CSSS 569 Visualizing Data and Models

Lab 7: Visualizing Network/Relational Data

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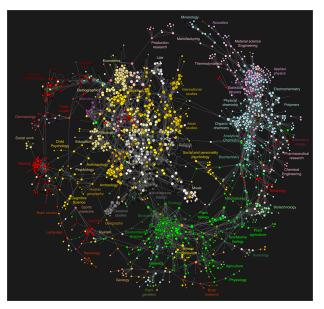
December 29, 2021

Prerequisite

▶ The following packages are required for this lab:

```
packages <- c("tidygraph", "ggraph", "reshape2", "cluster", "circlize")
install.packages(packages)</pre>
```

▶ Map of sciences (Bollen et al. 2009)



▶ Network data create many challenges for visualization

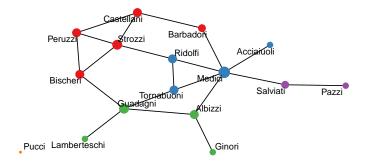
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 - Cursed by high dimensionality

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- Network data create many challenges for visualization
 - Cursed by high dimensionality
 - ▶ Network diagrams usually result in hairballs or spaghetti balls. . .
 - ► The main takeaway of this lab is actually to seek alternative visualization methods whenever possible

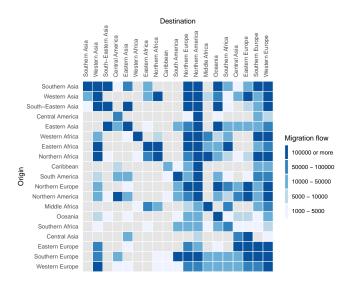
Examples in today's lab

▶ Florentine families and the rise of Medici: network diagram



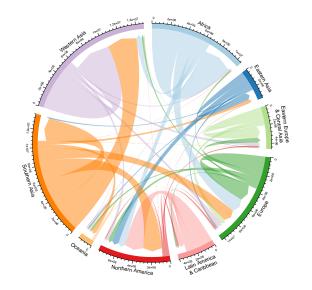
Examples in today's lab

- Global migration data: heat map
 - ▶ Additional tricks: making NAs explicit; cluster analysis



Examples in today's lab

► Global migration data: chord diagram



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 - More specifically, any data whose unit of observation is dyadic

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- ▶ In this lab, I want you to think more generically about relational data
 - More specifically, any data whose unit of observation is dyadic
 - Examples: Migration flow data, or import/export data, between countries...

► Two basic elements:

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 - Nodes (or vertices)

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 - Links (or edges)

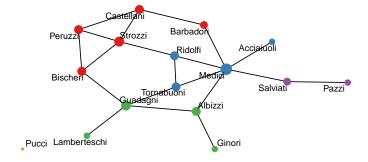
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- ► Two ways to represent relational data:
 - Matrix (or adjacency matrix)
 - Long data frame(or edge list)
- Example with the marriage network of Florentine families

Marriage ties between Florentine familes in early 15th century
 From Padget & Ansell (1993)



► Represent relational data with matrix (or adjacency matrix)

| ## | | Acciaiuoli | Albizzi | Barbadori | Bischeri | ${\tt Castellani}$ | Ginori | Guadagni |
|----|--------------|------------|---------|-----------|----------|--------------------|--------|----------|
| ## | Acciaiuoli | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| ## | Albizzi | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| ## | Barbadori | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| ## | Bischeri | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| ## | Castellani | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| ## | Ginori | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| ## | Guadagni | 0 | 1 | 0 | 1 | 0 | 0 | 0 |
| ## | Lamberteschi | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| ## | Medici | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| ## | Pazzi | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| ## | Peruzzi | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| ## | Pucci | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| ## | Ridolfi | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| ## | Salviati | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| ## | Strozzi | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| ## | Tornabuoni | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

