

## Abstract

We demonstrate a method for calculating the neutral  $B$ -meson decay constants and mixing matrix elements in unquenched lattice QCD with domain-wall light quarks and static  $b$ -quarks. Our computation is performed on the “2+1” flavor gauge configurations generated by the RBC and UKQCD Collaborations with a lattice spacing of  $a \approx 0.11$  fm ( $a^{-1} = 1.729$  GeV) and a lattice spatial volume of approximately  $(1.8 \text{ fm})^3$ . We simulate at three different light sea quark masses with pion masses down to approximately 430 MeV, and extrapolate to the physical quark masses using a phenomenologically-motivated fit function based on next-to-leading order heavy-light meson  $SU(2)$  chiral perturbation theory. For the  $b$ -quarks, we use an improved formulation of the Eichten-Hill action with static link-smearing to increase the signal-to-noise ratio. We also improve the heavy-light axial current used to compute the  $B$ -meson decay constant to  $\mathcal{O}(\alpha_s pa)$  using one-loop lattice perturbation theory. We present initial results for the  $SU(3)$ -breaking ratios  $f_{B_s}/f_{B_d}$  and  $\xi = f_{B_s}\sqrt{B_{B_s}}/f_{B_d}\sqrt{B_{B_d}}$ , thereby demonstrating the viability of the method. For the ratio of decay constants, we find  $f_{B_s}/f_{B_d} = 1.15(12)$  and for the ratio of mixing matrix elements, we find  $\xi = 1.13(12)$ , where in both cases the errors reflect the combined statistical and systematic uncertainties, including an estimate of the size of neglected  $\mathcal{O}(1/m_b)$  effects.

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