

# Hot-Electron Emission for Spectral Calibration

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Hot-electron thermal emission in graphite was studied as a broadband UV-VIS calibration source. Emission spectra under ultrafast excitation were compared to a two-temperature model with Planck's law. Derived spectrometer efficiencies matched expectations apart from stronger UV roll-off, attributed to sample absorption. Sensitivity analysis identified absorption depth and cooling time as dominant uncertainties. Calibration with a traceable spectrometer is recommended to validate the models accuracy. And selection of a material with a flatter absorption curve to increase the models accuracy.

Available at [www.github.com/leoole100/projekt-praktikum](https://www.github.com/leoole100/projekt-praktikum).

## 1 Introduction

Accurate spectral measurements require knowledge of an instrument’s spectral response—how efficiently the system transmits and detects light as a function of wavelength. The system response must be determined against a known reference and applied as a correction.

This work targets the ultraviolet (UV), where suitable calibration sources are limited. Deuterium lamps are the practical secondary standard in the UV (optionally combined with tungsten–halogen to bridge into the VIS–NIR), yet their spectral irradiance is sharply wavelength dependent and subject to aging and stability issues. In addition, they require periodic recalibration and careful handling, which adds cost and maintenance burden to UV calibration workflows. Primary radiometric scales are realized using high-temperature graphite-cavity blackbodies operated near  $\sim 3500\text{ K}$  and propagated via secondary calibrated transfer standards to working instruments [1, 2].

As an alternative to a source-based procedure, a calibrated, near-flat detector can be used as a secondary standard; this approach has been demonstrated in practice and can substitute the lamp in suitable setups [3].

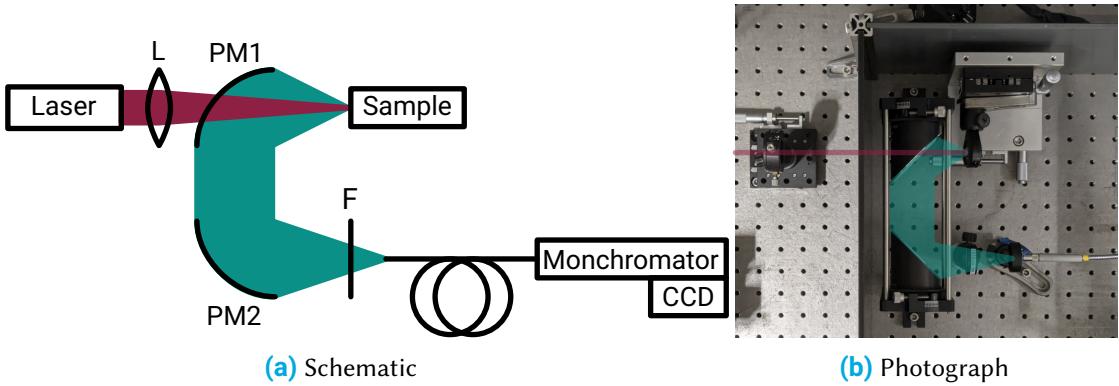
Motivated by these constraints, we explore thermal radiation from hot electrons in solids as a broadband reference. Under ultrafast excitation, the electronic subsystem can reach effective temperatures of several thousand K on picosecond time scales [4], producing smooth, thermal-like emission that spans the UV–VIS. Because the spectrum is broadband, predictable from basic physics, and largely free from narrow spectral features, hot-electron emission offers one of the most straightforward routes to generating stable UV reference light—potentially replacing deuterium lamps where a low-maintenance source is desirable. If stability, reproducibility, and an absolute radiometric scale can be established, hot-electron emission could offer a UV calibration route that competes with deuterium lamps while avoiding their spectral non-flatness.

## 2 Theory

To obtain the spectral shape, the ultrafast absorption and subsequent thermal emission is modelled with a zero-dimensional (lumped) two-temperature picture for the probed volume. The probed volume is approximated as the excited spot area times the optical absorption depth,  $V_{\text{probe}} \approx A_{\text{spot}} d_{\text{abs}}$ . A short laser pulse deposits power  $P(t)$  into the electronic system, which rapidly thermalizes; electron–phonon coupling then cools the electrons toward the lattice temperature  $T_l$  [5]. Neglecting transport and other slow losses on the picosecond timescale, the electron temperature  $T_e(t)$  obeys

$$\frac{dT_e}{dt} = -\frac{T_e - T_l}{g} + \frac{P(t)}{C_e(T_e)}. \quad (1)$$

Here  $C_e(T_e)$  is the electronic heat capacity of the probed volume (units J/K),  $g$  is the electron–phonon energy-relaxation time,  $T_l$  is the lattice temperature (taken approximately constant over this window since typically  $C_l \gg C_e$ ), and  $P(t)$  is the laser power deposited in the probed volume (units W).