Represent relational data with long data frame(or edge list)

```
[,1]
                      [,2]
    [1,] "Acciaiuoli" "Medici"
    [2,] "Albizzi"
                      "Ginori"
## [3,] "Albizzi"
                     "Guadagni"
  [4,] "Albizzi"
                      "Medici"
## [5,] "Barbadori" "Castellani"
## [6.] "Barbadori"
                     "Medici"
  [7.] "Bischeri"
                      "Guadagni"
## [8,] "Bischeri"
                      "Peruzzi"
   [9.] "Bischeri"
                      "Strozzi"
## [10,] "Castellani" "Peruzzi"
## [11,] "Castellani" "Strozzi"
## [12.] "Guadagni"
                      "Lamberteschi"
## [13.] "Guadagni"
                      "Tornabuoni"
## [14,] "Medici"
                      "Ridolfi"
## [15.] "Medici"
                      "Salviati"
## [16.] "Medici"
                      "Tornabuoni"
## [17,] "Pazzi"
                      "Salviati"
## [18,] "Peruzzi"
                      "Strozzi"
## [19.] "Ridolfi"
                      "Strozzi"
## [20,] "Ridolfi"
                      "Tornabuoni"
```

```
# install.packages(c("tidygraph", "ggraph"))
library(tidyverse)
library(tidygraph)
library(ggraph)

# Load data (from Chris's website::lab section)
medici <- read.table("data/medici.txt")
medici <- as.matrix(medici)</pre>
```

► First, we have to turn our matrix into a tidygraph object medici_graph <- as_tbl_graph(medici, directed = FALSE)

First, we have to turn our matrix into a tidygraph object

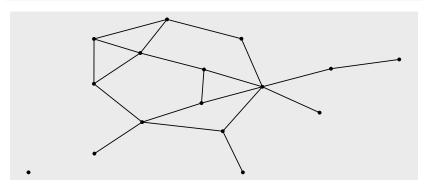
```
## # A tbl_graph: 16 nodes and 20 edges
## #
## # An undirected simple graph with 2 components
## #
## # Node Data: 16 x 1 (active)
##
    name
   <chr>
##
## 1 Acciaiuoli
## 2 Albizzi
## 3 Barbadori
## 4 Bischeri
## 5 Castellani
## 6 Ginori
## # ... with 10 more rows
## #
## # Edge Data: 20 x 3
##
     from to weight
    <int> <int> <dbl>
##
    1
## 1
## 2 2 6
## 3 2
## # ... with 17 more rows
```

Visualize network data using ggraph package

```
ggraph(medici_graph) +
  geom_node_point()
```

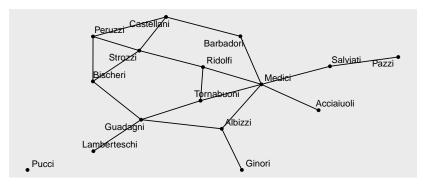
Visualize network data using ggraph package

```
ggraph(medici_graph) +
geom_node_point() +
geom_edge_link()
```



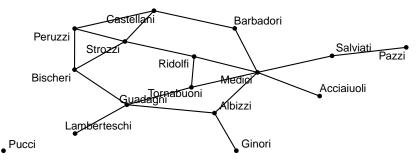
Visualize network data using ggraph package

```
ggraph(medici_graph) +
  geom_node_point() +
  geom_edge_link() +
  geom_node_text(aes(label = name), repel = TRUE)
```



Visualize network data using ggraph package

```
ggraph(medici_graph) +
  geom_node_point() +
  geom_edge_link() +
  geom_node_text(aes(label = name), repel = TRUE) +
  theme_graph()
```



Create new network measures using tidygraph

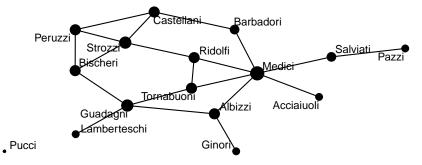
```
medici_graph <-
  medici_graph %>%
mutate(
    # Calculate degree centrality
  degree = centrality_degree(),
    # Implement community_detection algorithm
    community = group_edge_betweenness()
)
```

