

# REAL-TIME MULTIDIMENSIONAL VEHICLE DYNAMIC STABILITY DOMAIN CALCULATION AND ITS APPLICATION IN INTELLIGENT VEHICLES

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# Introduction



# 1.Introduction

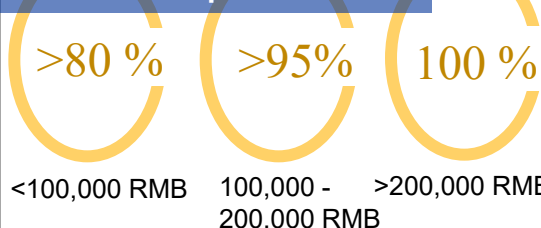
## ■ Stable driving is critical for safe path tracking in complex scenarios

- **high-precision control systems** and **intelligent chassis** will become key indicators for the next generation of smart vehicles.
- **The stability controller** is one of the **most common active safety control technologies** in modern vehicles.
- The future will focus on exploring **the vehicle's maximum safety performance** and improving **path tracking accuracy** in **extreme scenarios**.

driving safety



ESP adoption rate



emergency scenarios

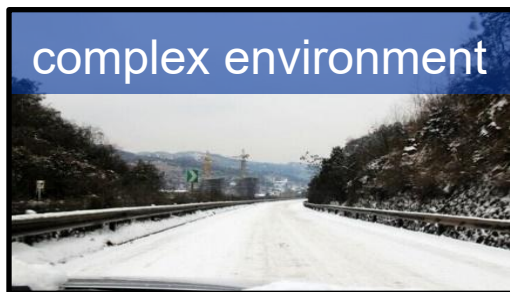


**Vehicle stability is fundamental to the safe operation of intelligent vehicles**

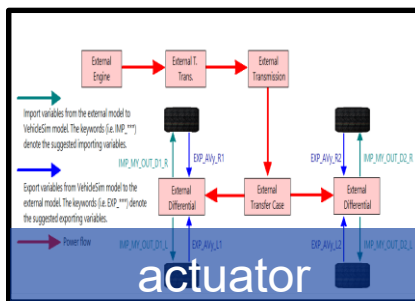
# 1.Introduction

## ■ Unclear stability domain under multidimensional input

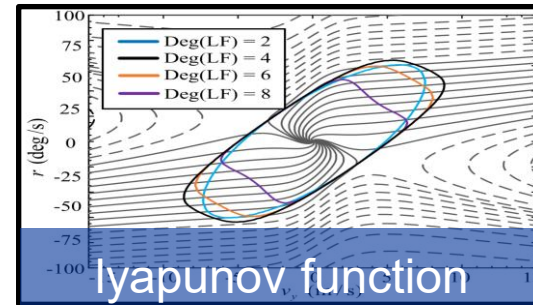
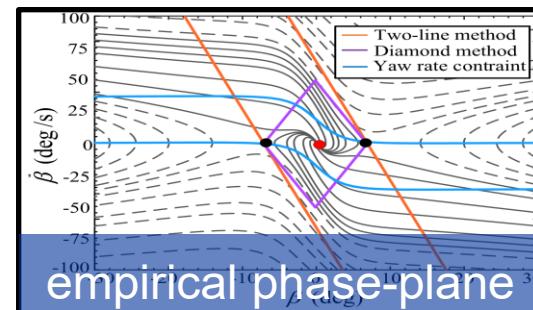
### Multidimensional Input



