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# Appendix A

## R code

All files referenced in the current appendix are available under the directory at:

https://github.com/tystan/thesis/tree/master/R.

## A.1 Morphological operators

Description	File	Functions		
Naive erosion and top-hat:				
	/00_erosion_slow.R	erode(), dilate(), tophat()		
Line segment	erosion:			
	/01_erosion_quick.R	$erode_quick()$		
Naive erosion for unequally spaced values:				
	<pre>/02_cts_erosion_slow.R</pre>	erode_cts_slow()		
Continuous line segment erosion:				
	/03_cts_erosion_quick.R	erode_cts_quick()		

#### A.1.1 Naive erosion and top-hat

Consider  $x \in \{1, 2, ..., n\} = X$  and  $f(x) \in \mathbb{R}$   $\forall x \in X$ . Because of the assumed even spacing of the elements of X, the R-function below simply requires the vector of intensities, f, and the size of the SE.

```
erode<-function(f,sesize) #f are the intensities
1
2
       if(!(sesize %% 2)) return(NULL) #SE must be of odd length
3
       nx<-length(f); erode<-rep(0,nx); halfse<-(sesize-1)/2;</pre>
4
       for(i in 1:nx) #for each m/z point across the spectrum
5
           erode[i]<-min(f[max(1,i-halfse):min(nx,i+halfse)])</pre>
6
7
       return(erode)
    }
8
    ### dilate is the same as erode except use max instead of min ...OR...
9
    dilate<-function(f,sesize) return(-erode(-f,sesize))</pre>
10
    ### as defined \tau_B(f) = f - (f \ominus B) \oplus B
    tophat<-function(f,sesize) return(f-dilate(erode(f,sesize),sesize))</pre>
```

Note, the code checks the SE provided is an odd integer as a centred, symmetric SE is required. The maximum and minimum statements on line 6 of the code segment above, namely max(1,i-halfse) and min(nx,i+halfse), check for when the SE sits over the 'edge' on the left or right of the series, respectively. This ensures only defined f values will be used.

#### A.1.2 Line segment erosion

```
erode.quick<-function(f,se.size){</pre>
       nx<-length(f)</pre>
2
       k<-se.size
3
      t1<-proc.time()[3] ### get start time
4
       if(k>=nx){
         cat("Warning: structuring element is >= in length as the input\n")
6
         cat("The input vector has been output \n")
         return(f)
       }else{
         if((k\%2) != 1){
10
           k < -k - 1
11
           cat("Structring Element not symmetric, using SE length -1 =",k,"\n")
12
13
         k.left < -(k-1)/2
14
         add.pix<-k-(nx%k)
15
         isMultiple<-(add.pix==k)</pre>
         if(!isMultiple){
17
           f<-c(f,rep(+Inf,add.pix))</pre>
18
           rem.indxs<-(nx+1):(nx+add.pix)</pre>
19
20
           nx<-nx+add.pix</pre>
21
         }
         g<-rep(0,nx)
22
         h<-rep(0,nx)
23
         r < -rep(0, nx)
         j<-nx
25
         for(i in 1:nx){
26
           if(i\%k==1){
^{27}
28
             g[i] \leftarrow f[i]
           }else{
29
             g[i] \leftarrow min(g[i-1], f[i])
30
31
           if(j\%k==0){
32
             h[j]<-f[j]
33
           }else{
34
35
             h[j] \leftarrow min(h[j+1], f[j])
           }
36
           j<-j-1
37
38
39
         r[1:(k.left+1)] < g[(k.left+1):k]
         r[(k.left+2):(nx-k.left-1)] < -pmin(g[(k+1):(nx-1)],h[2:(nx-k)])
40
         r[(nx-k.left):nx]<-h[(nx-k+1):(nx-k.left)]
41
         if(!isMultiple) r<-r[-rem.indxs]</pre>
42
43
         delta.t<-sprintf("%.2f",proc.time()[3]-t1) ### time elapsed</pre>
44
         cat("Completed morphological erosion in",delta.t,"seconds\n")
45
         return(r)
46
47
    }
48
```

#### A.1.3 Naive erosion for unequally spaced values

A vector of all the lower bounds (LB)  $x_l$  in Algorithm ?? for each corresponding  $x_i$  can be created using a O(n) algorithm using two pointers along the input vector X. One pointer is the current position, the other is a lagging pointer that moves along the vector when required. A simple algorithm to do this is described in Algorithm ??. To find the upper bound the same algorithm would be employed, but the pointers will start from the right and move down the vector with the second point lagging to the right.

```
get.lo.bounds<-function(x,k){</pre>
1
       nx <- length(x)</pre>
2
       k0 < - k/2
3
       L0 \leftarrow rep(0, nx)
       i <- 2
5
       i_lo <- 1
6
       L0[i_lo] \leftarrow i_lo \# x[1] has lower bound 1
7
       while(i \le nx)
9
         if((x[i]-x[i_lo]) \le k0){
10
            L0[i] <- i_lo
11
            i <- i+1
^{12}
         }else{
13
            i_lo <- i_lo+1
14
15
       }
16
       return(L0)
17
    }
18
     get.hi.bounds<-function(x,k){</pre>
19
20
       nx <- length(x)</pre>
       k0 < - k/2
21
       HI \leftarrow rep(0,nx)
22
       i <- nx-1
23
       i_hi <- nx
24
       HI[i_hi] \leftarrow i_hi \# x[nx] has upper bound nx
25
       while(i>0)
26
27
          if((x[i_hi]-x[i]) \le k0){
28
            HI[i] <- i_hi
29
            i <- i-1
30
31
         }else{
            i_hi <- i_hi-1
32
         }
33
       }
34
       return(HI)
35
36
    erode.cts.slow<-function(x,f,k){</pre>
37
       nx<-length(x)</pre>
38
```

```
39     r_min<-rep(0,nx)
40     L0<-get.lo.bounds(x,k)
41     HI<-get.hi.bounds(x,k)
42     for(i in 1:nx) r_min[i]<-min(f[L0[i]:HI[i]])
43     return(r_min)
44  }</pre>
```

