Implementing Baker's SUBTYPEP decision procedure

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♀ European Lisp Symposium



Introduction

Common Lisp type system, subtypep & Baker's decision procedure

 $\blacktriangleright \ \, \mathsf{Types} \to \mathsf{sets}, \, \mathsf{subtypes} \to \mathsf{subsets}$

 $lackbox{Types}
ightarrow \mathsf{sets}, \, \mathsf{subtypes}
ightarrow \mathsf{subsets}$

```
λ Common Lisp

(defun tr (M)
(declare (type (array real (3 3)) M))
(+ (aref M 0 0)
(aref M 1 1)
(aref M 2 2)))
```

- ightharpoonup Types ightarrow sets, subtypes ightarrow subsets
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- (subtypep $\langle A \rangle \langle B \rangle$) $\equiv A \subseteq B$?
- ▶ Predicate function

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- ▶ Predicate function

```
λ Common Lisp

(subtypep '(or my-class string (integer 0 (1024)))

(or super-class
(array * 1)
(unsigned-byte 10)))
```

```
ightharpoonup Types 
ightharpoonup sets, subtypes 
ightharpoonup subsets
\blacktriangleright Types \rightarrow first class values
           ▶ Type specifiers arbitrarily deep
           ▶ May take a while to retrun
                Problem #1 — complex input
            Arbitrarily complex input type specifiers
                              (unsigned-byte 10)))
```

- (satisfies $\langle predicate \rangle$) $\equiv \{x \mid predicate(x)\}$
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Problem #2 — undecidability

Subtypep cannot answer for some type specifiers

subtypep return values

$$(\text{subtypep } \langle A \rangle \ \langle B \rangle) = \begin{cases} (\texttt{T} \ \texttt{T}) & \to A \subseteq B \\ (\texttt{NIL} \ \texttt{T}) & \to A \not\subseteq B \\ (\texttt{NIL} \ \texttt{NIL}) & \to \text{``undecidable''} \end{cases}$$

▶ (NIL NIL) encodes undecidability

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- ▶ (NIL NIL) encodes undecidability "input too complex"
- ▶ Lack of reliability
- ▶ Painful limit for some applications
 - > Newton's regular type expressions
 - > Newton's optimized typecase implementation

- + focus on result accuracy
- never returns (NIL NIL) when it is possible to answer
- paper difficult to read
- not exhaustive
- very few solutions about satisfies

- no implementation available
- exponential complexity (theoretical)
- ? efficiency

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Content

- 1. Application using subtypep
- 2. Baker's decision procedure
 - 2.1 Pre-processing
 - 2.2 Types as bit-vectors
 - 2.3 Type specifier \rightarrow bit-vector expression
- 3. Going further

The problem

```
Common Lisp
(defclass point ()
   (y :type number
   (name :type string
 (:metaclass json-serializable))
(json-serialize (make-instance 'point
                               :y 3.2
                               :name "a1"))
```

The problem

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(defclass point ()
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```
    JSON serialization

1     {
2         "X": -10,
3         "Y": 3.2,
4         "NAME": "a1"
5     }
```

```
λ Common Lisp

(deftype json ()
'(or number
string
(and symbol
(not keyword))
list
hash-table))
```

Our employee class

- ▶ 2 slots ⇒ 2 calls to subtypep
- ▶ Trigger error if one fails

Application of our implementation to check employee.name ⊆ json

Pre-processing steps

Pre-processing steps

```
Common Lisp
(subtypep '(or string
                (and symbol
                     (not keyword))
               unsigned-byte)
          '(or number
               string
                (and symbol
                     (not keyword))
               list
               hash-table))
```

▶ Alias expansion

Pre-processing steps