### Vehicle Dynamic



### Stability Domain

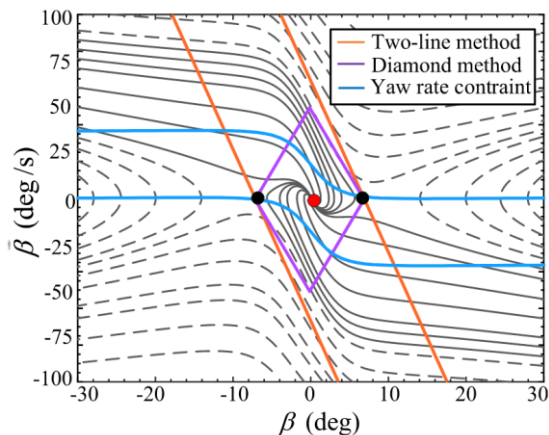


The real stability domain is difficult to parameterize accurately

# 1.Introduction

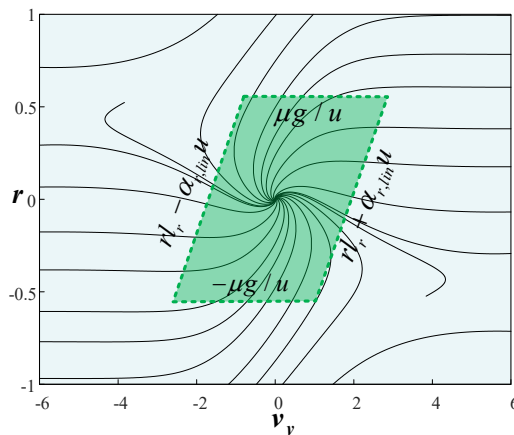
## ■ Challenge for real-time stability-domain estimation