**Figure 1** Experimental setup used to measure thermal emission from ultrafast-excited hot electrons. The schematic shows the optical path and key components; the photograph shows the arrangement inside the chamber.

Because the instantaneous radiant exitance scales with  $T^4$  (Stefan–Boltzmann law), the emission is dominated by the high-temperature portion of  $T_e(t)$  immediately after excitation; the later, lower-temperature evolution contributes comparatively little. This justifies treating  $T_l$  as constant and using the simplified dynamics above when we are interested in the relative spectral shape rather than absolute irradiance. [6]

To map  $T_e(t)$  to the emitted spectrum we use Planck's law. The blackbody spectral radiance is

$$B(\lambda, T) = \frac{2hc^2}{\lambda^5} \frac{1}{\exp(\frac{hc}{\lambda k_B T}) - 1}. \quad (2)$$

Here  $B$  has the units  $\text{W m}^{-2} \text{sr}^{-1} \text{nm}^{-1}$ . The emissivity is assumed to be unity, as is commonly done for the material used here [2].

The quantity compared to the measurement is the spectral power density  $P(\lambda)$  in  $\text{W nm}^{-1}$ . We obtain it from radiance by multiplying with the illuminated spot area  $A_{\text{spot}}$  and the collection solid angle  $\Omega_{\text{coll}}$  (emission approximated as constant within the collection cone) and integrating over the exposure window:

$$P(\lambda) = A_{\text{spot}} \Omega_{\text{coll}} \int B(\lambda, T_e(t)) dt. \quad (3)$$

### 3 Experimental Setup

The experimental setup, originally developed by Leon Roob [6], is shown in Figure 1. It is designed to measure broadband thermal emission from hot electrons in graphite using reflective collection optics and a fibre-coupled spectrometer.

The excitation source is a PHAROS PH1-20 (Light Conversion) at a centre wavelength of 1030 nm, with pulse duration 250 fs (FWHM) and repetition rate 40 kHz. The pulse energy is 7.5  $\mu\text{J}$  (average power 300 mW). The beam is stabilised in four axes and expanded to a diameter of  $D = 5$  mm before entering the chamber.

Parameter	Symbol	Value
Average laser power	$P_{\text{avg}}$	300(5) mW
Repetition rate	$f_{\text{rep}}$	40 kHz
Pulse duration	$\tau_{\text{fwhm}}$	250(50) fs
Spot diameter on sample <sup>1</sup>	$d_{\text{spot}}$	$50^{+20}_{-0}$ $\mu\text{m}$
Optical absorption depth	$d_{\text{abs}}$	200(100) nm [7]
Cooling time constant	$g$	250(50) fs [8]
Electronic heat capacity	$C_e(T_e)$	$\text{J m}^{-3}\text{K}^{-2}$ [9]
Lattice (ambient) temperature	$T_l$	300 K

**Table 1** Model parameters used in the spectrum calculation. Uncertainties in  $1\sigma$ .

Inside the chamber, a plano-convex lens with focal length  $f = 200$  mm focuses the beam onto the sample. Using the standard diffraction estimate  $d \approx 4\lambda f/\pi D$ , the expected spot diameter is  $\gtrsim 50 \mu\text{m}$ .

The target is a graphite sample mounted on a three-axis translation stage. Thermal emission from the irradiated spot is collected by two off-axis parabolic mirrors (UV-enhanced aluminium). The first mirror (PM1,  $f = 50$  mm) collimates the emission; the second (PM2,  $f = 101$  mm) focuses it onto a band-pass filter and into a multimode fibre with a 200  $\mu\text{m}$  core (Ocean Optics QP200-2-SR-BX). The magnification is  $M = f_{\text{PM2}}/f_{\text{PM1}} \approx 2$ , yielding an image spot of  $\sim 100 \mu\text{m}$  at the fibre entrance, comfortably within the core.

