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- [30] In the Heisenberg picture, the state vector of the system would be constant whereas the operator $\hat{\phi}$ evolve according to $i\hbar(d\hat{\phi}/dz) = [\hat{\phi}, \hat{H}]$. One can easily check that, with the Hamiltonian operator given by Eq.(18), the evolution equation of the operator $\hat{\phi}$ is precisely Eq.(3), where the c-field ϕ is replaced by the operator $\hat{\phi}$.
- [31] More precisely, the monochromatic limit is attained by assuming in Eqs.(21) and (22) $f^{(n)}(\mathbf{q}, \Omega, z) = g^{(n)}(\mathbf{q}, z)h(\Omega_1)h(\Omega_2)...h(\Omega_n)$, where $h(\Omega)$ is a spectrally narrow function at around $\Omega = 0$ normalized such that $\int d\Omega |h(\Omega)|^2 = 1$, and $g^{(n)}(\mathbf{q}, z)$ satisfies Eq.(22) with $\Omega_l = 0$. The operator $\hat{\phi}(\rho)$ is then formally defined as $\hat{\phi}(\rho) = \int d\Omega h(\Omega)\hat{\phi}(\rho, \Omega)$. The n -photon number state $|f^{(n)}\rangle$, given by Eq.(21), takes then the simplified form $|f^{(n)}\rangle = (1/(\sqrt{n!}) \int d\mathbf{q} g^{(n)}(\mathbf{q}, z)\hat{\phi}^\dagger(\rho_1)\hat{\phi}^\dagger(\rho_2)...\hat{\phi}^\dagger(\rho_n)|0\rangle$.
- [32] As the waveguides W_1 and W_2 are symmetrically placed at opposite sides from the slab waveguide S, if $(c_1(z), c_2(z), c_k(z))$ is a solution to Eqs.(5-7) with initial condition $c_1(0) = 1$, $c_2(0) = 0$ and $c_k(0) = 0$, then $(c_2(z), c_1(z), c_k(z))$ is the solution to Eqs.(5-7) with reversed initial condition $c_1(0) = 0$, $c_2(0) = 1$ and $c_k(0) = 0$. Light tunnelled into the slab waveguide S is thus given by the same superposition of continuous modes ($\sim \int dk c_k(z)u_k(\rho)$) for the two different initial conditions. This means that the last two terms on the right hand sides of Eqs.(38) and (39) are equal each other.
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