Create new network measures using tidygraph

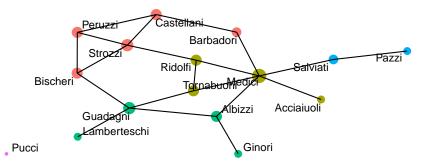
```
## # A tbl_graph: 16 nodes and 20 edges
## #
## # An undirected simple graph with 2 components
## #
## # Node Data: 16 x 3 (active)
##
    name degree community
  <chr> <dbl>
                       <int>
##
## 1 Acciaiuoli
## 2 Albizzi
## 3 Barbadori
## 4 Bischeri
## 5 Castellani
## 6 Ginori
## # ... with 10 more rows
## #
## # Edge Data: 20 x 3
##
     from to weight
##
    <int> <int> <dbl>
## 1
    1
## 2 2 6
## 3 2
## # ... with 17 more rows
```

Incorporate new network measures into our visualization

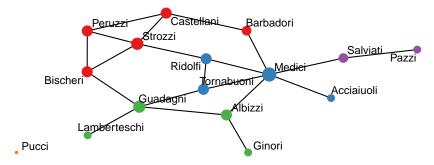
```
ggraph(medici_graph) +
  geom_node_point(aes(size = degree), show.legend = FALSE) +
  geom_edge_link() +
  geom_node_text(aes(label = name), repel = TRUE) +
  theme_graph()
```



Incorporate new network measures into our visualization



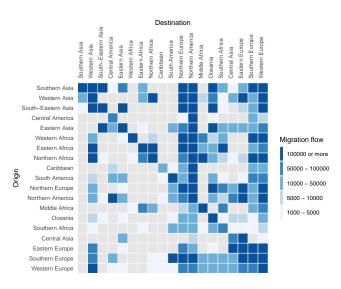
Incorporate new network measures into our visualization



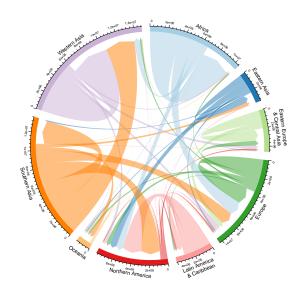
► Save the output

```
width = 7
ggsave("output/medici.pdf", width = width, height = width/2)
```

► Heat map



► Chord diagram



Original data are from Abel (2018)

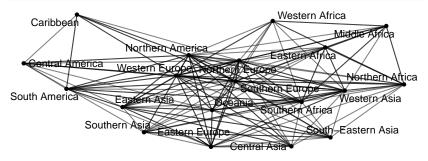
```
migrat2010 <- read_csv("data/migrat2010.csv")
head(migrat2010)</pre>
```

```
## # A tibble: 6 x 3
    origRegion destRegion
##
                                  flow
##
    <chr>
               <chr>>
                                 <dbl>
  1 Caribbean Caribbean
                                 40506
## 2 Caribbean Central America
                                  8183
## 3 Caribbean Northern America 533052
                                 15584
## 4 Caribbean Northern Europe
## 5 Caribbean
               South America
                                   3264
## 6 Caribbean Southern Europe
                                 21711
```

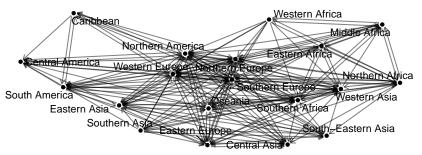
Network diagram doesn't work well here...

```
migrat2010_graph <- as_tbl_graph(migrat2010)

ggraph(migrat2010_graph)+
  geom_edge_link(alpha = 0.5) +
  geom_node_point() +
  geom_node_text(aes(label = name), repel = TRUE) +
  theme_graph()</pre>
```



Worse still, the data is actually bidirectional, which means you need to visualize two edges for each dyadic pair



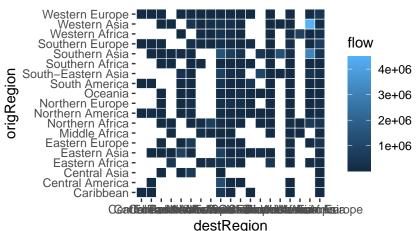
► Two alternative visualization methods:

- ► Two alternative visualization methods:
 - ► Heatmap

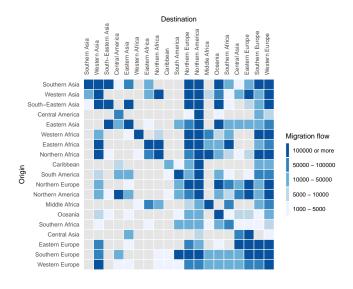
- ► Two alternative visualization methods:
 - Heatmap
 - Chord diagram

Like what we did in lab 4 using geom_tile()

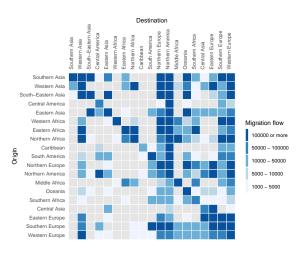
```
migrat2010 %>%
ggplot(aes(y = origRegion, x = destRegion, fill = flow)) +
geom_tile(color = "white", size = 0.2) +
coord_equal() +
theme(panel.background = element_blank())
```



- ► How can we improve the heat map?
 - ► Try to replicate the following example:



- ► Main tasks:
 - Make NA values explicit
 - Turn flow into a categorical variable
 - Cluster analysis and sorting



To make NA values explicit, use expand() and left_join() from tidyverse

```
migrat2010 %%
  expand(origRegion, destRegion) %>%
  head()
```

```
## # A tibble: 6 x 2
## origRegion destRegion
## <chr> <chr>
## 1 Caribbean Caribbean
## 2 Caribbean Central America
## 3 Caribbean Central Asia
## 4 Caribbean Eastern Africa
## 5 Caribbean Eastern Asia
## 6 Caribbean Eastern Europe
```

- To make NA values explicit, use expand() and left_join() from tidyverse
 - expand() creates all unique combinations of two (or more) variables

```
migrat2010 %>%
  expand(origRegion, destRegion) %>%
  head()
```

```
## # A tibble: 6 x 2
## origRegion destRegion

**chr> <chr>
## 1 Caribbean Caribbean

## 2 Caribbean Central America

## 3 Caribbean Eastern Africa

## 5 Caribbean Eastern Asia

## 6 Caribbean Eastern Europe
```

To make NA values explicit, use expand() and left_join() from tidyverse

```
migrat2010 <-
 migrat2010 %>%
 expand(origRegion, destRegion) %>%
 left_join(migrat2010, by = c("origRegion", "destRegion"))
head(migrat2010)
## # A tibble: 6 x 3
    origRegion destRegion
                                flow
##
    <chr>
            <chr>
                               <dbl>
##
## 1 Caribbean Caribbean
                            40506
## 2 Caribbean Central America 8183
## 3 Caribbean Central Asia
                                  NΑ
## 4 Caribbean Eastern Africa
                                 NA
## 5 Caribbean Eastern Asia
                                 NA
```

NΑ

6 Caribbean Eastern Europe

- To make NA values explicit, use expand() and left_join() from tidyverse
 - Use the result from expand() as a template for left_join()

```
migrat2010 <-
  migrat2010 %>%
  expand(origRegion, destRegion) %>%
  left_join(migrat2010, by = c("origRegion", "destRegion"))
head(migrat2010)
```

```
## # A tibble: 6 x 3
    origRegion destRegion
                               flow
##
    <chr> <chr>
                              <dbl>
##
## 1 Caribbean Caribbean
                           40506
## 2 Caribbean Central America 8183
## 3 Caribbean Central Asia
                                NΑ
## 4 Caribbean Eastern Africa
                                NA
## 5 Caribbean Eastern Asia
                                NA
## 6 Caribbean Eastern Europe
                                NΑ
```

Turn flow into a categorical variable

```
quantile(migrat2010$flow, na.rm = TRUE)
          0%
                    25%
                               50%
                                         75%
                                                   100%
##
##
     1058.00 9147.75 36104.00 153035.50 4497527.00
# Create breaks and labels
breaks <- c(1000, 5000, 10000, 50000, 100000, Inf)
labels <- c("1000-5000", "5000-10000", "10000-50000",
           "50000-100000", ">100000")
# Create a new variable `flowCat`
migrat2010 <-
 migrat2010 %>%
 mutate(flowCat = cut(flow, breaks, labels))
```

