

## L3 notes

### Some terms

$d(h * f)$   $h$  convolve with  $f$

Know what the math equations are doing and apply them

Pad the sides with 0 and shift the kernel across the numbers

$\text{floor}(\text{kernel size} / 2)$

$[1, 1, 1]$  symmetric

Linear (shift invariant) = output Is scaled accordingly

Correlation filter to shift pixels in image

Normalised = summed up add to 1

Effects are negligible for large images

Gaussian kernel depends more on the sigma

Salt and pepper = isolated pixels that are problematic

Smooth away the impulse and spread it all around

Impulse is salt without the pepper

Higher signal amplify both the signals and noise

Histogram stretching adjust contrast

Bitmap save the pixels independently

### Laplacian

the process to get the residual is [upsample (fill with 0s)  $\rightarrow$  blur  $\rightarrow$  subtract from original]

(the reason for the blur is to "spread out" the values over the filled-in black pixels)

Q: Does spatial quantization mean the quantisation of values of x and y?  
i.e. x and y can only take discrete integer values?

A: spatial quantization basically happens because we cant represent continuous x and y coordinates in a discrete system

Q: It seems that you always regard intensity as integers, is it a routine for this course?

A: Yes and no

Q: does adjusting abstract and brightness simply refer to the linear mapping or also include the non-linear gamma mapping

A: Non-linear mapping also just the contrast

Photography operation we dont use stretching ( we use images that stretch over the entire range)

Q: In practice, is convolution used more than correlation?

A: Convolution

Q: Is reconstructing the original image using laplacian pyramid 100% loss-less?

A: Up to the difference of quantisation

Q: Can we compensate motion blur by finding the motion blur kernel and use the inverse kernel to demotion blur?

A: Yes, finding the kernel is always hard

Q: Is convolution invertible? In a sense that let's say we have a convolved image, is there always a filter such that we can recover the original image using convolution? e.g, undoing blur convolution using a specific sharpening convolution

A: If we throw away half of the pixels

Q: Does laplacian pyramids take 2\* space than gaussian pyramids simply because laplacian pyramids have 2 sets of the pyramids (gaussian + residual)?

A: Same amount of space

## L4 notes

### Some terms

mean filter does not remove all noise and blurs the image only isolated values 0-255

median filter remove all noise and blurs the image slightly arrange in increasing starting from 0

difference filter sum up all the values in row same value for the entire row

each pixel has a tangent plane

kernel size controls the strength of the filter

border problem output is reduced in size for the pixels along the edge

the image patch and the template always contain positive numbers,  $\cos \Theta \in [0, 1]$ , i.e., the output of normalized cross-correlation is normalized to the interval  $[0, 1]$ , where 0 means no similarity and 1 means a complete similarity.

region of interest can benefit template matching

image has discrete representation we need approximation, positive gradient value when the image change from dark to bright and negative when reversed image

Image sharpening  $g(x,y)=f(x,y)-f(x,y) \circ h(x,y)$

Magnitude =  $\sqrt{(gx^2 + gy^2)}$

Approximated magnitude =  $|gx| + |gy|$

non maxim suppression if edge has a magnitude too small connected to another pixel above a threshold, dont prune

extract edges to detect start and end edges , useful for 3d to know the shape and geometry

why? resilient and lighting and color useful for recognition

## Template matching

This object is now the template (kernel) and by correlating an image with this template, the output image indicates where the object is. Each pixel in the output image now holds a value, which states the similarity between the template and an image patch (with the same size as the template) centered at this particular pixel position. The brighter a value, the higher the similarity.

Purely correlation since strongest response is when original image exactly matches output

what happens when u zoom the baby's face 2x (refer to image)?

