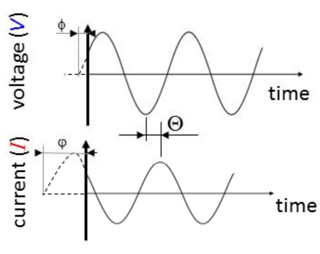
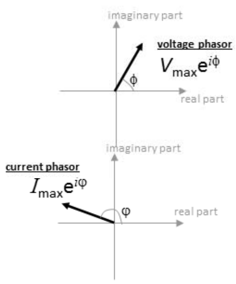
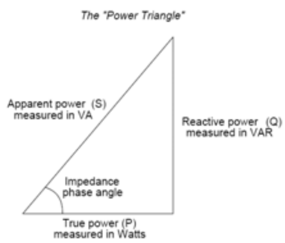
EEE 2015 ELECTRICS

(3ϕ)Three Phase Alternating Voltage and Current

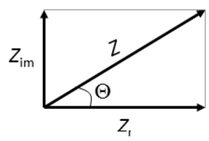
Monophase





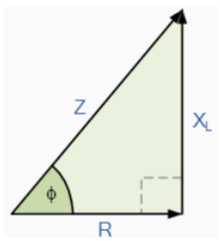


$$Z = \frac{V_{max}e^{i\phi}}{I_{max}e^{i\varphi}} = |Z|\,e^{i\Theta} = Z_r + i\cdot Z_{im}$$



P = true power $P = I^2R$ $P = \frac{E^2}{R}$

Measured in units of ***Watts***



$$Z^2 = R^2 + X_L^2$$

$$\cos\phi = \frac{R}{Z}$$

Q = reactive power $Q = I^2X$ $Q = \frac{E^2}{X}$

Measured in units of ***Volt-Amps-Reactive (VAR)***

S = apparent power $S = I^2Z$ $S = \frac{E^2}{Z}$ $S = IE$

Measured in units of ***Volt-Amps (VA)***

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Three phase

Three-phase electric power is a common method of alternating-current electric power generation, transmission, and distribution.

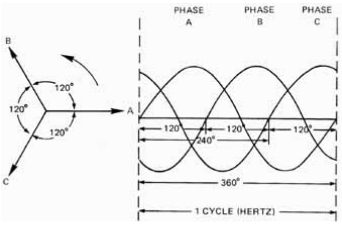
It is a type of polyphase system and is the most common method used by electrical grids worldwide to transfer power. It is also used to power large motors and other heavy loads.

A three-phase system is usually more economical than an equivalent single-phase or two-phase system at the same voltage because it uses less conductor material to transmit electrical power

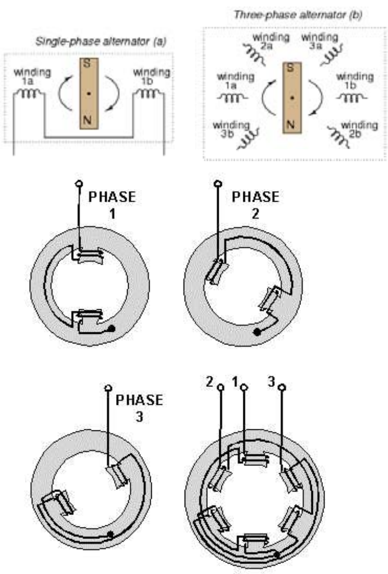
Definition

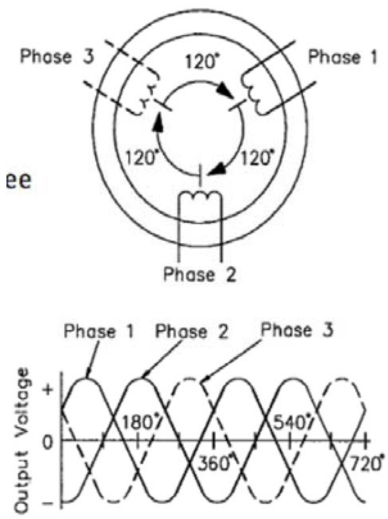
A three-phase (3ϕ) system is a combination of three single-phase systems. In a 3ϕ balanced system, power comes from a 3ϕ AC generator that produces three separate and equal voltages, each of which is 120° out of phase with the other voltages

A three-phase AC system consists of three-phase generators, transmission lines, and loads.

