

Financial Engineering and Computations Basic Financial Mathematics

Dai, Tian-Shyr

此章內容



Financial Engineering & Computation教課書
 第三章 Basic Financial Mathematics

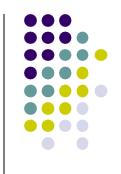
• C++財務程式設計的第三章 (3-4,3-5)

Outline



- Time Value of Money
- Annuities
- Amortization
- Yields
- Bonds

Time Value of Money

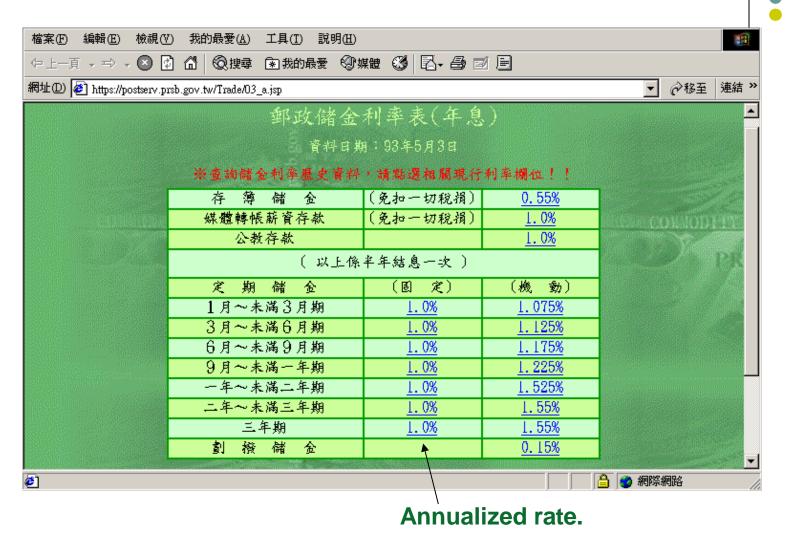


$$PV = FV(1+r)^{-n}$$

$$FV = PV(1+r)^n$$

- FV: future value
- PV: present value
- r: interest rate
- n: period terms

Quotes on Interest Rates



r is assumed to be constant in this lecture.

Time Value of Money



Periodic compounding
 (If interest is compounded m times per annum)

$$FV = PV\left(1 + \frac{r}{m}\right)^{nm} \tag{3.1}$$

Continuous compounding

$$FV = PVe^{rn}$$

$$\lim_{t \to \infty} (1 + \frac{1}{t})^t = e \to \lim_{m \to \infty} (1 + \frac{r}{m})^{nm} = \lim_{m \to \infty} (1 + \frac{1}{m/r})^{\frac{m}{r}} = e^{rn}$$

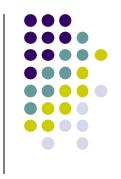
Simple compounding

Common Compounding Methods



- Annual compounding: m = 1.
- Semiannual compounding: m = 2.
 - Bond equivalent yield (BEY)
 - --Annualize yield with semiannual compounding
- Quarterly compounding: m = 4.
- Monthly compounding: m = 12.
 - Mortgage equivalent yield (MEY)
 - --Annualize yield with monthly compounding
- Weekly compounding: m = 52.
- Daily compounding: m = 365

Equivalent Rate per Annum



- Annual interest rate is 10% compounded twice per annum.
- Each dollar will grow to be 1.1025 one year from now.

$$(1+(0.1/2))^2 = 1.1025$$

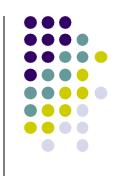
• The rate is equivalent to an interest rate of 10.25% compounded once *per annum*.

Conversion between compounding Methods



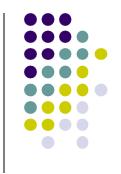
- Suppose r_1 is the annual rate with continuous compounding.
- Suppose r_2 is the equivalent compounded m times per annum.
- Then $\left(1+\frac{r_2}{m}\right)^m = e^{r_1}$
- Therefore $r_1 = m \ln \left(1 + \frac{r_2}{m} \right) \Rightarrow r_2 = m \left(e^{\frac{r_1}{m}} 1 \right)$

Are They Really "Equivalent"?



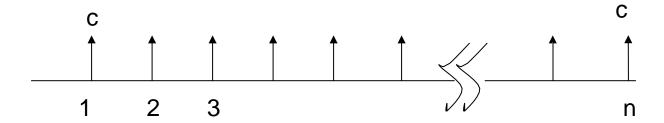
- Recall r_1 and r_2 on the previous example.
- They are based on different cash flow.
- In what sense are they equivalent?

Annuities



- An annuity pays out the same C dollars at the end of each year for years.
- With a rate or r, the FV at the end of the nth year is

$$\sum_{i=0}^{n-1} C(1+r)^{i} = C \frac{(1+r)^{n} - 1}{r}$$
(3.4)



General Annuities



• If m payments of C dollars each are received per year, then Eq.(3.4) becomes

$$C \frac{\left(1 + \frac{r}{m}\right)^{nm} - 1}{\frac{r}{m}}$$

• The PV of a general annuity is

$$\sum_{i=1}^{nm} C \left(1 + \frac{r}{m} \right)^{-i} = C \frac{1 - \left(1 + \frac{r}{m} \right)^{-nm}}{\frac{r}{m}}$$
 (3.6)

Perpetual annuity



• An annuity that lasts forever is called a perpetual annuity. We can drive its *PV* from Eq.(3.6) by letting *n* go to infinity:

$$PV = \lim_{n \to \infty} \sum_{i=1}^{nm} C \left(1 + \frac{r}{m} \right)^{-i} = \lim_{n \to \infty} C \frac{1 - \left(1 + \frac{r}{m} \right)^{-n}}{\frac{r}{m}} = \frac{mC}{r}$$

• This formula is useful for valuing *perpetual fix-coupon debts*.

