



FIG. 8: The imprecision functions  $\epsilon(p)$  test the merit of using  $k$ -shell,  $k$  and  $C_B$  to identify the most efficient spreaders in the CNI, actor, collaboration, and email contact networks. The  $k$ -shell based identification method yields consistently lower imprecision compared to the  $k$  and  $C_B$  based methods.

the number of nodes that we consider in the comparison. By definition,  $M_{eff}(p) \geq M_{k_s}(p)$ , and the equality is only reached if  $\Upsilon_{eff}(p) = \Upsilon_{k_s}(p)$ . We assess the imprecision of  $k$ -shell identification by calculating the ratio between  $M_{eff}(p)$  and  $M_{k_s}(p)$ :

$$\epsilon_{k_s}(p) \equiv 1 - \frac{M_{k_s}(p)}{M_{eff}(p)}. \quad (4)$$

Similarly, we can define  $\epsilon_k(p)$  and  $\epsilon_{C_B}(p)$ :

$$\epsilon_k(p) \equiv 1 - \frac{M_k(p)}{M_{eff}(p)}, \quad \epsilon_{C_B}(p) \equiv 1 - \frac{M_{C_B}(p)}{M_{eff}(p)}. \quad (5)$$

A value for  $\epsilon$  close to 0 denotes a very efficient process, since the nodes that are chosen are practically those that contribute most to epidemics. In all cases, the  $k_s$  method yields a