

# DataFrame Operations in Pandas

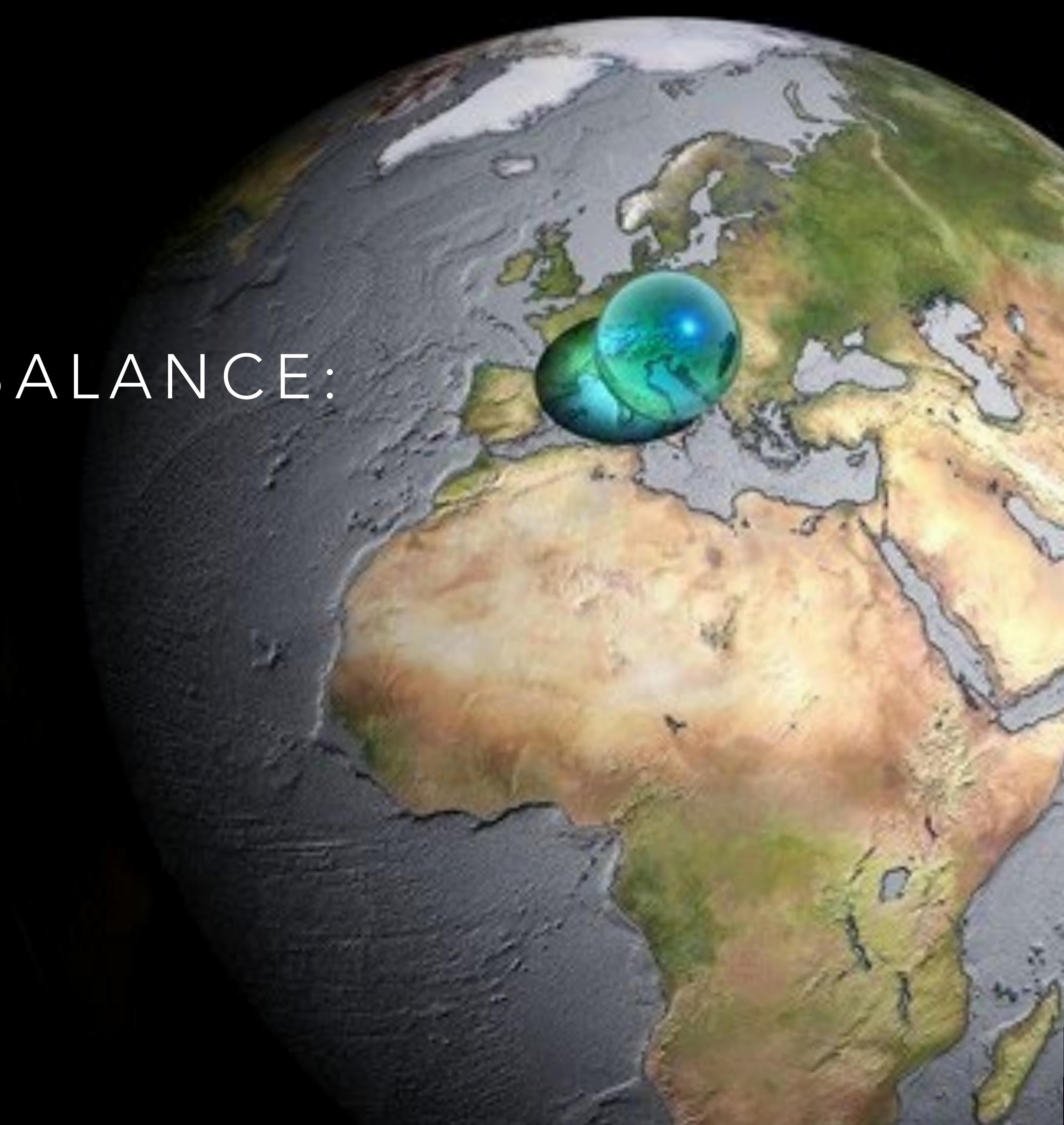
	A	B	
0	0.626386	1.52325	----axis=1----->