### Portrait Phase Method



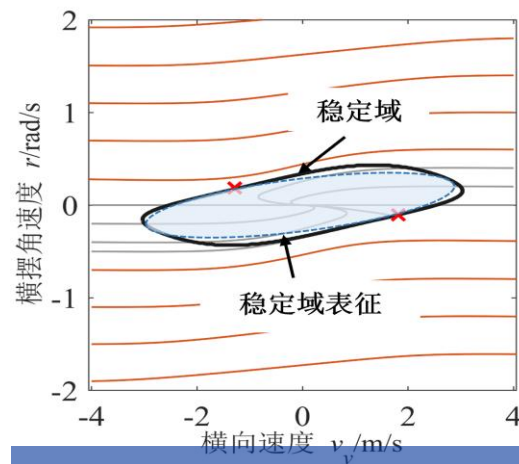
Lack of detailed  
analysis

### Dynamics Constraint



overly conservative for  
its linear assumption

### Graphical Fitting



Highly irregular for  
complex conditions

Real-time estimation is essential for effective vehicle stability control

2

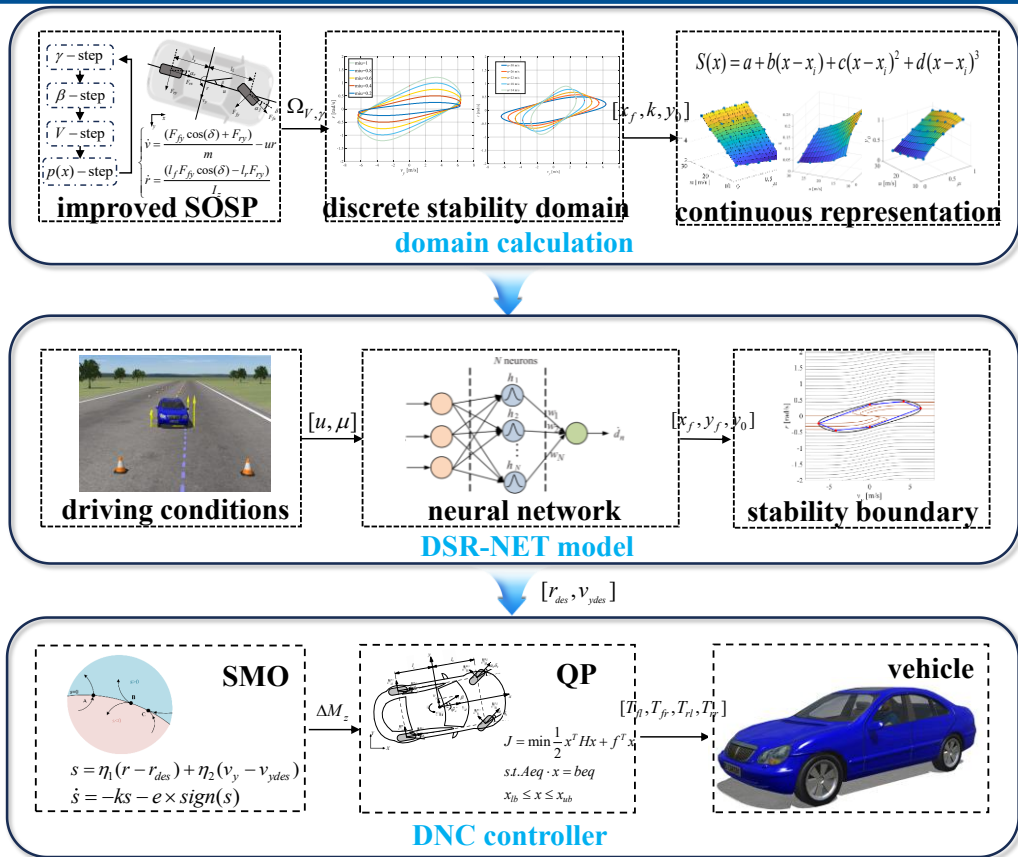
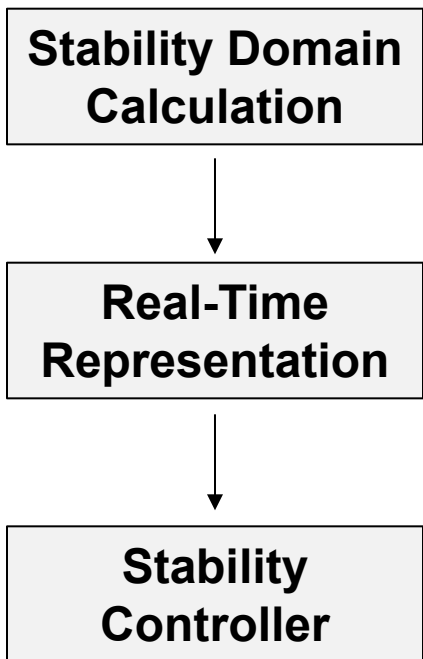


# Methodology



# 2.1 Technical Route

## ■ Structure of Article

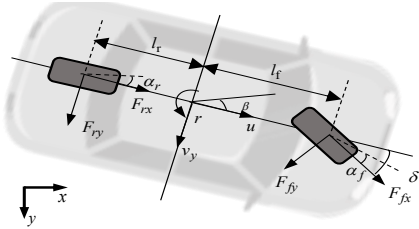




## 2.2 Dynamics Model

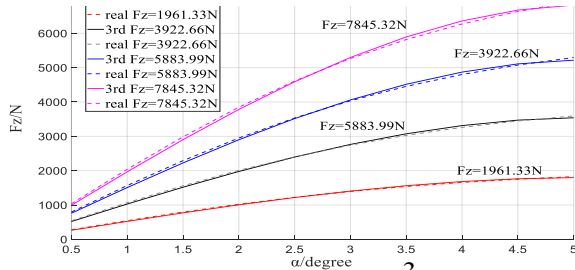
### ■ Dynamic model and SOSP

#### Vehicle Dynamic Model



$$\begin{cases} m(\dot{v}_y + ur) = F_{fy} \cos \delta + F_{ry} \\ I_z \dot{r} = l_f F_{fy} \cos \delta - l_r F_{ry} \end{cases}$$

