

Swimmer Environment - RLGlue Implementation

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1 State

In the current implementation of the environment, the state is stored in a double array l of size $2n + 4$, where n is the number of segments.

- A_0 , position of the swimmer head, is stored in l_0, l_1 .
- \dot{A}_0 , velocity of the swimmer head, is stored in l_2, l_3 .
- θ_i , the angle i at the beginning of the segment i , is stored in l_{3+i} , for $i \in \{1, \dots, n\}$.
- $\dot{\theta}_i$, the first derivative of the angle i at the beginning of the segment i , is stored in l_{3+n+i} , for $i \in \{1, \dots, n\}$.

2 Solving dynamics equations

2.1 Variables

- n is the number of segments.
- θ_i is the angle i at the beginning of the segment i , for $i \in \{1, \dots, n\}$. See the figure in Remy's paper.
- G_i is the mass center of the segment i , for $i \in \{1, \dots, n\}$.

2.2 Unknowns

The goal is to compute the following unknowns:

- n unknowns of dimension 1: $\ddot{\theta}_1, \ddot{\theta}_2, \dots, \ddot{\theta}_n$
- $n + 1$ unknowns of dimension 2: $\vec{f}_0, \vec{f}_1, \dots, \vec{f}_n$
- n unknowns of dimension 2: $\vec{G}_1, \vec{G}_2, \dots, \vec{G}_n$

Let $X \in \mathbb{R}^{5n+2}$ be the unknown vector encoding all the unknown variables. We index the components of this vector from 0 to $5n + 1$:

- $\ddot{\theta}_i$ corresponds to $X[i-1]$ for $i \in \{1, \dots, n\}$
- \vec{f}_i corresponds to $\begin{pmatrix} X[n+2i] \\ X[n+2i+1] \end{pmatrix}$ for $i \in \{0, \dots, n\}$
- \ddot{G}_i corresponds to $\begin{pmatrix} X[3n+2i] \\ X[3n+2i+1] \end{pmatrix}$ for $i \in \{1, \dots, n\}$

2.3 Equations

Since $X \in \mathbb{R}^{5n+2}$, we need to write $5n+2$ equations. From Remy's model in part B.4.3, we have the following equations.

- Equations 0 to $n-1$: for $i \in \{1, \dots, n\}$

$$m_i \frac{l_i}{12} \ddot{\theta}_i - l_i (\cos \theta_i (f_i^y + f_{i+1}^y) - \sin \theta_i (f_i^x + f_{i+1}^x)) = \mathcal{M}_i - u_i + u_{i-1} \quad (1)$$

- Equations n to $3n+3$: for $i \in \{1, \dots, n\}$:

$$\vec{f}_0 = 0 \quad (2)$$

$$\vec{f}_{i-1} - \vec{f}_i + m_i \ddot{G}_i = \vec{F}_i \quad (3)$$

$$\vec{f}_n = 0 \quad (4)$$

- Equations $3n+4$ to $5n+1$: for $i \in \{1, \dots, n-1\}$:

$$\begin{aligned} -\ddot{G}_{i+1} + \ddot{G}_i + \frac{l_i}{2} \ddot{\theta}_i \begin{pmatrix} -\sin \theta_i \\ \cos \theta_i \end{pmatrix} + \\ \frac{l_i}{2} \ddot{\theta}_{i+1} \begin{pmatrix} -\sin \theta_{i+1} \\ \cos \theta_{i+1} \end{pmatrix} = \frac{l_i}{2} \dot{\theta}_i^2 \begin{pmatrix} \cos \theta_i \\ \sin \theta_i \end{pmatrix} + \frac{l_i}{2} \dot{\theta}_{i+1}^2 \begin{pmatrix} \cos \theta_{i+1} \\ \sin \theta_{i+1} \end{pmatrix} \end{aligned} \quad (5)$$

which is the second derivative of the following equations:

$$G_{i+1} = G_i + \frac{l_i}{2} \begin{pmatrix} \cos \theta_i \\ \sin \theta_i \end{pmatrix} + \frac{l_i}{2} \begin{pmatrix} \cos \theta_{i+1} \\ \sin \theta_{i+1} \end{pmatrix} \quad (6)$$

Using the same indices of the unknowns as X , left members of the previous equations are stored in $A \in \mathbb{R}^{(5n+2) \times (5n+2)}$, right members of the previous equations are stored in $B \in \mathbb{R}^{5n+2}$.

Thus, we have the relation $AX = B$, and solving the linear system is done by using $X = A^{-1}B$.