axis=0

↓      ↓

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PRINCIPLES OF MASS BALANCE:  
HYDROLOGY & WATER  
RESOURCES



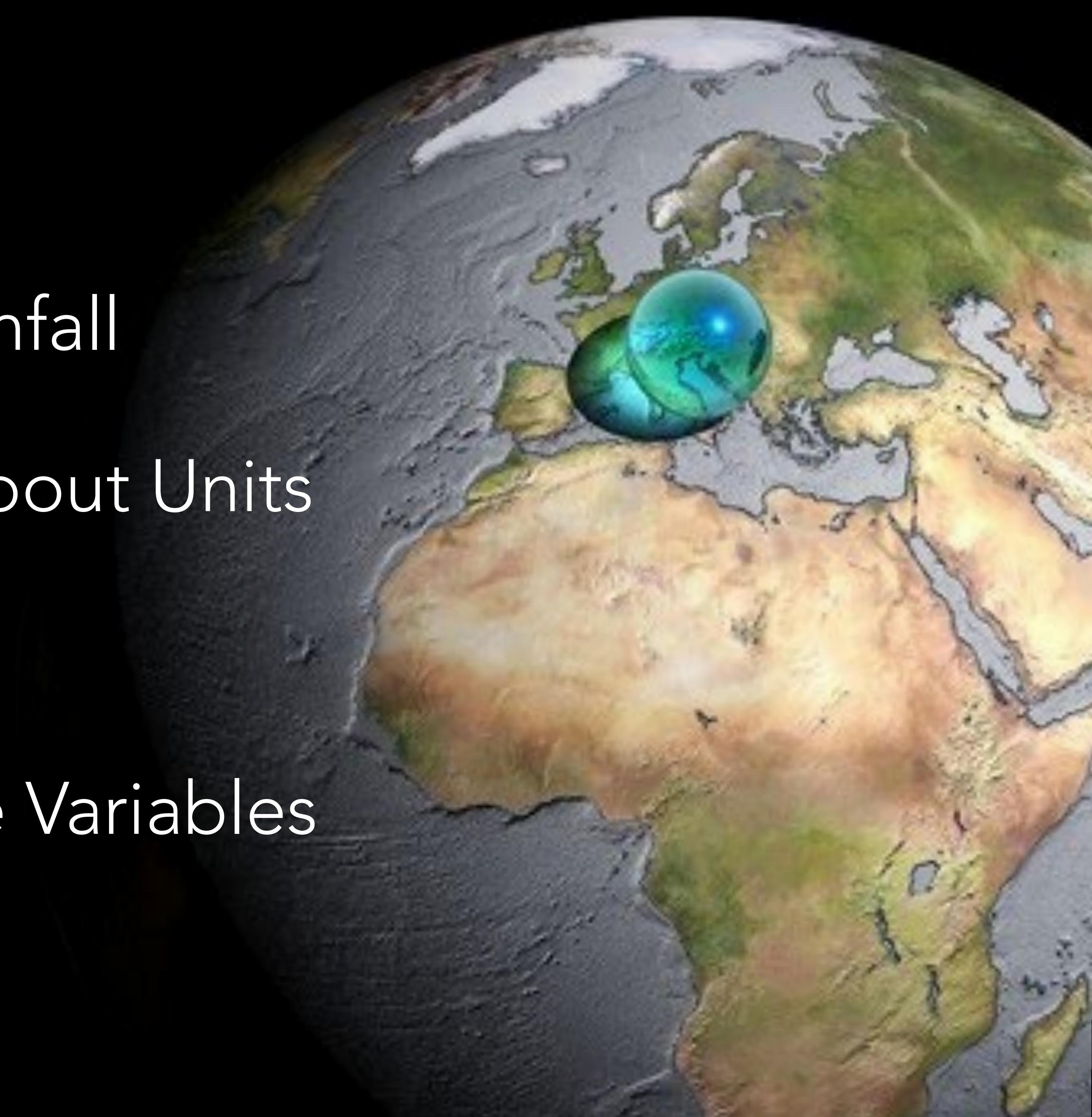
# TOPICS

1. Global Patterns of Rainfall

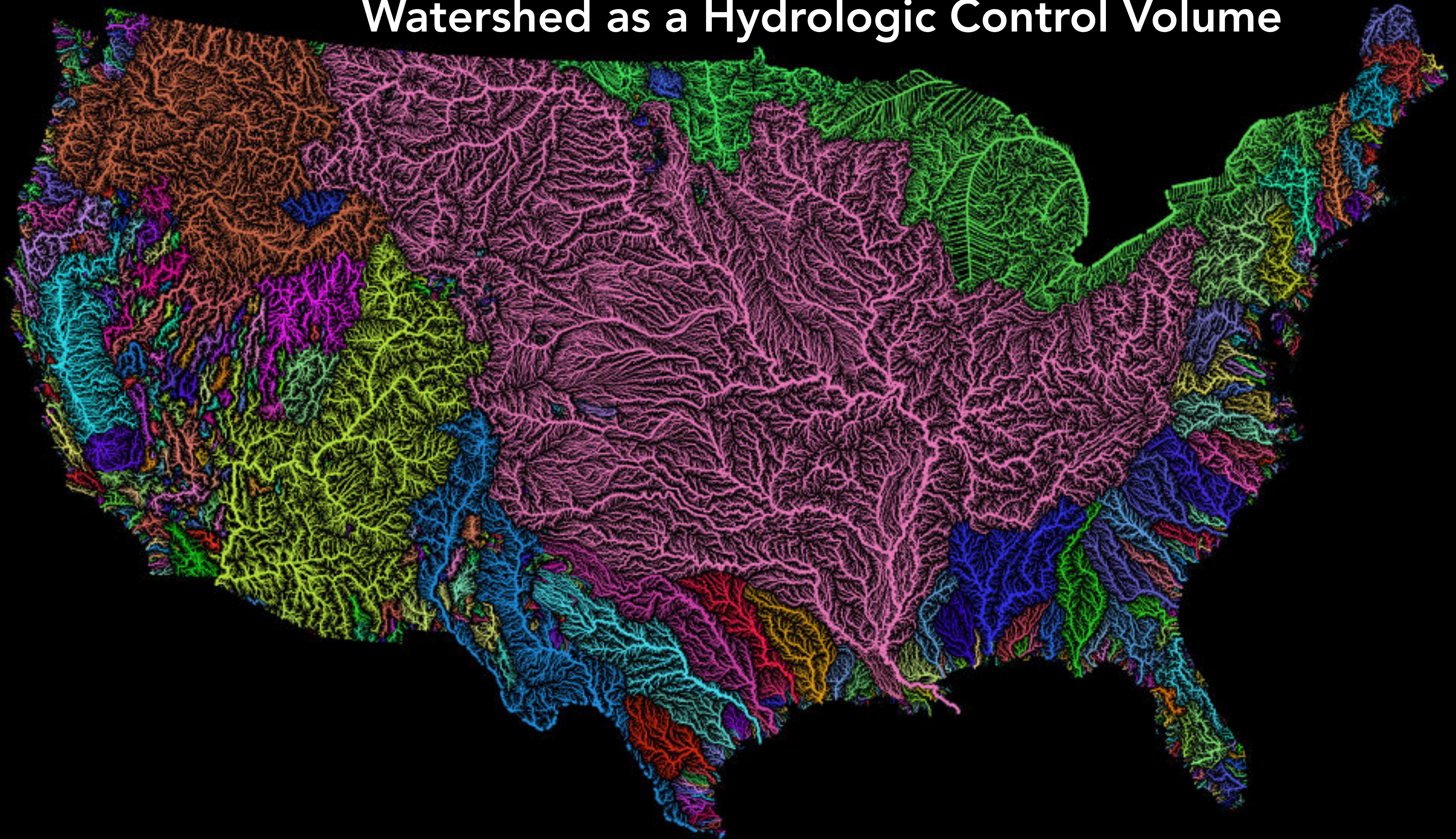