#### Cubic Polynomial Tire Model



$$F_y = F_z(-k_1\alpha_i + k_2\alpha_i^3) \quad i = f, r$$

#### Nonlinear System Model of SOSP

$$\begin{cases} \dot{v} = \frac{(F_{fy} \cos(\delta) + F_{ry})}{m} - ur \\ \dot{r} = \frac{(l_f F_{fy} \cos(\delta) - l_r F_{ry})}{I_z} \end{cases}$$

$$F_y = F_z(-k_1\alpha_i + k_2\alpha_i^3) \quad i = f, r$$

#### Sum of Squares Programming

$\gamma$  – step: find the  $V(x)$  that maximizes the value  $\gamma$

$\beta$  – step: find the  $p(x)$  that maximizes the value  $\beta$

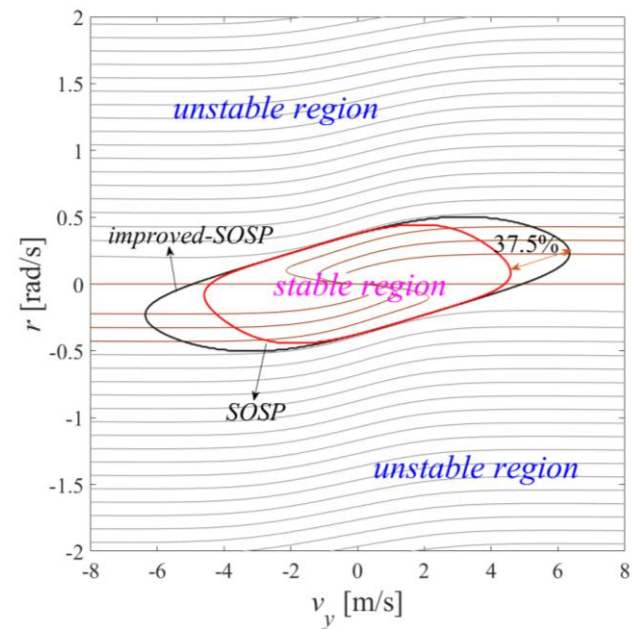
$V$  – step: ensuring  $V(x) > 0$  and  $\nabla V(x)f > 0$ .

$p$  – step:  $p(x)$  for next iteration =  $V(x)$

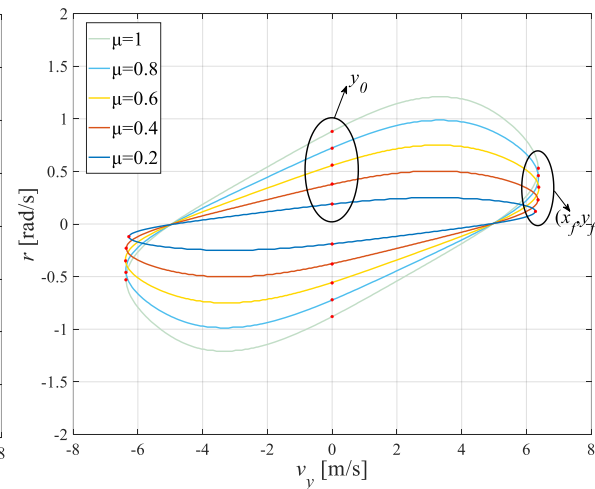
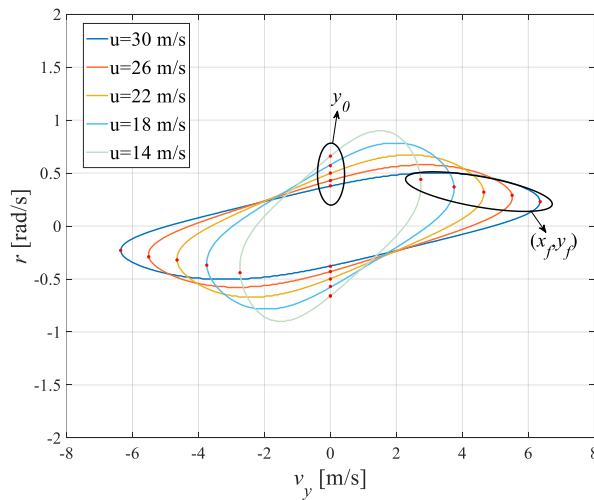
## 2.2 SOSP estimation