Amortization



- It is a method of repaying a loan through regular payment of interest and principal.
- The size of the loan (the original balance) is reduced by the principal part of each payment.
- The interest part of each payment pays the interest incurred on the remaining principal balance.
- As the principal gets paid down over the term of the loan, the the interest part of the payment diminishes.

See next example!

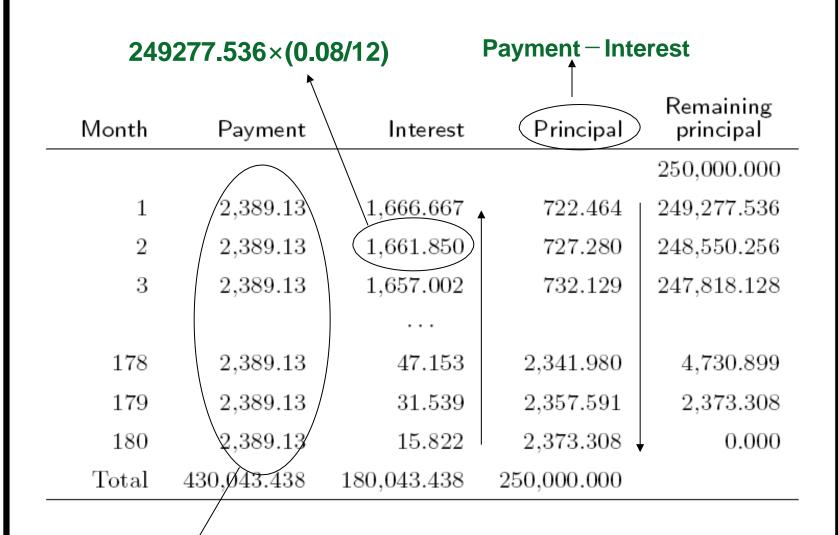
Example: Home mortgages



- Consider a 15-year, \$250,000 loan at 8.0% interest rate, repay the loan per month.
- Because PV = 250,000, n = 15, m = 12, and r = 0.08 we can get a monthly payment C is \$2,389.13.

$$$250000 = \frac{C}{(1+\frac{0.08}{12})} + \frac{C}{(1+\frac{0.08}{12})^2} + \dots + \frac{C}{(1+\frac{0.08}{12})^{12\times15}}$$

$$= \sum_{i=1}^{180} C \left(1 + \frac{0.08}{12}\right)^{-i} = C \left(\frac{1 - (1 + \frac{0.08}{12})^{-180}}{0.08/12}\right) \Rightarrow C = 2389.13$$



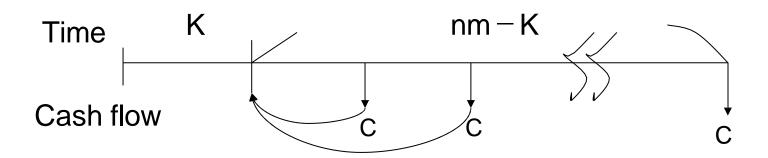
We compute it in last page

Calculating the Remaining Principal

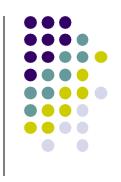


• Right after the kth payment, the remaining principal is the PV of the future nm-k cash flows,

$$C(1+\frac{r}{m})^{-1} + C(1+\frac{r}{m})^{-2} + \dots + C(1+\frac{r}{m})^{-(nm-k)} = C \frac{1-(1+\frac{r}{m})^{-nm+k}}{\frac{r}{m}}$$

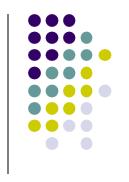


Yields



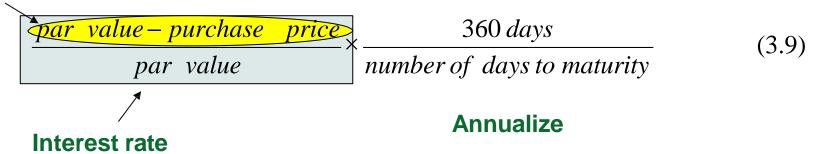
- The term **yield** denotes the return of investment.
- It has many variants.
 - (1) Nominal yield (coupon rate of the bond)
 - (2) Current yield
 - (3) Discount yield
 - (4) CD-equivalent yield

Discount Yield



- U.S *Treasury bills* is said to be issue on a discount basis and is called a discount security.
- When the discount yield is calculated for short-term securities, a year is assumed to have 360 days.
- The discount yield (discount rate) is defined as

Interest



Example 3.4.1: Discount yield



• If an investor buys a U.S. \$ 10,000, 6-month T-bill for U.S. \$ 9521.45 with 182 days remaining to maturity.

Discount yield =
$$\frac{10000 - 9521.45}{10000} \times \frac{360}{182} = 0.0947$$

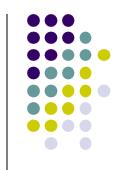
• Show that discount yield < CD equivalent yield

CD-equivalent yield



- It also called the money-market-equivalent yield.
- It is a simple annualized interest rate defined as

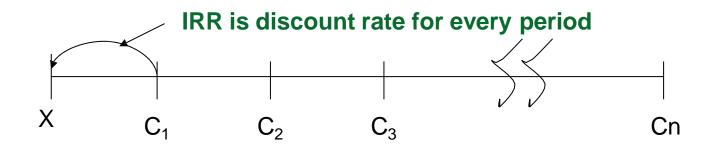
Internal Rate of Return (IRR)



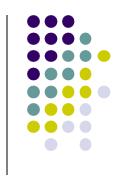
• It is the interest rate which equates an investment's PV with its price *X*.

$$X = C_{1} \times (1 + IRR)^{-1} + C_{2} \times (1 + IRR)^{-2} + \dots + C_{n} \times (1 + IRR)^{-n}$$

- IRR assumes all cash flows are reinvested at the same rate as the internal rate of return.
- It doesn't consider the reinvestment risk.