Some Shenanigans About Units

Flows and Fluxes

Extensive vs. Intensive Variables



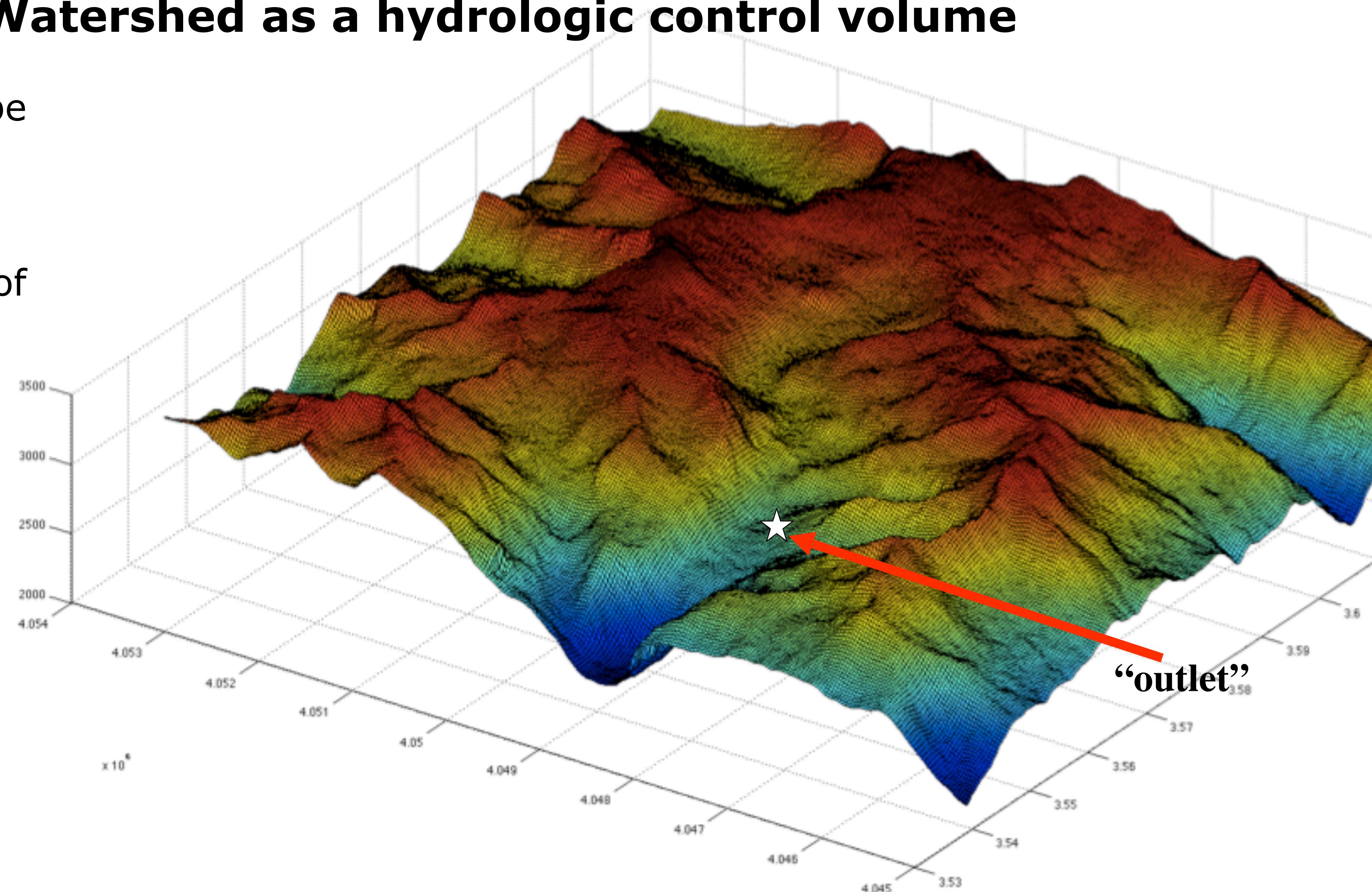
# Watershed as a Hydrologic Control Volume



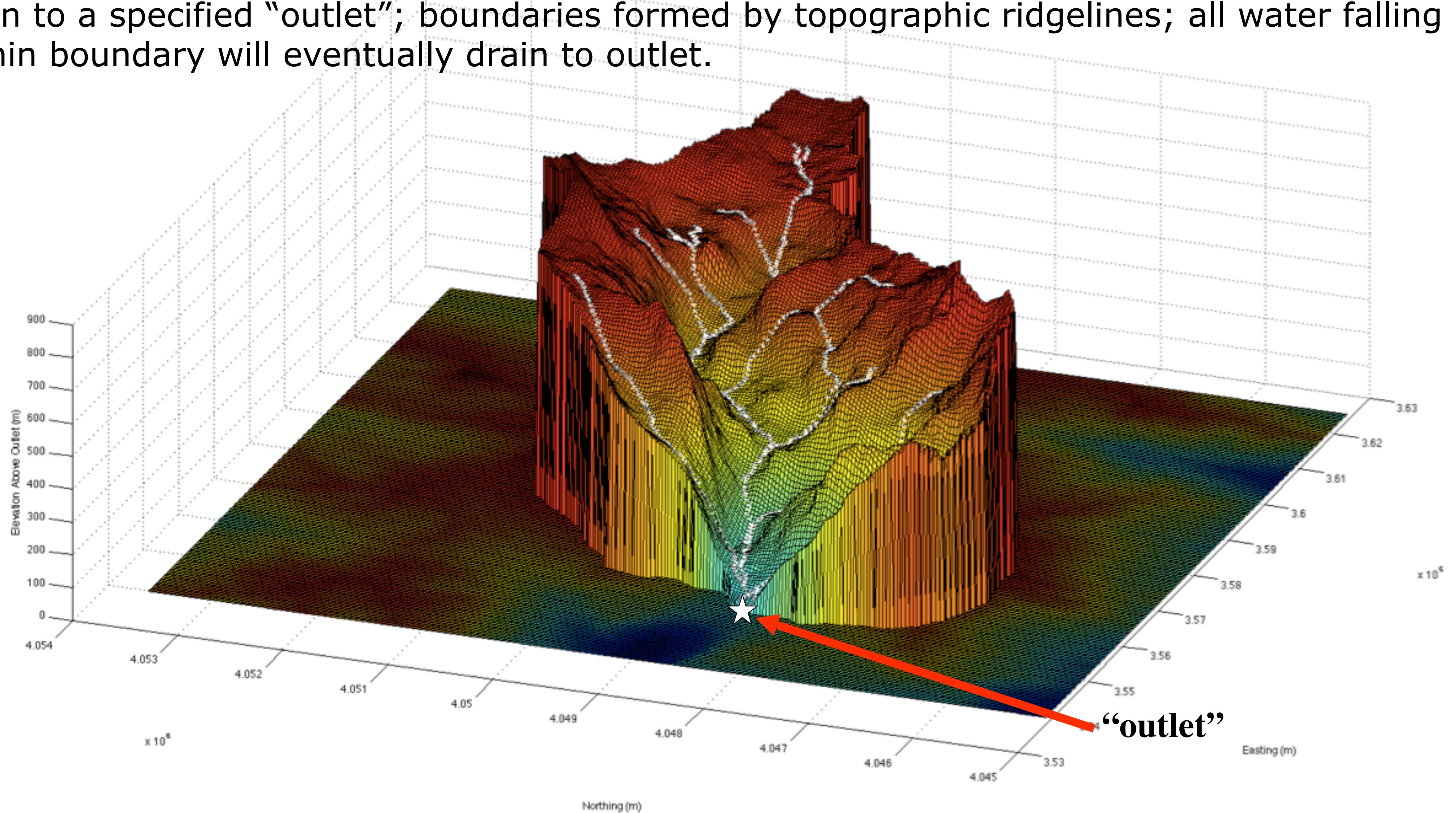
# Watershed as a hydrologic control volume