#### A.1.4 Continuous line segment erosion

```
erode.cts.quick<-function(x,f,se.span){</pre>
1
2
       out.vector<-NULL
3
       nx<-length(x)</pre>
4
       x.span < -x[nx] - x[1]
       k<-se.span
6
       t1<-proc.time()[3]
       isAppend<-FALSE
       if(k>=x.span){
10
         cat("Warning: structuring element spans the entire input set \n")
11
         cat("The input f vector has been output \n")
12
13
       }else{
14
         m<-ceiling(x.span/k)</pre>
15
         mk < -m * k
         if(!((x[1]+mk) == x[nx])){
17
           x < -c(x,x[1]+mk)
18
19
           f<-c(f,+Inf)
           isAppend<-TRUE
           nx < -nx + 1
21
           x.span < -x[nx] - x[1]
22
23
         k.blocks<-c(0,findInterval(x,seq(x[1],x[1]+(m-1)*k,by=k)),m+1)
         p<-k.blocks[1]
25
         q<-k.blocks[nx+2]
26
         g < -rep(0, nx)
^{27}
28
         h < -rep(0, nx)
         r<-rep(0,nx)
29
         i<-1
30
         j<-nx
31
         while(i<=nx){
32
           this.p<-k.blocks[i+1]
33
           this.q<-k.blocks[j+1]</pre>
34
35
           if(p==this.p){
              g[i] \leftarrow min(g[i-1], f[i])
36
           }else{
37
              g[i] \leftarrow f[i]
38
           if(q==this.q){
40
              h[j] \leftarrow min(h[j+1], f[j])
41
           }else{
42
43
              h[j] \leftarrow f[j]
           }
44
           p<-this.p
45
           q<-this.q
46
           i<-i+1
47
           j<-j-1
48
49
```

```
k.left<-k/2
50
        low.bound.index <-nx-rev(findInterval(rev(-x),rev(-(x+k.left))))+\\ 1
51
        upp.bound.index<-findInterval(x+k.left,x)</pre>
52
        out.vector<-pmin(h[low.bound.index],g[upp.bound.index])</pre>
53
        which.low <- which (k.blocks[low.bound.index] == k.blocks[upp.bound.index + 1])\\
54
        out.vector[which.low]<-h[low.bound.index[which.low]]</pre>
        which.hi<-which(k.blocks[low.bound.index+1]==k.blocks[upp.bound.index+2])
        out.vector[which.hi]<-g[upp.bound.index[which.hi]]</pre>
57
        if(isAppend) out.vector<-out.vector[-nx]</pre>
58
        cat("Completed morphological erosion (cts scale) in"
59
           ,sprintf("%.2f",proc.time()[3]-t1),"seconds \n")
60
        return(out.vector)
61
      }
62
    }
63
```

## A.2 Spectra normalisation

Description	File	Functions	
Empirical quantile normalisation:			
	/04_quant_norm.R	msEQN()	
Pairwise spectra MA normalisation:			
	/05_ma_adj.R	intensAdj()	

#### A.2.1 Empirical quantile normalisation

```
### Input: msData - the spectra intensities in matrix
                where columns are spectra 1, 2, \ldots, n
2
    msEmpiricalQuantNorm<-function(msData)</pre>
4
      msD<-msData
      nSpec<-ncol(msD)</pre>
6
      nDim<-nrow(msD)</pre>
      orders<-apply(msD, 2, order)</pre>
      reorders<-apply(orders, 2, order)</pre>
10
      # order each column into ascending order
11
      for(i in 1:nSpec) msD[,i]<-msD[orders[,i],i]</pre>
12
      #replace ordered columns with row means
13
      rmeans<-rowMeans(msD)</pre>
14
      for(i in 1:nSpec) msD[,i]<-rmeans</pre>
15
      #put back into the original order (with changed values)
      for(i in 1:nSpec) msD[,i]<-msD[reorders[,i],i]</pre>
17
18
      return(msD)
19
    }
```

#### A.2.2 Pairwise spectra MA normalisation

```
### adjM(): Used by intensAdj(), performs LOESS regression on ordered MA-vals
   ### Input: ordered dependent variable A with corresponding M
   ### Returns: adjusted M values, M_t^*
    adjM<-function(ordered.M,ordered.A)</pre>
      MA.finites<-is.finite(ordered.M) #only include values > -\infty
      finites.M<-ordered.M[MA.finites]</pre>
      finites.A<-ordered.A[MA.finites]</pre>
      MAloess<-loess(finites.M~finites.A
10
         , span=0.40, degree=2, family="symmetric", normalize=FALSE)
11
12
      finites.M<-finites.M-MAloess$fitted # make adjustments</pre>
13
      ordered.M[MA.finites]<-finites.M # and return adjusted values</pre>
14
      return(ordered.M)
15
    }
16
17
    ### intensAdj(): Perform MA adjustment on two vectors
18
    ### Input: Two spectra vectors F_1 and F_2
19
    ### Returns: MA adjusted F_1 and F_2 values, F_1^* and F_2^* respectively
    intensAdj<-function(F1,F2)</pre>
21
22
      t1<-proc.time()[3] ### get start time
23
      V1<-log2(F1) # Will produce -\infty for \log_2(0)
24
      V2 < -log2(F2)
25
      M < -V1 - V2
26
      A < -(V1+V2)/2
27
28
      \#\#\# A is the dependent regression variable,
      ### ordering required for adjM function
29
      ordered.indxs<-order(A)</pre>
30
      ordered.A<-A[ordered.indxs]</pre>
31
      ordered.M<-M[ordered.indxs]</pre>
      ordered.M<-adjM(ordered.M,ordered.A)</pre>
33
      ### get indexes of original ordering
34
      orig.order<-order(ordered.indxs)</pre>
35
      M.dash<-ordered.M[orig.order]</pre>
36
37
      orig.finites<-is.finite(M) #update values requiring updating
38
      F1[orig.finites]<-2^(A[orig.finites]+M.dash[orig.finites]/2)
39
      F2[orig.finites]<-2^(A[orig.finites]-M.dash[orig.finites]/2)
40
41
      delta.t<-sprintf("%.2f",proc.time()[3]-t1) ### time elapsed
42
      cat("Completed MA Normalisation in", delta.t, "seconds \n")
43
      return(list(F1adj=F1,F2adj=F2))
44
    }
45
```

## A.3 Peak alignment

Description	File	Functions	
Calculate $W$ matrix for an $N$ - and $M$ -alignment:			
	/06_create_w.R	Wmatrix()	
Dendrogram peak alignment:			
	/07_dendro_peak_align.R	<pre>dendro_peak_align()</pre>	

