

# Artificial Intelligence Report 5th Week-15th Problem

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## Note

- I originally wanted to spend more time on this project, but finally I decided to finish it on time.
- Fully tested on Ubuntu 32/64 bit and Macbook with Opengl library installed.
- Opengl library is installed by default on Mac, and it can be installed on Ubuntu by typing the following line in terminal:

```
$ sudo apt-get install mesa-common-dev
```

- Source codes:
  - **state.hpp, state.cpp**: Represent the game state
  - **alphabetAgent.hpp, alphabetAgent.cpp**: Alphabet agent
  - **minimaxAgent.hpp, minimaxAgent.cpp**: Minimax agent
  - **grid.hpp, grid.cpp**: Use to calculate shortest path between two grids
  - **utility.hpp, utility.cpp**: Evaluate states
  - **gsearch.hpp, mystl.hpp**: Template class for A\*, DFS, BFS
- In current report, I will not go too much in details about the source codes like I did in previous reports. Hopefully the above short description would be enough to understand to basic structure of my implementation.

# 1 Pacman

Pacman is classic game which was very popular in the 1980's. It is also a good benchmark to implement AI's algorithms, especially good for testing adversarial search algorithms. The original game's rules are quite complicated, and due to the time constraint, I will present its simpler version in this report:

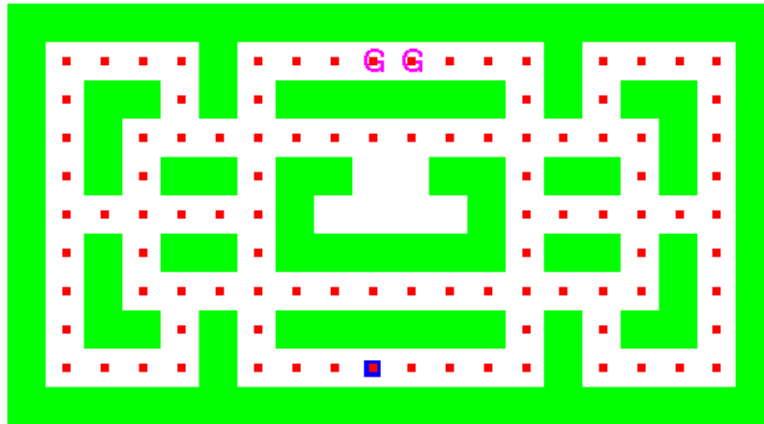


Figure 1: Start field of Pacman game (G is ghost, Blue dot is Pacman)

- Size of the board:  $9 \times 18$
- There are two ghosts and one Pacman on the field.
- Pacman wins when eating up foods.
- Pacman loses when being eaten by ghosts.
- The ghosts are always in chasing mode.
- Turn-taking game: Pacman first, then ghosts. Even though it looks like Pacman and Ghost simultaneously make their moves, but in my implementation, Pacman moves first, then ghosts choose their corresponding actions.

Normally, the task is to train Pacman to win the game, but I choose the opposition that is to make AI's ghosts. The two tasks have their own difficulty and appealing.

- AI's Pacman: Pacman wins only if he can eat all the foods without being eaten by ghosts. Therefore, when accessing a state from Pacman's point of view, we have to consider number of food left, distances from ghosts, distance to the nearest food.
- AI's Ghosts: Ghosts, on the other hand, do not care about foods, so their only concern is to chase Pacman. However, ghosts are not alone, so this is a **collaborative task**, when two or more ghosts have to act together to win their game.

In short, the most interesting point of making AI's ghosts are their collaborative behaviour toward the same goal, kill Pacman.

## 2 Adversarial Search

As the name suggests, adversarial search algorithms are in demand when adversary agents present. An agent cannot control its opponents or even its teammates' actions, that is why when making a move, it has to consider all possible outcomes of its and other agents' combined actions. The next following algorithms endeavour to deal with a specialized kind of games, which are deterministic, turn-taking.

## 2.1 Minimax

In Pacman game, Pacman is the Max player, while ghosts are Min players. The prototype for two main methods of MinimaxAgent class are:

```
1 virtual double Evaluate(const State &state, int depth, int player);  
2 vector<Action> ChooseCombinedGhostAction(const State &state, int depth, double *v = NULL);
```

There is an ChoosePacmanAction method, but because my focus is to make AI's ghosts, so I will not present it here.

- **Evaluate State:** The state space of Pacman is very big, so we have to access a state even if it is not a terminal one. Basically, this function will define the efficiency of the algorithm. The better it evaluates a state, the stronger the chosen move will be.
- **Choose Ghost Action:** After get all legal ghosts combined moves, those combinations are evaluated and the one that minimize the outcome is chosen.