The fibre feeds an Acton SpectraPro 300i monochromator equipped with a 150 lines  $\text{mm}^{-1}$  grating blazed at 500 nm. The dispersed spectrum is detected by an Andor iXon<sup>EM+</sup> 897 EMCCD operated in vertical binning mode, effectively serving as a 1D line detector. Wavelength calibration (performed once following the manufacturer's procedure [6]) was stable throughout the measurements.

For alignment and maximal throughput, the lens, sample, and fibre ferrule are mounted on independent precision translation stages, while PM1 and PM2 are fixed on the common optical axis.

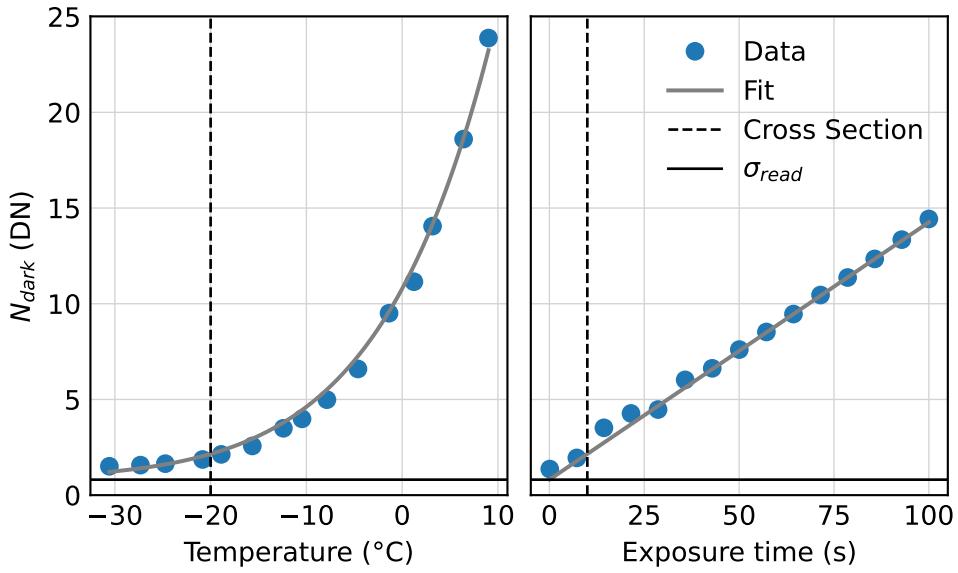
## 4 Methods

### 4.1 Model

We obtain the electron temperature trajectory  $T_e(t)$  by numerically integrating the ODE in the Theory section (Equation 1), using a Gaussian pulse for  $P(t)$  with per-pulse energy  $E_p = P_{\text{avg}}/f_{\text{rep}}$ . The time step  $\Delta t$  and integration window were chosen such that further refinement did not change the resulting spectrum appreciably. The parameters used are listed in Table 1.

The modeled spectral power density is then computed by inserting  $T_e(t)$  into Planck's law (Equation 3) and integrating numerically over time.

To estimate uncertainties, the parameters in Table 1 were sampled within their stated  $1\sigma$  ranges, the spectrum recomputed for each draw, and for each wavelength the mean and stan-



**Figure 2** Dark noise vs. sensor temperature and exposure time. Fit yields  $E = 0.597(4)$  eV and  $\sigma_{\text{read}} = 0.81(12)$  e<sup>-</sup>.

dard deviation reported.