Template is not symmetrical

## Neighborhood processing

Neighbor pixels play a role when determining the output value of a pixel

## Convolution vs Correlation

Convolution (rotated 180 degrees)

$$h(i, j) \cdot f(x - i, y - j)$$

Correlation

$$h(i, j) \cdot f(x + i, y + j)$$

To check if same result, the kernel before and after 180 degrees are same

Intuition of Sobel filter

$$g_x(x, y) = f(x + 1, y) - f(x - 1, y)$$

correlate  $[1, 0, 1]$  with the image

$$[-1, 0, 1]$$

$$[-2, 0, 2] = 2[-1, 0, 1] \text{ (put more weights at center)}$$

$$[-1, 0, -1]$$

Combine the both result using the horizontal and vertical Sobel to get

the final edge image

3x3 kernel is used as we need to include the neighbours as single row or single column kernel is sensitive to noise

## Derivatives

does not matter the order of the derivative and gaussian blur  
gaussian filter to remove noise before laplacian applied

vertical shows pixel of image row  
horizontal shows the gradient value

$f(x)$  grey level value

$f'(x)$  gradient value

$[1, -2, 1]$

$f''(x)$  gradient of the gradient

$$g_{xx}(x, y) \approx f(x-1, y) - 2 \cdot f(x, y) + f(x+1, y)$$

$$g_{yy}(x, y) \approx f(x, y-1) - 2 \cdot f(x, y) + f(x, y+1)$$

## First order derivative

Sobel is a combination of derivative kernel

Sobel results in wide edges as it is first order

First order derivative (thicker edges)

Roberts, Prewitt, Sobel filter

## Second order derivative

Second order derivative can know the exact edge and detect 1 px thin edge

Smoothing is needed

DoG (difference in gaussian)

laplacian is the second order derivative (most sensitive to noise)

-1 white 0 grey 1 black

To approximate the 2nd order derivatives

$g_{xx}(x, y) \approx f(x-1, y) - 2f(x, y) + f(x+1, y)$  represents  $[1; -2; 1]$

$g_{yy}(x, y) \approx f(x, y-1) - 2f(x, y) + f(x, y+1)$  represents  $[1 \ -2 \ 1]$

## Hysteresis

pixels below some value 0

hysteresis join the strong and weak pixels

thresholding depends on the image

cv2.canny is interpolated version

random forest is a learned model from human markups

gradient shift dark to light and light to dark

is the center a local maximum or not if yes keep it as part of the edge  
else discard it

Q: would there be multiple local maxes after performing the non-maximum suppression?

A: no multiple local maxes

Q: is horizontal gradient detection always from left to right? similar for vertical case.

A: left to right

Q: Could you explain the intuition behind why cross correlation isn't commutative/associative, even tho convolution is just flipping the kernel?

A:  $[1, 2, 3]$  cross correlation  $[3, 2, 1]$  is not the same as  $[3, 2, 1]$  cross correlation  $[1, 2, 3]$

$[1, 2, 3]$  cross convolution  $[0, 1, 0]$  is  $[3, 2, 1]$  so it is not identity

Q: From slide 9, how is the 1D derivative filter constructed from the finite differences discrete version equation with  $h = 2$ ?

A: 2 elements we are using

Q: When convolution/cross-correlation is mentioned, is full padding assumed by default?

A: is not full padding, lecture examples are only full padding

Q: is padding to just inserting zero rows and zero columns or that plus blurring/interpolation? It seems to have been used both ways having to do with interpolation (bilinear, linearly solve between 2 neighbours) or interspersed in rows and columns

blurring to reduce noise (to avoid enhancing the noise)

Q: I think it was mentioned last lecture that convolutions are generally invertible. How do we reconcile this with the notion that blurring is lossy?