The minimax algorithm performs a complete depth-first exploration of the game tree. If the maximum depth of the tree is  $m$  and there are  $b$  legal moves at each point, the the time complexity of the minimax algorithm is  $\Theta(b^m)$ . This is obviously infeasible for Pacman game, when  $b$  can be around 3, and  $m$  is very large. That is the reason why we need **Evaluate** method, instead of **Utility** method which only access the terminal state. The **depth** argument is used to limit the search space, that means, whenever the method reaches a terminal state or a state having the depth bound, it return a value.

## 2.2 Alphabeta Pruning

Alphabeta pruning is an enhanced version of Minimax algorithm in term of complexity. Therefore, AlphaBetaAgent class inherits almost all methods from MinimaxAgen class, except for the **Evaluation** method whose prototype is:

```
1 double Evaluate(const State &state, int depth, int player, double alpha, double beta);
```

- Alpha is the highest value we have found so far at any choice point along the path for MAX.
- Beta is the lowest value we have found so far at any choise point along the path for MIN.

Alphabeta pruning algorithm produces the same results as Minimax does, but its complexity is  $\Theta(b^{\frac{m}{2}})$ , which is far better.

## 2.3 Evaluation Function

Evaluation function is the one that decides Minimax or Alphabeta pruning algorithms' efficiency. Serveral features that I have tested are:

- + Pacman to ghosts Manhanttan distances: Ghosts want to minimize this distances
- - Ghosts to ghosts Manhattan distances: Ghosts should not be too far and too close to each other. If they are separated, they will not be able to combine to kill Pacman. If they are too close, they become one Ghost and which is an advantage for Pacman.
- + Pacman to ghosts graph distances:
- - Ghosts to ghosts graph distances  
+ means the bigger the better for MAX, while - means the smaller the better for MIN

At first, I used Manhattan distances as features and quickly recognized that they are not suitable for Pacman game because not every grids pair is connected. Therefore, I chose the latter two, which are the real distances between two grids. In order to do this, I used A\* algorithm to calculate all the shortest between all possible pairs of grids in advanced. The interesting point is I was able to utilize the same Gsearch class I wrote for 8-15 puzzle in previous report. It emphasizes the reusability of my code. Many references suggest that the evaluating result should be a linear combination of features. However, by doing so, we also ignore all dependency among features. That is not a good idea. Finally, I came up with the following evaluation functions:

$$v = c_1 * f_1 + c_2 * f_2 + c_3 * f_1 * f_2$$

In which,  $f_1$  is the total distance between Pacman and the two ghosts, and  $f_2$  is the distance between two ghosts. Very few features here, but it turns out to be very powerful. The effect of this function will be discussed in the next section.

The actual implementation looks like this:

```

1  if(features[0] <=6 && features[1]==1){
2      value += 100;
3  }
4  if(features[1] == 0)
5      value += 100;
6  value += coeff[0]*features[0] + coeff[1]*features[1]+coeff[2]*features[0]*features[1];

```

You can see there are two if clauses here. Because when Pacman is very close to Ghosts, the ghosts do not want to be next to each other. If they do so, they can not attack Pacman from different directions. Moreover, the two ghosts should never overlap each other. Therefore in those cases, I added an quite heavy weight to evaluation function.

## 3 Experiments

### 3.1 Execution

Please visit <https://www.youtube.com/watch?v=9TLatwHJ27E> to see numerous experiments I have done to test the algorithm with graphics user interface. I also ask some of my friends to play Pacman role, and they all lost to the Ghosts. Please give it a try if you have time.

An example of running my application in command line. Press 'r' to reset the game.

`./main algorithm depth  $c_1$   $c_2$   $c_3$`

	algorithm	depth	$c_1$	$c_2$	$c_3$
description	minimax or alphabeta	depth bound	1st coeff	2nd coeff	3rd coeff
default	a	12	10	-5	5

```

@:~/Dropbox/git/Pacman$ make
g++ -Wall -g -O2 -c -o state.o state.cpp
g++ -Wall -g -O2 -c -o common.o common.cpp
g++ -Wall -g -O2 -c -o minimaxAgent.o minimaxAgent.cpp
g++ -Wall -g -O2 -c -o utility.o utility.cpp
g++ -Wall -g -O2 -c -o alphabetaAgent.o alphabetaAgent.cpp
g++ -Wall -g -O2 -c -o main.o main.cpp
g++ -Wall -g -O2 -o main state.o common.o minimaxAgent.o utility.o alphabetaAgent.o
@:~/Dropbox/git/Pacman$ ./main a 12 10 -5 5
XXXXXXXXXXXXXXXXXXXXX
X----X---GG---X---X
X-XX-X-XXXXXX-X-XX-X