#### 4.2 Noise and detector considerations

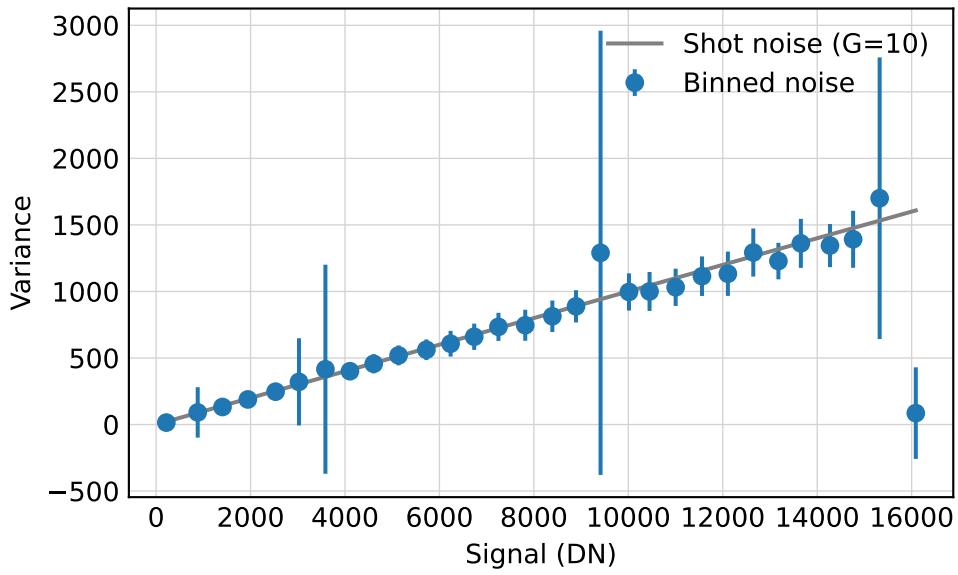
Detecting the weak thermal radiation from hot electrons requires careful optimisation of the signal-to-noise ratio (SNR). In this setup the dominant noise sources originate from the detector; laser power fluctuations and mechanical variations are treated as negligible. The EMCCD mechanisms are well documented by Andor [10, 11] and standards [12].

**Readout noise.** This is the fundamental noise from charge transfer and A/D conversion. For the present camera, the fit in Figure 2 yields a constant read noise of  $\sigma_{\text{read}} = 0.81(12)$  DN, consistent with the manufacturer's specification [13]. Because read noise is applied per read out bin, hardware binning (1D line-detector mode) reduces its impact by summing signal prior to the single read.

**Dark current noise.** Thermally generated charge scales with temperature and time,  $N_{\text{dark}} \propto \exp(-E/kT) t_{\text{exp}}$ . Figure 2 shows the measured dependence; fitting gives an effective activation energy  $E = 0.597(4)$  eV. With the sensor cooled to  $-80$  °C, the dark contribution is negligible at the exposure times used.

**Clock-induced charge (CIC).** CIC is created during high-speed clocking. Its apparent contribution grows with electron multiplication gain, so *EM gain is disabled* in this work (signal levels are well above the read-noise floor), which keeps CIC negligible [11].

**Shot noise and photon-transfer method.** Under these optimised conditions the dominant term is shot noise. Incident photons create photoelectrons with quantum efficiency  $\eta$ , so  $N_e =$



**Figure 3** Measured noise vs. signal (photon-transfer curve) demonstrating shot-noise-limited operation; the linear slope yields the conversion gain  $G$ .

$\eta N_{\text{photons}}$  and, for Poisson statistics,  $\text{var}(N_e) = N_e$  [12]. Let  $G$  denote the system conversion gain (DN per electron). The measured signal in data numbers (DN) is  $S = G N_e$ , and the measured variance becomes  $\sigma_{\text{meas}}^2 = \sigma_{\text{read}}^2 + G S$ . Thus a plot of variance vs. mean (photon-transfer curve) is linear in the shot-noise regime with slope  $G$ . Figure 3 shows this behaviour; from the slope  $G \approx 10 \text{ DN}/e^-$  can be measured. Note that this procedure does *not* determine  $\eta$ ; it only gives the DN-to-electron conversion.

**Practical settings for reproducibility.** (1) Keep the camera at  $\leq -80^\circ\text{C}$ ; (2) use vertical binning to treat the EMCCD as a 1D detector; (3) disable EM gain to avoid CIC and excess-noise-factor penalties; (4) fix slit width and exposure during noise characterisation; (5) verify the shot-noise regime by measuring  $\sigma^2$  vs.  $S$  and confirming linearity and slope  $G$

#### 4.3 Focusing and alignment

The aim is to image the excited spot on the sample onto the spectrometer fibre with maximal throughput. Parabolic mirrors (PM1/PM2) remain fixed once set; all focusing is done with the lamp, fibre/spectrometer port, and sample stages.

1. **Initial setup with a fiber coupled lamp.** Remove the sample and place a fiber-coupled lamp at the sample position. This will help align and focus the optics using visible light.
2. **Align the beam.** Adjust the lamp position and the parabolic mirrors so that the beam appears circular and sharply focused at the spectrometer fiber port. This ensures the optics are approximately aligned.
3. **Connect and optimize with spectrometer.** Connect the spectrometer to the spec-

trometer port and move the holder to maximize the signal roughly. Use the micrometer screws on the sample stage for fine adjustments.