### ■ SOSP based stability-domain estimation

#### Improved-SOSP Estimation



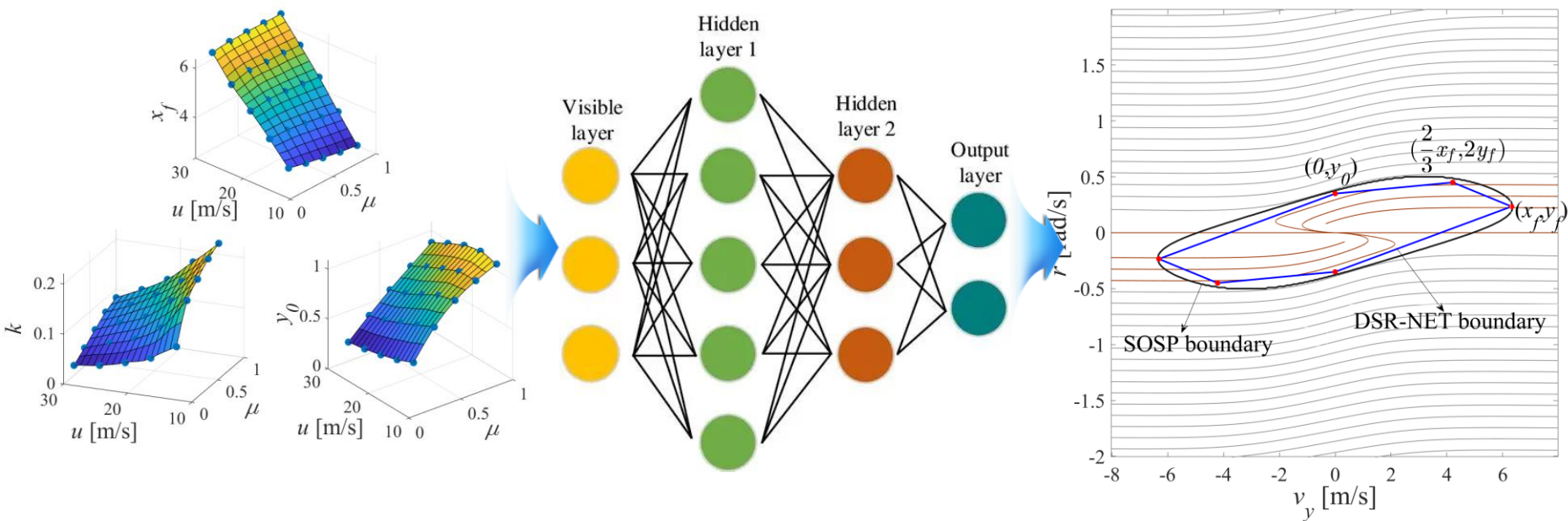
#### Variation Patterns at Different Speeds/Coefficients



## 2.3 Real-time Vehicle Stability-domain Representation

### ■ Neural Network-based Representation Method

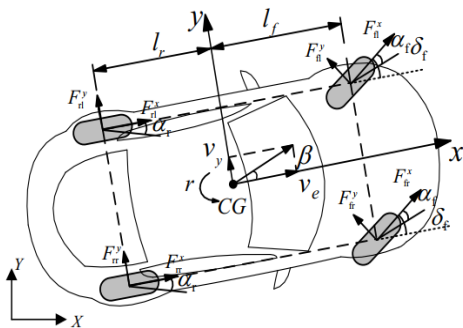
Interpolation Function    Feedforward Neural Network    Boundary Fitting Method



## 2.4 Design of A Path Tracking Controller

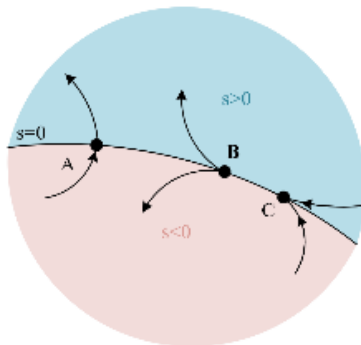
## ■ DSR-NET Stability Controller Design (DNC)