Evaluating real investment with IRR



- Multiple IRR arise when there is more than one sign reversal in the cash flow pattern, and it is also possible to have no IRR.
- Evaluating real investment, IRR rule breaks down when there are multiple IRR or no IRR
- Additional problems exist when the term structure of interest rates is not flat.
 - →there is ambiguity about what the appropriate hurdle rate (cost of capital) should be.

Class Exercise



• Assume that a project has cash flow as follow respectively, and initial cost is \$1000 at date 0, please calculate the IRR. If cost of capital is 10%, do you think it is a good project?

CF at da	ate				
0	1	2	3	4	IRR
-1000	800	1000	1300	-2200	?





12	Time	CF	•	
13	0	-1000		
14	1	800		
15	2	1000		
16	3	1300		
17	4	-2200	=IRR(B13:B17,0.1)	
18		7%		
19		37%	=IRR(B13:B17,0.2)	
20	Multiple	e IRR		
21				

Numerical Methods for Yield



• Solve $f(r) = \sum_{t=1}^{n} \frac{C_t}{(1+r)^t} - x = 0$, for $r \ge -1$, x is market price

Recall
$$X = C_1 \times (1 + IRR)^{-1} + ... + C_n \times (1 + IRR)^{-n}$$

$$\Rightarrow C_1 \times (1 + IRR)^{-1} + ... + C_n \times (1 + IRR)^{-n} - X = 0$$
Let $f(r) = C_1 \times (1 + r)^{-1} + ... + C_n \times (1 + r)^{-n} - X$

• The function f(r) is monotonic in r, if $C_t > 0$ for all t, hence a unique solution exists.

The Bisection Method



- Start with a and b where a < b and f(a) f(b) < 0.
- Then f(r) must be zero for some $r \in (a, b)$.
- If we evaluate f at the midpoint $c \equiv (a+b)/2$

$$(1) f(a) f(c) < 0 \Rightarrow a < r < c$$

$$(2) f(c) f(b) < 0 \Rightarrow c < r < b$$

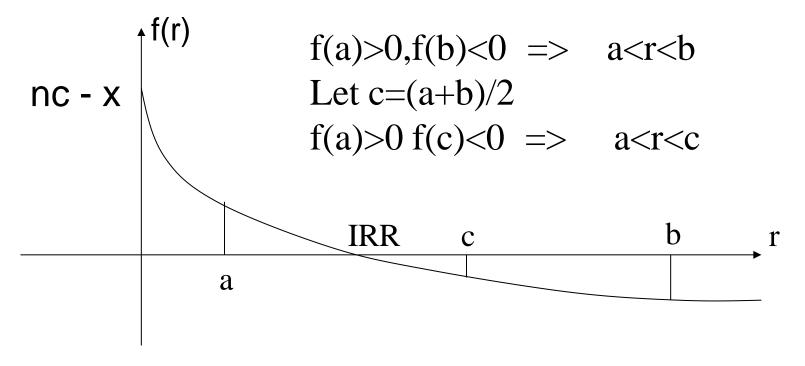
• After *n* steps, we will have confined *r* within a bracket of length $(b - a)/2^n$.

Bisection Method



• Let
$$f(r) = C \times (1+r)^{-1} + C \times (1+r)^{-2} + ... + C \times (1+r)^{-n} - X$$

• Solve f(r)=0



C++:使用while 建構二分法



printf("Yield rate=%f",High);

```
float Low=0, High=1;
輸入每期報酬c,期數n,期初投入X
                                    令 Middle =(High+Low)/2;
                                    找出R落在 (Low, Middle)或 (Middle, High)
                             true
                                                      float c,x,Discount;
     while(High-Low>=0.0001)
                                                      float Low=0, High=1;
                                                      int n;
                                                      scanf("%f",&c);
                 false
                                            程式碼:
                                                      scanf("\%f",&x);
                                                      scanf("%d",&n);
                                                      while(High-Low>=0.0001)
```

用Bisection method縮小根的範圍



- $C + C = c \times (1+r)^{-1} + c \times (1+r)^{-2} + ... + c \times (1+r)^{-n} x$
 - $f(r)<0 \rightarrow r>R$
 - $f(r)>0 \rightarrow r< R$
- 今 Middle=(High+Low)/2
 - 將根的範圍從(Low,High)縮減到
 - (Low,Middle)
 - (Middle,High)

$$c \times (1+r)^{-1} + c \times (1+r)^{-2} + \dots + c \times (1+r)^{-n}$$

用計算債券的公式計算

縮小根的範圍

```
float Middle=(Low+High)/2;
float Value=0;
for(int i=1;i \le n;i=i+1)
Discount=1:
for(int j=1; j <=i; j++)
         Discount=Discount/(1+Middle)
 Value=Value+Discount*c;
Value=Value-x:
if(Value>0)
          { Low=Middle;}
 else
          {High=Middle;}
```

計算IRR (完整程式碼)