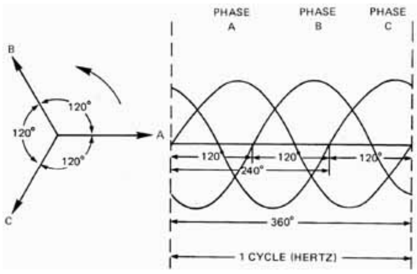


Three Phase Generation





Three Phase Waveform



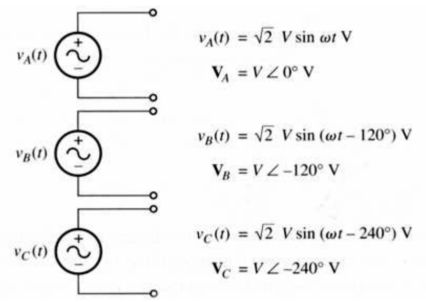
$V_{rms} = 220\ [V]$

$f = 50\ [Hz]$

$V_A(t) = 220\sqrt{2}\sin(2\pi 50\, t)$

$V_A(t) = 220\sqrt{2}\sin(2\pi 50\, t - 120°)$

$V_A(t) = 220\sqrt{2}\sin(2\pi 50\, t - 240°)$

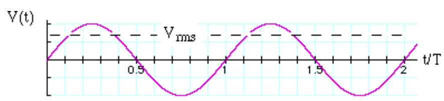


Three Phase Alternating Voltage and Current

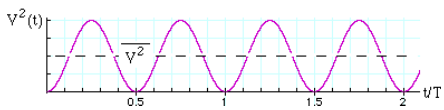
One Critical Advatage of Three Phase Waveform

Power delivered to a three-phase load is constant at all time, instead of pulsing as it does in a single-phase system.

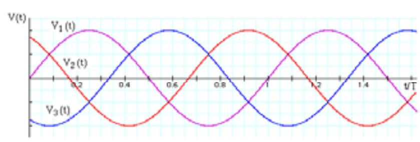
Concerning that the power is proportional to square of the voltage signal



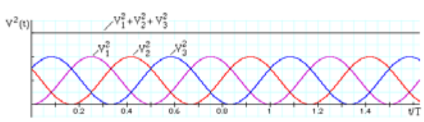
Monophase Power:



Three Phase Power:

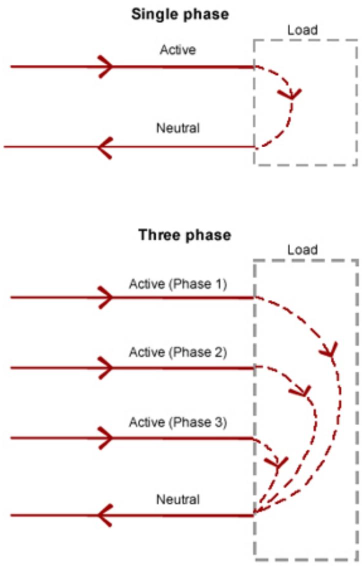


Power transfer into a linear balanced load is constant, which helps to reduce generator and motor vibrations.

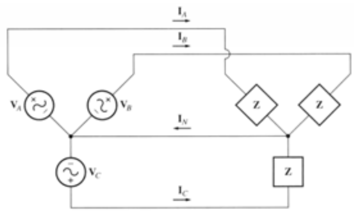


Three Phase Alternating Voltage and Current

Three Phase Distribution Lines



We can connect the negative (ground) ends of the three single-phase generators and loads together, so they share the common return line (neutral).



Then the three phase system reduces to necessary number of cable to transfer power from 6 to 4.