```

```

X-X-----X-X
X-X-XX-XX  XX-XX-X-X
X-----X    X-----X
X-X-XX-XXXXXX-XX-X-X
X-X-----X-X
X-XX-X-XXXXXX-X-XX-X
X----X---P----X----X
XXXXXXXXXXXXXXXXXXXX
Number of food left: 100

```

```

Number of Evaluate: 10247
Minvalue: 250
Ghost Minimax Move: (L, R, )
XXXXXXXXXXXXXXXXXXXX
X----X--G--G--X----X
X-XX-X-XXXXXX-X-XX-X
X-X-----X-X
X-X-XX-XX  XX-XX-X-X
X-----X    X-----X
X-X-XX-XXXXXX-XX-X-X
X-X-----X-X
X-XX-X-XXXXXX-X-XX-X
X----X----P---X----X
XXXXXXXXXXXXXXXXXXXX
Number of food left: 99

```

.....

```

Number of Evaluate: 1817
Minvalue: 140
Ghost Minimax Move: (L, L, )
XXXXXXXXXXXXXXXXXXXX
X----X-----X----X
X-XX-X-XXXXXX-X-XX-X
X-X----G-----X-X
X-X-XX-XX  XX-XX-X-X
X-----X    X-----X
X-X-XXPXXXXXX-XX-X-X
X-X---  G      ---X-X
X-XX-X-XXXXXX X-XX-X
X----X----  X----X
XXXXXXXXXXXXXXXXXXXX
Number of food left: 86

```

```

Number of Evaluate: 1499
Minvalue: 70
Ghost Minimax Move: (L, L, )
XXXXXXXXXXXXXXXXXXXX
X----X-----X----X
X-XX-X-XXXXXX-X-XX-X
X-X---G-----X-X
X-X-XX-XX  XX-XX-X-X
X-----PX    X-----X
X-X-XX XXXXXX-XX-X-X
X-X---  G      ---X-X

```

```

X-XX-X-XXXXXX X-XX-X
X----X---- X----X
XXXXXXXXXXXXXXXXXXXX
Number of food left: 85

```

```

Number of Evaluate: 2266
Minvalue: -1e+06
Ghost Minimax Move: (D, L, )
Pacman: LOSE

```

### 3.2 Minimax vs Alphabeta Pruning

The following table shows some comparison between Minimax and Alphabeta Pruning in term of number of evaluated nodes. The depth here is 12

Pacman Move	Ghost Moves	Minimax	Alphabeta Pruning
r	l,r	5824	1936
r	l,r	5299	1554
r	l,r	10514	1478
r	d,d	22021	2182
u	d,d	61080	1855
u	r,d	286179	20064
r	r,d	49025	1119
r	r,d	109956	3288
r	r,d	66916	5059
u	r,r	66804	9269
u	r,r	17848	2193
l	r,r	13621	1660
l	d,u	17056	1673

Clearly Alphabeta pruning is much more efficient than Minimax.

## 4 Discussion

Firstly, I want to talk about the Evaluation function. As mentioned above, this function is the most important aspect of Minimax and Alphabeta pruning algorithm. In a limited time, I think I considered a very simple version of it. In order to optimize the Evaluation function, we can add more features to it, and try to combine features in more sophisticated way such as Neural Network. I think it is possible to combine Neural Network and Genetic Algorithm to find the optimal evaluation function to this problem. That is maybe the theme for my next report.

Secondly, Alphabeta pruning is much more efficient than Minimax algorithm. In real applications, probably minimax will never be used. The game now is a deterministic one, however, if uncertainty is taken into account, we have another algorithm called Expectimax. In this case, opponents do not always take their best moves, they sometimes take other moves which produce different outcomes.

This is currently the most interesting report I have done so far. AI ghosts look very cool. I think the current version makes ghosts quite strong opponents for Pacman, still, it has flaws. I will continue developing the project even after submitting this report. My next target will be making a strong AI version of Pacman.

## References

- [1] Stuart Russell, Peter Norvig *Artificial Intelligence A Modern Approach*, Prentice Hall 3rd Edition, December 2009

- [2] George F. Luger *Artificial Intelligence, Structure and Strategies for Complex Problem Solving*, Addison Wesley Longman 3rd Edition, 2009
- [3] Robert Sedgewick, Kevein Wayne *Algorithms* Addison Wesley 4th Edition, January, 2012