用while控制根的範圍

縮小根的範圍

計算 $c \times (1+r)^{-1} + c \times (1+r)^{-2} + ... + c \times (1+r)^{-n}$

計算 (1+r)-i

```
float c,x,Discount;
float Low=0, High=1;
int n;
scanf("%f",&c);
\operatorname{scanf}("\%f",\&x);
scanf("%d",&n);
while(High-Low>=0.0001)
float Middle=(Low+High)/2;
float Value=0;
for(int i=1;i \le n;i=i+1)
 Discount=1;
 for(int j=1;j <= i;j++)
          Discount=Discount/(1+Middle);
  Value=Value+Discount*c;
 Value=Value-x;
if(Value>0)
           { Low=Middle; }
  else
           {High=Middle;}
```

Homework 1

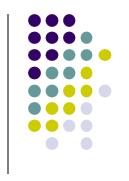


•第三章第十題

假定有一個投資計畫,該投資計畫可在現在獲得 9702元收益,在第一期結束時需支付19700元,第 二期計畫結束時,可再獲得10000元,請仿照上述 求內部收益率的程式,撰寫程式使用二分法求內部 收益率,請問這種解法會不會碰到問題? 請用Newton method 驗證計算結果

C++財務程式設計

The Newton-Raphson Method



- Converges faster than the bisection method.
- Start with a first approximation X_0 to a root of f(x) = 0.

• Then
$$x_{k+1} \equiv x_k - \frac{f(x_k)}{f'(x_k)}$$
 (3.15)

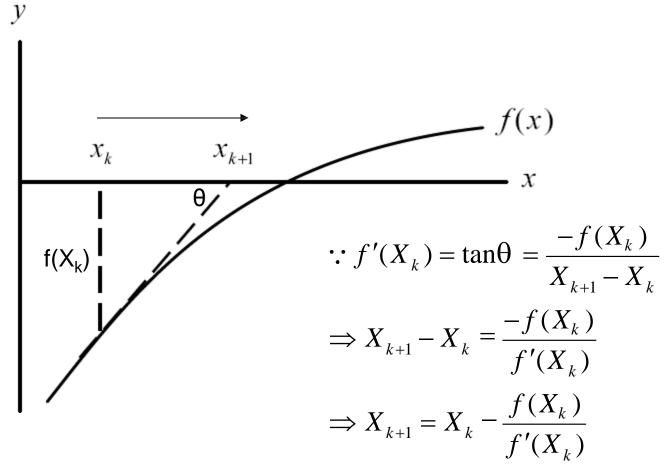
• When computing yields,

$$f'(x) = \sum_{t=1}^{n} \frac{t C_t}{(1+x)^{t+1}}$$

X Recall the bisection method, the X here is r (yield) in the bisection method!

Figure 3.5: Newton-Raphson method





If $f(X_{k+1})=0$, we can obtain X_{k+1} is yield



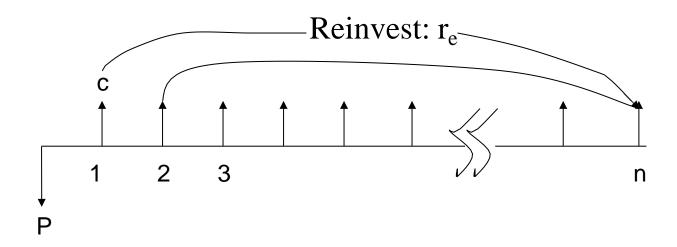
Holding Period Return

Holding period return is the **total return** received from holding an asset or portfolio of assets over a period of time



Holding Period Return





- The FV of investment in n period is $FV = P(1+y)^n$
- Let the reinvestment rates r_e , the FV of per cash income is $C \times (1+r_e)^{n-1} + C \times (1+r_e)^{n-2} + ... + C \times (1+r_e)^{n-2} + C \longrightarrow Value is given$
- We define HPR (y) is

$$P(1+y)^n = C \times (1+r_e)^{n-1} + C \times (1+r_e)^{n-2} + \dots + C \times (1+r_e) + C$$

Methodology for the HPR(y)



- Calculate the FV and then find the yield that equates it with the P
- Suppose the reinvestment rates has been determined to be r_e .

Step	Periodic compounding	Continuous compounding
(1)Calculate the future value	$FV = \sum_{t=1}^{n} C (1+r_{e})^{n-t}$	$FV = C \times \frac{(e^{r_e n} - 1)}{e^{r_e} - 1}$
(2)Find the HPR	$y = \sqrt[n]{\frac{FV}{P}} - 1$	$y = \frac{1}{n} \ln(\frac{FV}{P})$

Example 3.4.5:HPR



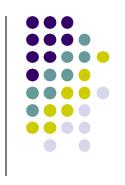
• A financial instrument promises to pay \$1,000 for the next 3 years and sell for \$2,500. If each cash can be put into a bank account that pays an effective rate of 5%.

The FV is
$$\sum_{t=1}^{3} 1000 \times (1 + 0.05)^{3-t} = 3152.5$$

The HPR is $2500(1+HPR)^3 = 3152.5$

$$\Rightarrow$$
 HPR = $\left(\frac{3152.5}{2500}\right)^{1/3} - 1 = 0.0804$

Bond



- A bond is a contract between the issuer (borrower) and the bondholder (lender).
- Bonds usually refer to long-term debts.
- Repay to the lender the amount borrowed plus interest over a specified period of time.
- Callable bond, convertible bond.
- Pure discount bonds vs. level-coupon bond

Bond

•••)
•••	

	A Treasury
Issue date	2002/5/15
Face value	1000000
Coupon rate	3.50%
Maturity date	2006/11/15
Frequency in a year	2

"Bond components"

		• •
bond		
Date	Cash f	low
2002/5/15		0
2002/11/15		17500
2003/5/15		17500
2003/11/15		17500
2004/5/15		17500
2004/11/15		17500
2005/5/15		17500
2005/11/15		17500
2006/5/15		17500
2006/11/15	1	017500

Bond





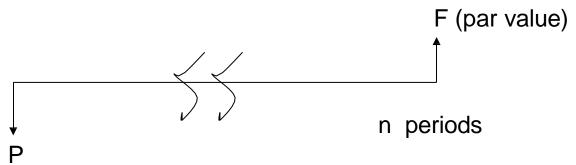
Zero-Coupon Bonds (Pure Discount Bonds)



• The price of a zero-coupon bond that pays F dollars in n periods is $P = \frac{F}{(1+r)^n}$

where r is the interest rate per period

- No coupon is paid before bond mature.
- Can meet future obligations without reinvestment risk.