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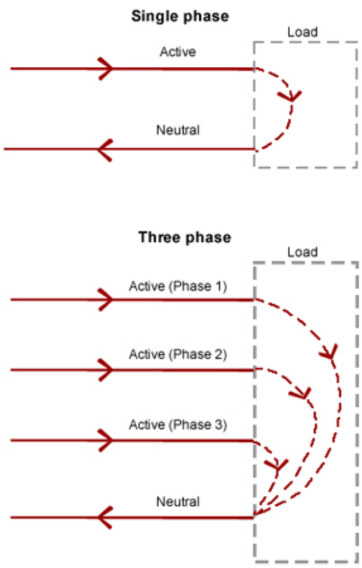
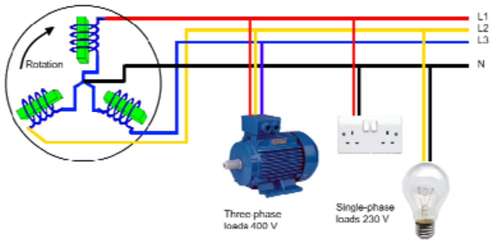
Three Phase Alternating Voltage and Current

Three Phase Distribution Lines



Three-phase systems may have a neutral wire. A neutral wire allows the three-phase system to use a higher voltage while still supporting lower-voltage single-phase loads. In high-voltage distribution situations, it is common not to have a neutral wire as the loads can simply be connected between phases (phase-phase connection).



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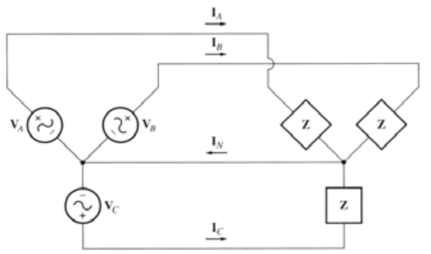
Three Phase Currents

If each of the phases transfers power to loads that have same impedance, such three-phase power systems (equal magnitude, phase differences of 120^0, identical loads) are called **balanced**.



$$I_A = \frac{V\angle 0^0}{Z\angle\theta} = I\angle -\theta$$

$$I_B = \frac{V\angle -120^0}{Z\angle\theta} = I\angle -120-\theta$$

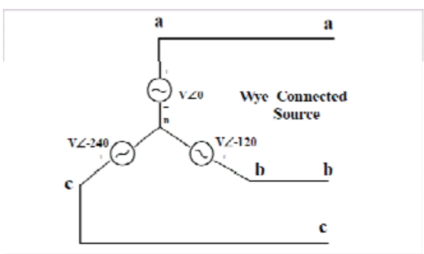
$$I_A = \frac{V\angle -240^0}{Z\angle\theta} = I\angle -240-\theta$$

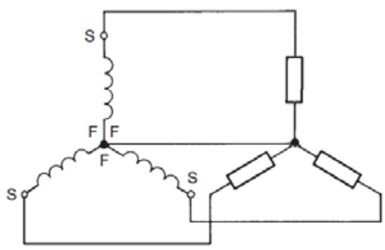
The phase currents tend to cancel out one another, summing to zero in the case of a linear balanced load. This makes it possible to reduce the size of the neutral conductor because it carries little to no current; all the phase conductors carry the same current and so can be the same size, for a balanced load.

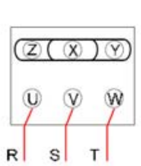
$$I_N = I\left[\cos(-\theta) - \frac{1}{2}\cos(-\theta) + \frac{\sqrt{3}}{2}\sin(-\theta) - \frac{1}{2}\cos(-\theta) - \frac{\sqrt{3}}{2}\sin(-\theta)\right]$$
$$+ jI\left[\sin(-\theta) - \frac{1}{2}\sin(-\theta) + \frac{\sqrt{3}}{2}\cos(-\theta) - \frac{1}{2}\sin(-\theta) - \frac{\sqrt{3}}{2}\cos(-\theta)\right]$$
$$= 0$$

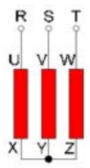
Star (Wye or Y) Connected Three Phase Systems

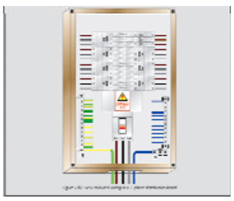
It is not necessary to have six wires from the three phase windings to the three loads. Each winding will have a ‘ start ’ (S) and a ‘ fi nish ’ (F) end. The star or wye (Y) connection mentioned is achieved by connecting the corresponding ends of the three phases together.



