

by  $\mathbf{a} = 001110101110$  with the simplified check matrix

$$\begin{bmatrix} 001110 & 101110 \\ 000111 & 010111 \\ 100011 & 101011 \\ 110001 & 110101 \\ 111000 & 111010 \\ 011100 & 011101 \end{bmatrix}.$$

We call this the *circulant* construction of EAQEC codes, which is used for standard stabilizer codes in [18].

We examined the simplified check matrices cyclicly generated by every possible binary  $2n$ -tuple  $\mathbf{a}$  by computer for  $n = 4, \dots, 10$  and  $r \leq 2(n-1)$ . Parameters of EAQEC codes not equivalent to any standard quantum stabilizer codes are listed in Table 10. The parameters  $[[4, 0, 4; 2]]$ ,  $[[4, 1, 3; 1]]$ ,  $[[5, 0, 4; 2]]$ ,  $[[5, 1, 4; 3]]$ ,  $[[5, 1, 5; 4]]$ ,  $[[6, 0, 6; 4]]$ ,  $[[6, 2, 3; 1]]$ ,  $[[6, 2, 4; 3]]$ ,  $[[6, 0, 4; 1]]$ ,  $[[6, 1, 5; 4]]$ ,  $[[7, 4, 3; 2]]$ ,  $[[7, 1, 6; 5]]$ ,  $[[7, 1, 7; 6]]$ ,  $[[8, 5, 3; 2]]$ ,  $[[9, 1, 9; 8]]$ , and  $[[10, 0, 10; 8]]$  also saturate the quantum singleton bound (11).

Table 10: Parameters of  $[[n, k, d; c]]$  EAQEC codes not equivalent to any standard  $[[n+c, k]]$  codes.

$n$	$[[n, k, d; c]]$
4	$[[4, 0, 4; 2]]$ , $[[4, 1, 3; 1]]$
5	$[[5, 1, 5; 4]]$ , $[[5, 1, 4; 3]]$ , $[[5, 1, 4; 2]]$ , $[[5, 0, 4; 2]]$ , $[[5, 2, 3; 2]]$
6	$[[6, 0, 6; 4]]$ , $[[6, 1, 5; 4]]$ , $[[6, 1, 4; 3]]$ , $[[6, 2, 4; 3]]$ , $[[6, 0, 4; 1]]$ , $[[6, 2, 3; 1]]$
7	$[[7, 1, 7; 6]]$ , $[[7, 2, 5; 5]]$ , $[[7, 0, 6; 4]]$ , $[[7, 3, 4; 4]]$ , $[[7, 1, 4; 2]]$ , $[[7, 3, 4; 3]]$ , $[[7, 4, 3; 2]]$
8	$[[8, 0, 8; 6]]$ , $[[8, 1, 6; 6]]$ , $[[8, 0, 6; 5]]$ , $[[8, 2, 6; 6]]$ , $[[8, 1, 6; 5]]$ , $[[8, 0, 6; 4]]$ , $[[8, 3, 5; 5]]$ , $[[8, 2, 5; 4]]$ , $[[8, 1, 4; 1]]$ , $[[8, 3, 4; 3]]$ , $[[8, 5, 3; 2]]$ ,
9	$[[9, 1, 9; 8]]$ , $[[9, 0, 7; 6]]$ , $[[9, 1, 7; 6]]$ , $[[9, 1, 7; 7]]$ , $[[9, 2, 6; 6]]$ , $[[9, 1, 6; 5]]$ , $[[9, 0, 6; 4]]$ , $[[9, 1, 6; 6]]$ , $[[9, 2, 5; 4]]$ , $[[9, 5, 3; 1]]$ ,
10	$[[10, 0, 10; 8]]$ , $[[10, 1, 8; 8]]$ , $[[10, 0, 8; 7]]$ , $[[10, 0, 8; 6]]$ , $[[10, 0, 7; 5]]$ , $[[10, 1, 7; 6]]$ , $[[10, 2, 7; 7]]$ , $[[10, 1, 6; 5]]$ , $[[10, 3, 6; 7]]$ , $[[10, 0, 6; 3]]$ , $[[10, 3, 6; 6]]$ , $[[10, 2, 6; 5]]$ , $[[10, 1, 6; 4]]$ , $[[10, 4, 5; 5]]$ , $[[10, 2, 5; 2]]$ , $[[10, 4, 5; 4]]$ , $[[10, 2, 5; 3]]$ ,