```
Common Lisp
(subtypep
 '(AND (or string
           (and symbol
                 (not keyword))
           unsigned-byte)
        (NOT (or number
                  string
                  (and symbol
                       (not keyword))
                  list
                  hash-table)))
NIL)
```

- Alias expansion
- $P \subseteq Q \Rightarrow P \cap \neg Q = \emptyset$

Bit-vector type representation

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Types represented as bit-vectors \mathcal{B}_P

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Types represented as bit-vectors \mathcal{B}_P

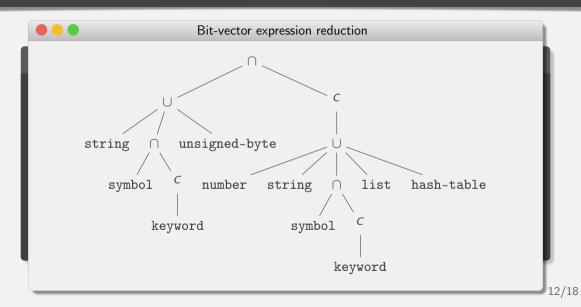
	t	nil	$\operatorname{\mathtt{sym}}$	"str"		(1 i s t)
$\mathcal{B}_{ exttt{nil}}$	0	0	0	0		0 \
\mathcal{B}_{t}	1	1	1	1		1
$\mathcal{B}_{ exttt{null}}$	0	1	0	0		0
$\mathcal{B}_{ t symbol}$	1	1	1	0		0
$\mathcal{B}_{\mathtt{string}}$	0	0	0	1		0
:	:	:	:	:	٠.,	:
$\mathcal{B}_{ exttt{list}}$	0 /	1	0	0		1 /

$egin{aligned} &igoplus & \mathsf{Properties} \ & \mathcal{B}_{P\cup Q} = \mathcal{B}_P ee \mathcal{B}_Q \ & \mathcal{B}_{P\cap Q} = \mathcal{B}_P \wedge \mathcal{B}_Q \ & \mathcal{B}_{\overline{P}} = eg \mathcal{B}_P \end{aligned}$

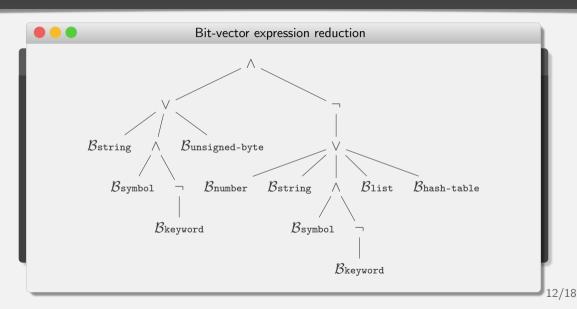
Back to our problem

```
Common Lisp
(subtypep '(and (or string
                     (and symbol
                          (not keyword))
                     unsigned-byte)
                 (not (or number
                          string
                          (and symbol
                                (not keyword))
                          list
                          hash-table)))
          nil)
```

Back to our problem



Back to our problem



```
✓ employee.name
```

```
1 (subtypep '(or string
2 (and symbol
3 (not keyword))
4 unsigned-byte)
5 'json)
```

```
(subtypep '(or string)
(and symbol)
(not keyword))
unsigned-byte)
'json'
```

```
 employee.name
 employee.half-time-p
```

```
(defclass employee ()
((name :type (or string
(and symbol
(not keyword))
unsigned-byte))
(half-time-p boolean))
(:metaclass json-serializable))
```

```
(subtypep '(or string)
(and symbol)
(not keyword))
unsigned-byte)
'json'
```

- employee.name
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```
✓ employee.name
```

```
✓ employee.half-time-p
```

Conclusion

```
employee is JSON-compatible!
```

CLOS classes & member type specifiers

Choosing representative elements right

CLOS classes

- lacktriangleright Issue ightarrow find a representative instance
- lacktriangle Cannot use make-instance ightarrow possible side-effects
- Baker's solution
 - > hook into defclass implementation
 - not portable
 - maybe not trivial
- ➤ Our solution → the Meta Object Protoco
 - ightarrow register class prototypes ightarrow "fake" instances
 - portable (for implementations supporting the MOP
 - easier to implement
 - packageable

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member type specifiers

- ▶ Explicitly provide type's elements
- (member $\langle A \rangle \langle B \rangle \langle C \rangle$) $\equiv \{A, B, C\}$
- "Anonymous" types
- ▶ Bit-vector $\mathcal{B}_{(\text{member } \langle A \rangle \ \langle B \rangle \ \langle C \rangle)}$
 - 1. add A, B, C as representatives
 - 2. $\mathcal{B}_{(\text{member }\langle A\rangle\ \langle B\rangle\ \langle C\rangle)}=\mathcal{B}_{\{A\}}\vee\mathcal{B}_{\{B\}}\vee\mathcal{B}_{\{C\}}$

Conclusion

- subtypep unreliability
- ▶ Baker's decision procedure
 - > no implementation given
 - > many details missing
 - > seems elegant and powerful
- ▶ Our implementation
 - > incomplete & experimental
 - > motivating accuracy & performance measures
- ▶ Future work
 - > implement missing type specifiers (array & complex)
 - > find solutions for cons & satisfies
 - > open source the implementation!

Thanks for listening! ...

Any question?