4. **Swap back in the sample.** Replace the lamp with the sample at the same position. Connect the lamp output to the spectrometer port to illuminate the sample.
5. **Fine-focus the sample.** Adjust the sample position to minimize the size of the visible spot on the sample.
6. **Focus the infrared laser.** Turn on the infrared laser and use an IR detection card to locate and focus the beam onto the sample. The white light and the IR be collinear.
7. **Optimize laser alignment.** Replace the lamp with the spectrometer and monitor the reflected laser signal on the spectrometer. Fine-tune the laser focus to maximize this signal.

#### 4.4 Data processing

All raw spectra were first corrected by subtracting a dark frame recorded with identical acquisition settings, removing the fixed electronic bias and dark current. Residual peaks at the fundamental and harmonic wavelengths of the pump laser, normally suppressed by laser line filters, were present due to the absence of suitable optical filtering. These peaks were identified and removed digitally, leaving gaps in the plotted spectra where the affected bins were excluded.

The corrected signal  $S(\lambda)$  in DN was converted to spectral power density  $P_{\text{meas}}(\lambda)$  via

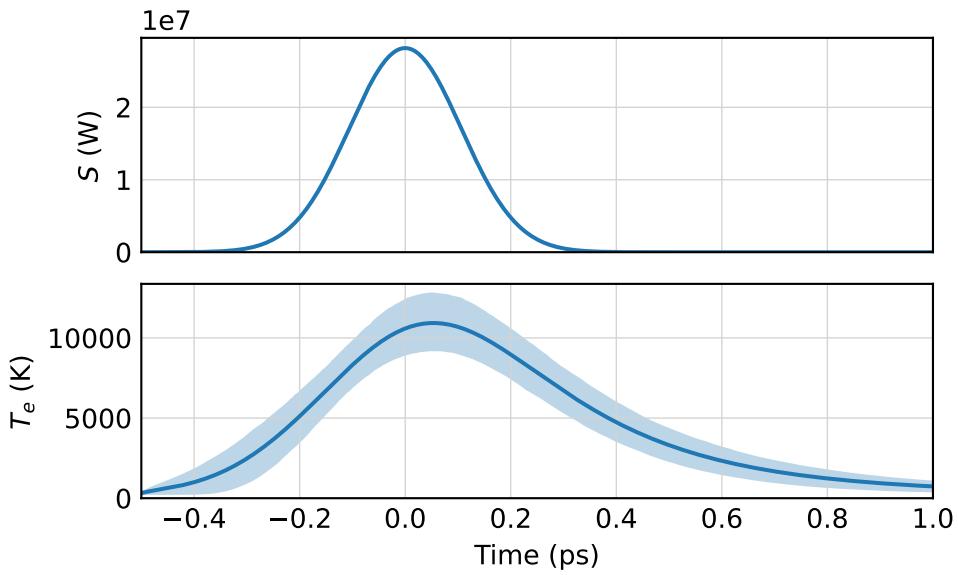
$$P_{\text{meas}}(\lambda) = \frac{S(\lambda)}{G t_{\text{exp}}} \frac{hc}{\Delta\lambda}, \quad (4)$$

with  $G$  the DN/ $e^-$  conversion gain,  $t_{\text{exp}}$  the exposure time, and  $\Delta\lambda$  the spectral bin width.