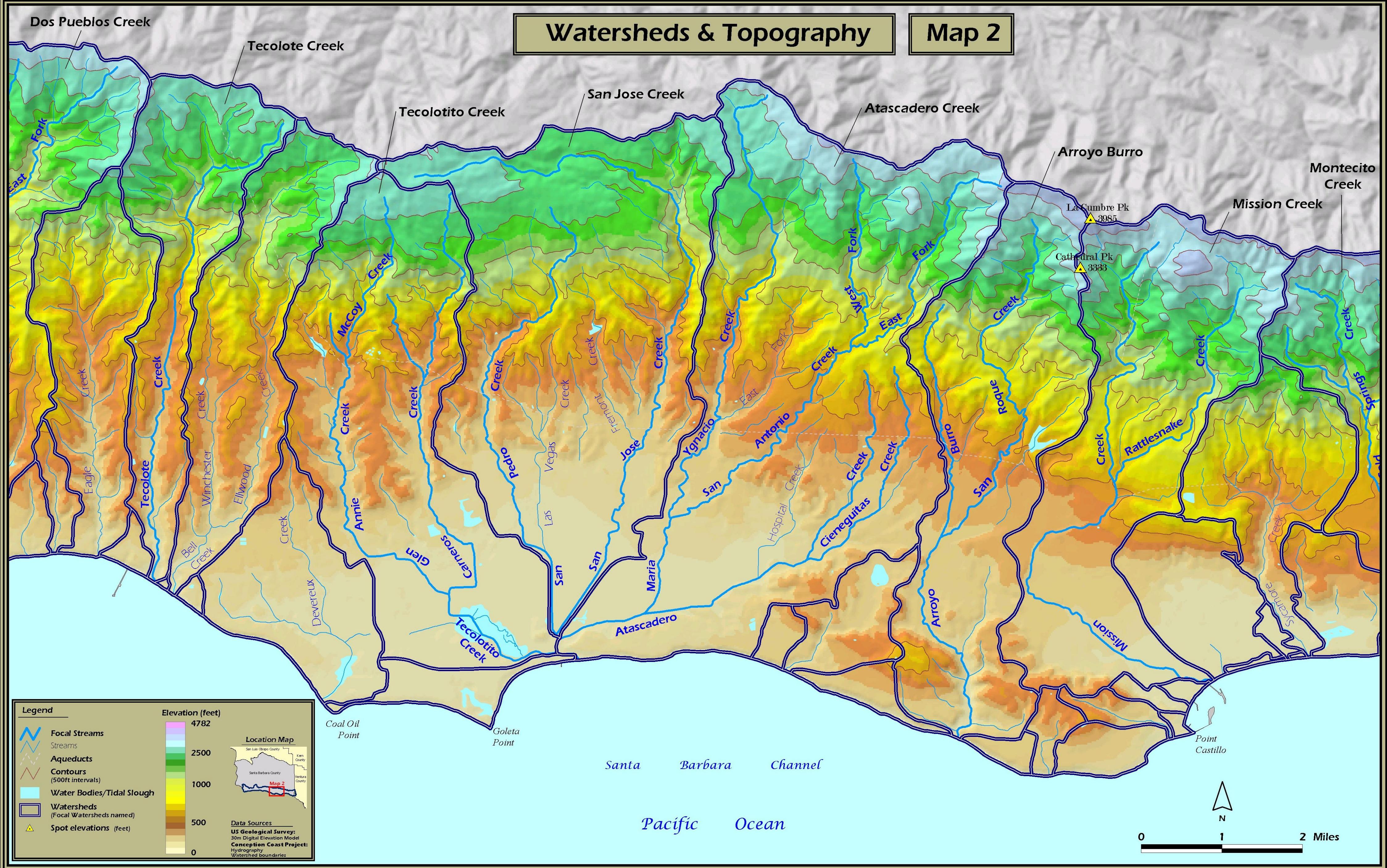
Topography can be a main driver of surface flow; topography often digitized in form of Digital Elevation Models (DEMs)

**Basic question:**  
If standing in a stream channel, from what upstream area is the water coming from?



A **watershed** (or river basin or catchment) is the topographically derived set of points that drain to a specified “outlet”; boundaries formed by topographic ridgelines; all water falling within boundary will eventually drain to outlet.





