Assessing Covid-19 Situation in Vietnam Using a Data-Driven Epidemiological Compartmental Model

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Outline

- Introduction
- 2 Literature review
- Methodologies
- 4 Results
- Discussion
- **6** Conclusion

Outline for Introduction

Introduction

The Covid-19 disease

- Health impacts
 - 230 million global infections
 - 4.7 million global deaths

The Covid-19 disease

- Health impacts
 - 230 million global infections
 - 4.7 million global deaths
- Economic impacts
 - Delayed shipments
 - Increased transaction cost

Why do we need a Covid-19 model?

 Lack of research on the impacts of Non-Pharmaceutical Intervention (NPI) in Vietnam

Why do we need a Covid-19 model?

- Lack of research on the impacts of Non-Pharmaceutical Intervention (NPI) in Vietnam
- Need of a simple tool for assessing the disease current and future progression

Goals

• A model that works with the data availability in Vietnam

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- An explainable model that can be used by experts

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- A model that works with the data availability in Vietnam
- An explainable model that can be used by experts
- Assess the effectiveness of mobility data in predicting future cases

Outline for Literature review

- 2 Literature review
 - Related works
 - Artificial neural networks

Mathematical models: Compartmental

Susceptible-Exposed-Infective-Removed (SEIR) model [1]

$$S' = -\beta(N)SI$$

$$E' = \beta(N)SI - \kappa E$$

$$I' = \kappa E - \alpha I$$

$$R' = f\alpha I$$

$$N' = -(1 - f)\alpha I$$

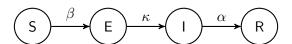


Figure: States graph for the SEIR model

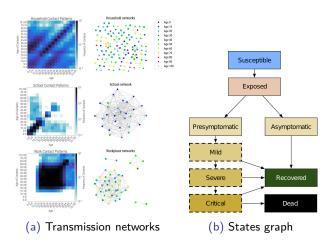


Figure: Covasim model [2]

Mathematical models: Pros & cons

Pros

- Explainable
- Based on many years of research
- Easy to understand and implement

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- Explainable
- Based on many years of research
- Easy to understand and implement

Cons

- Low representational capabilities
- The represented dynamics are stationary
- Unrealistic assumptions about real-world scenarios

Data-driven models

Autoregressive Integrated Moving Average (ARIMA) models
 [3]–[5]

Data-driven models

- Autoregressive Integrated Moving Average (ARIMA) models
 [3]–[5]
- Explainable Artificial Neural Network (ANN) encoder [6]

Data-driven models

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- Explainable Artificial Neural Network (ANN) encoder [6]
- Recurrent Neural Network (RNN) [7], [8]
 - Long Short Term Memory (LSTM)
 - Bidirectional Long Short Term Memory (Bi-LSTM)
 - Gated Recurrent Unit (GRU)

Data-driven models: Pros & cons

Pros

- High prediction accuracy
- Allow for modeling without needing domain knowledge

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- High prediction accuracy
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Cons

- Unexplainable
- Relied on large amount of data
- Inability to capture the true disease dynamics

Novel compartmental models: Using mobility data

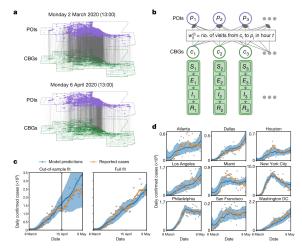


Figure: SEIR model informed with mobility data [9]

Novel compartmental models: Using neural networks

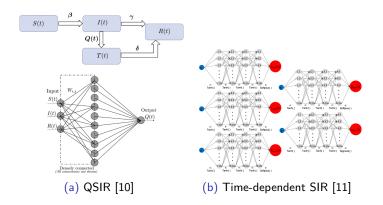


Figure: Predict the parameters of compartmental models with Artificial Neural Networks (ANNs)

Artificial neural networks

Multi-layer perceptron: Graph representation

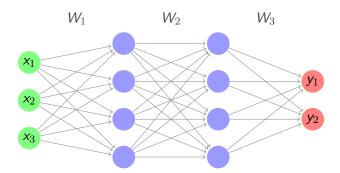


Figure: A Multi-Layer Perceptron (MLP) with four layers

Artificial neural networks

Multi-layer perceptron: Mathematical representation

Definition

$$g(X) = \phi_n(W_n\phi_{n-1}(\cdots(W_2\phi_1(W_1X + b_1) + b_2) + \cdots) + b_n)$$

Multi-layer perceptron: Mathematical representation

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Theorem

Given appropriate weights, ANNs can approximate any arbitrary function $f: \mathbb{R}^M \to \mathbb{R}^N$ [12]–[14]

Artificial neural networks

Training neural networks: Back-propagation

Mean Squared Error (MSE)

$$\mathcal{L} = \frac{1}{N} \sum_{i=1}^{N} (g(X_i) - Y_i)^2$$

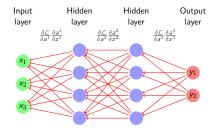


Figure: Graph representation of the back-propagation algorithm

Artificial neural networks

Physics-informed neural networks

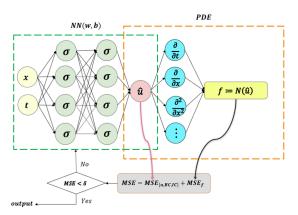


Figure: The schematic of Physics-Informed Neural Networks (PINNs) for solving Partial Differential Equations (PDEs) [15].

