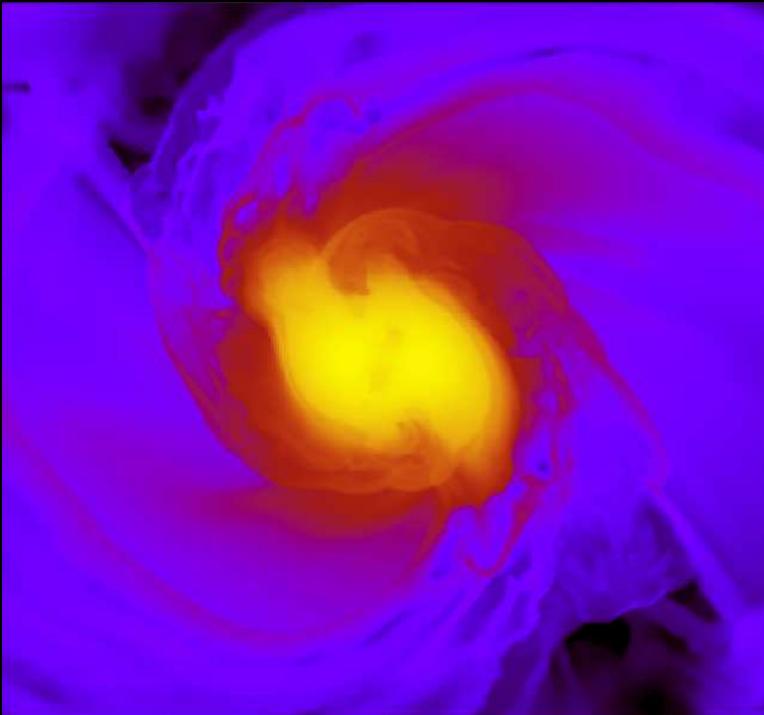


# An update on the **IllinoisGRMHD** (“IGM”) code & accurate, long-term evolutions with the **HandOff+HARMNUC** codes

Leo Werneck

In collaboration with Z.B. Etienne,  
F.L. Armengol, A. Murguia-Berthier, S.C. Noble, T. Gupte  
& the TCAN-80NSSC18K1488 BNS collaboration



2022 North American Einstein Toolkit School  
University of Idaho, Moscow, ID

Baryonic density from a magnetized, equal-mass BNS simulation performed with **IllinoisGRMHD** using the LS220 **tabulated EOS**, shortly after merger

# TCAN-80NSSC18K1488 on Binary Neutron Stars Collaboration



Zach Etienne  
[BlackHoles@Home](mailto:BlackHoles@Home)



Thiago Assumpção  
[NRPyElliptic](https://NRPyElliptic)



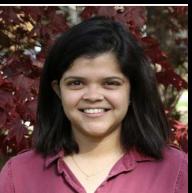
Manuela Campanelli  
[Overview of NR](https://nrpyelliptic.org/Overview_of_NR)



Fede Armengol



Josh Faber



Tanmayee Gupte



Scott Noble



Ari Murguia-Berthier



Funding acknowledgement NASA-TCAN-80NSSC18K1488

<https://compact-binaries.org>

# Overview

- Introduction & motivation
- An overview of **IllinoisGRMHD**
- Updates:
  - New primitive recovery infrastructure
  - Microphysical finite-temperature equation of state (EOS) support
  - **NRPyEOS**: NRPy+-based microphysics equation of state (EOS) table interpolator
  - **NRPyLeakage**: NRPy+-based neutrino leakage (**NRPyLeakageET**)
- Latest results
- Recap and future work

# Introduction & motivation

In August 2017...



LIGO-Hanford



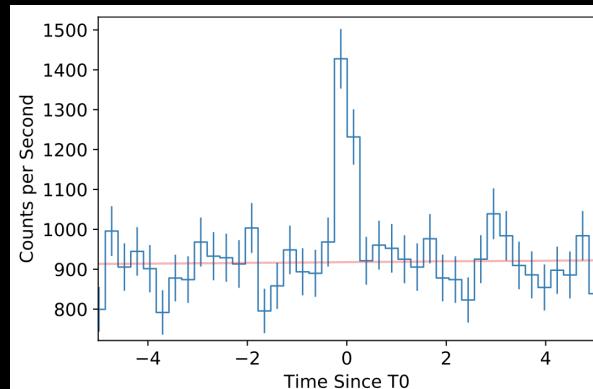
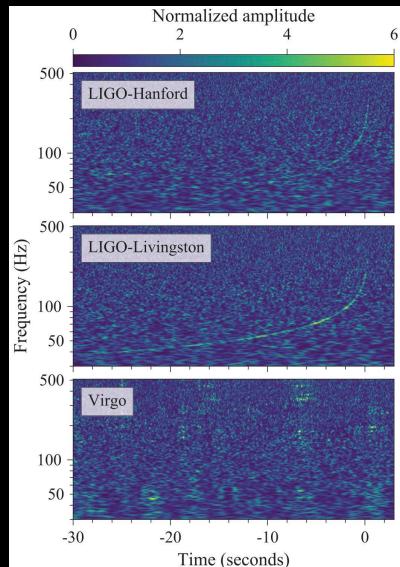
LIGO-Livingston



Virgo



*Fermi* Gamma-ray Burst Monitor



Goldstein et al., [APJL 848:L14 \(2017\)](#)

