

Biologists observe 27 nests of barn owls.

Response: Number of Calls

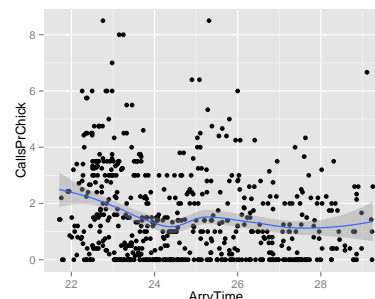
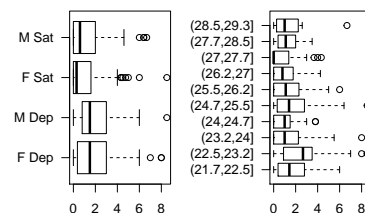
Predictors:

Size of brood (1 to 7)

Sex of parent (245 female, 354 male)

Food "Treatment" (satiated vs deprived)

Arrival Time (21.7 to 29.2 hours)



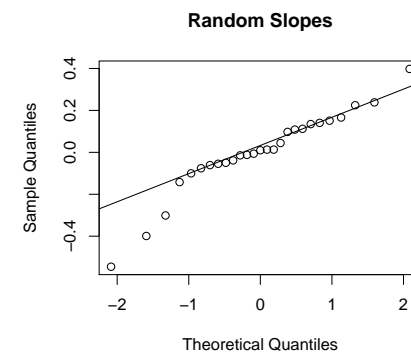
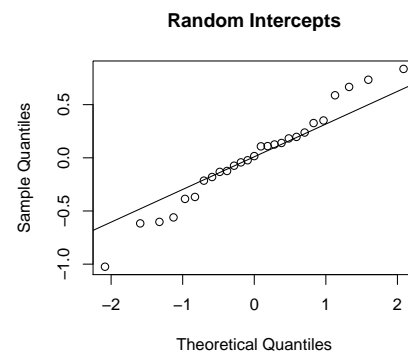
Possible interaction between treatment and gender.

```
fit1 <- glmer(Ncalls ~ offset(log(BroodSize)) + FoodTrt *
  SexParent + bs(cTime, df = 5) + (1 | Nest), data = owls,
  family = poisson)
fit2 <- glmer(Ncalls ~ offset(log(BroodSize)) + FoodTrt *
  SexParent + bs(cTime, df = 5) + (1 + cTime | Nest),
  data = owls, family = poisson)
fit3 <- glmer(Ncalls ~ offset(log(BroodSize)) + FoodTrt *
  SexParent + SexParent * bs(cTime, df = 5) + (1 + cTime |
  Nest), data = owls, family = poisson)
xtable(anova(fit1, fit2, fit3), digits = c(0, 0, 0, 0, 0,
  0, 1, 0, 4))
```

	Df	AIC	BIC	logLik	deviance	Chisq	Chi Df	Pr(>Chisq)
fit1	10	4851	4895	-2416	4831			
fit2	12	4697	4750	-2337	4673	157.7	2	0.0000
fit3	17	4658	4733	-2312	4624	49.2	5	0.0000

Evidence that slopes vary from nest to nest. Large interaction.

```
par(mfrow = c(1, 2))
qqnorm(ranef(fit3)$Nest[, 1], main = "Random Intercepts")
qqline(ranef(fit3)$Nest[, 1])
qqnorm(ranef(fit3)$Nest[, 2], main = "Random Slopes")
qqline(ranef(fit3)$Nest[, 2])
```

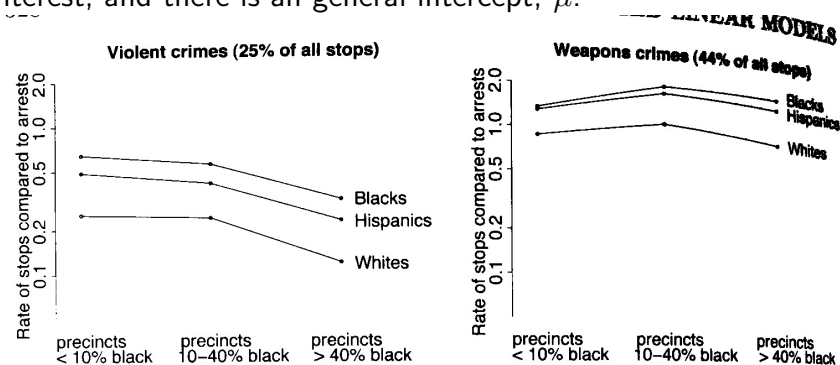


May not be "Gaussian" errors. Are we missing a predictor?

We don't have access to the data. The Poisson Mixed Model:

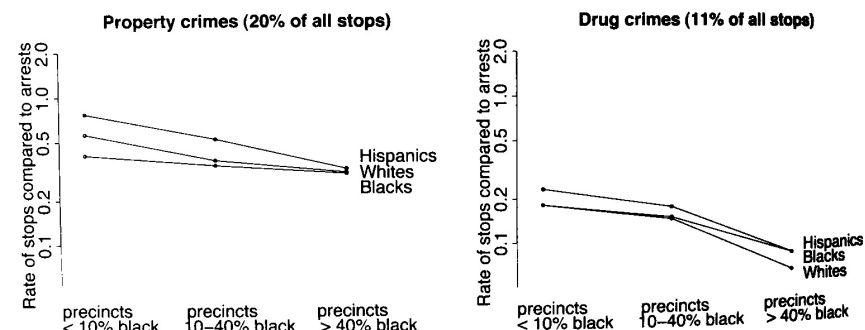
$$y_i \sim \text{Poisson}(u_i e^{X_i \beta + \epsilon_i}), \quad \epsilon_i \sim N(0, \sigma_\epsilon^2)$$

Their example adds random effects $[\beta_p \sim N(0, \sigma_p^2)]$ for Precincts and (indeed) of extra overdispersion. Race effects, α_e are of interest, and there is an general intercept, μ .



Stat 506

Gelman & Hill, Chapter 15



Stat 506

Gelman & Hill, Chapter 15

Gelman Storable Votes §15.2

Multinomial is like 2 logistic regressions:

$$\text{invlogit}[\Pr(y_i > 1)] = X_i \beta; \quad \text{invlogit}[\Pr(y_i > 2)] = X_i \beta - c_2$$

or

$$y_i = \begin{cases} 1 & \text{if } z_i < c_{1.5} \\ 2 & \text{if } z_i \in (c_{1.5}, c_{2.5}) \\ 3 & \text{if } z_i > c_{2.5} \end{cases}; \quad z_i \sim \text{logistic}(x_i, \sigma^2)$$

Use Normal distributions for each of $c_{1.5}$, $c_{2.5}$, $\log(\sigma_j)$ to allow varying cutoffs and variances for each student. Estimate

$\sigma_{1.5}$, $\sigma_{2.5}$, $\mu_{\log(\sigma)}$, $\sigma_{\log(\sigma)}$ from the data.

Figure 15.6 looks at optimal versus observed strategies for 2, 3, 6 player games.

Social Networks §15.3

How many people do you know?

If you know 2 Nicoles out of 358K in the US, we compute size of your network as:

$$\frac{2}{358000} \times 280000000 = 1560$$

Cross check with other names.

But there are “clumps” of data (JayCeas), so we need overdispersed Poisson.

Additional analysis looks at selective memory, positive/negative experiences and residuals.

Stat 506

Gelman & Hill, Chapter 15

Stat 506

Gelman & Hill, Chapter 15