A: convolution is multiplicity in the inverse domain (division can have problems)

blurring in itself is not lossy only downsampling

for every single element, composed of several pixels, mixture of weights, same kernel applied to next kernel blurring + downsampling makes it lossy

factor all of this in the system of equations should be able to recover the image

Q: why not take the residual of the original versus upsampled of previous image

A: remove some values these are the values we want to preserve in the residual else will keep some of the detailing

## L6 notes

### Some terms

bandwidth is too narrow not very representative  
we don't know what is the correct/ incorrect value for bandwidth  
sum of all the gaussian forms the new curve  
dirac delta - bandwidth is very small  
number of textons can be smaller/larger than the filter banks  
euclidean distance between histogram ends up compensating for each other  
What are textures used for?  
cue to tell us on the underlying 3d structure  
scale of the envelope, single or many wavelengths

running across all the images where each image is a pixel  
run the cluster where every single pixel and image is a datapoint replace all  
pixels in the email with the texton id, compute the histogram based on the  
samples, each of the texton image is represented with a histogram  
texton id is per pixel  
x and y then the texton would not be purely texture

texture is independent feature to the segment it belongs to, we don't have  
to do segmentation to find the segment in the first place  
the responses is for the whole filter bank  
Do k-means twice  
first k means to form texton dictionary  
second k means NN search (can also apply mean-shift)

histogram is 100 dimension vector also  
Feature Representation  
Filter bank Response  
Texton histogram

Note: Texton histogram as a feature for segmentation will not give a clear  
segmentation, problematic edges, results in a pixelated image for the texture  
(not localised)  
Good localization, pixel from the 1 pixel or all over is the same  
CNN is aggregation of many filters, take a feature response and apply an-  
other kernel to it



blurring each channel independently (2d blurring), now we are blurring the filter response

we have consider the location of the pixel for segmentation

region is bounded by two separate histograms, then u would have separate results

Q: Are we able to somehow use a filter to extract coloraturas as a filter inside the filter bank? So that we can run clustering algo on both texture and colour at the same time?

A: you can mix the colors if you want, create a gabor filter for each channel

Q: can I clarify whether textons are generated based on clustering done over all filter results within a filterbank? Or is it done using only some sort of 'most differentiating' filter result?

A: filter bank only to apply to all images

apply 2d convolution

Q: how does using the same filter bank ensure the bins are the same

A: having very different feature response

1 image per type then maybe

Q: Why 3 clusters?

A: there is nothing to distinguish the skin from the background

## Quiz 1

Red and green considered equally, but blue is not considered at all  
Maximum shades of grey will not be the shade

## L7 notes

### Some terms

SSD

keypoints are also corners or interest points

low error will look dark, high error will look bright

shape is going to affect the ellipse, size does not matters

$H = \begin{bmatrix} 0 & 0 \\ 0 & C \end{bmatrix}$  gradient is x direction is 0

$H = \begin{bmatrix} A & 0 \\ 0 & 0 \end{bmatrix}$  gradient is y direction is 0

greedy approach non-maximum suppression has keypoints approximately

in the same location as it looks for areas that has high contrast  
automatic scale selection, harris is equivariant to changes of scale

## Weights of derivative

gaussian before we do the summation for the weights, more weight at the center, less weights at the edge

Instead of applying the effects, we are looking at two viewpoints under two different lighting conditions

highest response has a signal has characteristic scale that has the same as gaussian, width of signal corresponds in signal characteristic

Harris operator is more efficient compared to eigen value decomposition  
If the region is unusual then it is difficult for matching, approximated distinctiveness with SSD error

Linearize with 2nd moment matrix

Quantify distinctiveness with eigenvalues of H

R is the cornerness is defined as

$$R = \det(H) - k \text{trace}^2(H)$$

Values can be obtained from the matrix itself

LoG finds blobs (keypoint detector that tries to find roughly circular regions) maximum scale is already built-in (maximum size of the kernel wrt to image)

Auto correlation: Create a template of the patch, shift it around where I use the local patch

Q: Is template the benchmark for comparison? A: strongest peak where it matches to itself Refer to template matching

No matter where u shift the template, will get a strong response at the sky

Third dimension is the intensity

We need 3d How do we analyse the points without looking at 3d

$\lambda_{min}$  and  $\lambda_{max}$  are perpendicular to each other

SSD error  $E(u, v)$

Error will be 0 or greater

H is always positive definite

Semi definite where there is 0 case, flat region only in synthetic images

Cross section is approximately circular ( a lot of change in all directions)