#### A.3.1 Calculate W matrix for an N- and M-alignment

```
# Wmatrix(): Create a peak similarity matrix between an N- and M-alignment
6
  10
  # Nmatchedpeaks: K x N matrix of matched pairs of the N alignment
11
  # Npeaklists: a list object containing N matricies of
         (time,intensityVector) pairs: (n_a \times (n_{Comp}+1) \text{ matrix, a=1,...,N})
13
  # Mmatchedpeaks: L x M matrix of matched pairs of the M alignment
  # Mpeaklists: a list object containing M matricies of
15
          (time,intensityVector) pairs: (n_b \times (n_{Comp}+1) \text{ matrix}, b=1,...,M)
16
17
  18
19
  # e.g. Nmatchedpeaks =
  #[1010]
  # [ 0 1 2 1 1
22
  # [ 0 0 0 2 1
23
  # [ 2 2 0 0 ]
25
  # [ 3 3 3 3 1
  # [ 0 4 0 4 ]
26
  # [ . . . . ]
27
  # [ . . . . ]
  # [ . . . . ]
29
30
  # here K \times N (N=4) matrix
31
32
  # Npeaklist=
33
  # [[1]]
34
  # [t_{1,1} \ t_{1,2} \ \dots \ t_{1,n_1}]
  # [x_{1,1} \ x_{1,2} \ \dots \ x_{1,n_1}]
37
  # [[2]]
38
  # [t_{2,1} \ t_{2,2} \ \dots \ t_{2,n_2}]
39
40
  # [x_{2,1} \ x_{2,2} \ \dots \ x_{2,n_2}]
41
  # ...
42
  #
43
  # [[N]]
44
  # [t_{N,1} \ t_{N,2} \ \dots \ t_{N,n_N}]
45
  # [x_{N,1} \ x_{N,2} \ \dots \ x_{N,n_N}]
46
  # where t_{i,j} is the time point j-th peak for the i-th spectrum
48
  # where x_{i,j} is the vector of intensities (n_{Comp} \ \text{long})
```

```
i.e. n_{Comp} x 1 matrix for the j-th peak for the i-th spectrum
    #
50
    # NB: each list item is a (n_{Comp}+1) \times n_N matrix
51
    # the \_i\_ co-ord is the row in the Nmatchedpeaks
53
    # the _a_ co-ord is the column number of Nmatchedpeaks (the spectrum number)
54
    # the _p_ co-ord is the peak number for the _a_th spectrum
55
    # the _{j}, _{b} and _{q} co-ords are defined similarly for the M-alignment
57
58
    Wmatrix<-function(Nmatchedpeaks, Npeaklists, Mmatchedpeaks, Mpeaklists
59
               ,D,expon,lambda){
60
61
       K<-nrow(Nmatchedpeaks)</pre>
62
       N<-ncol(Nmatchedpeaks)
63
64
       L<-nrow(Mmatchedpeaks)
       M<-ncol(Mmatchedpeaks)
65
       W<-matrix(0, nrow=K, ncol=L)</pre>
66
67
       for(i in 1:K){
68
           for(j in 1:L){
69
              numerator<-0
70
              denominator<-0
71
              for(a in 1:N){
72
                  p<-Nmatchedpeaks[i,a]</pre>
73
74
                  if(p>0){
75
                     for(b in 1:M){
                        q<-Mmatchedpeaks[j,b]
76
                        if(q>0){
77
                            t_a<-Npeaklists[[a]][1,p]</pre>
78
79
                            p_a < -Npeaklists[[a]][-1,p]
                            t_b<-Mpeaklists[[b]][1,q]</pre>
80
                            p_b < -Mpeaklists[[b]][-1,q]
81
82
                            numerator<-numerator+
                              PeakSim(p_a,t_a,p_b,t_b,D,expon,lambda)
83
                            denominator<-denominator+1</pre>
84
                        }
85
                     }
86
                  }
              }
88
              if(denominator>0) W[i,j]<-numerator/denominator</pre>
89
90
              else W[i,j] < -0
           }
91
       }
92
       return(W)
93
    }
94
```

