Computerphysik I: Blatt 05

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Aufgabe 5 - Numerov-Verfahren

a)

In Programm 1 ist die Implementierung von Analytisch

Numerisch:
$$-0.039788$$
 (1)

Analytisch:
$$-\frac{1}{8\pi} \approx -0.039788$$
 (2)

b)

Aufgabe 6 - Shooting-Methode

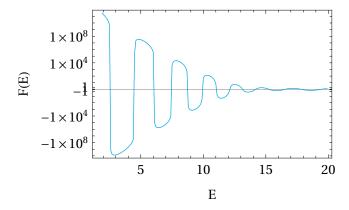


Abbildung 1: Fehlerfunktion für verschiedene Energien

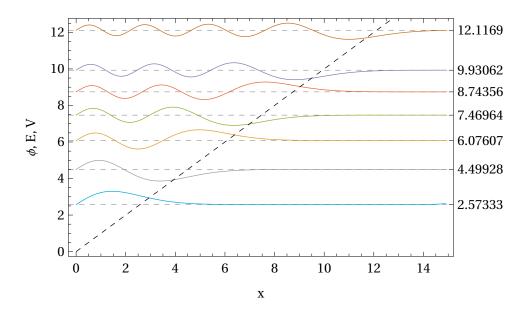


Abbildung 2: Potential mit verschiedenen Wellenfunktionen

Code

5 a)

Listing 1: Programm zum lösen der Poisson-Gleichung mit dem Numerov-Verfahren.

```
1 #include <stdio.h>
2 #include <math.h>
5 #define H 0.001
6 #define rstart 100
9 double rho(double r);
10 void numerov(double* y1, double* y2, double r);
12
13 int main(){
14
      double y1=0, y2 = 0;
15
16
      for(double r = rstart; r > 0; r -= H){
17
          numerov(&y1, &y2, r);
          printf("%f\n", y2);
19
      }
20
      // Ergebnis:
                                            -0.039789
22
      // Analytisch: -1/(8 pi) \approx
                                            -0.0397887
23
      return 0;
25
26 }
27
29 double rho(double r){
      double wert = exp(-r)/(8 * M_PI);
      return wert;
31
32 }
34 void numerov(double* y1, double* y2, double r){
      double y = 2 * *y2 - *y1 - H*H/12*(rho(r+H)+10*rho(r)+rho(r-H));
      *y1 = *y2;
      *y2 = y;
37
38 }
```

6

Listing 2: Programm zum aufzeichnen der Error-Funktion für verschiedene Energien.

```
1 #include <stdio.h>
2 #include <stdlib.h>
3 #include <math.h>
5 #define H 1.e-4
6 #define XMAX 15.
8 void integ(double E);
10 void numerov(double *y1, double *y2, double x, double E);
12 double V(double x);
14 FILE *file;
16 int main(){
      file = fopen("errorFkt.dat", "w+");
19
20
      for(double E = 0.0; E < 20; E += 0.1){</pre>
           integ(E);
23
24
      //integ(5.0);
25
26
27
      fclose(file);
29
30
      return 0;
31
32 }
33
35 void integ(double E){
      double y1 = 0, y2 = H;
37
      for(double x = XMAX; x > 0; x -= H){
           numerov(&y1, &y2, x, E);
39
           //fprintf(file, "%f %f \n", x, y1);
      }
41
```

Listing 3: ...

```
1 #include <stdio.h>
2 #include <stdlib.h>
3 #include <math.h>
4 #include <stdbool.h>
5 #include <pthread.h>
7 #define H 1.e-4
8 #define X_MAX 15.
9 #define N ((int) (X_MAX/H))
10 #define EXPORT_STEPS 1e3
12 #define UNCERT_END .5e-15
14 #define UNCERT_GUESS 0.5
15 //double guess[] = {2.5, 4.5, 6, 7.5, 8.5, 10, 12, 14, 16, 18.5};
16 double guess[] = {2.5, 4.5, 6, 7.5, 8.5, 10, 12};
18 void integ(double E, double* phi);
19 void numerov(double *y1, double *y2, double x, double E);
20 void *findAndExport(void *argument);
21 double V(double x);
24 int main(){
    const uint NUM_THREADS = sizeof(guess)/sizeof(double);
    int thread_args[NUM_THREADS];
    pthread_t threads[NUM_THREADS];
    // crate a thread for each guess
29
    for (int i = 0; i < NUM_THREADS; i++){</pre>
30
         thread_args[i] = i;
      pthread_create(&threads[i], NULL, findAndExport, &thread_args[i]);
32
33
34
    //wait for each thread to complete
    for (size_t i = 0; i < NUM_THREADS; i++) {</pre>
36
      pthread_join(threads[i], NULL);
37
38
39
40
    return 0;
41
42 }
43
```

```
_{
m 44} // find the root of the error function near the n-th guess and save the
      generated wave function
45 void *findAndExport(void *argument){
    // get the index of the thread
    const int n = *((int *)argument);
    // create array for the wave Function
49
    // in the heap because the stack is too small
    double* phi = malloc(N*sizeof(double));
    // bisection to find the root
53
    double E0 = guess[n]-UNCERT_GUESS;
54
    double E1 = guess[n]+UNCERT_GUESS;
    double Ex, tmp;
    do {
57
      Ex = (E1+E0)/2.0;
58
      integ(Ex, phi);
60
      tmp = phi[N-1];
61
      integ(E0, phi);
62
      if (tmp*phi[N-1] >0)
64
65
        E0=Ex;
      else
        E1=Ex;
    } while (fabs((E1-E0)/E0)>UNCERT_END);
68
69
    printf("guess: %.2f E: %f\n", guess[n], E1);
    // normalizing
72
    double norm = 0;
    for(int i=0; i<N; i++){</pre>
     norm += phi[i]*phi[i]*H;
75
76
    norm = sqrt(norm);
77
    for(int i=0; i<N; i++){</pre>
      phi[i] /= norm;
80
81
    // exporting
82
    FILE *file;
    char filename[210];
84
    snprintf(filename, 10, "out%02d.dat", n);
    printf("saving in: %s\n", filename);
```

```
file = fopen(filename, "w+");
     fprintf(file, "%f\n", E1);
     for(int i=0; i<N; i+=EXPORT_STEPS){</pre>
     fprintf(file, "%f %f\n", i*H, phi[i]);
90
91
    fclose(file);
92
     // end the task successfully
    return 0;
96 }
98 // integrating the wave function
99 void integ(double E, double *phi){
100
    double y1 = 0, y2 = H;
101
    for(int i=0; i < N; i++){</pre>
102
     numerov(&y1, &y2, i*H, E);
      phi[i] = y2;
104
105
106 }
108 // numerov step
109 void numerov(double *y1, double *y2, double x, double E){
     double y = 2* *y2*(1 - H*H*5/12*(E-V(x))) - *y1*(1 - H*H/12*(E-V(x-H)))
111
112
    *y1 = *y2;
     *y2 = y;
114 }
115
117 double V(double x){
118 return x;
119 }
```