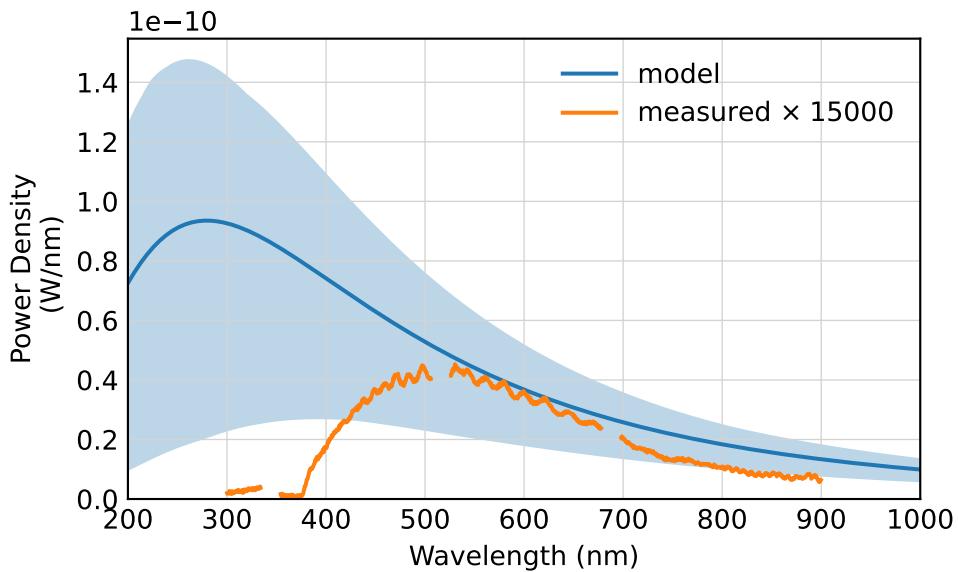
## 5 Results and Discussion

The time evolution of the electron temperature  $T_e(t)$ , obtained by solving the ODE in [Equation 1](#) with the parameters from [Table 1](#), is shown in [Figure 4](#). A Gaussian pump pulse drives a rapid temperature rise, followed by electron–phonon cooling on the timescale  $g$ . The shaded band indicates the propagated  $1\sigma$  uncertainty from the Monte Carlo analysis. The inferred peak temperature is 8500(2500) K.

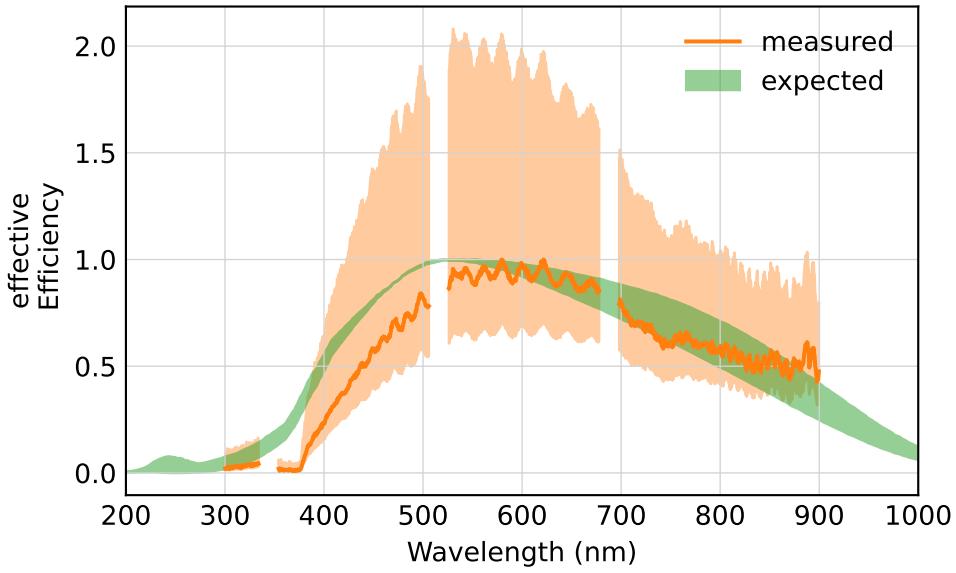
Using  $T_e(t)$  as input to Planck’s law ([Equation 2](#)), the modelled spectral power density  $P_{\text{model}}(\lambda)$  is computed and compared with the measured spectrum in [Figure 5](#). The measured spectrum  $P_{\text{measured}}(\lambda)$  is significantly lower in absolute scale than the model; for visual comparison, it is scaled to match the model peak. The measured spectrum is also narrower, consistent with the finite sensitivity window determined by the Si detector quantum efficiency and the blazed-grating envelope.



**Figure 4** Gaussian pump  $S$  and computed electron temperature  $T_e(t)$  from the lumped two-temperature model (parameters in Table 1). The fast rise is followed by electron–phonon cooling with time constant  $g$ . The shaded band shows the  $1\sigma$  Monte Carlo uncertainty.



**Figure 5** Measured spectral power density  $P_{\text{measured}}(\lambda)$  compared with the model spectrum. The measurement is scaled to match the model. The measured peak is narrower than the model, consistent with the instrument's finite sensitivity window.



**Figure 6** Effective efficiency (peak-normalised) from  $P_{\text{meas}}(\lambda)/P_{\text{model}}(\lambda)$ . The overlay shows the expected relative efficiency from component specifications (camera QE  $\times$  blazed-grating model). The shaded range reflects the  $1\sigma$  uncertainty of the model parameters and the uncertainty in the blaze parameters. The measured curve shows stronger roll-off at both band edges and oscillations over wavelength.

