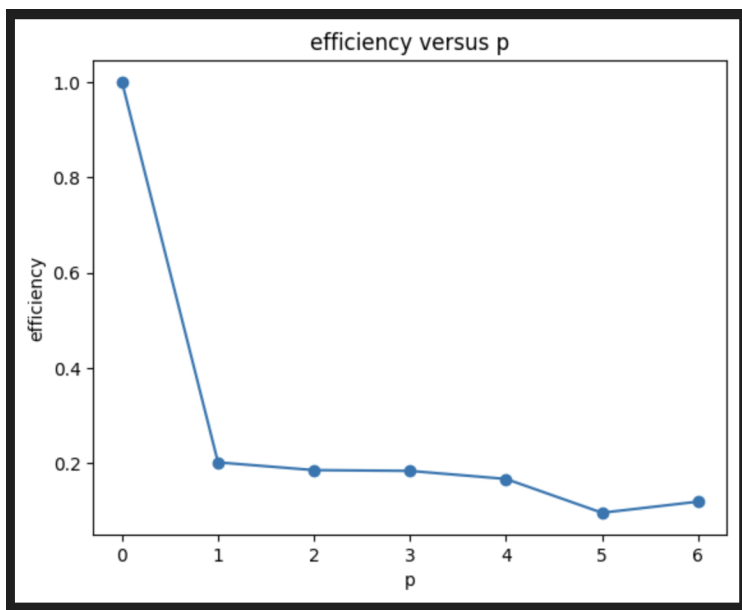


5.2. (10 points) Plot speedup versus  $p$  to demonstrate the change in speedup with  $p$ .  
Speedup = [[1.0, 0.40374263009484745, 0.7425742574257426, 1.47196261682243, 2.67402376910017, 3.076171875, 7.645631067961165]]



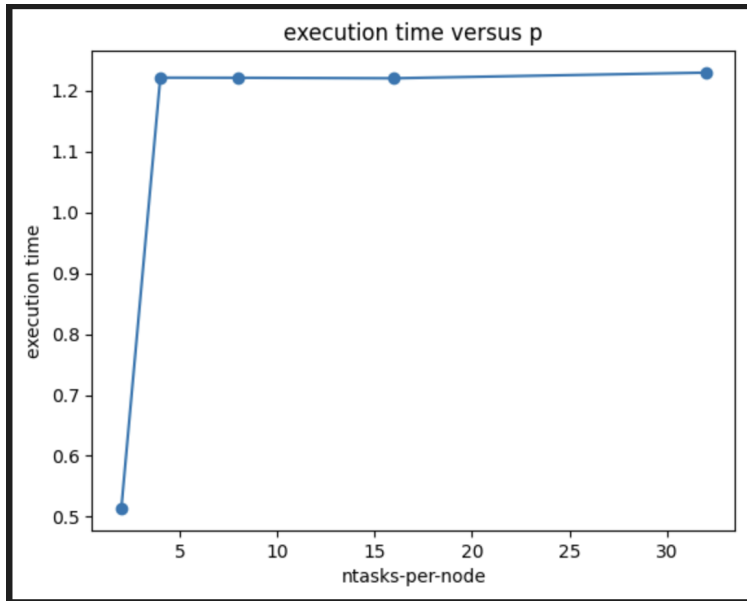
5.3. (5 points) Using the definition:  $\text{efficiency} = \text{speedup}/p$ , plot efficiency versus  $p$  to demonstrate how efficiency changes as the number of processes is increased.

Efficiency = [[1.0, 0.20187131504742373, 0.18564356435643564, 0.18399532710280375, 0.1671264855687606, 0.09613037109375, 0.11946298543689321]]



5.4. (5 points) What value of  $p$  minimizes the parallel runtime?  
When value of  $p$  is 64, it minimizes the parallel runtime.

6. (10 points) With  $n=1010$  and  $p=64$ , determine the value of  $\text{ntasks-per-node}$  that minimizes the `total_time`. Plot time versus  $\text{ntasks-per-node}$  to illustrate your experimental results for this question.  
When  $\text{ntasks-per-node}$  is 2, it minimizes the total time.  
 $\text{Ntasks-per-node}: 2, 4, 8, 16, 32$

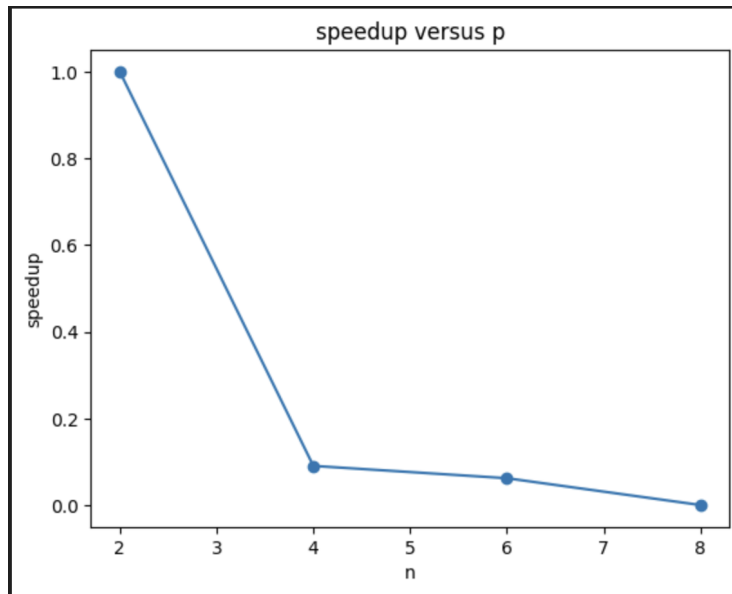


7. Execute the code with  $p=64$  for  $n=10^2$ ,  $10^4$ ,  $10^6$  and  $10^8$ , with  $\text{ntasks-per-node}=4$ .

```
10^2
n = 100, p = 64, pi = 3.1416009869231249, relative error = 2.65e-06, time (sec) = 0.0033
10^4
n = 10000, p = 64, pi = 3.1415926544231265, relative error = 2.65e-10, time (sec) = 0.0017
10^6
n = 1000000, p = 64, pi = 3.1415926535898753, relative error = 2.62e-14, time (sec) = 0.0040
10^8
n = 100000000, p = 64, pi = 3.1415926535897940, relative error = 2.83e-16, time (sec) = 0.0151
```

7.1. (5 points) Plot the speedup observed as a function of  $n$  on  $p=64$  w.r.t.  $p=1$ . You will need to obtain execution time on  $p=1$  for  $n=10^2$ ,  $10^4$ ,  $10^6$  and  $10^8$ .

```
10^2
n = 100, p = 1, pi = 3.1416009869231254, relative error = 2.65e-06, time (sec) = 0.0001
10^4
n = 10000, p = 1, pi = 3.1415926544231341, relative error = 2.65e-10, time (sec) = 0.0011
10^6
n = 1000000, p = 1, pi = 3.1415926535897643, relative error = 9.19e-15, time (sec) = 0.0016
10^8
n = 100000000, p = 1, pi = 3.1415926535904264, relative error = 2.02e-13, time (sec) = 0.1542
```



7.2. (5 points) Plot the relative error versus  $n$  to illustrate the accuracy of the algorithm as a function of  $n$ .

