

of the connection is presented in Figure 1, and the models are formulated in system (4.11). We will show that the chaos that appears in  $A_1$  spreads to all the other models.  $A_2$  serves as a replicator of the chaos of  $A_1$  and as a generator of chaos in  $A_3$  and  $A_4$ . Model  $A_4$  is a replicator of the chaos of  $A_2$  and a generator of chaos in  $A_5$ .

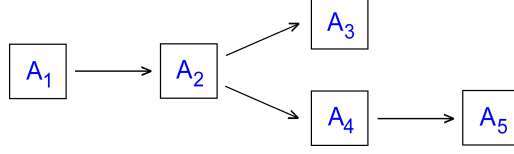


Figure 1: The connection topology of the systems  $A_1 - A_5$ .

The following is a system of five unidirectionally coupled models  $A_1 - A_5$ .

$$\begin{aligned}
& \left. \begin{aligned} \kappa_{j+1} &= \mu \kappa_j (1 - \kappa_j), \end{aligned} \right\} A_1 \\
& \left. \begin{aligned} y_1' &= (1/8)y_1 - (5/16)k_1 - a_1 y_1^3 - \frac{3\sqrt{a_1}}{2} y_1^2 + \nu_1(t, \theta), \\ k_1' &= (1/4)y_1 - (3/8)k_1 - a_1 y_1^3 - \frac{3\sqrt{a_1}}{2} y_1^2, \end{aligned} \right\} A_2 \\
& \left. \begin{aligned} y_2' &= (1/3)y_2 - k_2 - a_2 y_2^3 - \frac{\sqrt{6a_2}}{2} y_2^2 + 0.6y_1(t) + \nu_2(t, \zeta), \\ k_2' &= (1/2)y_2 - (5/4)k_2 - a_2 y_2^3 - \frac{\sqrt{6a_2}}{2} y_2^2, \end{aligned} \right\} A_3 \\
& \left. \begin{aligned} S' &= 0.23Y + 0.1S(1 - Y^2), \\ Y' &= 0.5(S + F) + 2(y_1(t) + 0.5), \\ F' &= 0.19S - 0.25Y, \end{aligned} \right\} A_4 \\
& \left. \begin{aligned} y_3' &= (3/5)y_3 - (4/5)k_3 - a_3 y_3^3 - \frac{3\sqrt{a_3}}{\sqrt{10}} y_3^2 + 0.01Y(t), \\ k_3' &= (7/10)y_3 - (9/10)k_3 - a_3 y_3^3 - \frac{3\sqrt{a_3}}{\sqrt{10}} y_3^2, \end{aligned} \right\} A_5
\end{aligned} \tag{4.11}$$

where  $a_1, a_2, a_3$  are constants and the piecewise constant functions  $\nu_1(t, \theta)$  and  $\nu_2(t, \zeta)$  are defined as follows:

$$\nu_1(t, \theta) = \begin{cases} 0.019, & \text{if } \theta_{2j} < t \leq \theta_{2j+1}, \\ 0.002, & \text{if } \theta_{2j-1} < t \leq \theta_{2j}, \end{cases} \tag{4.12}$$

and

$$\nu_2(t, \zeta) = \begin{cases} 0.0006, & \text{if } \zeta_{2j} < t \leq \zeta_{2j+1}, \\ 0.0017, & \text{if } \zeta_{2j-1} < t \leq \zeta_{2j}, \end{cases}. \tag{4.13}$$

The sequence  $\theta = \{\theta_j\}$ ,  $j \in \mathbb{Z}$ , of the discontinuity instants of the function (4.12) satisfies the relation  $\theta_j = j + \kappa_j$ , where the sequence  $\{\kappa_j\}$  is a solution of the logistic map  $A_1$  with  $\kappa_0 \in [0, 1]$ . The sequence  $\zeta = \{\zeta_j\}$ ,  $j \in \mathbb{Z}$ , of the discontinuity instants of (4.13) satisfies the relation  $\zeta_j = 2\sqrt{2}j$  for each  $j$ .