# Introduction & motivation

Model BNS systems

Evolve metric quantities  
*Baikal, ML\_BSSN, Lean, ...*

GRMHD evolution  
*IllinoisGRMHD, GRHydro, Spritz, ...*

Realistic equations of state  
*NRPyEOS, EOS\_Omni, ...*

Neutrino physics  
*NRPyLeakage, ZelmaniLeak, ZelmaniM1, ...*



Adaptive Mesh Refinement  
*Carpet, CarpetX, ...*

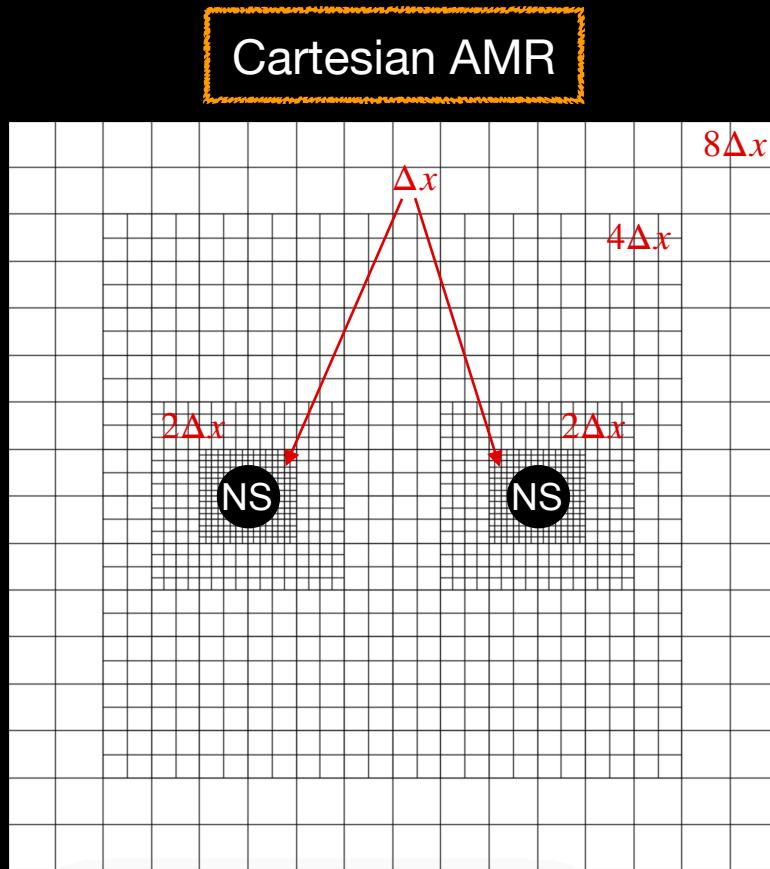
I/O  
*1D, 2D, 3D data, checkpoints, ...*

Diagnostics  
*Gravitational waves, volume integrals, ...*

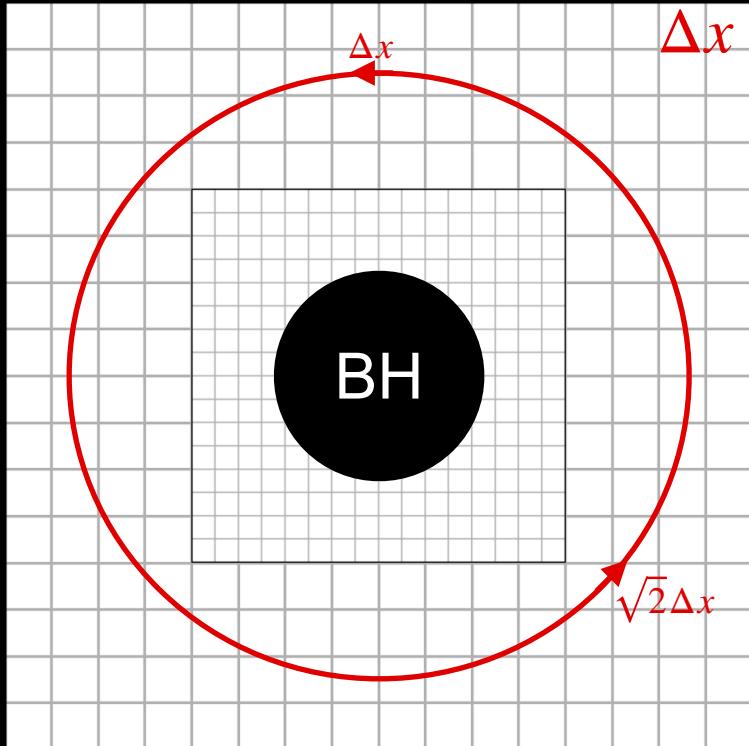
# Introduction & motivation

- We must be capable of accurately and reliably model these systems
- From a computational point of view, we must do it as efficiently as possible
- For typical separations and masses, simulating the full inspiral + merger + postmerger can take months on high-end supercomputers!
- Caveat: we are only modeling  $O(100 \text{ ms})$ , but really need  $O(\text{seconds})$
- Just keep the code running for  $O(\text{years})$ ?
- Or we could try thinking outside of the box!

# Introduction & motivation

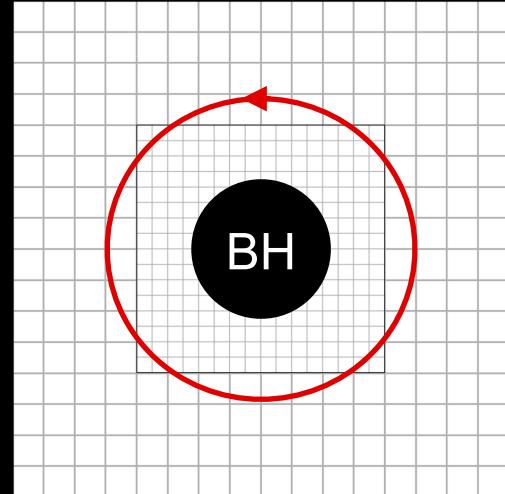


# Introduction & motivation



AMR in the postmerger

~15x more inefficient  
Than spherical grids!

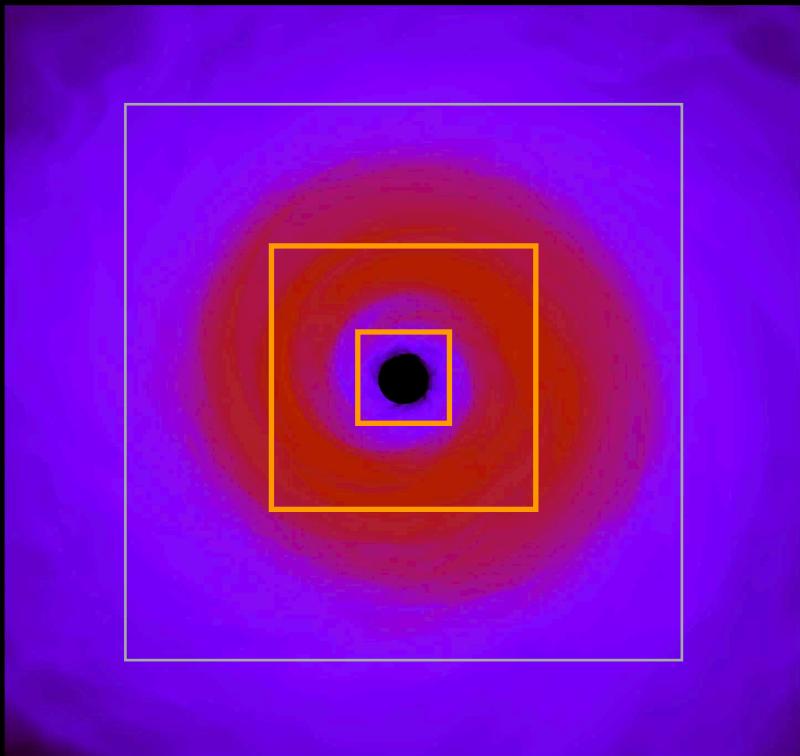


Inefficiencies:

- Changes in resolution: ~2x
- Jumps in radial resolution: ~2x
- Sharp AMR corners wasted: ~2x
- Coarse grid under fine grid: ~1.2x
- Fine grids' wide AMR boundary: ~1.5x

Courtesy Zach Etienne

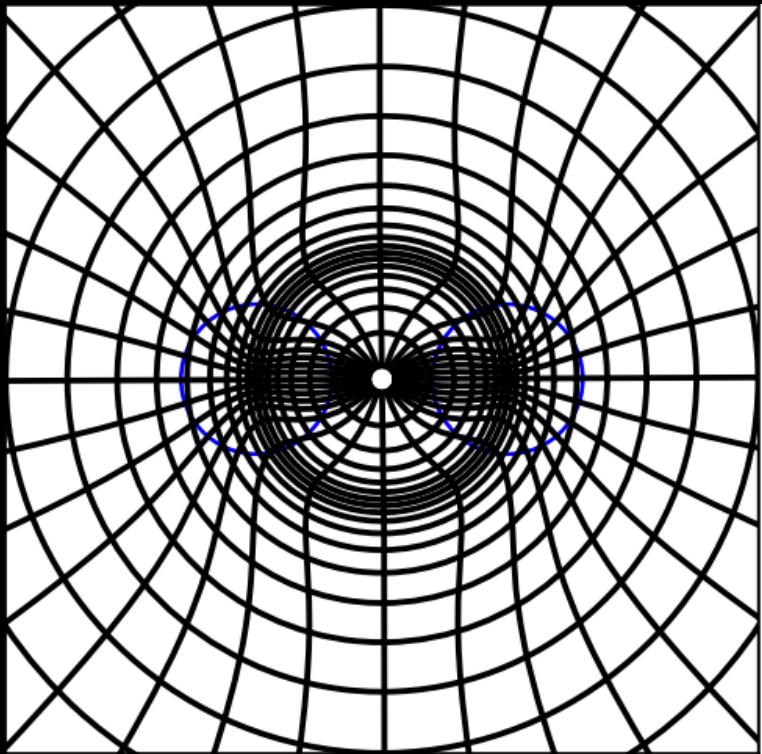
# Introduction & motivation



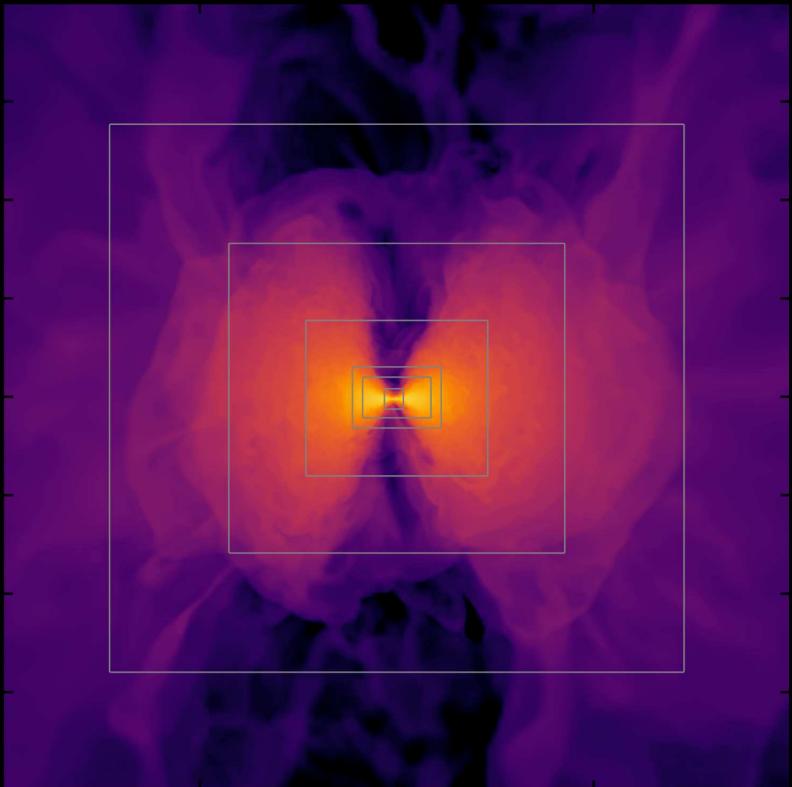
Can we  
do better?



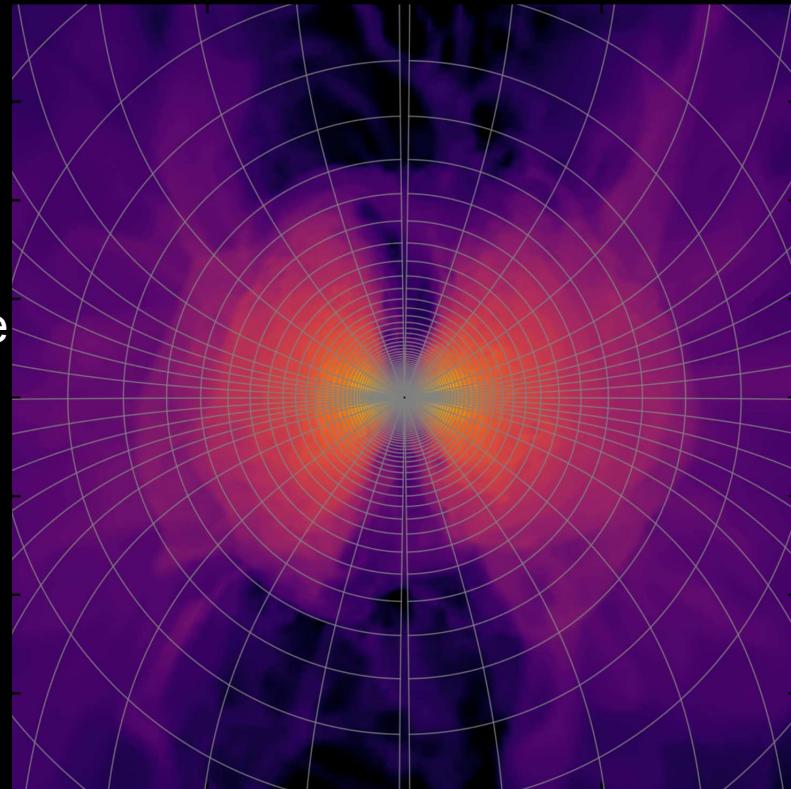
Yes!