# Catchment Water Balance

$P$ : Precipitation

$ET$ : Evapotranspiration

$Q$ : Streamflow

$S$ : Soil Water Storage



Assumes no groundwater  
flows between basins

$$\frac{dS}{dt} = P - ET - Q$$

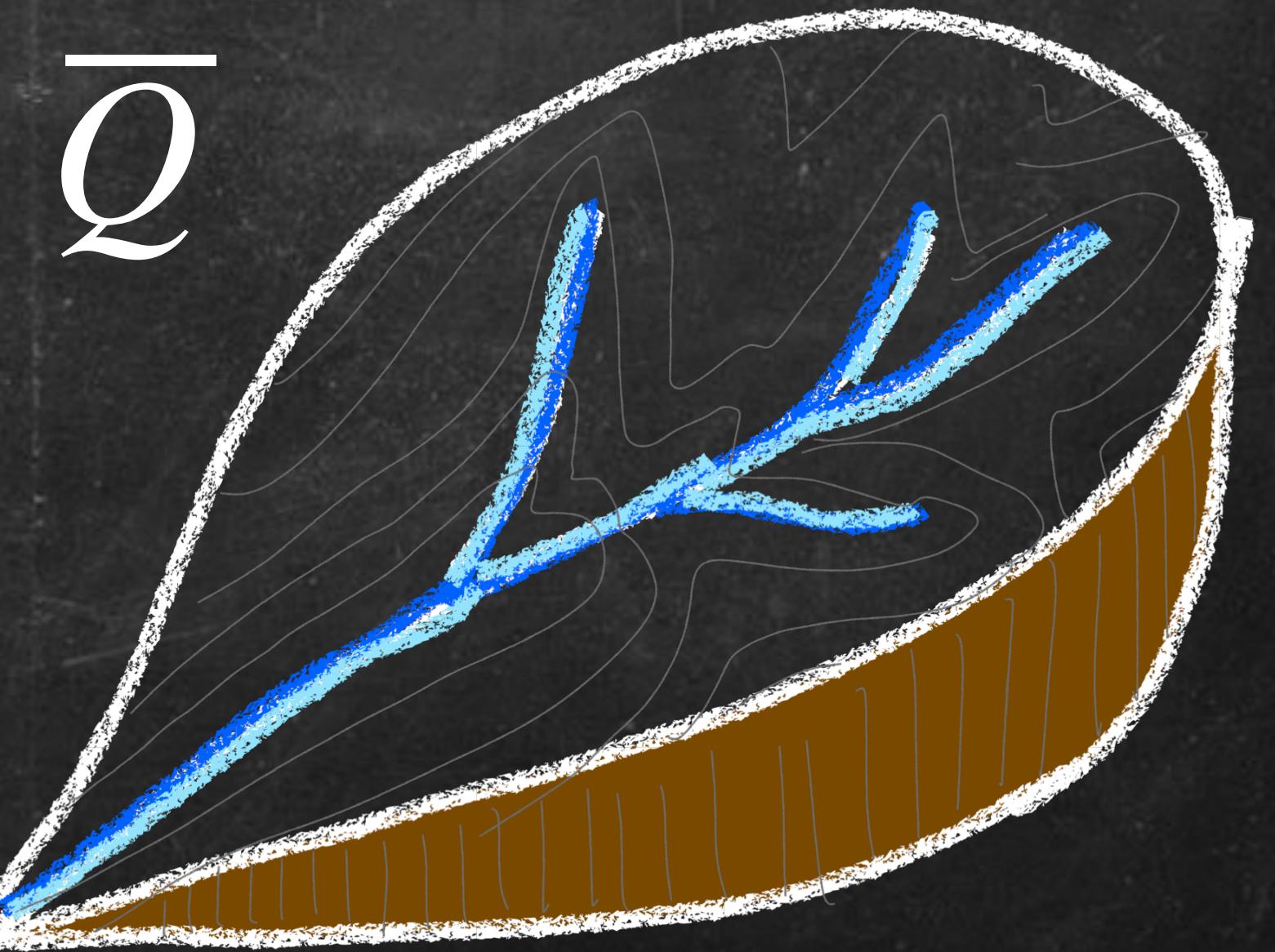
# EVAPORATION From MASS BALANCE

Over long (annual, or multi-year) time-scales,

$\frac{dS}{dt}$  is zero:

$$\frac{\overline{dS}}{dt} = 0 = \overline{P} - \overline{ET} - \overline{Q}$$

$$\overline{ET} = \overline{P} - \overline{Q}$$



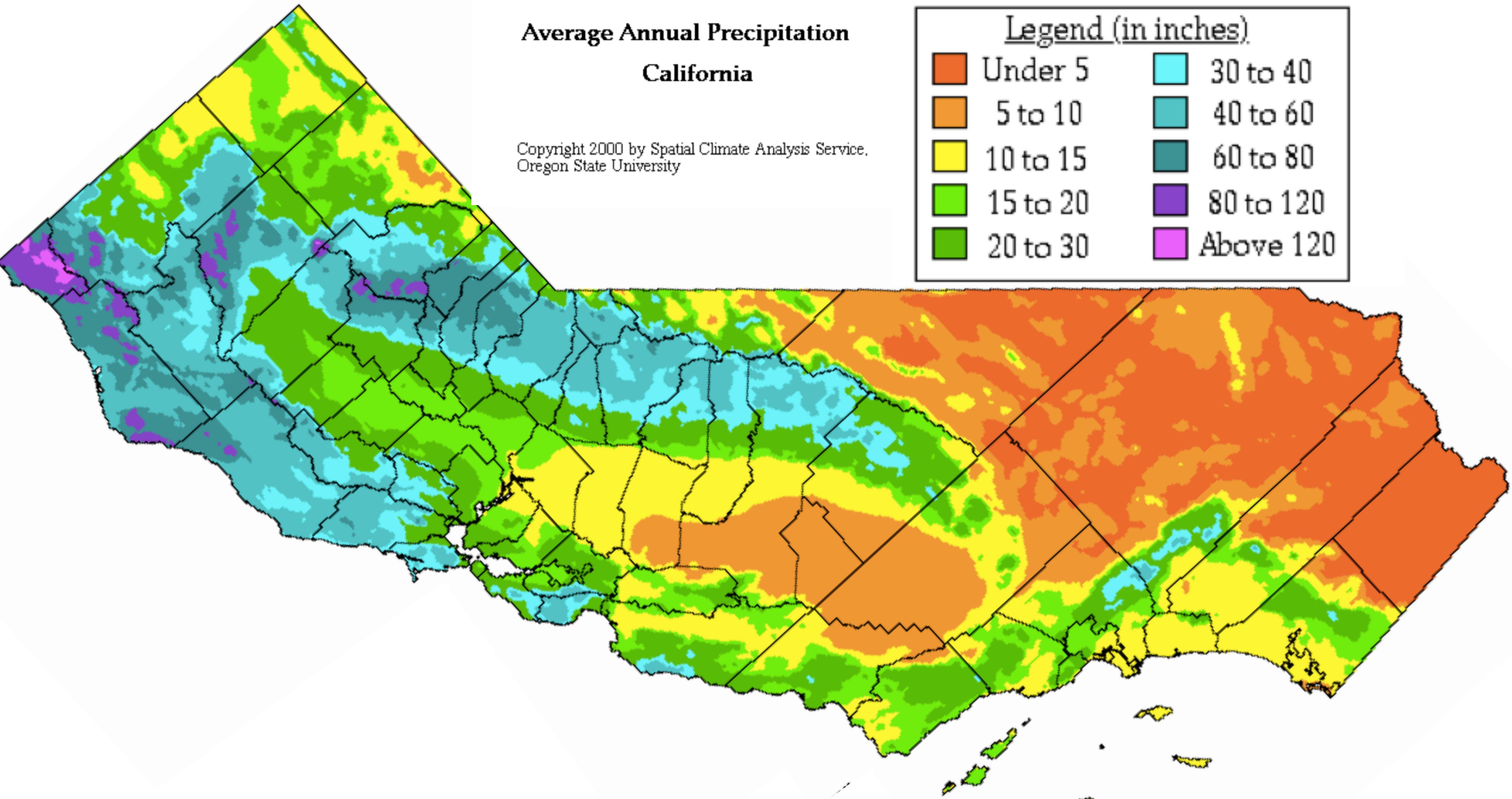
# Average Annual Precipitation

## California

Copyright 2000 by Spatial Climate Analysis Service.  
Oregon State University

### Legend (in inches)

Under 5	30 to 40
5 to 10	40 to 60
10 to 15	60 to 80
15 to 20	80 to 120
20 to 30	Above 120



