

is basically the parton density distribution function.

In fitting data to construct PDFs, it is usual to use the \overline{MS} (modified minimal subtraction) renormalization scheme whereas, in regard of factorization, there are two commonly used schemes. The DIS scheme (Altarelli *et al.*, 1978) was designed to ensure there are no higher-order corrections to the expression for the F_2 structure function in terms of the quark PDFs; i.e., all finite contributions are absorbed into the PDF. On the other hand, in the more widely used \overline{MS} scheme (Bardeen *et al.*, 1978), in addition to the divergent piece, only the usual $(\ln 4\pi - \gamma_E)$ combination is absorbed into $q(x)$ and hence the expression for F_2 exhibits explicit $O(\alpha_s)$ corrections. [See (Brock *et al.*, 1995) for more on these points.]

The CTEQ6L (leading-order) structure functions shown in Fig. II.3 were evaluated using the \overline{MS} -scheme (modified minimal subtraction). At leading-order there is no difference between factorization schemes. As we will subsequently see (Fig. II.4), radiated gluons give rise to the scaling violation or Q^2 -dependence of the structure functions. They, and the quark distribution functions defined therefrom, then depend on both x and Q^2 . The Q^2 dependence is now routinely described within the framework of next-to-leading-order (NLO) QCD evolution.

An important and extremely useful feature of factorization is that a measurement of a structure function at relatively-low Q^2 permits the calculation, through the use of pQCD, of the structure function at high Q^2 . In leading order, a set of integro-differential equations, now known as the DGLAP evolution equations (Altarelli and Parisi, 1977; Dokshitzer, 1977; Gribov and Lipatov, 1972; Lipatov, 1975), are used for this purpose. Intuitively, one may think that as Q^2 increases, a parton can sometimes be resolved into two partons; e.g., a quark can split into a quark and a gluon, or a gluon into two gluons – see Fig. II.4 for a graphical representation of the leading order DGLAP equations. The two resolved partons then share in the fraction of the nucleon momentum carried by the initial unresolved parton at lower Q^2 . The parton distribution thus becomes a function of Q^2 . Such evolution of the parton distribution function (PDF) can be seen in Fig. II.3. At the highest values of Q^2 the structure function is shifted toward lower values of x . This work has been generalized to other reaction processes (Furmanski and Petronzio, 1982).

We note that in principle the domain of “relatively-low Q^2 ” means, nevertheless, $Q^2 \gg \Lambda_{\text{QCD}}^2$. Notwithstanding this, in some empirical determinations of PDFs through data fitting [see Sec. V.C] and in the application of models to their calculation [see Sec. VI],