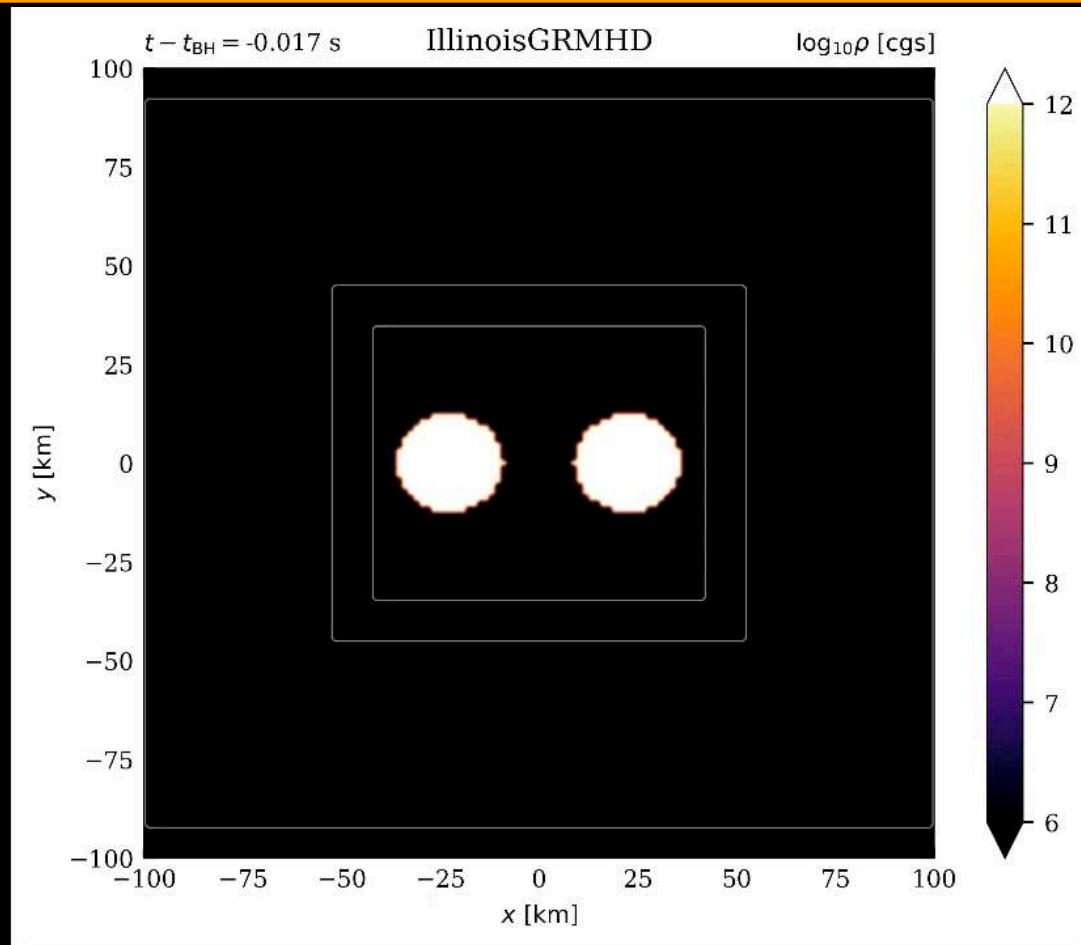
# The HandOff package



Interpolate  
→



# The HandOff package



# The HandOff — What physics can we include?

Feature	IllinoisGRMHD	HARM+NUC	Production HandOff
Equation of state: Gamma-law	✓	✓	<a href="#">F.L.Armengol++TCAN (arXiv:2112.09817)</a>
Equation of state: Tabulated	✓	✓	
Neutrino physics (leakage)	✓	✓	Coming soon!

This talk!

L.W., Z. Etienne++TCAN, In Preparation

[A.Murquia-Berthier++TCAN ApJ 919 95 \(2021\)](#)

# IllinoisGRMHD

- A rewrite of the original GRMHD code of the Illinois NR Group (arXiv:1501.07276)
  - Roundoff agreement with the original code; faster and concise
  - Open-sourced and available as part of the Einstein Toolkit
- 
- GRMHD for dynamical spacetimes:
    - Single and binary neutron stars with and without magnetic fields
    - Black hole accretion disks;
    - White dwarves;
    - Hypermassive neutron stars;
    - And many more!
  - Latest improvements:
    - Hybrid EOS support (including piecewise polytropes)
    - Microphysical finite-temperature equation of state (EOS) support
    - Electron fraction and temperature evolution
    - Neutrino physics via a leakage scheme (**NRPyLeakage**)

# NRPyEOS

- New [NRPy+](#)-based EOS table interpolation routines, fully documented using Jupyter notebooks
- Clean interface for interpolating finite-temperature EOS tables
- Avoids unnecessary interpolations by generating specialized functions
- NRPy+-version is fully open-source and ET-version will be released soon

