

FIG. 10: (Color online) Mean square displacement  $\Delta r^2(t_w, t_w + t)$  as defined in Eq. (7) for the temperature quench from 5000 K to 2500 K and for O-atoms. Waiting times and corresponding line styles are the same as in Fig. 4.

### C. Mean Square Displacement

In the previous section, we have focused on the analysis of  $C_q(t_w, t_w + t)$  and identified different time-windows. In this section, we consider the mean square displacement

$$\Delta r^2(t_w, t_w + t) = \frac{1}{N} \sum_{i=1}^N \left\langle (\mathbf{r}_i(t_w + t) - \mathbf{r}_i(t_w))^2 \right\rangle. \quad (7)$$

Figure 10 shows  $\Delta r^2(t_w, t_w + t)$  for the temperature quench from 5000 K to 2500 K and for O-atoms. As in Fig. 4, for times  $t \lesssim 5 \cdot 10^{-5}$  ns and zero waiting time, the mean square displacement  $\Delta r^2(t_w = 0, t)$  is well approximated by  $\Delta r^2$  of the high temperature  $T_i = 5000$  K from which the system has been quenched (see dashed line in Fig. 10) and thus independent of  $T_f$ . For times  $t \approx 10^{-3}$  ns,  $\Delta r^2(t_w, t_w + t)$  is oscillatory due to the small system size [31], while for times  $t \gtrsim 10^{-3}$  ns and waiting times  $t_w \geq 0.33$  ns, we find that  $\Delta r^2$  forms a plateau which is independent of  $t_w$ . As for  $C_q$ , we find that the plateau is the more horizontal the smaller  $T_f$  and the plateau height depends on the particle type but is independent of  $T_i$ .

For waiting times  $t_w \geq 0.33$  ns and times  $t \gtrsim 0.1$  ns, the mean square displacement leaves the plateau and increases further. To characterize the dependence of this  $\alpha$ -relaxation we define the time  $t_r^{\text{msd}}$  as the time  $t = t_r^{\text{msd}}$  for which  $\Delta r^2(t_w, t_w + t_r^{\text{msd}}) = 1.35 \text{ \AA}^2$  (see Fig. 11). We can identify again the three time windows (I) of waiting times  $t_w \lesssim 0.3$  ns with a dependence on  $T_i$ ,  $T_f$  and particle type, (II) the aging regime of intermediate waiting times where  $t_r^{\text{msd}}$  follows roughly a power law, and (III) for very long waiting times when equilibrium is reached. The transition from (II) to (III) occurs at approximately the

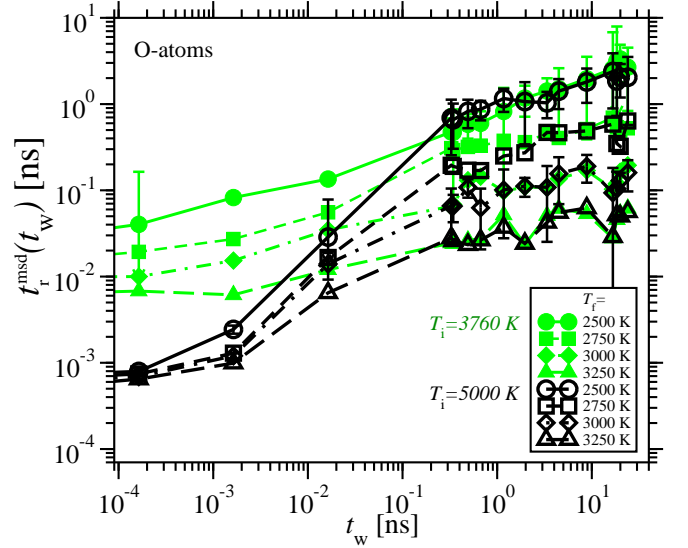


FIG. 11: (Color online)  $t_r^{\text{msd}}$  for O-atoms. Symbols for the different  $(T_i, T_f)$  combinations are the same as in Fig. 7. Error bars are indicated exemplarily for (3760 K, 2500 K), (5000 K, 2500 K) and (5000 K, 3000 K).

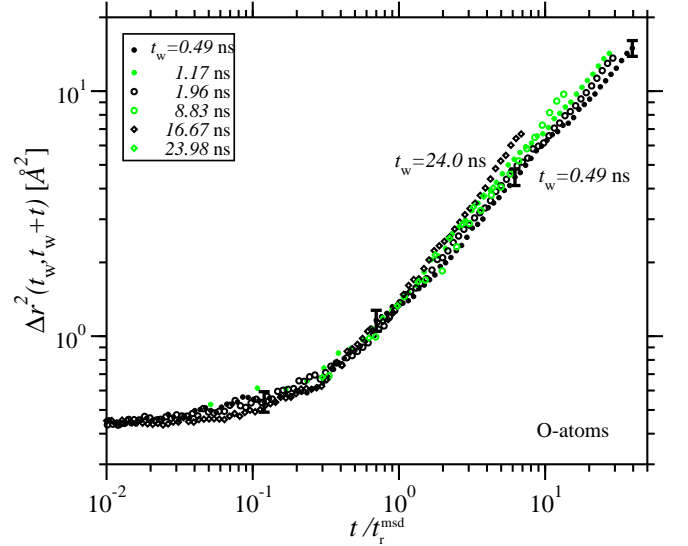


FIG. 12: (Color online)  $\Delta r^2(t/t_r^{\text{msd}})$  for the temperature quench from 5000 K to 2500 K and for O-atoms.

same times  $t_{23}$  as for  $C_q$ , i.e.  $t_{23} \approx 0.3$  ns for  $T_f = 3250$  K,  $t_{23} \approx 1$  ns for  $T_f = 3000$  K,  $t_{23} \approx 3$  ns for  $T_f = 2750$  K and  $t_{23} \approx 10$  ns for  $T_f = 2500$  K.

Figure 12 shows the equivalent of Fig. 8 to test time superposition. We find for  $\Delta r^2(t/t_r^{\text{msd}})$  that time superposition is valid for waiting times  $0.34 \text{ ns} \leq t_w \lesssim 8.83 \text{ ns}$ , i.e. for the time window (II) but not for the time window (III).