## the control model



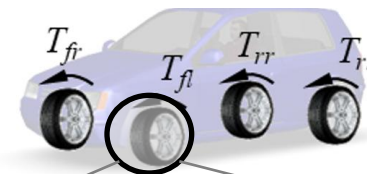
$$\begin{cases} m(\dot{v}_y + ur) = F_{fy} \cos \delta + F_{ry} \\ I_z \dot{r} = l_f F_{fy} \cos \delta - l_r F_{ry} + \Delta M_z \\ \Delta M_z = (F_{xfr} + F_{xrr} - F_{xfl} - F_{xrl}) \frac{B}{2} \end{cases}$$

## the SMO design



$$\begin{aligned} s &= \eta_1(r - r_{des}) + \eta_2(v_y - v_{ydes}) \\ \dot{s} &= -ks - e \times \text{sign}(s) \end{aligned}$$

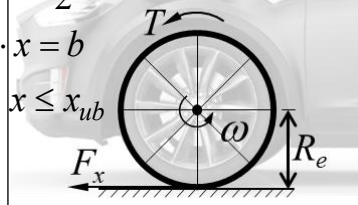
## the optimal torques



$$J = \min \frac{1}{2} x^T H x + f^T x$$

$$\text{s.t. } A \cdot x = b$$

$$x_{lh} \leq x \leq x_{uh}$$