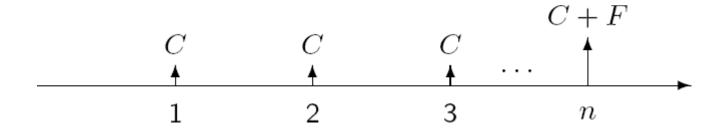


Level-Coupon Bonds



- It pays interest based on coupon rate and the par value, which is paid at maturity.
- F denotes the par value and C denotes the coupon.

$$P = C \times (1+r)^{-1} + C \times (1+r)^{-2} + \dots + C \times (1+r)^{-n} + F \times (1+r)^{-n}$$



Pricing of Level-Coupon Bonds



$$P = \frac{C}{(1 + \frac{r}{m})} + \frac{C}{(1 + \frac{r}{m})^2} + \dots + \frac{C}{(1 + \frac{r}{m})^{nm}} + \frac{F}{(1 + \frac{r}{m})^{nm}}$$

$$= \sum_{i=1}^{nm} \frac{C}{(1 + \frac{r}{m})^i} + \frac{F}{(1 + \frac{r}{m})^{nm}} = C \left(\frac{1 - (1 + \frac{r}{m})^{-nm}}{\frac{r}{m}}\right) + \frac{F}{(1 + \frac{r}{m})^{nm}}$$
(3.18)

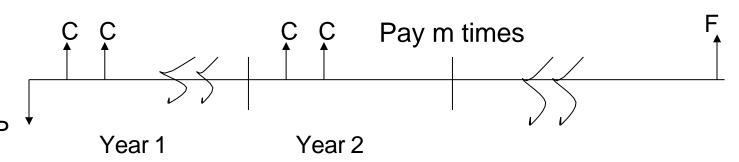
where

n: time to maturity (in years)

m : number of payments per year.

r: annual rate compounded m times per annum.

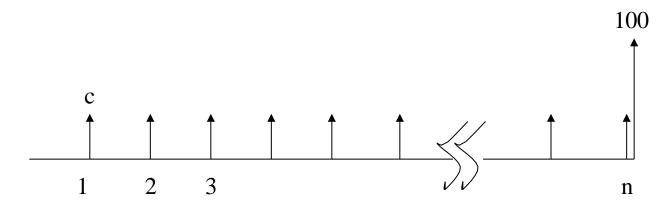
C = Fc/m where c is the annual coupon rate.



C++:計算債券價格



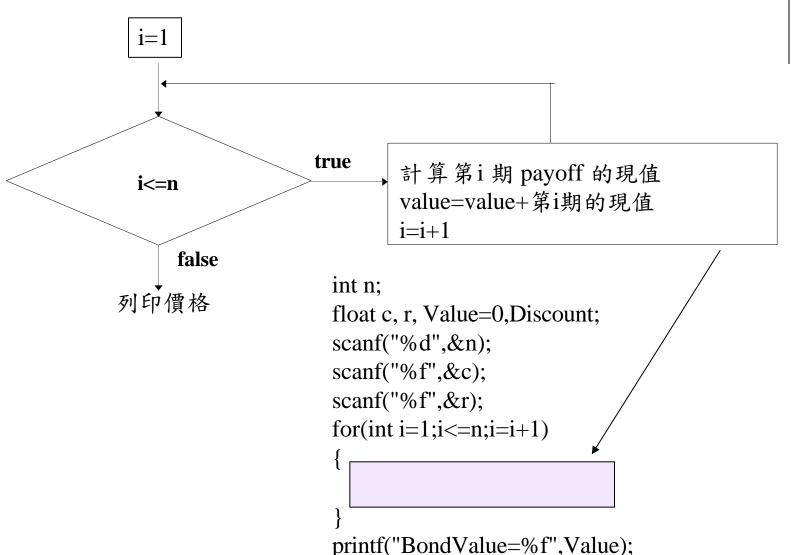
- 考慮債券價格的計算
 - 假定單期利率為r
 - 每一期支付coupon c,共付n期
 - 到期日還本100元



債券價格 $P = c \times (1+r)^{-1} + c \times (1+r)^{-2} + ... + c \times (1+r)^{-n} + 100 \times (1+r)^{-n}$

程式想法





計算第i次 payoff的現值



- i<n 現值= $(1+r)^{-i} \times c$
- i=n 現值= $(1+r)^{-n} \times (c+100)$
- 用for計算 (1+r)-i

計算第i次 payoff的現值

```
Discount=1;
for(int j=1;j<=i;j++)

計算 (1+r)<sup>-i</sup> {
    Discount=Discount/(1+r);
    }
    Value=Value+Discount*c;
    if(i==n)
    {
        Value=Value+Discount*100;
    }
```

完整程式碼(包含巢狀結構)

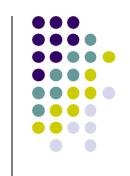
```
#include <stdio.h>
             void main()
                       int n;
                       float c, r, Value=0, Discount;
                     scanf("%d",&n);
                       scanf("%f",&c);
                       scanf("%f",&r);
                     for(int i=1;i <= n;i=i+1)
                                                               第i次 payoff的現值
                        Discount=1;
                        for(int j=1; j<=i; j++)
                        Discount=Discount/(1+r);
                                                               Value為前i次payoff 現值
Use pow(x,y) to
                      Value=Value+Discount*c;
evaluate x^y
                        if(i==n)
                        Value=Value+Discount*100;
                printf("BondValue=%f",Value);
```



• The YTM of a level-coupon bond is its IRR when the bond is held to maturity.