The effective efficiency is obtained by taking the wavelength-wise ratio

$$\eta(\lambda) = \frac{P_{\text{meas}}(\lambda)}{P_{\text{model}}(\lambda)}$$

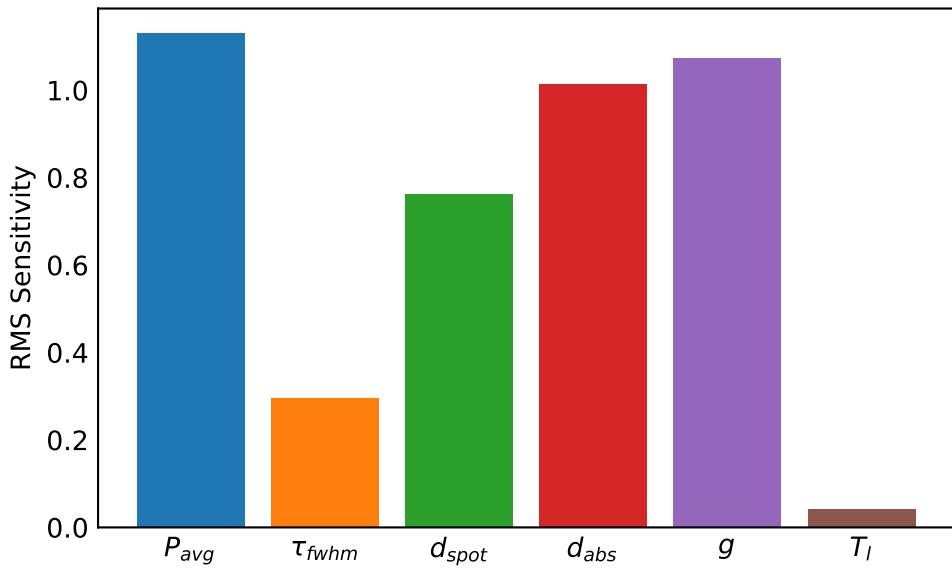
and normalising it to unity at the peak (Figure 6). The expected curve is calculated from the manufacturer’s QE data for the camera when new [13], multiplied by a blazed-grating efficiency model [14]; the shaded interval reflects uncertainty in the blaze parameters.

The measured efficiency declines more rapidly than expected in the UV region. This could result from aging and partial degradation of the UV-enhancing anti-reflection coating on the CCD sensor. However, a more likely explanation is inaccuracy in the model due to neglecting the material’s absorption spectrum, which rises steeply in the UV [7].

The uncertainty in the measured efficiency is high, primarily due to the large uncertainty in the modelled spectrum. To assess how the model uncertainty depends on its inputs, the sensitivity of the model to each parameter is calculated. The dimensionless sensitivity of a function  $f(a)$  to a parameter  $a$  is defined as

$$\frac{\partial f(a)}{\partial a} \cdot \frac{a}{f(a)},$$

corresponding to the fractional change in  $f$  per fractional change in  $a$ . This is computed for each wavelength of  $P(\lambda)$ , and the root-mean-square is taken over wavelength. Results are shown in Figure 7.



**Figure 7** Root-mean-square sensitivity of  $P(\lambda)$  to the model parameters.

The model is most sensitive to the average power input  $P_{avg}$ , the optical absorption depth  $d_{abs}$ , and the cooling time constant  $g$ . Sensitivity to the lattice temperature  $T_l$  is low, as expected. While  $P_{avg}$  and the excitation spot size can be measured accurately,  $d_{abs}$  and  $g$  are sample-dependent and thus represent the limiting factors for calibration accuracy.

## 6 Conclusion

Hot-electron thermal emission in graphite was investigated as a potential broadband UV–VIS calibration source. The measured spectrum was qualitatively reproduced by a two-temperature model, though the absolute scale was overestimated and the measured bandwidth was narrower due to the detector’s finite sensitivity range. The derived spectrometer efficiency agreed in overall shape with expectations but showed stronger UV roll-off, likely from unaccounted sample absorption. Sensitivity analysis identified the absorption depth and cooling time constant as the main limits to calibration accuracy. To refine the model, measurements with a calibrated spectrometer are required, and potential alternative materials with flatter absorption coefficients should be explored. With these improvements, hot-electron emission could offer a compact and stable alternative to conventional UV calibration sources.

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