$$J_w \dot{\omega}_{ij} = T_{ij} - F_{ij}^x R_e$$

3

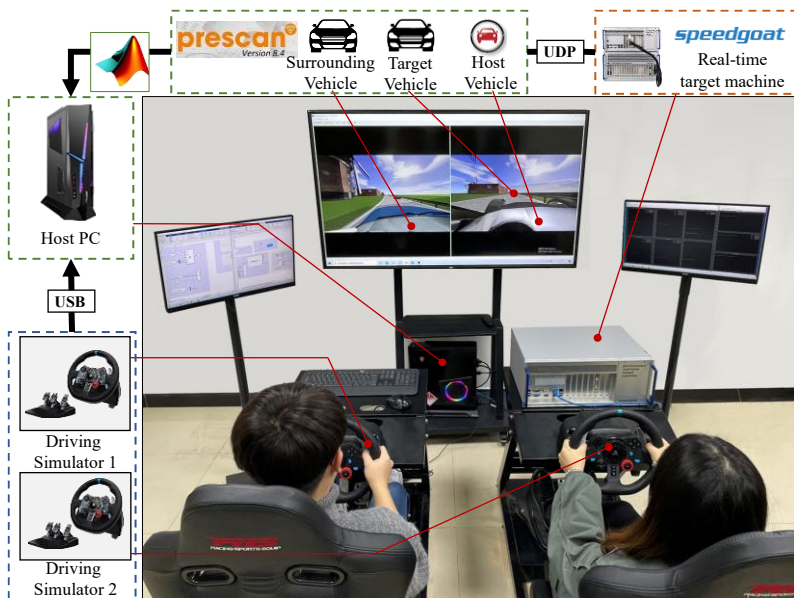


# Experiment Test



## 3.1 Test Platform

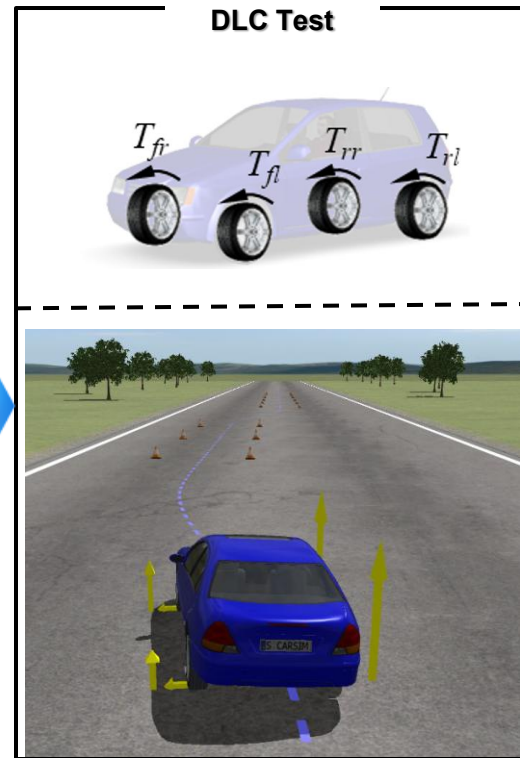
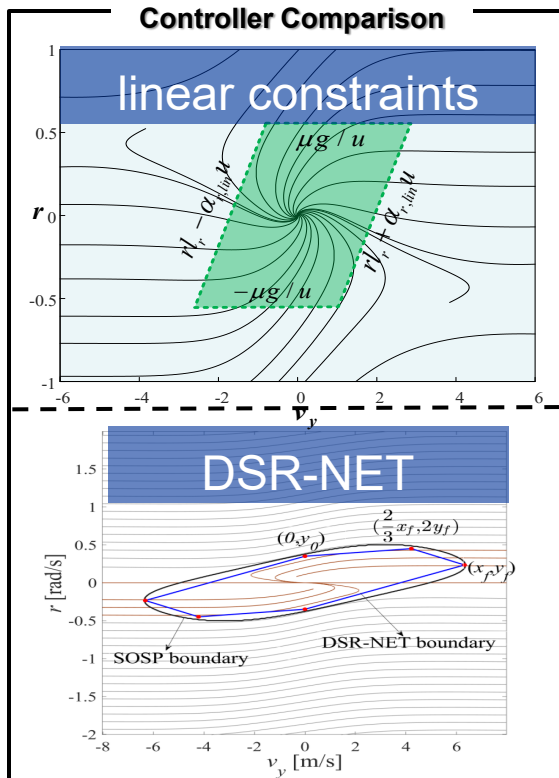
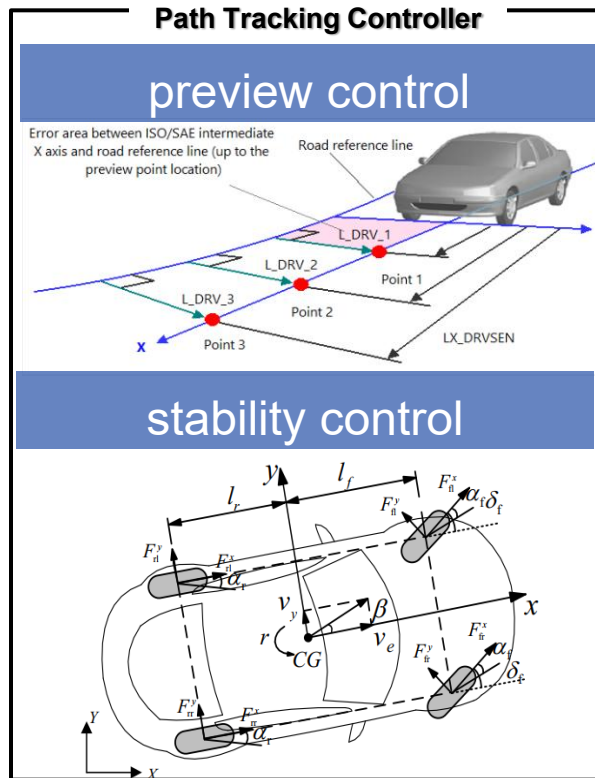
### ■ HiL System Platform



<b>hardware</b>	Driving simulator, Speedgoat real-time target machine, Host machine, displayer
<b>software</b>	Matlab/Simulink, Carsim, Prescan, Logitech driver
<b>controller</b>	Driving simulator, Speedgoat real-time target machine
<b>comm</b>	UDP (Speedgoat-Host machine), Serial port (Driving simulator-Host machine)

