

In the left panels ( $t = 0$  s), the level crossing length at  $\sin^2 2\theta_{13} = 10^{-2}$  and  $10^{-3}$  are larger than the oscillation length at all region. Therefore, the resonance is adiabatic. On the other hand, in the case of  $\sin^2 2\theta_{13} = 10^{-4}$  and  $10^{-5}$ , the level crossing length at the resonance is almost same as or slightly smaller than the oscillation length of  $\bar{\nu}_e$ . Therefore, the resonance is non-adiabatic. In the right panels ( $t = 3$  s) when the shock wave reaches the H-resonance, the level crossing length,  $\delta r$ , is of the same order or smaller than the oscillation length  $L_{\text{osc}}$  for all cases of the mixing angle, except for  $\sin^2 2\theta_{13} = 10^{-2}$ . This satisfies non-adiabatic condition  $\gamma < 1$  as discussed above. We understand, therefore, that the resonance becomes non-adiabatic by the effect of the shock wave. In Figure 2, the influence of the shock wave appears about 2 s after core bounce. This result is consistent with our simulation (see Figure 1).

In the case of normal hierarchy, the survival probability of  $\bar{\nu}_e$  does not change much because there is no resonance in the  $\bar{\nu}$  sector. Therefore, the survival probability of  $\bar{\nu}_e$  in normal hierarchy is always  $\sim 0.7$  regardless of the value of  $\sin^2 2\theta_{13}$  or independently of the shock wave.

We note that there is L-resonance in  $\nu$  sector even in the case of inverted hierarchy. However, the value of  $\theta_{12}$  which is related to L-resonance is very large (see Eq. (3)), and the level crossing length of our simulation is not as small as the oscillation length at the resonance. Therefore,  $\gamma$  at the L-resonance is larger than 1. As a result, the survival probability of  $\nu_e$  in inverted hierarchy does not change drastically, and stays always  $\sim 0.3$ .

## B. Supernova neutrino spectrum

We calculate the supernova neutrino spectra using the survival probabilities. Figure 4 shows the spectra of  $\nu_e$ . Left panels of Figure 4 show the spectra in the case of normal hierarchy, and right panels show the results of inverted hierarchy. Figure 5 is same as Figure 4 but for  $\bar{\nu}_e$  spectra. Red solid and blue dotted lines are the spectra with and without shock wave, respectively. In order to clearly observe the shock wave effects, we display these ratio,  $\phi_{\text{with}}/\phi_{\text{without}}$ , of the spectra with to without shock in lower part of each panel.

We see clearly the shock wave effects in the  $\nu_e$  spectra in Figure 4 in normal hierarchy. In the case of  $\sin^2 2\theta_{13} = 10^{-3}$  and  $10^{-4}$ , an enhancement in low energy component of the neutrino spectra is seen when the shock wave reaches the H-resonance. At later times, the