## Step 8: Adding all functions to the dictionary [Back to [Top](#)]

The function below can be called to add all functions defined in this tutorial notebook to the C function dictionary.

```
In [10]: # Step 8: Add all C functions to the dictionary
def add_all_Cfuncs_to_dict():
    # Step 8.a: Functions for which the temperature is known
    Cfunc_known_T([P])
    Cfunc_known_T([eps])
    Cfunc_known_T([P,eps])
    Cfunc_known_T([P,eps,S])
    Cfunc_known_T([P,eps,S,cs2])
    Cfunc_known_T([P,eps,depsdT])
    Cfunc_known_T([P,eps,mu_e, mu_p, mu_n, muhat])
    Cfunc_known_T([mu_e, mu_p, mu_n, muhat, X_p, X_n])

    # Step 8.b: Functions for which the temperature is unknown
    # Step 8.b.i: Temperature is determined using the specific internal energy
    Cfunc_unknown_T(eps, [P])
    Cfunc_unknown_T(eps, [P, S, depsdT])
    # Step 8.b.ii: Temperature is determined using the pressure
    Cfunc_unknown_T(P, [eps, S])
    # Step 8.b.iii: Temperature is determined using the entropy
    Cfunc_unknown_T(S, [P, eps])

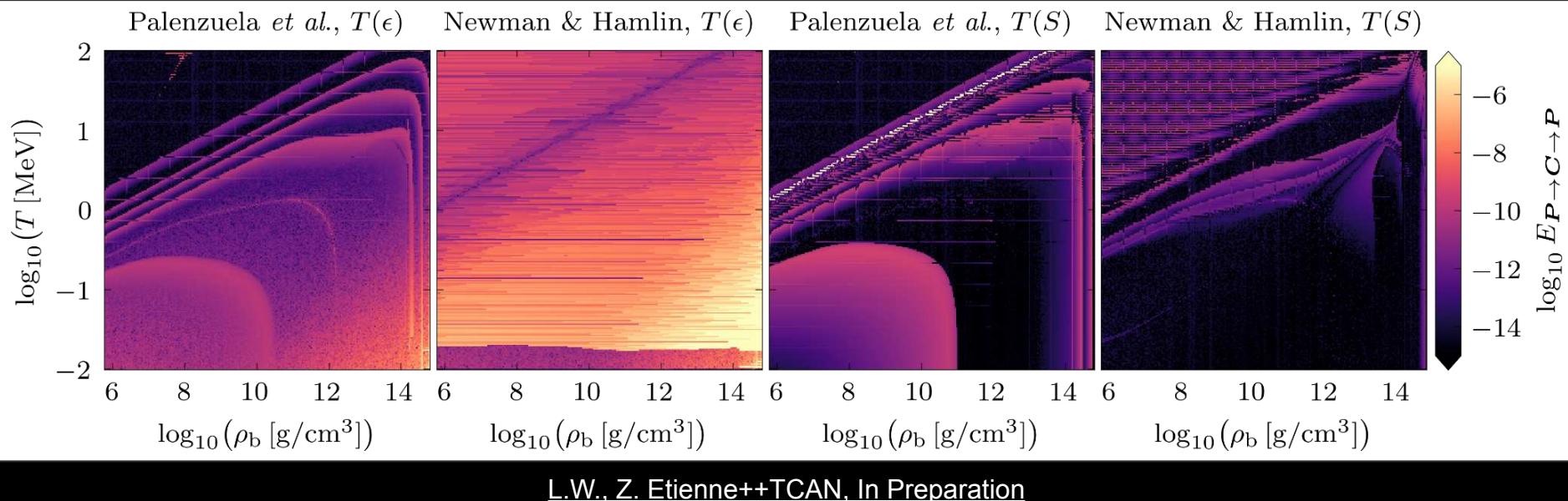
    # Step 8.c: Interpolation helpers
    gen_Cheader_Interpolation_helpers()

    # Step 8.d: General interpolation wrappers
    Cfunc_general_wrapper_known_T()
    Cfunc_general_wrapper_unknown_T()

    # Step 8.e: Table reader and memory allocation
    Cfunc_read_table_setEOS_params()

    # Step 8.f: Memory deallocation
    Cfunc_free_memory()
```

# New conservative-to-primitive infrastructure



Based on: [Palenzuela \*et al.\* \(2015\)](#), [Newman & Hamlin \(2014\)](#), and the implementation by [Siegel \*et al.\* \(2018\)](#)

Adapted routines to use the entropy equation as a backup, if desired

RePrimAnd support will be available once it supports tabulated EOS

# GRMHD with neutrino leakage

$$\nabla_\mu (n_b u^\mu) = 0$$

$$\nabla_\mu T^{\mu\nu} = Q u^\nu$$

$$\nabla_\mu {}^*F^{\mu\nu} = 0$$

$$\nabla_\mu (n_e u^\mu) = \mathcal{R}$$

$$\nabla_\mu (S u^\mu) = 0$$

Standard GRMHD equations

Neutrino emission & cooling

Additional evolution equations

# NRPyLeakage

- New [NRPy+](#)-based neutrino leakage code, fully documented using Jupyter notebooks
- Fast & efficient C code for computing neutrino emission and cooling rates, as well as opacities
- Local “path of least resistance” algorithm for computing the optical depths [[Neilsen et al. \(2011\)](#)]
- Cartesian AMR-compatible [Einstein Toolkit](#) thorn—**NRPyLeakageET**

## Step 4.f: Total emission and cooling rates for free neutrinos [\[Back to Top\]](#)

Finally, we compute the total emission and cooling rates for free neutrinos:

$$\begin{aligned}\mathcal{R}_{\text{total}}^{\nu_e} &= \mathcal{R}_{e^-e^+}^{\nu_e, \bar{\nu}_e} + \mathcal{R}_{\gamma}^{\nu_e, \bar{\nu}_e} + \mathcal{R}_{\text{Brems}}^{\nu_e, \bar{\nu}_e} + \mathcal{R}_{\text{cc}}^{\nu_e}, \\ \mathcal{R}_{\text{total}}^{\bar{\nu}_e} &= \mathcal{R}_{e^-e^+}^{\bar{\nu}_e, \nu_e} + \mathcal{R}_{\gamma}^{\bar{\nu}_e, \nu_e} + \mathcal{R}_{\text{Brems}}^{\bar{\nu}_e, \nu_e} + \mathcal{R}_{\text{pc}}^{\bar{\nu}_e}, \\ \mathcal{R}_{\text{total}}^{\nu_x} &= \mathcal{R}_{e^-e^+}^{\nu_x, \bar{\nu}_x} + \mathcal{R}_{\gamma}^{\nu_x, \bar{\nu}_x} + \mathcal{R}_{\text{Brems}}^{\nu_x, \bar{\nu}_x}, \\ \mathcal{Q}_{\text{total}}^{\nu_e} &= \mathcal{Q}_{e^-e^+}^{\nu_e, \bar{\nu}_e} + \mathcal{Q}_{\gamma}^{\nu_e, \bar{\nu}_e} + \mathcal{Q}_{\text{Brems}}^{\nu_e, \bar{\nu}_e} + \mathcal{Q}_{\text{cc}}^{\nu_e}, \\ \mathcal{Q}_{\text{total}}^{\bar{\nu}_e} &= \mathcal{Q}_{e^-e^+}^{\bar{\nu}_e, \nu_e} + \mathcal{Q}_{\gamma}^{\bar{\nu}_e, \nu_e} + \mathcal{Q}_{\text{Brems}}^{\bar{\nu}_e, \nu_e} + \mathcal{Q}_{\text{pc}}^{\bar{\nu}_e}, \\ \mathcal{Q}_{\text{total}}^{\nu_x} &= \mathcal{Q}_{e^-e^+}^{\nu_x, \bar{\nu}_x} + \mathcal{Q}_{\gamma}^{\nu_x, \bar{\nu}_x} + \mathcal{Q}_{\text{Brems}}^{\nu_x, \bar{\nu}_x},\end{aligned}$$