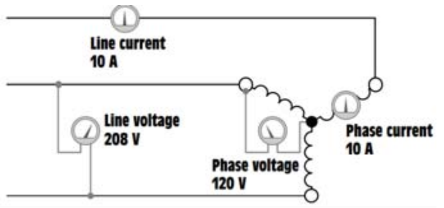


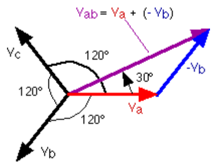


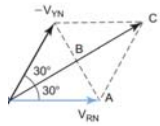


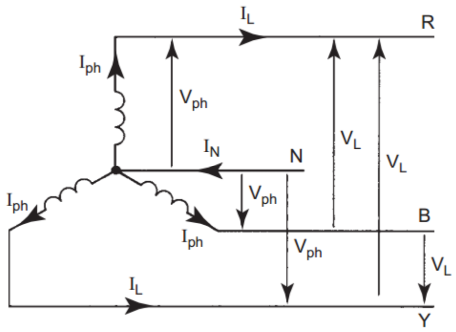


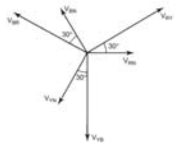
Star (Wye or Y) Connected Three Phase Systems











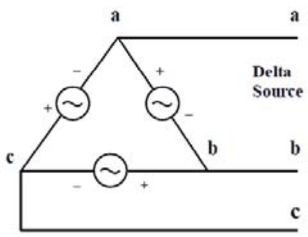
in star configuration, $V_L = \sqrt{3}V_{ph}$

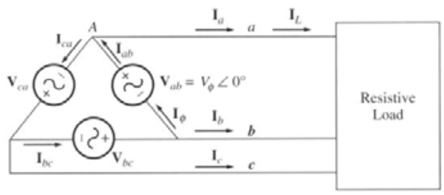
in star configuration, $I_L = I_{ph}$

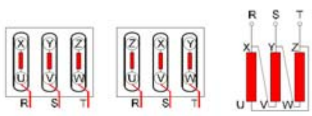
V_{ph} = Phase Voltage, V_L = Line Voltage, I_{ph} = Phase Current, I_L = Line Current

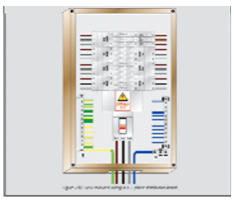
Delta (Mesh or Δ) Connected Three Phase Systems

It is not necessary to have six wires from the three phase windings to the three loads. Each winding will have a ' start ' (S) and a ' fi nish ' (F) end. The star or wye (Y) connection mentioned is achieved by connecting the corresponding ends of the three phases together.

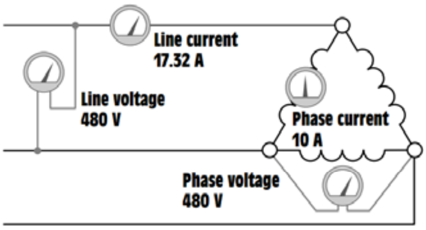


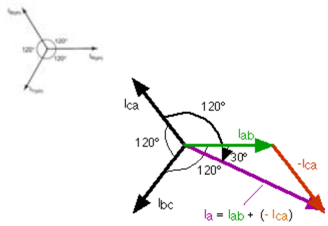


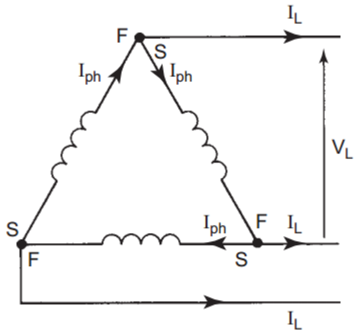


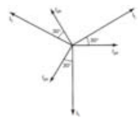


Delta (Mesh or Δ) Connected Three Phase Systems









$$V_L = V_{ph} \qquad I_L = \sqrt{3} I_{ph}$$

V_{ph} = Phase Voltage, V_L = Line Voltage, I_{Ph} = Phase Current, I_L = Line Current

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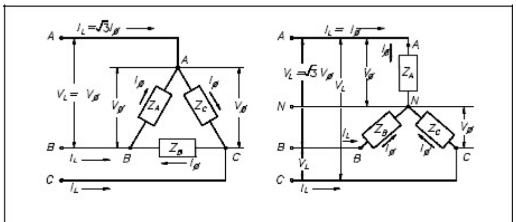
Three Phase Power

