

# Solitary Wave Families in Two Non-Integrable Models Using Reversible Systems Theory

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# Overview

- Definitions
- Background
- Literature Review
- Method of Solution
- The Generalized Pochhammer-Chree Equations
- A Generalized Microstructure Equation

# Reversible Dynamical System (Iooss & Adelmeyer)

Overview

Definitions

Reversible  
System

Solitary Wave

Background

Normal Forms

Bilinear  
Functions

Literature Review

The Models

GPC

MS

Results

GPC

MS

Consider

$$\frac{dz}{dt} = F(z; \mu), z \in \mathbb{R}^n, \mu \in \mathbb{R} \quad (1)$$

where

$$F(0; 0) = 0$$

. If there exists a **unitary** map

$$S : \mathbb{R}^n \mapsto \mathbb{R}^n, S \neq I$$

such that

$$F(Sz; \mu) = -SF(z; \mu) \forall z, \mu$$

then (1) is a reversible system.

# Families of Solitary Waves

Here we will use the term solitary wave or "solitons" in the broadest sense, as a solution to a nonlinear equation which ETC

# Normal Form Theory

# Properties of Bilinear Functions

# Selected Literature Review

# The Generalized Pochhammer-Chree Equations



# A Generalized Microstructure PDE

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# Results: The Generalized Pochhammer-Chree Equations

# Results: A Generalized Microstructure PDE