Neural ordinary differential equations: Idea

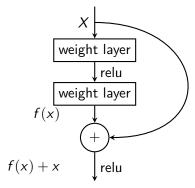
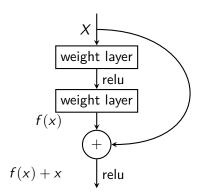


Figure: Skip connection

Neural ordinary differential equations: Idea



Observation

$$h_{t+1} = h_t + f(h_t, \theta_t)$$

$$\Leftrightarrow \frac{dh(t)}{dt} = f(h(t), t, \theta)$$

Figure: Skip connection

$$z(t_1) = z(t_0) + \int_{t_0}^{t_1} f(z(t), t, \theta) dt$$

Neural Ordinary Differential Equation (NeuralODE) output

$$z(t_1) = z(t_0) + \int_{t_0}^{t_1} f(z(t), t, \theta) dt$$

Memory efficiency

$$z(t_1) = z(t_0) + \int_{t_0}^{t_1} f(z(t), t, \theta) dt$$

- Memory efficiency
- Adaptive computation

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- Memory efficiency
- Adaptive computation
- Scalable and invertible normalizing flows
- Continuous time series models

Artificial neural networks

Neural ordinary differential equations: Outputs

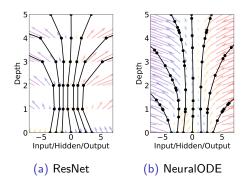


Figure: Comparison between ResNet's discrete state transformations and Neural Ordinary Differential Equation (NeuralODE) continuous state transformations

Neural ordinary differential equations: Gradients

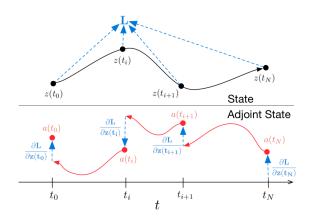


Figure: Reverse-mode differentiation of an Ordinary Differential Equation (ODE) solution. [16]

Outline for Methodologies

- Methodologies
 - Model definition
 - Datasets
 - Parameters estimation
 - Experiments

Universal differential equation

Universal Differential Equation (UDE) [17] is a neural network architecture based on NeuralODE

Definition

$$u' = f(u, t, U_{\theta}(u, t))$$

Definition

$$S' = -\frac{\beta(t)SI}{N}$$

$$E' = \frac{\beta(t)SI}{N} - \gamma E$$

$$I' = \gamma E - \lambda I$$

$$R' = (1 - \alpha(t)) * \lambda * I$$

$$D' = \alpha(t) * \lambda * I$$

$$N' = -\alpha * \lambda * I$$

$$C' = -C + \gamma * E$$

$$T' = \gamma * E$$

System parameters

Box constraints for time-independent parameters

$$\gamma = \gamma_L + (\gamma_U - \gamma_L) * \sigma(\gamma')$$
$$\lambda = \lambda_L + (\lambda_U - \lambda_L) * \sigma(\lambda')$$

System parameters

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Neural networks for time-dependent parameters

$$\begin{split} \beta(t) &= \mathcal{NN}_{\theta_1}(\mathcal{F}) \\ \alpha(t) &= \mathcal{NN}_{\theta_2}(\frac{t}{t_{\text{max}}}, \frac{\textit{I}(t-1)}{\textit{N}(t-1)}, \frac{\textit{R}(t-1)}{\textit{N}(t-1)}, \frac{\textit{D}(t-1)}{\textit{N}(t-1)}) \end{split}$$

- Hidden layers activation: mish [18]
- Output layer activation $\nu_i = \nu_{i,L} + (\nu_{i,U} \nu_{i,L}) * \sigma(z_i)$

Neural network input features

1st. set of input features

$$\mathcal{F}_1(t) = \left\{ \frac{t}{t_{\mathsf{max}}}, \frac{S(t-1)}{\textit{N}(t-1)}, \frac{\textit{E}(t-1)}{\textit{N}(t-1)}, \frac{\textit{I}(t-1)}{\textit{N}(t-1)} \right\}$$