Total power (P_T) is equal to three times the single-phase power. Then the mathematical representation for total power in a balanced delta or wye load is

$$\boxed{P_{3\phi} = 3P_{\phi} = 3V_{\phi}I_{\phi}}$$



(a) Balanced Δ load, $Z_A = Z_B = Z_C = Z_\Delta$ (b) Balanced Y load, $Z_A = Z_B = Z_C = Z_Y$

For Star or Y connected systems

$$V_L = \sqrt{3}V_{\phi}, I_L = I_{\phi}$$

$$P_{3\phi} = 3V_{\phi}I_{\phi} = 3\frac{V_L}{\sqrt{3}}I_L$$

$$P_{3\phi} = \sqrt{3}V_L I_L$$

For Delta or Δ connected systems

$$V_L = V_{\phi}, I_L = \sqrt{3}I_{\phi}$$

$$P_{3\phi} = 3V_{\phi}I_{\phi} = 3V_L\frac{I_L}{\sqrt{3}}$$

$$P_{3\phi} = \sqrt{3}V_L I_L$$

$$\boxed{P_{3\phi} = \sqrt{3}V_L I_L}$$

V_{ϕ} = Phase Voltage, V_L = Line Voltage, I_{ϕ} = Phase Current, I_L = Line Current

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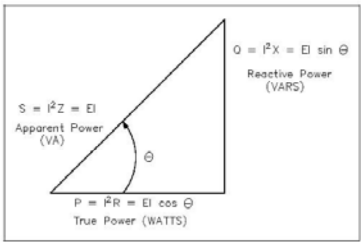
Three Phase Power Triangle

If the 3ϕ system is connected to a balanced load with impedance:

$$Z_\phi = |Z_\phi| \angle \varphi°$$

Then the power triangle and the power values of the 3ϕ system is similar to monophase systems:



$$S_{3\phi} = \sqrt{3} V_L I_L \quad [VA] \qquad S_{3\phi} = 3 V_\phi I_\phi \quad [VA]$$

$$Q_{3\phi} = \sqrt{3} V_L I_L \sin\varphi \quad [VAR] \qquad Q_{3\phi} = 3 V_\phi I_\phi \sin\varphi \quad [VAR]$$

$$P_{3\phi} = \sqrt{3} V_L I_L \cos\varphi \quad [W] \qquad P_{3\phi} = 3 V_\phi I_\phi \cos\varphi \quad [W]$$

V_ϕ = Phase Voltage, V_L = Line Voltage, I_ϕ = Phase Current, I_L = Line Current

Three Phase Analysis

Problem: An asynchronous electric that runs using three phase grid has a power factor of 0.85 and measured that it gets 7 [A] from grid. What are the powers it gets from R-S-T phases if the phases balanced?

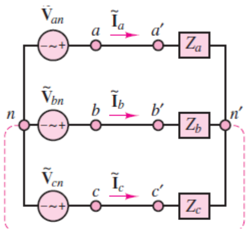
Solution: P : Real Power[Watt] ; Q : Apparent Power [VAR]; S : ReactivePower [VA]
U : 380 [V] → The voltage between the phases is 380 [V]
I : It is the current taken from one phase [A]

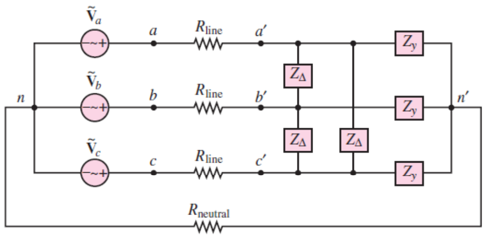
P = √ 3 x U x I x cos ϕ = √ 3 x 380 x 7 x 0,85 = 3916 [W]
Q = √ 3 x U x I x sin ϕ = √ 3 x 380 x 7 x 0,5268 = 2427 [VAR]
S = √ 3 x U x I = √ 3 x 380 x 7 = 4607 [VA]

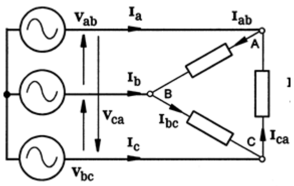
Three Phase Analysis

To do per phase analysis

1. Convert all Δ load/sources to equivalent Y's
2. Solve phase "a" independent of the other phases
3. Total system power S = 3 $V_a I_a^*$
4. If desired, phase "b" and "c" values can be determined by inspection (i.e., ±120° degree phase shifts)
5. If necessary, go back to original circuit to determine line-line values or internal Δ values