Turn flow into a categorical variable

head(migrat2010)

```
## # A tibble: 6 x 4
    origRegion destRegion flow flowCat
##
##
    <chr>
              <chr>
                             <dbl> <fct>
## 1 Caribbean Caribbean
                             40506 10000-50000
## 2 Caribbean Central America 8183 5000-10000
## 3 Caribbean Central Asia
                                NA <NA>
## 4 Caribbean Eastern Africa
                                NA <NA>
## 5 Caribbean Eastern Asia
                                NA <NA>
## 6 Caribbean Eastern Europe
                                NA <NA>
```

Clustering analysis and sorting

```
# Load packages
library(reshape2)
library(cluster)

# Convert long data frame into a full matrix
migrat2010_matrix <-
migrat2010 %>%
reshape2::acast(origRegion ~ destRegion, value.var = "flow", fill = 0)
```

Clustering analysis and sorting

```
# Convert long data frame into a full matrix
print(migrat2010_matrix[1:4, 1:4])
```

| ## | | Caribbean | Central | America | Central | Asia | Eastern | Africa |
|----|-----------------|-----------|---------|---------|---------|-------|---------|--------|
| ## | Caribbean | 40506 | | 8183 | | 0 | | 0 |
| ## | Central America | 0 | | 99171 | | 0 | | 0 |
| ## | Central Asia | 0 | | 0 | 7 | 77252 | | 0 |
| ## | Eastern Africa | 0 | | 0 | | 0 | | 444352 |

Cluster analysis and sorting

```
migrat2010_hclust <-
  dist(migrat2010_matrix) %>%
  hclust(method = "ward.D") # Several other methods are available

countryOrder <- migrat2010_hclust$order
print(countryOrder)</pre>
```

```
## [1] 15 18 13 2 5 17 4 8 1 12 10 9 7 11 14 3 6 16 19
```

Clustering analysis and sorting

```
# Sort the countries using the order produced by cluster analysis
countryLevels <- row.names(migrat2010_matrix)[countryOrder]
print(countryLevels)</pre>
```

```
[1] "Southern Asia"
##
                              "Western Asia"
                                                    "South-Eastern Asia"
    [4] "Central America"
                                                    "Western Africa"
##
                              "Eastern Asia"
##
    [7] "Eastern Africa"
                              "Northern Africa"
                                                    "Caribbean"
   [10] "South America"
                              "Northern Europe"
                                                    "Northern America"
## [13] "Middle Africa"
                              "Oceania"
                                                    "Southern Africa"
## [16] "Central Asia"
                              "Eastern Europe"
                                                    "Southern Europe"
## [19] "Western Europe"
```

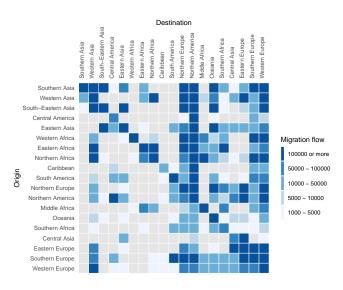
Clustering analysis and sorting

```
# Re-level `origRegion` and `destRegion` according to the level
migrat2010 <- migrat2010 %>%
  mutate(
    origRegion = factor(origRegion, levels = rev(countryLevels)),
    destRegion = factor(destRegion, levels = countryLevels)
)
```