• For a 15% BEY, a 10-year bond with a coupon rate of 10% paid semiannually sells for

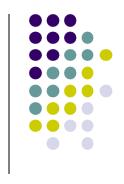
$$P = \frac{5}{(1 + \frac{0.15}{2})} + \dots + \frac{5}{(1 + \frac{0.15}{2})^{20}} + \frac{100}{(1 + \frac{0.15}{2})^{20}}$$
$$= 5 \times \frac{1 - (1 + (0.15/2))^{-2 \times 10}}{0.15/2} + \frac{100}{(1 + (0.15/2))^{2 \times 10}} = 74.5138$$



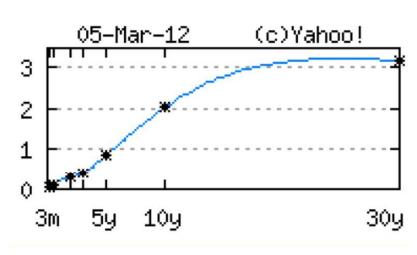
Approxmate YTM =
$$\frac{C + \frac{FV - PV}{N}}{\frac{FV + PV}{2}}$$

Suppose you were offered a 14-year, 10% annual coupon, \$1,000, par value bond at a price of \$1,494.93

Approxmate YTM =
$$\frac{1000-1494.93}{\frac{14}{2}} \approx 5\%$$

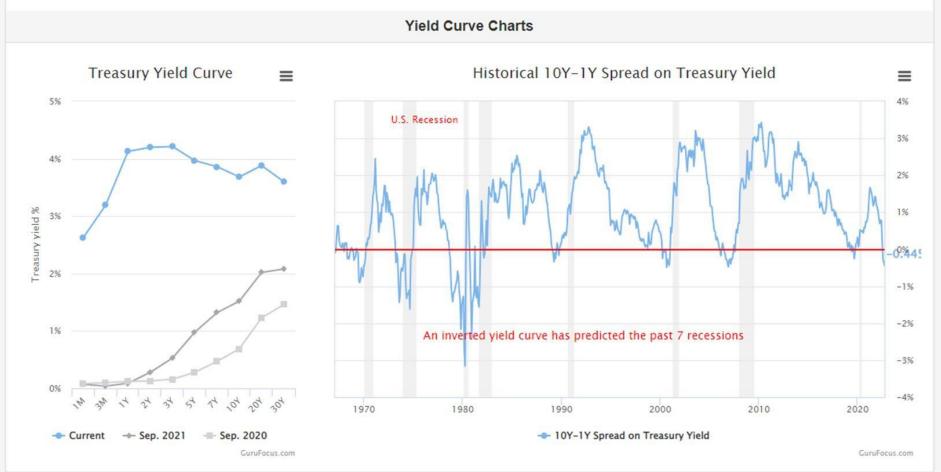


US Treasury Bonds Rates				
Maturity	Yield	Yesterday	Last Week	Last Month
3 Month	0.04	0.04	0.08	0.06
6 Month	0.11	0.1	0.13	0.08
2 Year	0.29	0.27	0.28	0.23
3 Year	0.41	0.38	0.4	0.32
5 Year	0.85	0.82	0.82	0.76
10 Year	2.01	1.97	1.92	1.92
30 Year	3.15	3.1	3.04	3.12

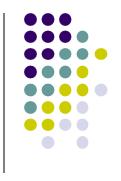


- Interest is inversely related to bond prices
- Under normal conditions, YTM tends to increase over time, forming an upward-sloping curve.

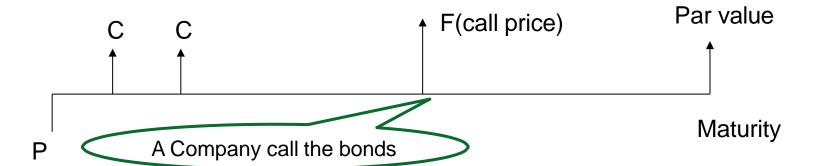




Yield To Call

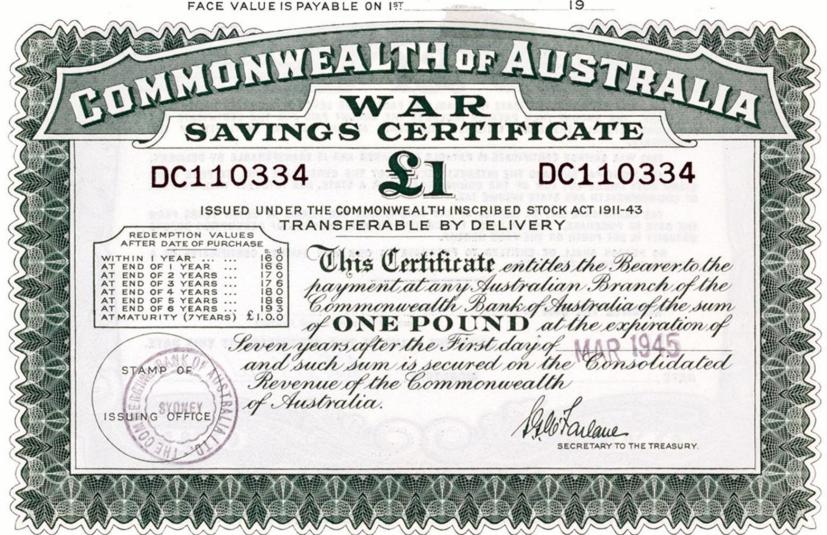


- For a callable bond, the yield to states maturity measures its yield to maturity as if were not callable.
- The yield to call is the yield to maturity satisfied by Eq(3.18), when *n* denoting the number of remaining coupon payments until the first call date and *F* replaced with call price.