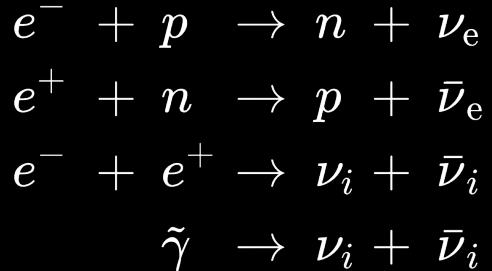
```
In [13]: # Step 4.f: Total emission and cooling rates for free neutrinos

# Step 4.f.i: Electron neutrinos
R_free_total_nue = R_pair_nue_anue + R_plasmon_nue_anue + R_Brems_nui_anui + R_beta_nue
Q_free_total_nue = Q_pair_nue_anue + Q_plasmon_nue_anue + Q_Brems_nui_anui + Q_beta_nue

# Step 4.f.ii: Electron antineutrinos
R_free_total_anue = R_pair_nue_anue + R_plasmon_nue_anue + R_Brems_nui_anui + R_beta_anue
Q_free_total_anue = Q_pair_nue_anue + Q_plasmon_nue_anue + Q_Brems_nui_anui + Q_beta_anue

# Step 4.f.iii: Heavy lepton neutrinos or antineutrinos (single species)
R_free_total_nux = R_pair_nux_anux + R_plasmon_nux_anux + R_Brems_nui_anui
Q_free_total_nux = Q_pair_nux_anux + Q_plasmon_nux_anux + Q_Brems_nui_anui
```

# Neutrino emission and cooling

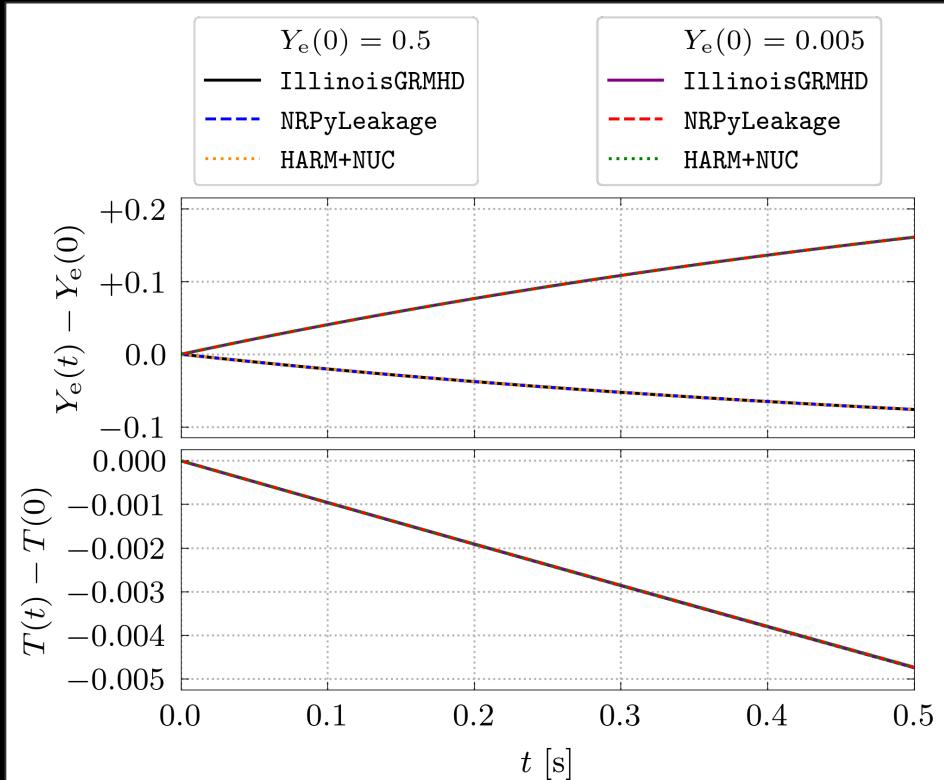


Based on [Ruffert et al. \(1996\)](#):

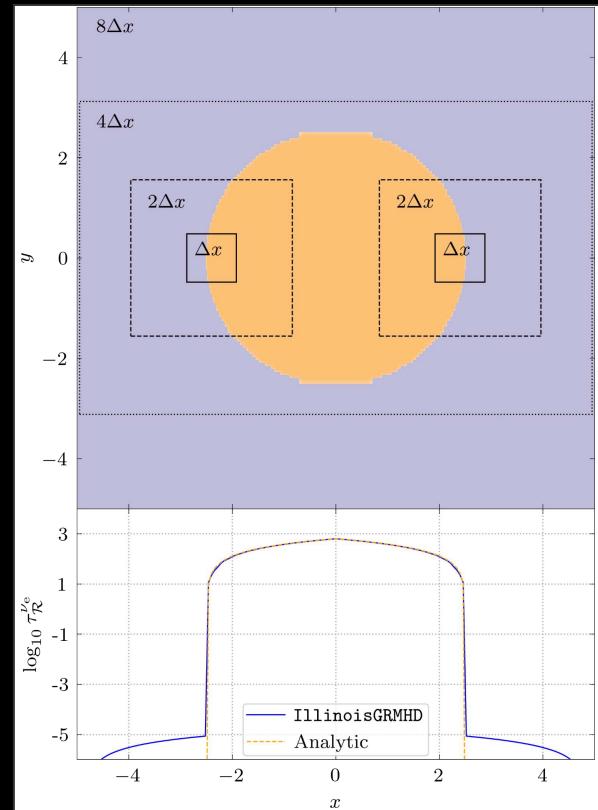
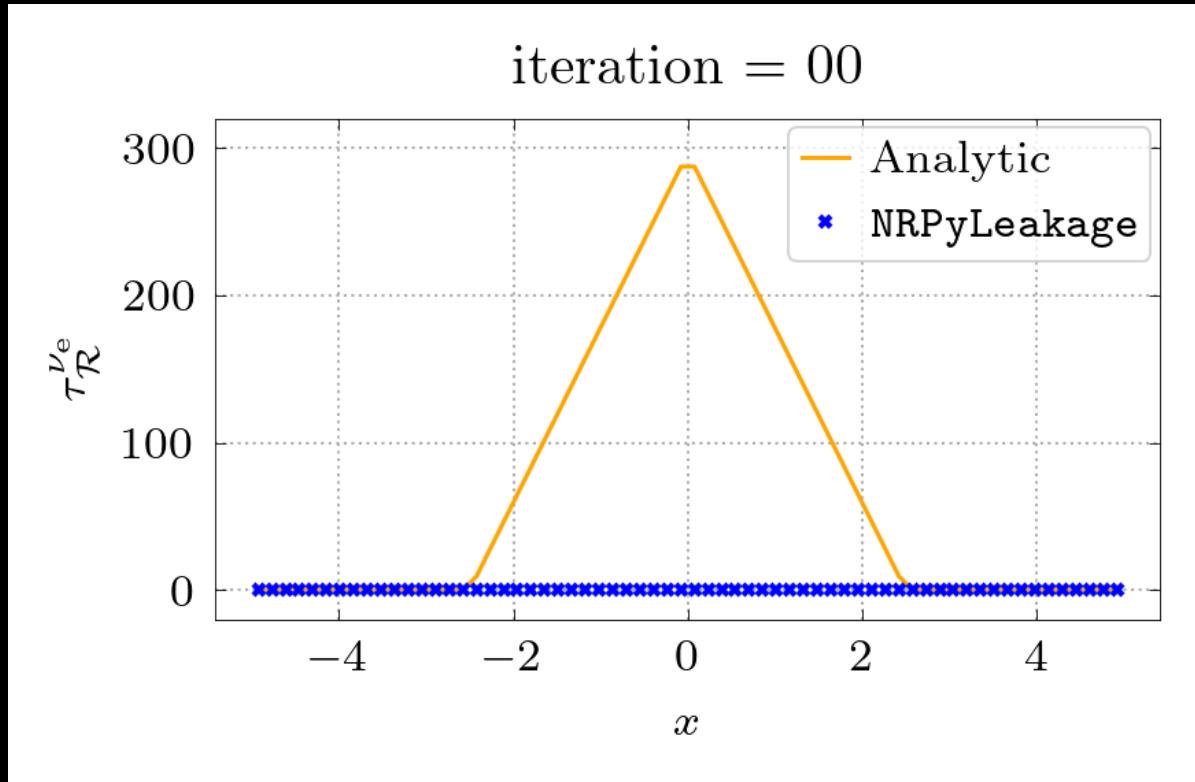
- Electron absorption by protons
- Positron absorption by neutrons
- Pair annihilation
- Transverse plasmon decay



