

Appendix B

We present the derivation of the expression (3.21) for the time relaxation $\tau_{\text{do},1}$. Substitution of the equation (3.20) for the irreversible time evolution of the configurational variable Q into the Doi-Ohta relaxation equation (1.7a) gives

$$\frac{1}{\tau_{\text{do},1}} = -\frac{l(\mathbf{r}_1)}{Q(\mathbf{r}_1)} \int_V d^3 r_2 M_{P_\epsilon}^{(2)',\text{dif}}(\mathbf{r}_1, \mathbf{r}_2) \frac{1}{T(\mathbf{r}_2)}. \quad (\text{B1})$$

Under the assumption of a homogeneous system, integration over the whole system size of the above expression gives

$$\frac{1}{\tau_{\text{do},1}} = -\frac{l}{QVT} \int_V d^3 r_1 \int_V d^3 r_2 M_{P_\epsilon}^{(2)',\text{dif}}(\mathbf{r}_1, \mathbf{r}_2). \quad (\text{B2})$$

The general expression (3.19) for the coarse-grained friction matrix $M^{(2)',\text{dif}}$ gives

$$\begin{aligned} M_{P_\epsilon}^{(2)',\text{dif}}(\mathbf{r}_1, \mathbf{r}_2) &= \int \mathcal{D}x \rho_y[x] \int_V d^3 r'_1 \int_V d^3 r'_2 \chi(\mathbf{r}_1 - \mathbf{r}'_1) \chi(\mathbf{r}_2 - \mathbf{r}'_2) \\ &\quad \times \int_V d^3 r_3 \int_V d^3 r_4 \frac{\delta \Pi_P[c](\mathbf{r}'_1)}{\delta c(\mathbf{r}_3)} M_{c\epsilon}^{(1),\text{dif}}(\mathbf{r}_3, \mathbf{r}_4) \frac{\delta \Pi_\epsilon[\epsilon](\mathbf{r}'_2)}{\delta \epsilon(\mathbf{r}_4)}, \end{aligned} \quad (\text{B3})$$

which after substitution of the appropriate functional derivatives, $M^{(1),\text{dif}}$ element, and the integration over \mathbf{r}_4 , \mathbf{r}'_1 , and \mathbf{r}'_2 becomes

$$\begin{aligned} M_{P_\epsilon}^{(2)',\text{dif}}(\mathbf{r}_1, \mathbf{r}_2) &= \int \mathcal{D}c \rho_{(Q,\mathbf{q})}[c] \int_V d^3 r' 2\kappa_E MT \frac{\partial}{\partial r'_\alpha} \left(\left(\frac{\partial^2 c}{\partial \mathbf{r}'^2} \right) \chi(\mathbf{r}_2 - \mathbf{r}') \right) \\ &\quad \times \frac{\partial^2}{\partial r'_\alpha \partial r'_\beta} \left(\frac{\partial c}{\partial r'_\beta} \chi(\mathbf{r}_1 - \mathbf{r}') \right), \end{aligned} \quad (\text{B4})$$

where we have used the assumption of a homogeneous ($M = \text{const.}$) and isothermal system, as well as the approximations based on a difference between the Cahn-Hilliard and Doi-Ohta length scales, as in Appendix A. Substitution of the friction matrix element (B4) into equation (B2), gives after using the normalization condition $\int_V d^3 r' \chi(\mathbf{r} - \mathbf{r}') = 1$, the final formula for the Doi-Ohta time relaxation

$$\frac{1}{\tau_{\text{do},1}} = \frac{2\kappa_E M l}{VQ} \int \mathcal{D}c \rho_{(Q,\mathbf{q})}[c] \int_V d^3 r \left[\frac{\partial}{\partial \mathbf{r}} \left(\frac{\partial^2 c(\mathbf{r})}{\partial \mathbf{r}^2} \right) \right]^2. \quad (\text{B5})$$

[1] R. G. Larson, *The Structure and Rheology of Complex Fluids* (Oxford University Press, New York, 1999).