#### A.3.2 Dendrogram peak alignment

```
4
 # guideTreePeakAlign(): for peak list data, create successive N- and M-alignments
          until all spectra are aligned.
6
 10
11
 # msD: MS Data, a <math>T x n matrix of MS intensities. One column per spectra.
 # peaklistlist: see below
13
 # in.param: [ D expon lambda G maxM ]-tuple as a vector
14
15
  16
  17
  18
19
 ### A list containing the following elements:
 # stepwise.peaks: a list where each element is the successive amalgamation data
  # amalpeaks: the final matrix of aligned peaks. Columns are named spectra, rows
23
25
  26
27
 ### peaklistlist=
 # [[1]]
29
 # [t_{1,1} t_{1,2} ... t_{1,n_1}]
30
 \# [x_{1,1} x_{1,2} ... x_{1,n_1}]
31
32
 # [[2]]
33
 \# [t_{2,1} t_{2,2} ... t_{2,n_2}]
34
 \# [x_{2,1} x_{2,2} ... x_{2,n_2}]
37
38
 # .
39
40
 # [[N]]
41
42 \# [t_{N,1} t_{N,2} ... t_{N,n}]
 \# [x_{N,1} x_{N,2} ... x_{N,n}]
44
 # where t_{i,j} is the time point j-th peak for the i-th spectrum
45
 \# where x_{i,j} is the vector of intensities (nComp long i.e. nComp x 1 matrix)
46
       for the j-th peak for the i-th spectrum
  # NB: each list item is a (n_{Comp}+1) x n_{N} matrix
48
49
```

```
quideTreePeakAlign<-function(msD,peaklistlist,in.param)</pre>
50
51
52
       D<-in.param[1]</pre>
53
       nC<-nrow(peaklistlist[[1]])-1
54
       expon<-in.param[2]
55
       lambda<-in.param[3]</pre>
       G<-in.param[4]
57
       maxM<-in.param[5]</pre>
58
59
       nPat<-length(peaklistlist)</pre>
60
       Pats<-1:nPat
61
62
       cat("Calculating merge sequence for spectra \n")
63
64
       fordist<-t(msD$intensity)</pre>
65
       hc<-hclust(as.dist(fordist,diag=FALSE,upper=FALSE),"average")</pre>
66
67
       ### find amalgamation sequence
68
       ### see ?hclust for information on the merge matrix:
69
            "an n-1 by 2 matrix. Row i of merge describes the merging of clusters
70
            at step i of the clustering. If an element j in the row is negative,
71
            then observation -j was merged at this stage. If j is positive then
72
            the merge was with the cluster formed at the (earlier) stage j of the
73
            algorithm. Thus negative entries in merge indicate agglomerations of
74
75
          singletons, and positive entries indicate agglomerations of
            non-singletons."
76
       amalg<-hc$merge
77
78
       nAmal<-nrow(amalg)</pre>
79
       # alignment of peaklistlist (a.pll)
80
       a.pll<-vector(length=nAmal,mode="list")</pre>
81
82
       Npeaks<-NULL
       Npeaklist<-NULL
83
       Mpeaks<-NULL
84
       Mpeaklist<-NULL
85
86
       # start
       for(aindx in 1:nAmal)
88
89
       {
90
         # if patsToGetN or patsToGetM are positive,
91
              ... it is a single spectrum (1-alignment)
92
         # if negative, it is a previous N/M-alignment (N,M>1)
93
         patsToGetN<--amalg[aindx,1]</pre>
94
         patsToGetM<--amalg[aindx,2]</pre>
95
96
         printPatsN<-sprintf("%03d",patsToGetN)</pre>
97
         printPatsM<-sprintf("%03d",patsToGetM)</pre>
98
         amalg.str<-"Amalgamting patient"
99
         if(patsToGetN>0 && patsToGetM>0){
100
           cat(amalg.str,"s ",printPatsN," and ",printPatsM,"\n",sep="")
101
```

```
}else if(patsToGetN>0 && patsToGetM<0){</pre>
102
           cat(amalg.str,printPatsN,"to previously amalgamated patients\n")
103
         }else if(patsToGetN<0 && patsToGetM>0){
104
            cat(amalg.str,printPatsM,"to previously amalgamated patients\n")
105
         }else{
106
107
            cat("Amalgamting two clusters of previously amalgamated patients\n")
109
         ### prepare N-Alignment data
110
         if(patsToGetN>0){ # if a single spectrum (1-alignment)
111
           Npeaks<-matrix(1:ncol(peaklistlist[[patsToGetN]]),ncol=1)</pre>
112
           Npeaklist<-peaklistlist[patsToGetN]</pre>
113
         }else{ # if a previously aligned N-alignment (N>1)
114
           Npeaks<-a.pll[[-patsToGetN]]</pre>
115
            patsToGetN<-as.numeric(colnames(Npeaks))</pre>
116
           Npeaklist<-peaklistlist[patsToGetN]</pre>
117
118
119
         ### prepare M-Alignment data
120
         if(patsToGetM>0){ # if a single spectrum (1-alignment)
121
           Mpeaks<-matrix(1:ncol(peaklistlist[[patsToGetM]]),ncol=1)</pre>
122
123
           Mpeaklist<-peaklistlist[patsToGetM]</pre>
         }else{ # if a previously aligned M-alignment (M>1)
124
           Mpeaks<-a.pll[[-patsToGetM]]</pre>
125
           patsToGetM<-as.numeric(colnames(Mpeaks))</pre>
126
           Mpeaklist<-peaklistlist[patsToGetM]</pre>
127
128
129
         ### use Wmatrix() function
130
         Wm<-Wmatrix(Npeaks, Npeaklist, Mpeaks, Mpeaklist, D, expon, lambda)</pre>
         ### use S-W alignment function to estimate maximum path
132
         ### see: https://code.google.com/p/swalign/
133
         estPM<-SWalign(Wm,G,maxM)</pre>
134
         ### estPM is a data.frame of (i,j) locations of the maximum path
135
         ### the data.frame is 2 columns for i,j points
136
137
         nN<-ncol(Npeaks) ### no. of peaks in N-align
138
         nM<-ncol(Mpeaks) ### no. of peaks in M-align
         nK<-nrow(estPM) ### no. of peaks in new N:M-align
140
         ### apllTemp:
141
142
         ###
                   (a) lignment of (p) eak (l) ist (l) ist, (temp) or ary
         ### Matrix of peak indicators. The n_K rows represent the n_K peaks
143
                 from the N:M-alignment.
144
         ### Entries apllTemp[i,j] are ==
145
         ### { 0 if that N:M-aligned peak does not exist in spec j (column j)
146
         ### { _else_ a non-zero indicator, the peak number from within the
147
                                          1-alignment from spectrum j (column j)
148
         apllTemp<-matrix(0,nrow=nK,ncol=nN+nM)</pre>
149
         mzValsTemp<-NULL
150
         AveMzValsTemp<-NULL
151
         for(n.k in 1:nK)
152
         {
153
```

```
if(estPM[n.k,1]>0) # if the peak exists in the N-alignment
154
155
              # transfer peak info from N-align to new N:M-align matrix
              apllTemp[n.k,1:nN]<-Npeaks[estPM[n.k,1],]</pre>
157
              for(i in 1:nN) if(apllTemp[n.k,i]>0) mzValsTemp<-</pre>
158
                  c(mzValsTemp,Npeaklist[[i]][1,apllTemp[n.k,i]])
159
           if(estPM[n.k,2]>0) # if the peak exists in the M-alignment
161
           {
162
              # transfer peak info from N-align to new N:M-align matrix
163
              apllTemp[n.k, (nN+1): (nN+nM)]<-Mpeaks[estPM[n.k,2],]
164
              for(i in (nN+1):(nN+nM)) if(apllTemp[n.k,i]>0) mzValsTemp<-
165
                  c(mzValsTemp,Mpeaklist[[i-nN]][1,apllTemp[n.k,i]])
166
           }
167
           # get ave m/z of all aligned peaks
168
           AveMzValsTemp<-c(AveMzValsTemp, mean(mzValsTemp))</pre>
169
           mzValsTemp<-NULL</pre>
170
171
         ### change row order if averaging m/z has changed peak location order
172
         mzReOrder<-order(AveMzValsTemp)</pre>
173
         apllTemp<-apllTemp[mzReOrder,]</pre>
174
         allPat<-c(patsToGetN,patsToGetM)</pre>
176
         colnames(apllTemp)<-allPat</pre>
177
         ### clean up N:M-alignment to preserve spectrum order
178
179
         patOrder<-order(allPat)</pre>
         apllTemp<-apllTemp[,patOrder]</pre>
180
181
         a.pll[[aindx]]<-apllTemp</pre>
182
       ### return list() object of peak amalgamation/alignment,
184
                including intermediate steps
185
       outlist<-list(dendro=hc,stepwise.peaks=a.pll[-nAmal],amalpeaks=a.pll[[nAmal]])
186
       return(outlist)
187
188
     }
189
```

