

CP-violating phases; these would manifest themselves as apparent inconsistencies among different measurements of quantities which should be identical within the standard CKM picture. Thus a precise determination of the ratio  $\xi$  will help to constrain physics beyond the Standard Model. Furthermore, possible indications of new physics in  $B_d^0$ -mixing at the  $\sim 2.7\text{-}\sigma$  level [13] make the lattice calculation of  $B$ -meson mixing parameters timely.

Recently, the HPQCD Collaboration published the first unquenched determination of  $\xi$  with an accuracy of 2.6% [14], and the Fermilab Lattice and MILC Collaborations expect to have a result with similar errors soon [15]. The HPQCD calculation employs a nonrelativistic QCD (NRQCD) action for the heavy  $b$ -quark [16], while the Fermilab/MILC calculation uses the relativistic “Fermilab” action for the  $b$ -quark [17]. Both of these computations, however, rely on the same “2+1” flavor asqtad-improved staggered ensembles generated by the MILC Collaboration [18], which include the effects of two degenerate light quarks and one heavier close-to-strange quark in the sea sector.

For such a phenomenologically important quantity as  $\xi$ , it is valuable to have an independent crosscheck using different formulations of the lattice action for both the light and heavy quarks. Our calculation employs the 2+1 flavor dynamical domain-wall ensembles generated by the RBC and UKQCD Collaborations with a lattice spacing of  $a \approx 0.11$  fm ( $a^{-1} = 1.729$  GeV) [19]. The use of domain-wall fermions [20–22] has the advantage over other light-quark formulations that the chiral perturbation theory expressions needed to extrapolate domain-wall lattice results to the physical  $u$ - and  $d$ -quark masses are closer to the continuum forms and have fewer parameters than in the Wilson or staggered cases [23, 24]. We compute the  $b$ -quarks in the static limit ( $m_b \rightarrow \infty$ ), which leads to correlation functions that are noisier than those with propagating  $b$ -quarks such as in the Fermilab [17] or NRQCD actions [16]. We therefore use the static-quark formulation of Refs. [25, 26] with either APE [27, 28] or HYP [29] smearing of the static-quark gauge links to increase the signal-to-noise ratio and reduce scaling violations (for some quantities) as compared to the Eichten-Hill action [30]. Furthermore, the approximate chiral symmetry of the domain-wall action combined with the spin symmetry of the static action simplifies the lattice-to-continuum operator matching as compared to the Wilson case by reducing the number of additional lattice operators which appear [31, 32]. The results of this work extend an earlier study with two flavors of dynamical quarks and heavier light-quark masses in Ref. [33].

The primary purpose of this paper is to demonstrate the viability of our method for