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2nd. set of input features

$$\mathcal{F}_2(t) = \mathcal{F}_1(t) \cup \{\mathsf{MovementRange}(t)\}$$

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2nd. set of input features

$$\mathcal{F}_2(t) = \mathcal{F}_1(t) \cup \{\mathsf{MovementRange}(t)\}$$

3rd. set of input features

$$\mathcal{F}_3(t) = \mathcal{F}_2(t) \cup \{ SocialProximityToCases(t) \}$$

Covid-19 cases time series

Datasets

date	infective	confirmed	recoveries	deaths
1/22/20	0	0	0	0
1/23/20	2	2	0	0
1/24/20	2	2	0	0

Table: Structure of the processed Covid-19 time series datasets

- John Hopkins University (JHU) Covid-19 public datasets
- VNExpress Covid-19 public dashboard
- VnCDC Covid-19 public dashboard



VNM

. . .

2021-01-03

ds country polygon rel. change stay put ratio 2021-01-01 VNM VNM.1.10 1 0.125 0.270 2021-01-02 VNM VNM.1.10 1 0.052 0.259

0.185

. . .

Table: Structure of Facebook's Movement Range Maps (MRMs) dataset.

VNM.1.10 1

0.269

. . .

Datasets

Facebook's social connectedness index

Social Connectedness Index (SCI)

$$SCI_{i,j} = \frac{FB \text{ connections}_{i,j}}{FB \text{ users}_i * FB \text{ users}_j},$$

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Social Proximity to Cases (SPC) index [19]

$$\mathsf{SPC}_{i,t} = \sum_{j}^{C} \mathsf{Cases} \ \mathsf{per} \ \mathsf{10k}_{j,t} \frac{\mathsf{SCI}_{i,j}}{\sum_{h}^{C} \mathsf{SCI}_{i,h}},$$

Datasets

Population data

ID_1	NAME_1	AVGPOPULATION	
3	Ha Noi	8.2466e6	
62	Vinh Phuc	1.1712e6	
		• • •	
1001.0	Autauga, Alabama, US	55869	
1003.0	Baldwin, Alabama, US	223234	
		• • •	

Table: Structure of the processed average population datasets

.

- Vietnam General Statistics Office (GSO)
- JHU Covid-19 datasets



Loss function

Regularized MSE with scaled outputs

$$\mathcal{L}(\hat{y}, y) = \frac{1}{T} \sum_{i=1}^{N} \sum_{t=0}^{T-1} \left[e^{\zeta t} \left(\frac{\hat{y}_{i,t} - y_{i,t}}{\max(y_i) - \min(y_i)} \right)^2 \right] + \frac{\lambda}{2T} (\|\theta_1\|_2^2 + \|\theta_2\|_2^2)$$

Parameters estimation

Training process

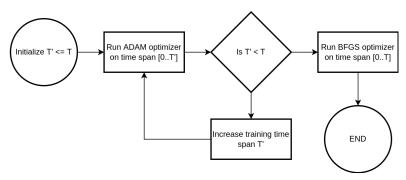


Figure: Model training procedure

Jaca preprocessing

- Applied 7-day moving average to all datasets
- Applied min-max scaling on the Movement Range Map (MRM) dataset and Social Proximity to Cases (SPC) index

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- Training period: 48 days
 - Vietnam: First date when the total confirmed cases passed 500
 - United States: 1st July 2021

Data preprocessing

- Applied 7-day moving average to all datasets
- Applied min-max scaling on the Movement Range Map (MRM) dataset and Social Proximity to Cases (SPC) index
- Training period: 48 days
 - Vietnam: First date when the total confirmed cases passed 500
 - United States: 1st July 2021
- Testing period: 28 days

Experiments

Differential equation solver configurations

- Tsit5 solver (Tsitouras Runge-Kutta 5/4 method [20])
- InterpolatingAdjoint technique for approximating gradients in NeuralODE [21]

Experiments

Optimizer configurations

- Initial time span of 4 days
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 - Learning rate 0.05
 - decay rate 0.5
 - decay step 1000
 - decay limit 0.00001
 - 1000 iterations on each time span

Optimizer configurations

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- Time weighting parameter $\zeta = -0.001$
- ADAM optimizer
 - Learning rate 0.05
 - decay rate 0.5
 - decay step 1000
 - decay limit 0.00001
 - 1000 iterations on each time span
- BFGS optimizer
 - Initial stepnorm 0.01
 - 1000 iterations on the full time span



Initial conditions

Location	S (0)	E(0)	I (0)	R(0)
Vietnam	9.75e7	25	5	2817
Ho Chi Minh city	9.22e6	173.5	34.7	360.1
Binh Duong	2.58e6	206.4	41.2	314.7
Dong Nai	3.17e6	295	59	194.8
Long An	1.71e6	217.8	43.5	300.5
United States	2.99e8	71890	14378	3.31e7
Los Angeles, California	8.78e6	2500	500	1.22e6
Cook, Illinois	4.59e6	615	123	546508
Harris, Texas	4.30e6	930	186	396430
Maricopa, Arizona	3.92e6	1325	265	549899