### A.4 Surrogate variable analysis

Description	File	Functions		
Get SVA adjusted expression matrix:				
	/08_do_sva.R	doSVA()		

#### A.4.1 Get SVA adjusted expression matrix

Please note the function getH() (line 47 below) is the code available in the DanteR package to determine the number of significant surrogate variables. The function mulReg(Y,X) performs sequential linear regressions on the columns of the input Y using a fixed effects design matrix X. mulReg() returns a list containing the following vectors and matrices:  $RES_{n\times P}$ , residual matrix after Y has been regressed;  $BETA_{d\times P}$ , matrix of the regression coefficients, P columns for each regression;  $TVALS_{d\times P}$ , the corresponding t-statistics;  $PVALS_{d\times P}$  the corresponding p-values of TVALS;  $FPVALS_{P\times 1}$ , p-value for each linear regression corresponding to the null model F-statistic.

```
#### doSVA: Perform SVA using the model:
              Y_i = \mu_i + X\alpha_i + Z\beta_i + W\delta_i + \mathbf{e}_i
3
   4
   #### Y: is a n 	imes p matrix, where each p columns are regressed
   #### Intecept: boolean; do we want to fit a mean value? (yes, in most cases)
   #### X: is a n 	imes d_{lpha} design matrix of the factors of interest
   #### Z: is a n 	imes d_{eta} design matrix of the incidental experimental factors
   #### nosigsv: the number (referred to as H in some papers) of significant
10
               eigen vecs if NULL, the function will determine. If less than
               1, no W computed
11
   #### verbose: boolean, whether the surragate variable matrix, W is returned
12
   #### seed: an integer to feed into 'set.seed()' for reproducable results
13
   14
   #### Ytilde: the Y matrix with Z\beta_{j} \ + \ W\delta_{j} removed
15
   #### pvals: the p-values of Ytilde regressed on \mu_i + X\alpha_i + Z\beta_i + W\delta_i
16
   #### tvals: the corresponding t-statistics
17
   #### betas: the corresponding \alpha_i, \beta_i, \delta_i estimates
18
   #### paramlabels: a combination of I (intercept), X, Z, W to signify the
19
               relevent rows of p-vals/tvals/betas
20
   #### W: the eigen vectors matrix
21
   #### H: the number of columns of W (used eigen-vectors)
22
   23
   doSVA<-function(</pre>
24
25
     Y,Intercept=TRUE,X=NULL,Z=NULL,nosigsv=NULL,verbose=FALSE,seed=NULL
   ) {
26
     n < -nrow(Y)
27
     thisInt<-IXZ<-NULL
28
     if(Intercept) thisInt<-matrix(1,nrow=n,ncol=1,dimnames=list(NULL,"Intcpt"))</pre>
     if(is.null(thisInt) && is.null(X) && is.null(Z))
30
31
       cat("At least one of: Intercept, X and Z must be specified \n")
32
       return(NULL)
33
     } else IXZ<-cbind(thisInt,X,Z)</pre>
34
     kparam<-ncol(IXZ)</pre>
35
     colmarkers<-rep("",kparam)</pre>
37
     if(!is.null(thisInt)) colmarkers[indx<-indx+1]<-"I"</pre>
38
     if(!is.null(X)) colmarkers[(indx<-indx+1):(indx<-indx+ncol(X)-1)]<-"X"</pre>
39
```

```
if(!is.null(Z)) colmarkers[(indx<-indx+1):(indx<-indx+ncol(Z)-1)]<- "Z"</pre>
40
41
      RIXZ<-multReg(Y,IXZ,createNAvals=TRUE,seed=seed)
42
      thissvd<-svd(RIXZ$RES)</pre>
43
44
      W<-H<-NULL
45
      if(is.null(nosigsv)){
        H<-getH(RIXZ$RES,IXZ,nullsig=0.1,verbose=FALSE)
47
        if(H<1) cat("No significant surrogate variables found \n")</pre>
48
      }else{
^{49}
        H<-nosigsv
50
      }
51
      if(H<1){
52
        cat("No surrogate variables will be used \n")
53
54
        cat("Using H=",H," significant surrogate variables \n",sep="")
55
        W<-as.matrix(thissvd$u[,1:H])</pre>
56
        colnames(W)<-paste("W",1:H,sep="")</pre>
57
        colmarkers<-c(colmarkers, rep("W", H))</pre>
58
      }
59
      IXZW<-cbind(IXZ,W)</pre>
60
      Rtilde<-multReg(Y,IXZW)</pre>
61
      removecols<-colmarkers %in% c("Z","W")</pre>
62
      ZBetaWDelta<-0
63
      if(sum(removecols)) ZBetaWDelta<-as.matrix(IXZW[,removecols]) %*%</pre>
64
65
                      as.matrix(Rtilde$BETA[removecols,])
      Ytilde<-Y-ZBetaWDelta
66
      if(verbose) return(list(Ytilde=Ytilde,paramlabels=colmarkers,W=W,H=H))
67
      else return(Ytilde)
68
69
    }
```

### A.5 Pairwise fusion linear discriminant analysis

Description	File	Functions
Create a PFDA object	:	
	/09_create_pfda_obj.R	<pre>create_pfda_obj()</pre>
Predict class for new data and a PFDA object:		
	/10_pfda_predict.R	<pre>pfda_predict()</pre>