## 3.2 Test Scene

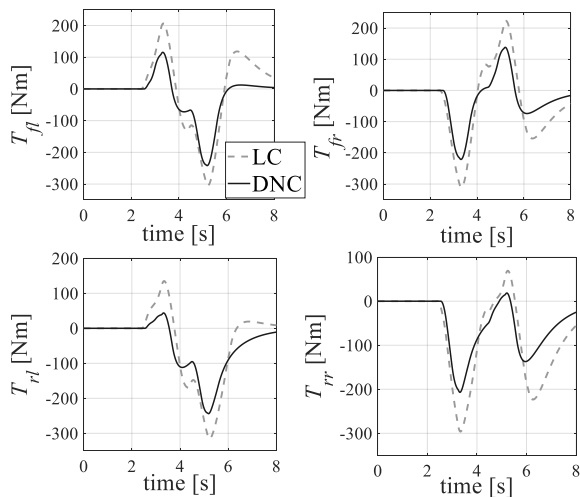
### Linear controller (LC) VS DSR-NET controller (DNC)



## 3.3 Validation Results

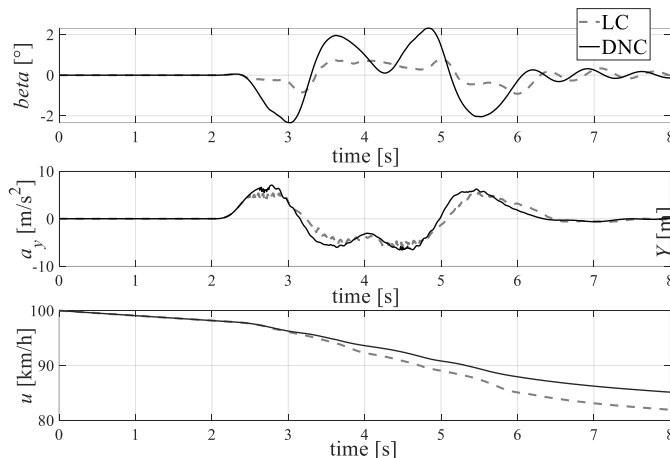
### Results under DLC (100km/h, $u=0.6$ )

#### Optimal Wheel Torques



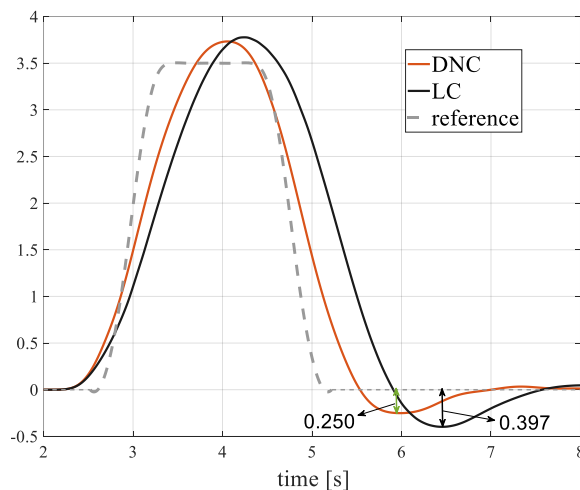
DNC intervenes less and  
optimize smaller torques

#### States Responses



DNC has a better motility

#### Path Tracking Error



DNC achieves smaller  
tracking errors



4



# Conclusion



## 4. Conclusion

### ➤ Conclusion

1) By adding an iterative shape-function to the traditional SOSP, **the estimated stability-domain is developed.**

2) An FNN-based model maps between driving factors and stability boundaries to achieve **a continuous stability-domain description.**

3) A HiL platform is built to show that the DNC halves peak tracking error due to a **reasonable stability threshold for vehicle motion.**

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### ➤ Outlook

Future work will aim to demonstrate the practical value of the DNC **through full-vehicle tests, integrate advanced path-tracking control method, and apply machine-learning methods to capture the characteristics of the extended stability domain under varying control inputs.**

# Thanks

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