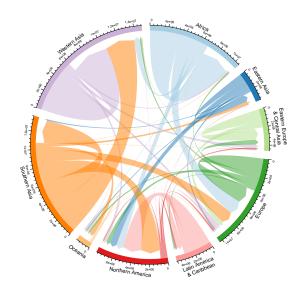
Visualize the heat map again:

```
migrat2010 %>%
 ggplot(aes(y = origRegion, x = destRegion, fill = flowCat)) +
 geom tile(color = "white", size = 0.2) +
  # Scale fill values with "Blues" palette and "grey90" for NAs
 scale_fill_brewer(palette = "Blues", na.value = "grey90",
                    breaks = rev(labels)) +
  # Put x-axis labels on top
 scale_x_discrete(position = "top") +
 coord equal() +
 theme(panel.background = element_blank(),
        axis.ticks.x = element blank(),
        axis.ticks.y = element_blank(),
        # Rotate and align x-axis labels
        axis.text.x.top = element_text(angle = 90, hjust = 0),
        legend.key.height = grid::unit(0.8, "cm"),
        legend.key.width = grid::unit(0.2, "cm")
 guides(fill = guide_legend(title = "Migration flow")) +
 labs(y = "Origin", x = "Destination")
```

▶ Visualize the heat map again:



► Chord diagram has become growingly popular



► We'll use the circlize package: full documentation here library(circlize)

▶ But first, we have to aggregate regions and further reduce the dimensionality

```
# Create vectors of countries to be aggregated
Europe <- c("Southern Europe", "Western Europe", "Northern Europe")
EECA <- c("Eastern Europe", "Central Asia")</pre>
Africa <- c("Eastern Africa", "Middle Africa", "Northern Africa",
            "Southern Africa", "Western Africa")
LACarib <- c("Central America", "South America", "Caribbean")
SAsia <- c("South-Eastern Asia", "Southern Asia")
# Use mutate() and across() to recode
# `origRegion` and `destRegion` simultaneously
migrat2010 <-
 migrat2010 %>%
 mutate(across(c(origRegion, destRegion),
                ~ case when(
                  .x %in% Europe ~ "Europe",
                  .x %in% EECA ~ "Eastern Europe \n& Central Asia",
                  .x %in% Africa ~ "Africa",
                  .x %in% LACarib ~ "Latin America \n& Caribbean",
                  .x %in% SAsia ~ "Southern Asia",
                  TRUE ~ as.character(.x)
```

▶ But first, we have to aggregate regions and further reduce the dimensionality

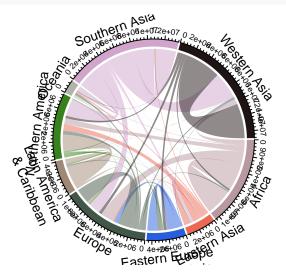
```
# Collapse (sum) flow values according by newly aggregated regions
migrat2010 <- migrat2010 %>%
group_by(origRegion, destRegion) %>%
summarize(flowTotal = sum(flow, na.rm = TRUE)) %>%
ungroup()
```

`summarise()` has grouped output by 'origRegion'. You can override using the head(migrat2010)

```
## # A tibble: 6 x 3
                                                  flowTotal
##
    origRegion destRegion
##
    <chr>
                <chr>>
                                                      <dbl>
## 1 Africa
               "Africa"
                                                    3412806
## 2 Africa
                "Eastern Asia"
                                                       1083
## 3 Africa
                "Eastern Europe \n& Central Asia"
                                                      14504
## 4 Africa
                "Europe"
                                                    1634143
                "Latin America \n& Caribbean"
                                                      10694
## 5 Africa
## 6 Africa
                "Northern America"
                                                     813775
```

Basic chord diagram

chordDiagram(migrat2010)



Advanced chord diagram settings (based on Abel's GitHub)

► Advanced chord diagram settings (based on Abel's GitHub)

```
# Get nice colors
colors <- RColorBrewer::brewer.pal(9, "Paired")</pre>
# More advanced settings in `chordDiagram()`
chordDiagram(migrat2010,
             # Set colors
             grid.col = colors,
             # Indicate chords are directional
             directional = 1,
             # Directionality is illustrated by arrows and height differences
             direction.type = c("arrows", "diffHeight"),
             # Set height difference
             diffHeight = -0.04,
             # Use big arrows
             link.arr.type = "big.arrow",
             # Sort the chords and plot the smallest chords first
             link.sort = TRUE, link.largest.ontop = TRUE,
# Save the output
dev.copy2pdf(file = "output/migratChord.pdf", height = 8, width = 8)
```

► Final output