#### A.5.1 Create a PFDA object

```
####### FUNCTION: createPFldaobj()
    ### estimate parameters of PF-DA model, so that a discrim function created
2
3
   ###### input:
4
   ### X: a n x p matrix, of n obs and p variables
    ### Xclass: a vector of length n of the classes (must be a factor variable)
6
    ### priors: a vector of length K (#classes) with elements in (0,1)
9
    createPFldaobj<-function(X,Xclass,lambdar=1,priors=NULL,alph=NULL,wts=NULL)</pre>
10
      N<-length(Xclass)
11
      P<-ncol(X)
12
      nks<-table(Xclass)</pre>
13
      classnames<-levels(Xclass)</pre>
14
      K<-length(classnames)</pre>
15
      ### if not supplied, make \hat{\pi}_k data proportions
17
      if(is.null(priors)) priors<-nks/N
18
19
      if(length(priors)!=K){
20
        cat("The length of priors and the total number
21
             of groups must be equal \n")
22
        return(NULL)
23
      }else if(is.null(alph) & (N<P)){</pre>
        cat("Alpha is suggested for n
25
      }else if(N!=nrow(X)){
26
        cat("The length of Xclass and the number
^{27}
28
             of rows in X must agree \n")
        return(NULL)
29
      }else if(!all(nks>1)){
30
         cat("There needs to be at least two obs in each
31
             group for variances to be computed \n")
32
        return(NULL)
33
      }
34
35
      Xclassint<-as.integer(Xclass)</pre>
36
      transMeans<-colMeans(X)
37
      X{<-}X{-}matrix(rep(transMeans,N),nrow{=}N,byrow{=}TRUE)
38
39
      ##### create \mu_k = [\mu_{k1}, \ldots, \mu_{kp}] vectors
40
      ##### place on top of each other to get KxP matrix
41
      MuMat<-matrix(0,nrow=K,ncol=P)</pre>
42
      for(k in 1:K) MuMat[k,]<-colMeans(X[Xclassint==k,])</pre>
43
      MuIter<-MuMat
44
45
      ##### create \Sigma
46
      Sigma<-matrix(0,nrow=P,ncol=P)</pre>
47
      for(k in 1:K)
48
      {
49
```

```
rowuse<-which(Xclassint==k)</pre>
 50
                      Sigma<-Sigma+length(rowuse)*cov.wt(X[rowuse,],cor=FALSE
 51
                                                                                                                  ,center=TRUE,method="ML")$cov
 52
 53
                 Sigma<-Sigma/N
 54
                 ##### extract Diag elements
 55
                  sigmasqs<-diag(Sigma)</pre>
 57
                  if(!(is.null(alph) | is.null(wts))) sigmasqs<-sigmasqs+alph*wts
 58
                  else if(!is.null(alph)) sigmasqs<-sigmasqs+rep(alph,P)</pre>
 59
 60
                  #### Now start iterative estimation of the \ell_1 penalised means
 61
                  #### Note "squig" is used for the ML estimates
 62
                 G<-matrix(0, nrow=K, ncol=K)</pre>
 63
                  deltatol<-1e-10
 64
                  deltaMu<-1
 65
                 maxIter<-500
 66
 67
                  itcount<-0
                 while(deltaMu>(1e-5) && itcount<maxIter)
 68
 69
                      deltaMuNumer<-0
 70
                      deltaMuDenom<-0
 71
                       itcount<-itcount+1
 72
 73
                       ### For each of the features
 74
                       for(j in 1:P)
 75
 76
                            beta.t.j<-MuIter[,j]</pre>
 77
                            musqig.j<-MuMat[,j]</pre>
 78
                            sqigY<-X[,j]</pre>
                            sqigX<-matrix(0,nrow=N,ncol=K)</pre>
 80
                            G<-matrix(0, nrow=K, ncol=K)</pre>
 81
 82
                           ### \sum_{k=1}^{K-1} \sum_{k \neq a}^{K}
 83
                            for(k in 1:(K-1))
 84
                            {
 85
                                 for(kdash in (k+1):K)
 86
                                      PFweight<-1/abs(musqiq.j[k]-musqiq.j[kdash])
 88
                                      ### assign updated iterations, or tol value if "zero"
 89
                                      muDiffIter<-max(abs(beta.t.j[k]-beta.t.j[kdash]),deltatol)</pre>
                                      G[k,kdash]<-G[kdash,k]<- -PFweight/muDiffIter
 91
                                 }
 92
                            }
 93
                            for(k in 1:K)
 95
                                 sqigX[which(Xclassint==k),k]<-1</pre>
 96
                                 ### note the diag elements of G can be calculated as the sum of the column
 97
                                 G[k,k] \leftarrow -sum(G[,k])
 99
                            #### \ddot{M} = \left(B^T B + \lambda \sigma_i^2 G\right)^{-1} B^T J
100
                            \label{eq:multer_sigmasqs_j} \\ \text{Multer_sigmasqs_j} <-solve(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigY) \\ \\ \text{Multer_sigmasqs_j} <-solve(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%*%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%*%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_j]*G)%(t(sqigX)%sqigX+lambdar*sigmasqs_
101
```

```
deltaMuNumer<-deltaMuNumer+sum(abs(MuIter[,j]-beta.t.j))</pre>
102
            deltaMuDenom<-deltaMuDenom+sum(abs(beta.t.j))</pre>
103
104
          ### our break loop value
105
          deltaMu<-deltaMuNumer/deltaMuDenom
106
107
        cat("Iterations performed to aquire a solution:",itcount
109
             ,"| Final tol val:",deltaMu," \n")
110
111
       MuIter[which(MuIter<deltatol)]<-0</pre>
112
113
       ### \frac{1}{2}\sum_{j=1}^{p}\hat{\mu}_{kj}^{2} constant term
114
        consts<-rep(0,K)
115
        for(k in 1:K) consts[k]<-0.5*sum(MuIter[k,]^2/sigmasqs)
116
       ### \hat{\mu}_{kj}^2/\sigma_p^2 term
117
        lins<-vector(mode="list",length=K)</pre>
118
        for(k in 1:K) lins[[k]]<-MuIter[k,]/sigmasqs</pre>
119
120
       ### return calculated information as list object
121
        return(list(classes=classnames,consts=consts,lins=lins,prior=priors
122
                      ,meanadj=transMeans,MuIter=MuIter,InitMu=MuMat))
123
124
     }
```

