

One checks easily that G is stable under θ , and that

$$K = G^\theta = \left\{ k = \begin{pmatrix} K_{11} & 0 & K_{13} \\ 0 & K_{22} & 0 \\ K_{31} & 0 & K_{33} \end{pmatrix} \left| \begin{array}{l} K_{11}, K_{13}, K_{31}, K_{33} \in \text{Mat}(p, p) \\ \begin{pmatrix} K_{11} & K_{13} \\ K_{31} & K_{33} \end{pmatrix} \in O(2p, \mathbb{C}) \\ K_{22} \in O(2q+1, \mathbb{C}) \\ \det(k) = 1 \end{array} \right. \right\}$$

$$\cong S(O(2p, \mathbb{C}) \times O(2q+1, \mathbb{C})).$$

This choice of K corresponds to the real form $G_{\mathbb{R}} = SO(2p, 2q+1)$ of G .

Let $S \subseteq K$ be a maximal torus of K contained in T . This is an equal rank case, so in fact $S = T$. We formally distinguish coordinates on \mathfrak{s} (labeled by X variables) from those on \mathfrak{t} (labelled by Y variables), with restriction given by $\rho(Y_i) = X_i$.

This is the first time that we have encountered a K which is not connected. We handle this by considering the connected components of the closed orbits separately. As we will see, each closed orbit has two components. Each is a single K^0 -orbit, with $K^0 = SO(2p, \mathbb{C}) \times SO(2q+1, \mathbb{C})$ the identity component of K . These K^0 -orbits coincide with the closed \tilde{K} -orbits, with $\tilde{K} = S(Pin(2p, \mathbb{C}) \times Pin(2q+1, \mathbb{C}))$ the corresponding (connected) symmetric subgroup of the simply connected cover $\tilde{G} = Spin(2n+1, \mathbb{C})$ of G . Since $S \subset K^0$, each such component is stable under S , and hence has a S -equivariant class. We apply our usual method to find formulas for these S -equivariant classes. Having done so, we next identify exactly how the closed K -orbits break up as unions of these components. We find a formula for each closed K -orbit by simply adding the formulas for the two components. Finally, we parametrize the K -orbits by $(2p, 2q+1)$ -clans satisfying a certain additional combinatorial property, and describe the weak closure order on $K \backslash G/B$ in terms of this parametrization. This allows us to perform the rest of the computation as in the type A cases.