Table: Initial conditions for the system of ODEs

Initial parameters

Parameter	Value	Lower bound	Upper bound
β	N/A	0.05	1.67
γ	1/4	1/4	1/4
λ	1/14	1/14	1/14
α	N/A	0.005	0.05
θ_1	glorot_normal	N/A	N/A
θ_2	glorot_normal	N/A	N/A

Table: Initial parameters for the system of ODEs

Outline for Results

- 4 Results
 - Model's outputs for Vietnam and the United States
 - Model's outputs for counties in the United States
 - Model's outputs for provinces in Vietnam

Forecasts: Country-level data

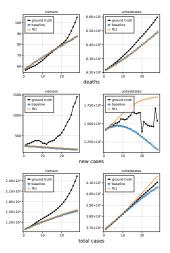


Figure: Forecasts made by different versions of the model

Model's outputs for Vietnam and the United States

R_0 and fatality rate: Country-level data

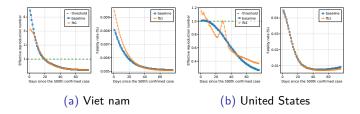


Figure: Disease metrics learned by different versions of the model

Forecasts: Counties in the United States

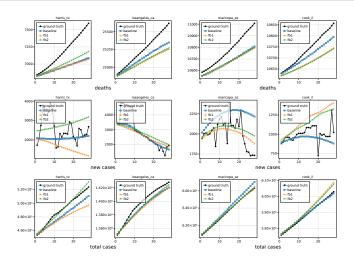


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R_0 and fatality rate: Counties in the United States

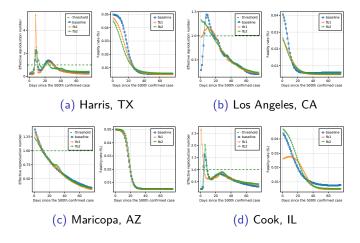


Figure: Disease metrics learned by different versions of the model



Forecasts: Provinces in Vietnam

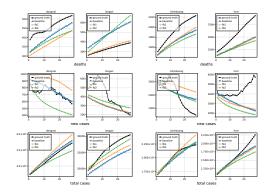


Figure: Forecasts made by different versions of the model

R_0 and fatality rate: Provinces in Vietnam

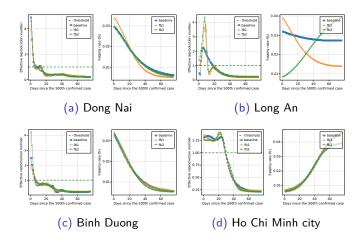


Figure: Disease metrics learned by different versions of the model



Outline for Discussion

- Discussion
 - Model's convergence and generalizability
 - Model's limitations

About the results

Could capture the disease trends with high accuracy

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- Could capture the disease trends with high accuracy
- Accuracy get lower as we extrapolated further into the future
- Bad fit and low forecast accuracy when applied to data with high fluctuation
- No improvement in the forecast accuracy when mobility data was incorporated

Model's convergence and generalizability

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 - ODEs stiffness
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- The model could get stuck in bad local minima, due to
 - ODEs stiffness
 - High frequency changes
- The model was separately trained at each location and only capable of making forecast for the location that it was trained with
- Forecast can only be made for a short period after the training period

Model's limitations

• Issues with ground truth data

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- Inability to capture rapid trend changes

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- Inability to capture rapid trend changes
- Bad local minima
- Compartmental model bias
- Covariates bias
- Inability to capture real dynamics of the disease
- Neural network interpretability

Outline for Conclusion

6 Conclusion

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• Collect and process Covid-19 related data for various locations



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- Collect and process Covid-19 related data for various locations
- Implement a model an explainable Covid-19 model using UDE
 - Progression of all compartments can be given by the model
 - Metric about the disease, e.g. \mathcal{R}_0 , can be derived

Goals: An explainable Covid-19 model that can work with the low data availability in Vietnam

- Collect and process Covid-19 related data for various locations
- Implement a model an explainable Covid-19 model using UDE
 - Progression of all compartments can be given by the model
 - Metric about the disease, e.g. \mathcal{R}_0 , can be derived
- Add mobility data to the model and show that ineffectiveness of the approach

 Increase the model complexity with additional compartments and parameters

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- Increase the model complexity with additional compartments and parameters
- Include additional time-varying covariates
- Implement better methods and algorithms for training UDE
- Use methods such as SINDy to find a governing equation and improve the model interpretability

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