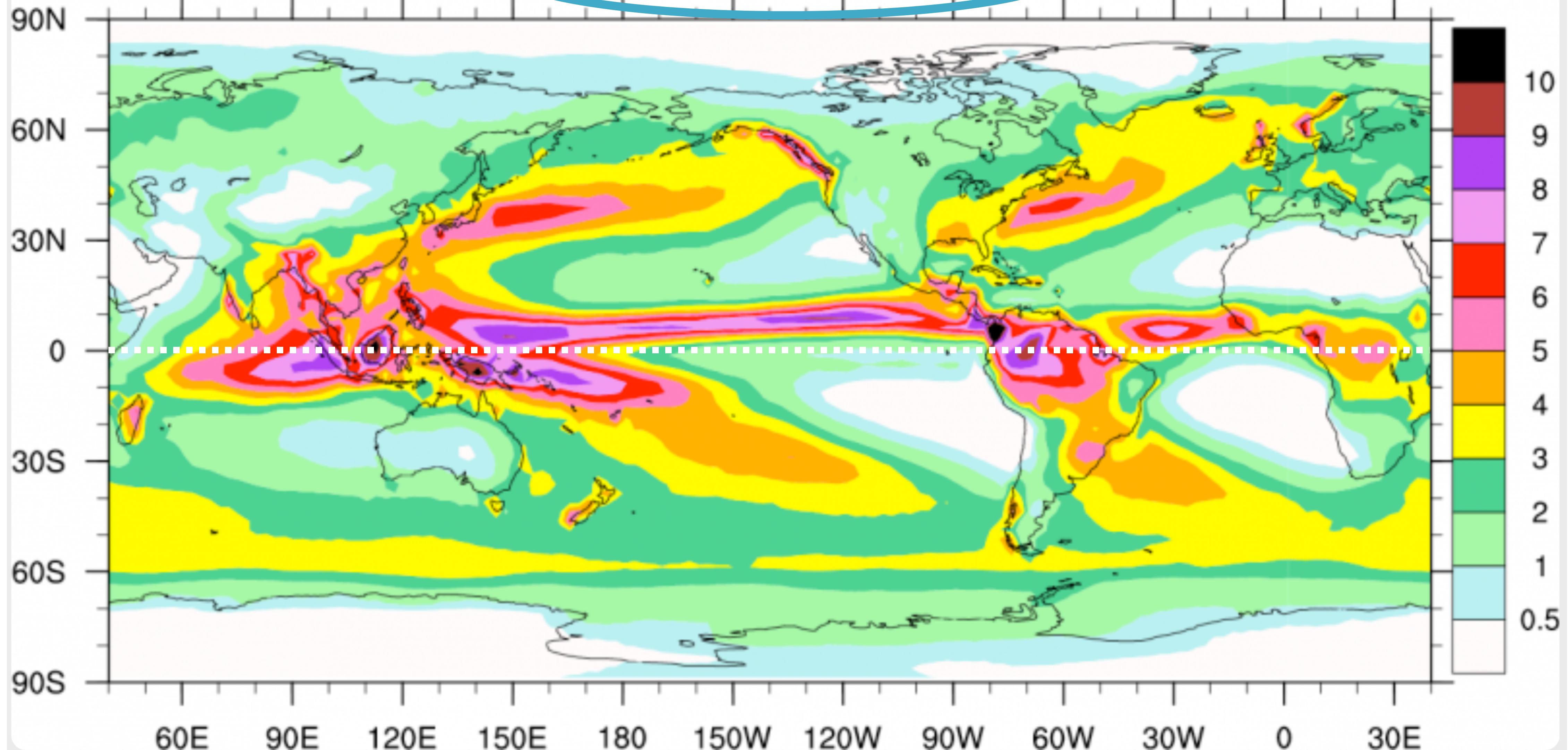
# Global Rainfall Patterns

**TRMM GPCP: 1979-2010**

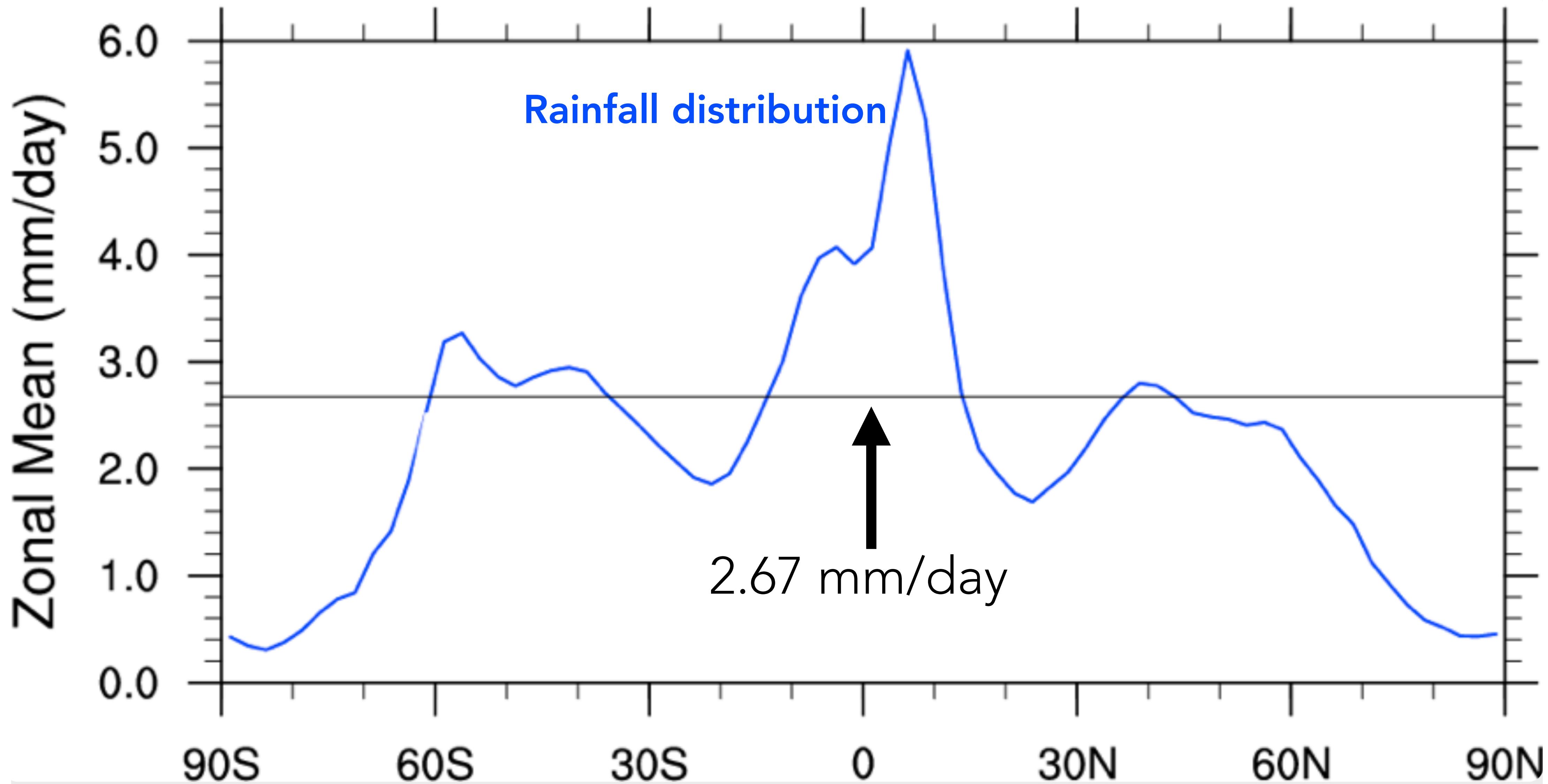
precipitation

Areal Mean=2.67 mm/day

mm/day



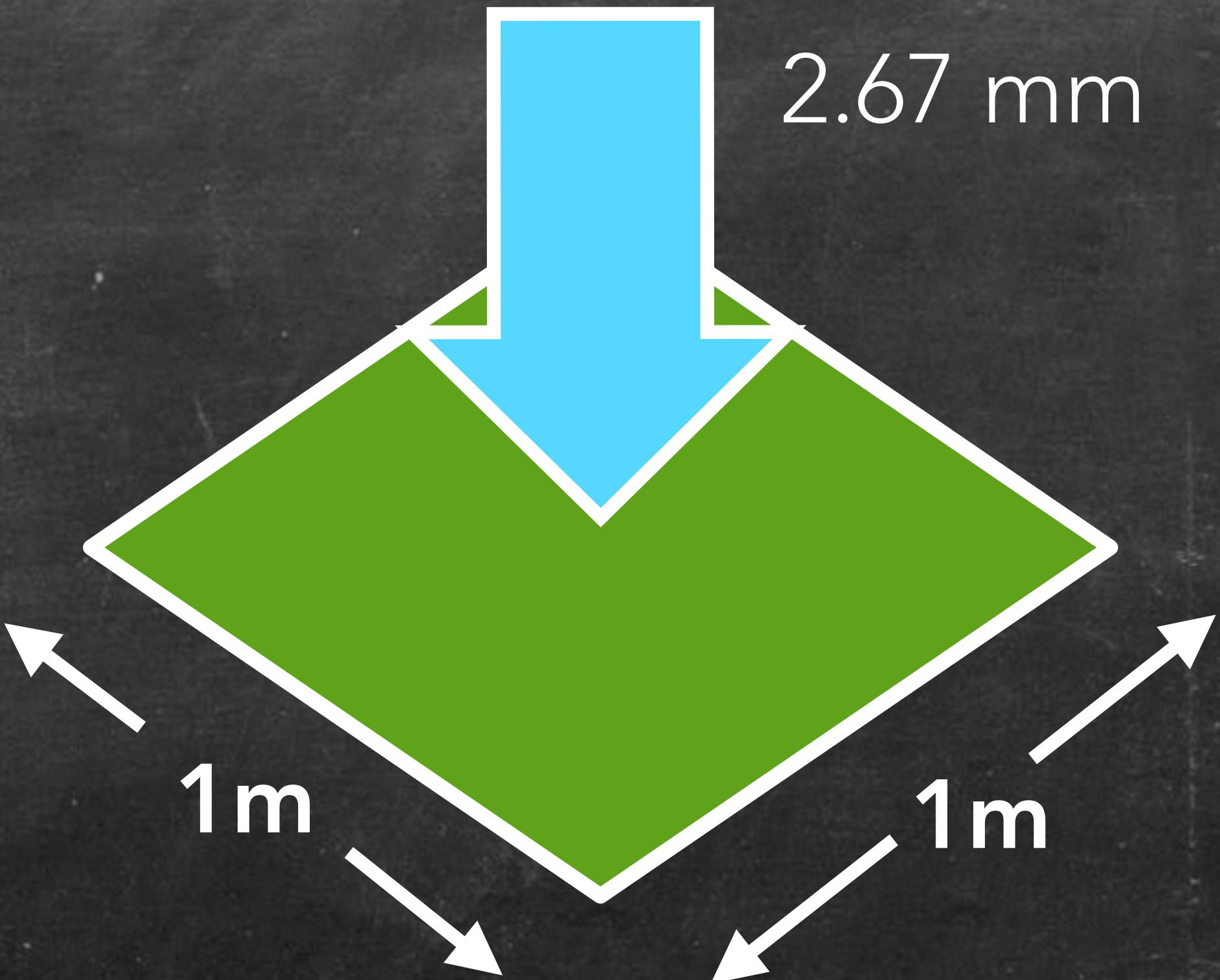
# Latitudinal Distribution of Rainfall



# Global