Example of a Call Schedule



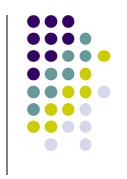


Price Behaviors



- Bond price falls as the interest rate increases, and vice versa.
- A level-coupon bond sells
 - at a premium (above its par value) when its
 coupon rate is above the market interest rate.
 - at par (at its par value) when its coupon rate is equal to the market interest rate.
 - at a discount (below its par value) when its
 coupon rate is below the market interest rate.

Figure 3.8: Price/yield relations

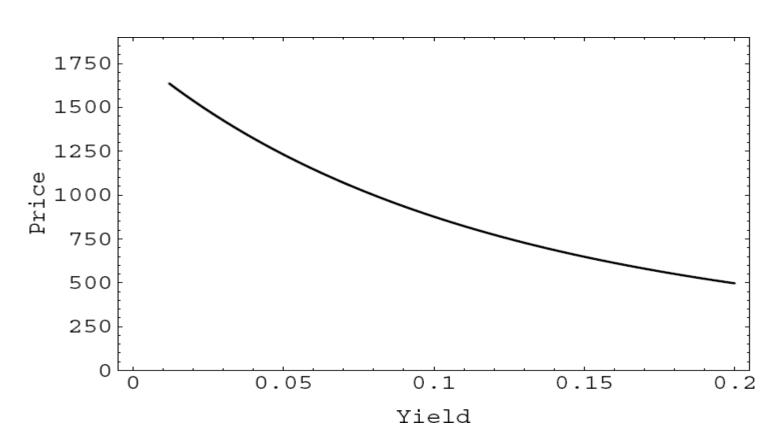


)	Price (% of par	Yield (%)
	113.37	7.5
→ Premium bond	108.65	8.0
	104.19^{J}	8.5
→Par bond	100.00	9.0
	96.04	9.5
→Discount bond	92.31	10.0
	88.79	10.5

Figure 3.9: Price vs. yield.



Plotted is a bond that pays 8% interest on a par value of \$1,000,compounding annually. The term is 10 years.



Day Count Conventions: Actual/Actual



- The first "actual" refers to the actual number of days in a month.
- The second refers to the actual number of days in a year.
- Example: For coupon-bearing Treasury securities, the number of days between June 17, 1992, and October 1, 1992, is *106*.
 - →13 days (June), 31 days (July), 31 days (August), 30 days (September), and 1 day (October).

Day Count Conventions:30/360

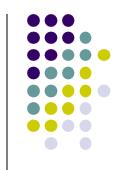


- Each month has 30 days and each year 360 days.
- The number of days between June 17, 1992, and October 1, 1992, is *104*.
 - 13 days (June), 30 days (July), 30 days (August),30 days (September), and 1 day (October).
- In general, the number of days from date1 to date2 is

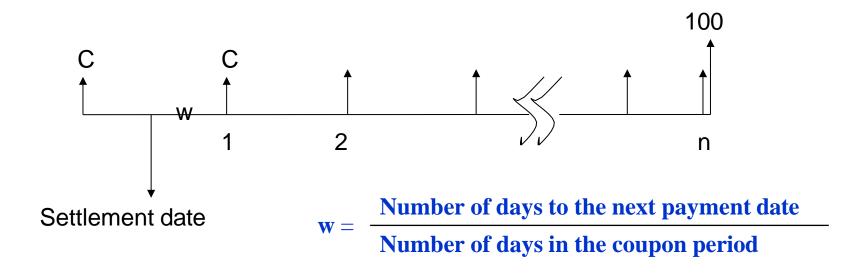
$$360 \times (y2 - y1) + 30 \times (m2 - m1) + (d2 - d1)$$

Where Date1 = $(y1, m1, d1)$ Date = $(y2, m2, d2)$

Bond price between two coupon date (Full Price, Dirty Price)

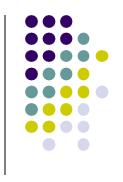


• In reality, the settlement date may fall on any day between two coupon payment dates.



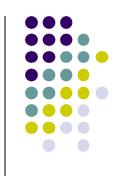
Dirty Price=
$$C \times (1+r)^{-\omega} + C \times (1+r)^{-\omega-1} + \dots + C \times (1+r)^{-\omega-n+1} + 100 \times (1+r)^{-\omega-n+1}$$

Accrued Interest



- The original bond holder has to share accrued interest in 1-ω period
 - Accrued interest is $C \times (1-\omega)$
- The quoted price in the U.S./U.K. does not include the accrued interest; it is called the *clean price*.
- Dirty price= Clean price+ Accrued interest

Example 3.5.3

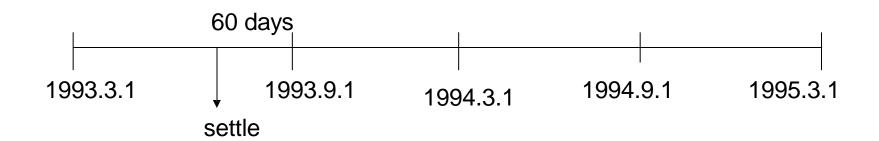


• Consider a bond with a 10% coupon rate, par value\$100 and paying interest semiannually, with clean price 111.2891. The maturity date is March 1, 1995, and the settlement date is July 1, 1993. The yield to maturity is 3%.

