1. A hypothetical population is given in the table below. Consider stratified sampling with SRSs of size  $n_1 = n_2 = 3$  taken from the two strata, respectively.

Stratum 1		Stratum 1	
Unit	y	Unit	$\overline{y}$
1	1	5	5
2	4	6	6
3	4	7	9
4	5	8	11

- (a) (1pt) What are the values of  $\overline{y}_{1U}$  and  $\overline{y}_{2U}$ ?
- (b) (1pt) What are the values of  $S_1^2$  and  $S_2^2$ ?
- (c) (1pt) What are the values of  $V(\hat{t}_1)$  and  $V(\hat{t}_2)$ ?
- (d) (1pt) What are the values of  $V(\hat{t}_{str})$  and  $V(\hat{y}_{Ustr})$ ?
- (e) (2.5pt) Write out all possible stratified SRSs (with  $n_1 = n_2 = 3$ ), and for each stratified sample, calculate  $\hat{t}$ .
- (f) (1pt) What is the sampling distribution of  $\hat{t}$ ? That is, list all possible values of  $\hat{t}$  and their associated probabilities.
- (g) (1pt) Use the sampling distribution of  $\hat{t}$  to verify that  $\hat{t}$  is an unbiased estimator of t.
- 2. (2.5pt) Exercise 6(a), page 103. Use the optimum allocation formulas using  $S_1 = 2S_2$  and  $S_3 = S_2$ . That is, replace  $S_1$  with  $2S_2$  and  $S_3$  with  $S_2$ , and simplify.
- 3. (3pt) Exercise 11 (a), page 105. Also, include a 95% confidence interval and its interpretation in the context of the problem. The *seals.dat* file will be mailed to you and posted on the webpage.
- 4. (1.5pt) Exercise 12, page 106.
- 5. (3.5pt) Exercise 16(a), page 107. Also, include a 95% confidence interval and its interpretation in the context of the problem. The *otters.dat* file will be mailed to you and posted on the webpage.
- 6. (2pt) For Stat Graduate Students: Exercise 21, p. 110. You are to work alone on this problem with no discussion with other students.