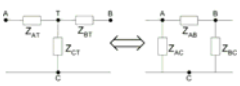


Three Phase Alternating Voltage and Current

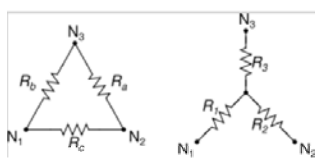
Three Phase Analysis

Delta to wye conversion

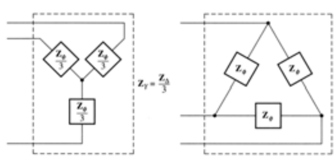
The Y-Δ transform is known by a variety of other names, mostly based upon the two shapes involved, listed in either order. The Y, spelled out as wye, can also be called T or star; the Δ, spelled out as delta, can also be called triangle, Π (spelled out as pi), or mesh. Thus, common names for the transformation include wye-delta or delta-wye, star-delta, star-mesh, or T-Π.



$$R_a = \frac{R_1R_2 + R_2R_3 + R_3R_1}{R_1}$$
$$R_b = \frac{R_1R_2 + R_2R_3 + R_3R_1}{R_2}$$
$$R_c = \frac{R_1R_2 + R_2R_3 + R_3R_1}{R_3}$$



$$R_1 = \frac{R_bR_c}{R_a + R_b + R_c}$$
$$R_2 = \frac{R_aR_c}{R_a + R_b + R_c}$$
$$R_3 = \frac{R_aR_b}{R_a + R_b + R_c}$$



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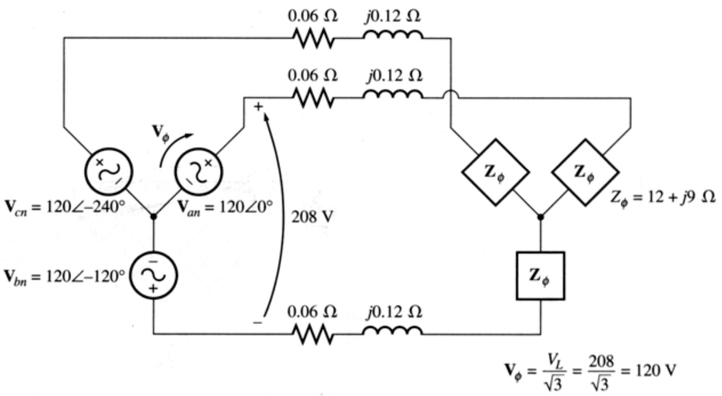
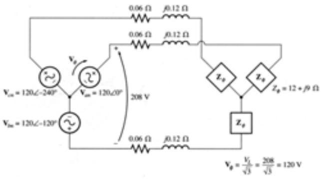
Three Phase Analysis



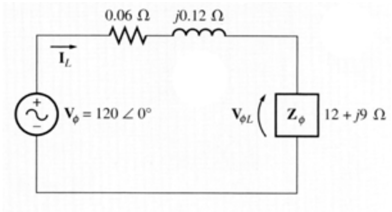
For a 208-V three-phase ideally balanced system, find:

a) the magnitude of the line current I_L;
b) The magnitude of the load's line and phase voltages V_{LL} and $V_{\phi L}$;
c) The real, reactive, and the apparent powers consumed by the load;
d) The power factor of the load.

Three Phase Analysis



Per phase circuit :



Is the load inductive or capacitive??

a) The line current:

[illegible]

b) The phase voltage on the load:

[illegible]

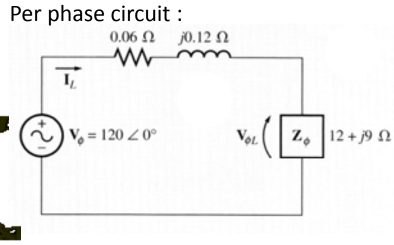
The magnitude of the line voltage on the load:

$$V_{LL} = \sqrt{3} V_\phi = 206.3\ V$$

Three Phase Alternating Voltage and Current

Three Phase Analysis

Per phase circuit :



c) The real power consumed by the load:

[illegible]

The reactive power consumed by the load:

[illegible]

The apparent power consumed by the load:

[illegible]

d) The load power factor:

[illegible]