Example: solutions



- There are 60 days between July 1, 1993, and the next coupon date, September 1, 1993.
- The ω = 60/180, C=5,and accrued interest is $5 \times (1-(60/180)) = 3.3333$
- Dirty price=114.6224 clean price = 111.2891



Exercise 3.5.6



- Before: A bond selling at par if the yield to maturity equals the coupon rate. (But it assumed that the settlement date is on a coupon payment date).
- Now suppose the settlement date for a bond selling at par (i.e., the *quoted price* is equal to the par value) falls between two coupon payment dates.
- Then its yield to maturity is less than the coupon rate.
 - → The short reason: Exponential growth is replaced by linear growth, hence "overpaying" the coupon.

WRDS apply



• 圖書館主頁->搜索框輸入"WRDS"-> 整合查詢改成資料庫->依據文檔申請賬號。

申請步驟:

Step 1: 到WRDS網站註冊新帳號,並到信箱點擊確認信;

Step 2: 到線上表單 網址: https://forms.gle/hnP94tJ4fFSZC5o39填報申 請審核;

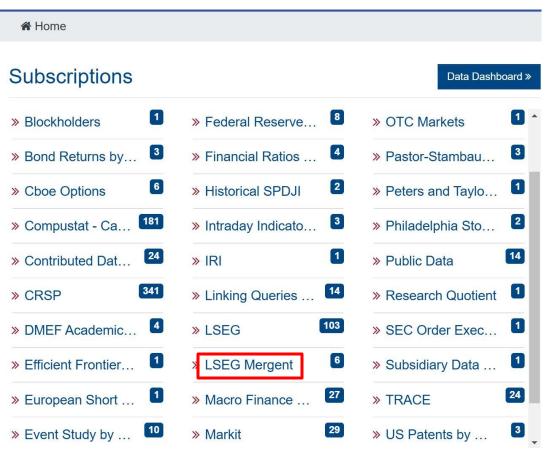
Step 3: 通過審核,系統寄發審核通過信件,按指示操作。若有相關問題,請洽林小姐(yulin@lib.nycu.edu.tw)。

FISD

進入WRDS主頁

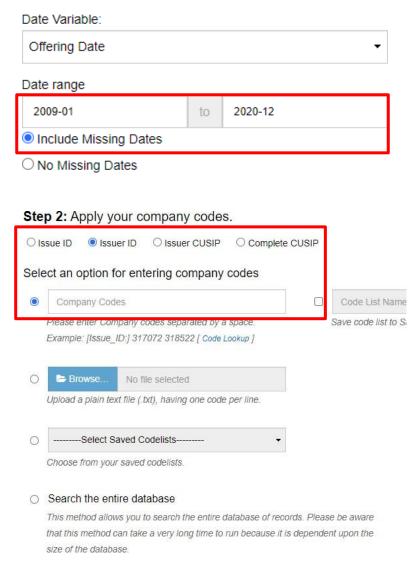
http://wrds-web.wharton.upenn.edu/

在Subscriptions找LSEG Mergent->選擇Bond Issues



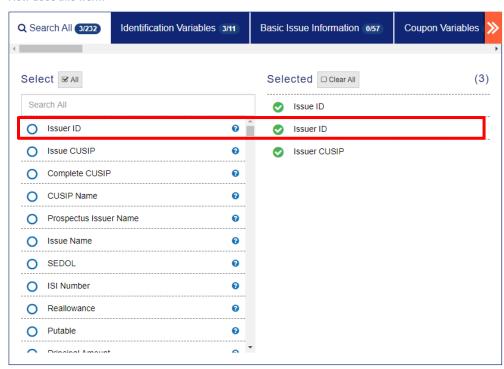


Step 1: Choose your date range.



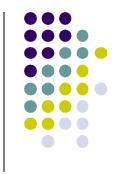
Step 3: Query Variables.

How does this work?



- 在搜索框一次輸入查詢所需變量
- 例子:
 - Date: 2020-01 to 2020-12
 - Issuerid: 33695 (Goldman Sachs 的issuer id)
 - Variables : coupon
- 最後選擇所需格式導出即可

Homework 2



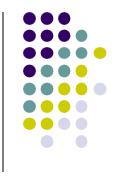
• Download NEEDED issuer data during time period (1990/01-2020/12) from FISD: use the given

```
issuer\_id = 34216
```

- OFFERING_DATE,
- *MATURITY*,
- COUPON, (coupon rate)
- DELIVERLY_DATE,(settlement date)
- *OFFERING_PRICE*,(*Present value*)
- OFFERING_YIELD.

^{*(}delete if variables are NA or Blank)

Homework 2



- Use the following data to calculate the bond YTM
 - OFFERING_DATE,
 - *MATURITY*,
 - COUPON,
 - OFFERING_PRICE,
 - OFFERING_YIELD.

(Use the previous formula to calculate IRR)

Note: The bond is assumed to pay coupons semiannually.

• and compare YTM with *OFFERING_YIELD*.

Note: OFFERING_YIELD is the actual YTM

Homework 2



- Continuing with the YTM calculated above, use the following data to calculate the dirty and the clean price for a bond under actual/actual and 30/360 day count conversion.
 - OFFERING_DATE,
 - *MATURITY*,
 - COUPON,
 - *DELIVERY_DATE*(settlement date)

Assum the par value is \$100