Nucleon-nucleon Bremsstrahlung following  
[Burrows et al. \(2006\)](#) and [O'Connor & Ott \(2011\)](#)



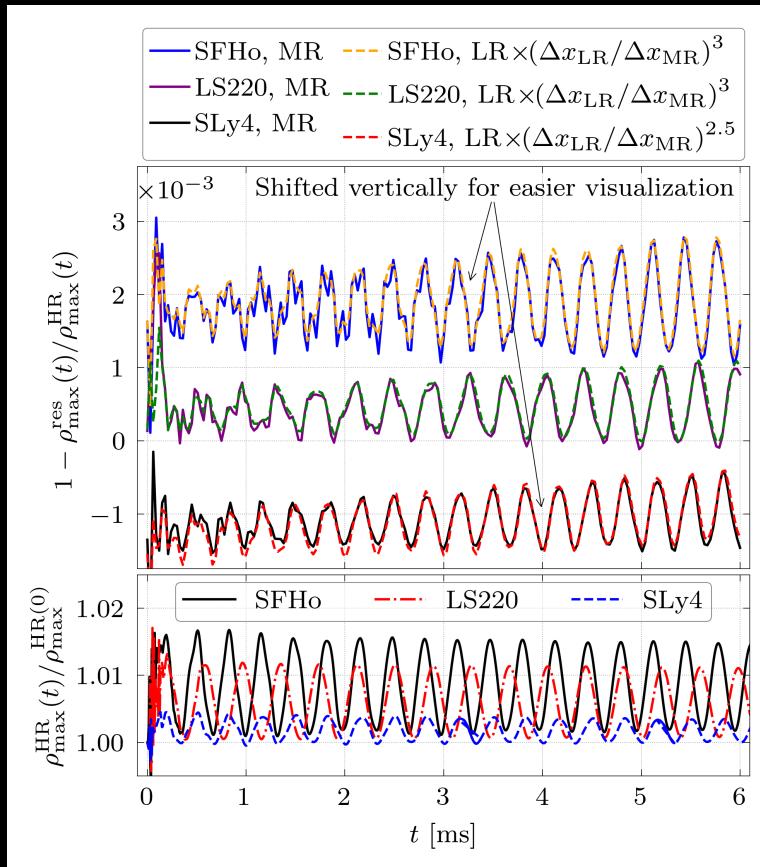
# Neutrino opacities & optical depths



Based on [Ruffert et al. \(1996\)](#) and [Neilsen et al. \(2011\)](#)

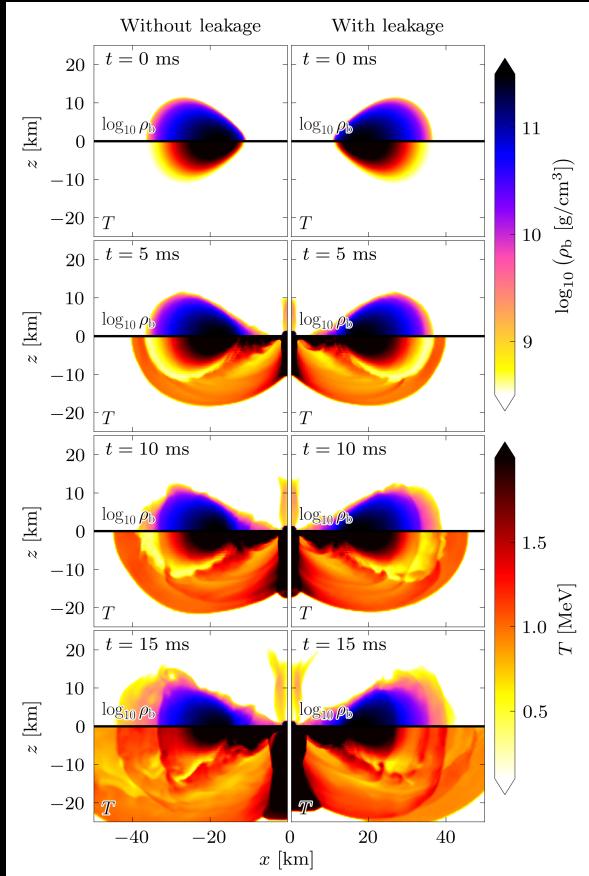
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# Single neutron stars: convergence test