#### A.5.2 Predict class for new data and a PFDA object

```
####### FUNCTION: PFldapredict()
    ### estimate probabilities and class of new inputs
2
3
    ###### input:
4
    ### ldaobj: an object created by createPFldaobj()
    ### Xnew: a n x p matrix, of n obs and p variables.
6
                May also be a single numeric vector (n=1) of length p
    ### priors: a vector of length K (#classes) with elements in (0,1)
    PFldapredict<-function(ldaobj,Xnew,priors=NULL)</pre>
10
11
      if(is.vector(Xnew,mode="numeric")){
12
         Xnew<-matrix(Xnew,nrow=1)</pre>
13
      }else if(!is.matrix(Xnew)){
14
         cat("Xnew must be numeric and either a vector or matrix \n ")
15
16
17
      Nnew<-nrow(Xnew)
18
       ### centre each feature at 0, as done on the training data
19
      Xnew<-Xnew-matrix(rep(ldaobj$meanadj,Nnew),nrow=Nnew,byrow=TRUE)</pre>
20
      Xclasses<-ldaobj$classes
21
      K<-length(Xclasses)</pre>
22
      if(is.null(priors)) priors<-ldaobj$prior</pre>
23
       outposteriors<-matrix(0,nrow=Nnew,ncol=K)
25
       colnames(outposteriors)<-Xclasses</pre>
26
27
28
       ### discrim function: \delta_k(x_{new})
       for(i in 1:Nnew){
29
         for(k in 1:K){
30
           outposteriors[i,k]<-log(priors[k]) - ldaobj$consts[k]</pre>
31
                                         + sum(Xnew[i,]*ldaobj$lins[[k]])
32
33
         }
       }
34
35
       ### predicted class is arg max
36
      ### p(G_K|x_{new}) = \frac{P(x_{new}|G_k)P(G_k)}{\sum_{i=1}^{K} P(x_{new}|G_i)P(G_i)}
37
       predclasses<-rep(0,Nnew)
38
       for(i in 1:Nnew){
39
         outposteriors[i,]<-exp(outposteriors[i,])</pre>
40
         predclasses[i]<-which.max(outposteriors[i,])</pre>
         outposteriors[i,]<-outposteriors[i,]/sum(outposteriors[i,])</pre>
42
43
      outpred<-factor(Xclasses[predclasses])</pre>
44
       return(list(pred=outpred,posteriors=outposteriors))
46
    }
47
```

### A.6 Pareto Fronts for variable ranking

Description	File	Functions	
Calculate dominating features:			
	/11_dom_feat.c	<pre>domfeat()</pre>	
Pareto Front wrapper functions:			
	/12_pareto_fronts.R	<pre>paretoRanking()</pre>	

#### A.6.1 Calculate dominating features

Below is the core of the Pareto Front code, finding features that are the dominated as per the definition. Written in C to be compiled to a <code>.so</code> file (or <code>.dll</code> on Windows operating systems) that in turn can be loaded into R.

```
#include <R.h>
2
   void domfeat(int *n, double *obja, double *objb, int *domvec)
3
4
     int i, j, nonDomI;
     for (i=0; i<*n; i++)
6
       j=<mark>0</mark>;
       nonDomI=1;
9
       while(nonDomI && j < *n)
10
11
         else if((objb[i]<objb[j]) && (obja[i]<=obja[j])) nonDomI=0;
13
         j+=1;
14
       }
15
       domvec[i]=-nonDomI+1;
16
17
     }
   }
18
```

