



FIG. 11:  $\bar{\lambda}_s$  vs  $\bar{\Omega}_0$ . The plots for different orders are  $1^{st}$  (continuous line),  $2^{nd}$  (long dashed line),  $3^{rd}$  (short dashed line) and  $4^{th}$  (dotted line).

that limit, we expand the solutions obtained at various orders Eqs.(39)-(41) and (44) in the powers of  $1/\bar{\Omega}$  as follows –

$$\lambda + C_1 = \bar{\Omega} \quad (45a)$$

$$\lambda + C_2 = \bar{\Omega} \pm \ln \bar{\Omega} - \left(\frac{1}{\bar{\Omega}}\right) \mp \frac{1}{2} \left(\frac{1}{\bar{\Omega}}\right)^2 - \frac{1}{3} \left(\frac{1}{\bar{\Omega}}\right)^3 + \dots \quad (45b)$$

$$\lambda + \tilde{C}_3 = \bar{\Omega} \pm \ln \bar{\Omega} + \left(\frac{1}{\bar{\Omega}}\right) \pm \frac{3}{2} \left(\frac{1}{\bar{\Omega}}\right)^2 + \frac{1}{3} \left(\frac{1}{\bar{\Omega}}\right)^3 + \dots \quad (45c)$$

$$\lambda + \tilde{C}_4 = \bar{\Omega} \pm \ln \bar{\Omega} + \left(\frac{1}{\bar{\Omega}}\right) \mp 0.7526 \left(\frac{1}{\bar{\Omega}}\right)^2 - 2.6699 \left(\frac{1}{\bar{\Omega}}\right)^3 + \dots \quad (45d)$$

where constant terms have been absorbed as  $\tilde{C}_3 = C_3 + \frac{3\pi}{2\sqrt{7}}$  and  $\tilde{C}_4 = C_4 + 1.74045$ .

We can write all of these as  $\lambda + C = \bar{\Omega} + \delta$  where  $\delta$  represents the corrections over the Ricci flow due to the higher order terms in the RG flow equation. We plot these  $\delta$  over the Ricci flow obtained at various order in Fig.12. We see that the leading correction over the Ricci flow is  $\sim \ln \bar{\Omega}$ , and other higher order corrections then vanish in the limit of large  $\bar{\Omega}$ .

We can see that the  $2^{nd}$  order solution is correct upto  $\ln \bar{\Omega}$  term and the  $3^{rd}$  order upto  $1/\bar{\Omega}$ . We suspect, similarly, that the  $4^{th}$  order solution will be correct till  $1/\bar{\Omega}^2$ , but this can be verified only if even higher order solutions are available.