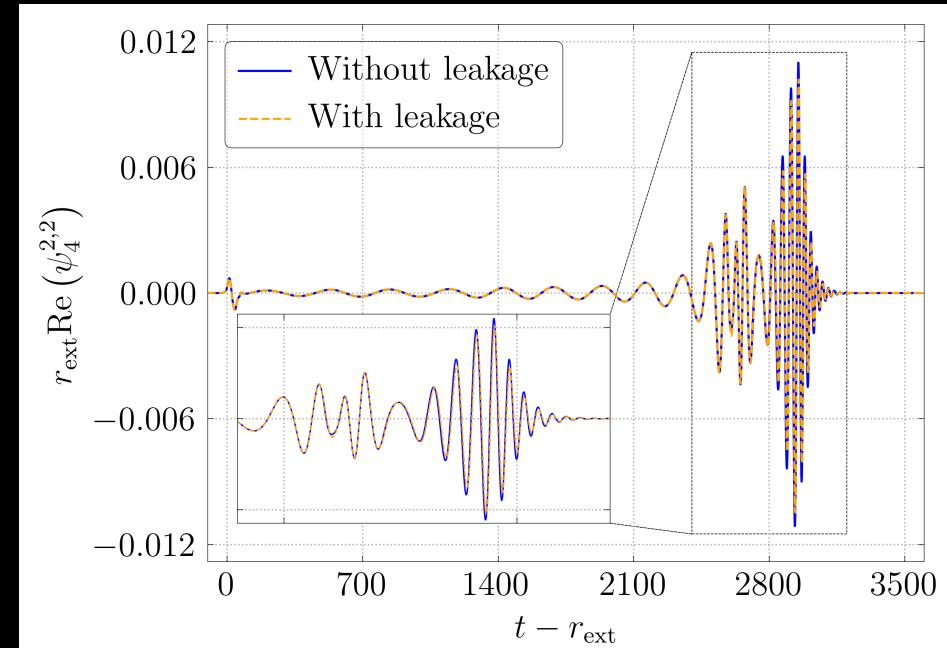
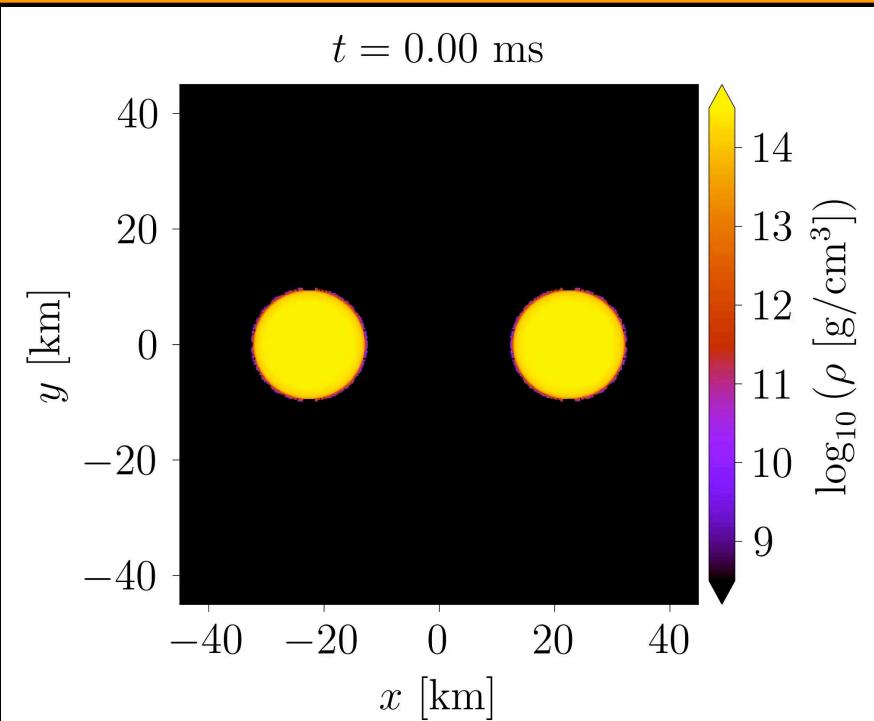
- $M_{\text{TOV}} = 1.4M_{\odot}$
- Unmagnetized
- Fully dynamical spacetime
- Finite resolution induces oscillations
- Should converge away with resolution

# BH accretion disks: Fishbone–Moncrief



- Unmagnetized
- Fully dynamical spacetime
- Disk structure is reasonably well preserved
- Neutrinos lead to slightly cooler system

# Magnetized, equal-mass BNS with tabulated EOS + neutrino leakage



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- Equal-mass (1.39 solar masses)
- Magnetized
- Microphysical, tabulated EOS ([O'Connor & Ott LS220 EOS](#))
- Neutrino leakage enabled ([NRPyLeakageET](#))
- Initial data produced by Tanmayee Gupte using LORENE

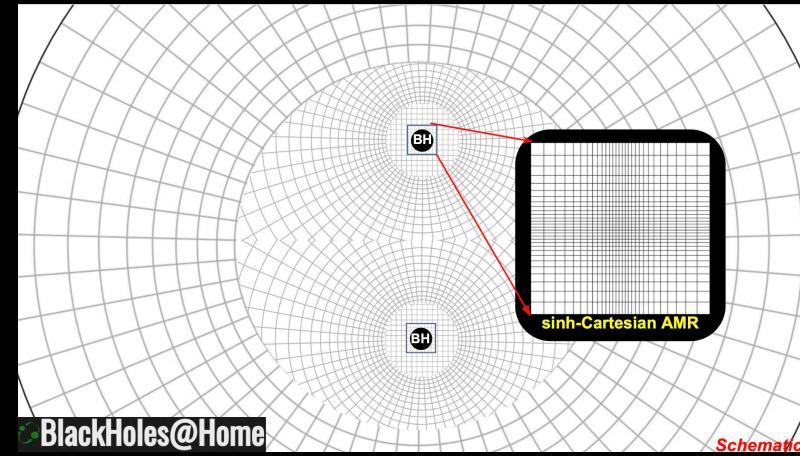


## Recap

- Goal: Reliably and accurately evolve the remnant black hole for astrophysically relevant (very very long) time scales
- Infrastructure to **HandOff** data from **IllinoisGRMHD** to **HARM+NUC** is ready!
- **IllinoisGRMHD** has been updated with:
  - New conservative-to-primitive infrastructure
  - Microphysical finite-temperature equation of state (EOS) support
  - Electron fraction and temperature evolution
  - Neutrino physics via a leakage scheme (**NRPyLeakage**)

# Future work

- CarpetX  
(Lorenzo Ennogi/Erik Schnetter's Talk)
- GPU support  
(F. Armengol/L. Ennogi/J. Kalinani's Tutorial)
- “Curvi-IllinoisGRMHD”  
(T. Pierre Jacques's Talk)
- BlackHoles@Home grids  
(Z. Etienne's Talk)
- Open source the code
- Include in future ET release



# Thank you

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