II. OLM-MEM WITH THE q-AVERAGE

A. q-Gaussian PDF

We consider N-unit nonextensive systems whose PDF, $p_q^{(N)}(\boldsymbol{x})$, is derived with the use of the OLM-MEM [5] for the Tsallis entropy given by Eq. (1) [1, 2]. We impose four constraints given by (for details, see Appendix B of Ref. [20])

$$1 = \int p_q^{(N)}(\boldsymbol{x}) d\boldsymbol{x}, \tag{11}$$

$$\mu = \frac{1}{N} \sum_{i=1}^{N} [x_i]_q, \tag{12}$$

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{N} [(x_i - \mu)^2]_q, \tag{13}$$

$$s \sigma^2 = \frac{1}{N(N-1)} \sum_{i=1}^{N} \sum_{j=1(\neq i)}^{N} [(x_i - \mu)(x_j - \mu)]_q.$$
 (14)

Here μ , σ^2 and s express the mean, variance, and degree of intrinsic correlation, respectively, and the bracket $[\cdot]_q$ denotes the q-average over the escort PDF, $P_q^{(N)}(\boldsymbol{x})$,

$$[Q]_q = \int P_q^{(N)}(\boldsymbol{x}) Q(\boldsymbol{x}) d\boldsymbol{x}, \qquad (15)$$

with

$$P_q^{(N)}(\boldsymbol{x}) = \frac{\left(p_q^{(N)}(\boldsymbol{x})\right)^q}{c_q^{(N)}},\tag{16}$$

$$c_q^{(N)} = \int \left(p_q^{(N)}(\boldsymbol{x}) \right)^q d\boldsymbol{x}, \tag{17}$$

where Q(x) stands for an arbitrary function of x.

The OLM-MEM with the constraints given by Eqs. (11)-(14) leads to the PDF given by [20, 36]

$$p_q^{(N)}(\boldsymbol{x}) = \frac{1}{Z_q^{(N)}} \exp_q \left[-\left(\frac{1}{2\nu_q^{(N)}\sigma^2}\right) \Phi(\boldsymbol{x}) \right], \tag{18}$$