#### A.6.2 Pareto Front wrapper functions

```
library(animation)
   dyn.load("domfeat.so")
2
3
   4
   # Pairwise case of Pareto Fronts
        obj is the 2\ \times\ n matrix of the two vectors of length n for
        the features/observations of the 2 criteria/objective functions
        istomin is a boolean vector of whether the criteria obj<sub>1</sub>, obj<sub>2</sub>
10
        are to be minimised (=TRUE), respectively
11
12
  13
  14
15
16
   # This function returns a vector of 'dominated' observations (Boolean,
17
   \# length n vector) FALSE=Pareto front, TRUE=dominated observation
18
19
20
   domFeaturesPW<-function(obj,istomin)</pre>
21
22
     #if to be minimised then just make negative and maximise
23
     obj[,istomin]<- -obj[,istomin]</pre>
24
     n<-as.integer(nrow(obj))</pre>
25
     obj1<-as.double(obj[,1])
26
     obj2<-as.double(obj[,2])
27
     domvec < -as.integer(rep(0,n)) #output vector
29
     return(as.logical(.C("domfeat",n,obj1,obj2,domvec)[[4]]))
30
   }
31
32
   33
   34
35
   # General case
36
        objmatrix is n \times m matrix. n features/observations and
37
        m criteria/objective functions istominvec is a boolean vec
38
        of length m to say whether the criteria are to be minimised
39
40
   41
   42
43
44
  # This function returns a vector of 'dominated' observations (Boolean,
45
  \# length n vector) FALSE=Pareto front, TRUE=dominated observation
   # same as pairwise but the input can take more than two objective functions
47
48
49
```

```
domFeatures<-function(objmatrix,istominvec)</pre>
50
51
      n<-as.integer(nrow(objmatrix))</pre>
52
      m<-ncol(objmatrix)</pre>
53
      objmatrix[,istominvec]<- -objmatrix[,istominvec]</pre>
54
      vecdomvec<-rep(1,n)</pre>
55
      indxs<-combn(m,2)
      nm<-ncol(indxs)</pre>
57
      i<-0
58
      while(i<nm)
59
      {
60
61
        # call pairwise function, take the intersection of previous
62
        # dominated observations remembering the intersection(s)
63
        # of dominated in the same as unions(s) of Pareto fronts
64
        vecdomvec<-vecdomvec * .C("domfeat"</pre>
65
66
                  ,as.double(objmatrix[,indxs[1,i]])
67
                  ,as.double(objmatrix[,indxs[2,i]])
68
                  ,as.integer(rep(0,n)))[[4]]
69
      }
70
      return(as.logical(vecdomvec))
71
72
    }
73
    74
    75
76
    # Sucessive Pareto Fronts
77
          noFronts is the # of pareto fronts required
78
79
          fn returns a vector of length n
80
                each element is labelled the pareto front #,
81
                O is dominated even after noFronts found
82
83
    84
    85
86
    paretoFronts<-function(noFronts,objmatrix,istominvec)</pre>
87
    {
88
      objmatrix[,istominvec]<- -objmatrix[,istominvec]</pre>
89
90
      n<-as.integer(nrow(objmatrix))</pre>
      m<-ncol(objmatrix)</pre>
91
      pfvec<-rep(0,n) #output vector
92
      #once a front is found we need to set the correponding values to \infty or
93
      # -\infty so they won't be chosen again
      #try: as.numeric(c(TRUE,FALSE,TRUE))*2-1 to see what the next line is doing
95
      #if Min then set 1, ifMax then set -1 (the sign of the Inf if we find front
96
         and have to put to a value)
97
      ourInfs<-min(objmatrix)-1
98
      allFrontsFound<-FALSE
99
100
      i<-0
101
```

```
while(i<noFronts && !allFrontsFound) #go thru all fronts required
102
103
        i<-i+1
104
        df<-domFeatures(objmatrix,rep(FALSE,m)) #general m obj vectors function</pre>
105
        # pf.i are the indexs of the output vector that need to be updated
106
        # with the pareto front number
107
        pf.i<-(!df) & (pfvec<1)
108
        pfvec[pf.i]<-i
109
        # re-assign values were pareto front found
110
        objmatrix[pf.i,]<-ourInfs
111
        if(all(pfvec>0)) allFrontsFound<-TRUE</pre>
112
      }
113
      return(pfvec)
114
115
    }
116
    117
    118
119
    # Leave-one-out/k-fold feature ranking
120
121
    # returns a vector of length n with values \in (0,1] for feature importance
122
123
    124
    125
126
127
    # Same inputs of previous functions, with folds (aka k-fold cross
128
    # validation) and reps is the number of times we re-do the cross
129
    # validation fold=1 or the length of the input (i.e. n) creates
130
    # leave-one-out cross validation
132
    paretoRanking<-function(objmatrix,istominvec,noFronts=20,folds=1,reps=5)</pre>
133
134
      objmatrix[,istominvec]<- -objmatrix[,istominvec]</pre>
135
      m<-ncol(objmatrix)</pre>
136
      n<-nrow(objmatrix)</pre>
137
      pfmetric<-rep(0,n) #output vector
138
      nfolds<-n
      if(folds>1) nfolds<-folds
140
      if(nfolds==n) reps<-1
141
142
      blocks<-kfcv(nfolds,n)
143
      block.nos<-rep(1:nfolds,blocks)
144
145
      for(r in 1:reps)
146
147
        indxs<-sample(1:n) #fresh randomisation each repetition</pre>
148
        k.f.mat<-cbind(indxs,block.nos) # create the fold 'blocks' of data
149
        for(i in 1:nfolds)
150
151
          rows<-k.f.mat[k.f.mat[,2]==i,1] # find the ith fold to leave out
152
          # call general function with ith fold removed
153
```

```
calcfronts<-paretoFronts(noFronts,objmatrix[-rows,],rep(FALSE,m))</pre>
154
         # which are non-dominated
155
         whichnondom<-calcfronts>0
156
         # if you are ont the first front you get 1, second=1/2, third=1/3,
157
         # ..., jth=1/j, else 0
158
         pfmetric[-rows][whichnondom]<-</pre>
159
             pfmetric[-rows][whichnondom]+1/calcfronts[whichnondom]
161
      }
162
163
      #now divide by maximum posible value i.e. (nfolds-1)*reps so output in [0,1]
      pfmetric<-pfmetric/((nfolds-1)*reps)</pre>
164
      return(pfmetric)
165
    }
166
167
    168
    # Below are three metrics that can possibly describe the value of
169
       variables/fetures to discriminate betwwen classes
170
    171
172
    # minIntraClassVar(): find the minimum WITHIN class variance of the K groups
173
   # interClassVar(): find the variance of means/centroids of the K groups
174
    # maxInterClassDist(): possibly correlated with interClassVar, find the dist
175
                 MAXIMUM between the K group's centroids/means
176
177
   # The rationale of the last metric is that a variable/feature that only
178
   # seperates two of the K classes is undervalued by the Fisher score because
   # it may not separate the K-2 classes remaining well.
180
   # ... And a separation of two classes (in conjunction with other variables)
181
          is important information for the discriminant model
182
    184
    #### ds: a data.frame or matrix (numeric values only/factors will be dealt
185
    #### with as integers) class vec: a vector correspong to the class of
186
          the rows of ds
187
    188
189
190
    minIntraClassVar<-function(ds,class.vec){</pre>
      dsfs<-ds
192
      if(!is.matrix(dsfs)) dsfs<-data.matrix(dsfs)</pre>
193
194
      p<-ncol(dsfs)</pre>
195
      K<-length(levels(class.vec))</pre>
196
      n.all<-length(class.vec)</pre>
197
      n.i < -0
198
      intraClassVar<-Inf
200
      mean.j<-colMeans(dsfs)</pre>
201
202
      for(i in 1:K){
203
        true.vec<-(as.integer(class.vec)==i)</pre>
204
        n.i<-length(which(true.vec))</pre>
205
```

```
mean.class<-colMeans(as.matrix(dsfs[true.vec,],ncol=p))</pre>
206
          var.class<-colSums(as.matrix((dsfs[true.vec,]-rep(mean.class,each=n.i))^2,ncol=p))</pre>
207
          intraClassVar<-pmin(intraClassVar,var.class/(n.i-1))</pre>
208
       }
209
        return(intraClassVar)
210
     }
211
     interClassVar<-function(ds,class.vec){</pre>
213
214
        dsfs<-ds
215
        if(!is.matrix(dsfs)) dsfs<-data.matrix(dsfs)</pre>
216
217
        p<-ncol(dsfs)</pre>
218
       K<-length(levels(class.vec))</pre>
219
220
221
        interClassVar<-0
       mean.j<-colMeans(dsfs)</pre>
222
223
224
        for(i in 1:K){
225
          true.vec<-(as.integer(class.vec)==i)</pre>
          n.i<-length(which(true.vec))</pre>
226
          mean.class<-colMeans(as.matrix(dsfs[true.vec,],ncol=p))</pre>
          var.class<-((mean.j-mean.class)^2)</pre>
228
          interClassVar<-interClassVar+var.class</pre>
229
230
        }
        return(interClassVar/(K-1))
231
     }
232
233
     maxInterClassDist<-function(ds,class.vec){</pre>
234
235
236
        if(!is.matrix(dsfs)) dsfs<-data.matrix(dsfs)</pre>
237
238
        p<-ncol(dsfs)</pre>
239
       K<-length(levels(class.vec))</pre>
240
241
        interClassDist<--Inf
242
       mean.j<-colMeans(dsfs)</pre>
244
        for(i in 1:K){
245
^{246}
          true.vec<-(as.integer(class.vec)==i)</pre>
          mean.class<-colMeans(as.matrix(dsfs[true.vec,],ncol=p))</pre>
247
          interClassDist<-pmax(interClassDist,abs(mean.j-mean.class))</pre>
248
       }
249
        return(interClassDist)
250
251
```