Direction of the fastest change perpendicular to the slowest change will be approximately equal

Which direction I change in it is going to be different

Contrast causes the threshold

$\lambda_{min}$  would be small as  $(\lambda_{min})^{-\frac{1}{2}}$  where there is no change on the straight line

Q: Clustering the responses of the textons

A: The response are the data points, each feature response is 1 dimension, each data point cluster in 38 dimensions

Dimensionality: Refer to L6 supplements

One blue dot is 1 pixel, x location is 1 feature value and y location is 1 feature value

Eigenvalue decomposition of pixel then u would get every pixel also axis length is very long

Q: Texture and template matching are they the same?

A: Correlate the long, what is the pattern vs the individual image. Detecting many texture in 1 image, so the feature response will be different in different part of images. Only a particular filter is tuned to that signature response. Normally we don't have to hand-create the filters. Deep learning to learn whole bunch of features, or gabor filter, can tune the filters. Over many dimensions can get a unique response to that example.

Q: Filter bank to find the size

A: Large enough filter bank or some way to count

Binary classification if the sheet is defect or not

Q: Why is the skin and background cannot be segmented?

A: Texture of the background is very large, approximate scale of the marble is on par with the arm. Doing agnostic segmentation, we don't model the content in the image, only based on filter response. There is no reason why

it should end up in certain segmentations.

Clustering is done over all of the pixels over all of the images. Creating the local histogram is trial and error

## **L8 notes**

### **Some terms**

SIFT - scaling iterative feature response

Pixel wise difference (gradients) - more sensitive to relative location but sensitive to deformations

Color histogram - 3d histogram

What size of the cells do we want, fine grids, overlap etc Bin sizes - more finely tuned, a small shift will affect the histogram

Compare histogram - chi square

Orientation normalization

### **Averaging**

Bimodal distribution average end up with dominant orientation with no gradient

MOPS or GIST is no longer used as a descriptor

### **Mode - SIFT**

SIFT - understand the implication of doing this

Can be combined with other keypoint detector

as the threshold is larger, it removes more keypoints, depends on illumination difference

poorly localised if it sits on an edge and not a corner  
corners have high curvature, edges have low curvature

needs to be clear where the keypoint is matched to when moving in a straight line

ratio of eigenvalues to be below the edge thresh high threshold more tolerant of edges  
 smaller bar to be corner, longer bar is edge  
 white on black and black on white difference  
 black bar cannot be keypoints as we also have the surrounding neighbors

We don't assign gradients in original orientation - dominant orientation  
 Taking the original histogram with some wrapping operation, form of normalisation wrt dominant orientation  
 Normalize to unit length  
 If it exceeds the threshold set the threshold value, rectify and assign it. Then renormalize.  
 Clamping is to encourage invariance to small changes to illumination, over count in certain orientations.  
 can use in the dense form where it can use in any rotation  
 High robust

## Feature matching

### Image transformation

Filtering  
 Only changes on the actual image intensities  
 $G(x) = h \{ F(x) \}$  Warping  
 $G(x) = F \{ h(x) \}$  changes the location of the pixels

### 2d projective transformation

affine: parallel lines are still preserved projective: also known as a homography, try to solve for the parameters for a projective transformation  
 Not an arbitrary matrix with 9 degrees of freedom (3x3)  
 Solve for H using direct linear transform

## SVD

$A = U \Sigma V^T$   
 V is a singular matrix  
 singular values found on diagonal values of sigma

columns of  $V$  are single vectors

$N$  number of correspondences

Normalization such that the centroid is  $(0, 0)$  of the similarity transformation is a whitening step

RANSAC deal with outliers, sample from the set of noisy observations

Even though we can sample more, we usually  $s$  to be equal to the number of the outliers