Average Rainfall: 2.67 mm per day

Consider a single square meter:

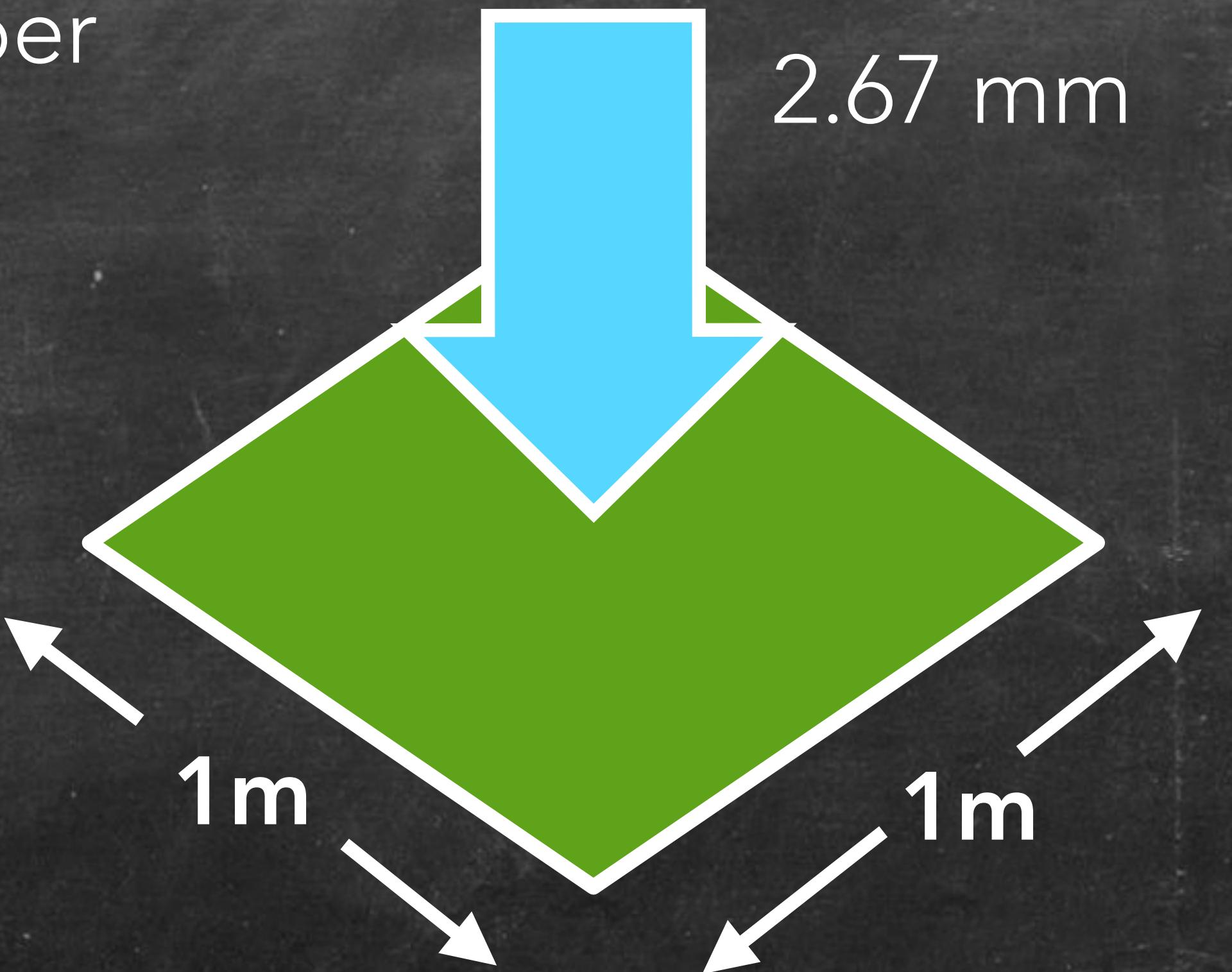
Each day, there is an average of 2.67 mm of rainfall onto each  $\text{m}^2$  of the planet



Global Average Rainfall:  $2.67 \frac{\text{mm}}{\text{m}^2}$  per day

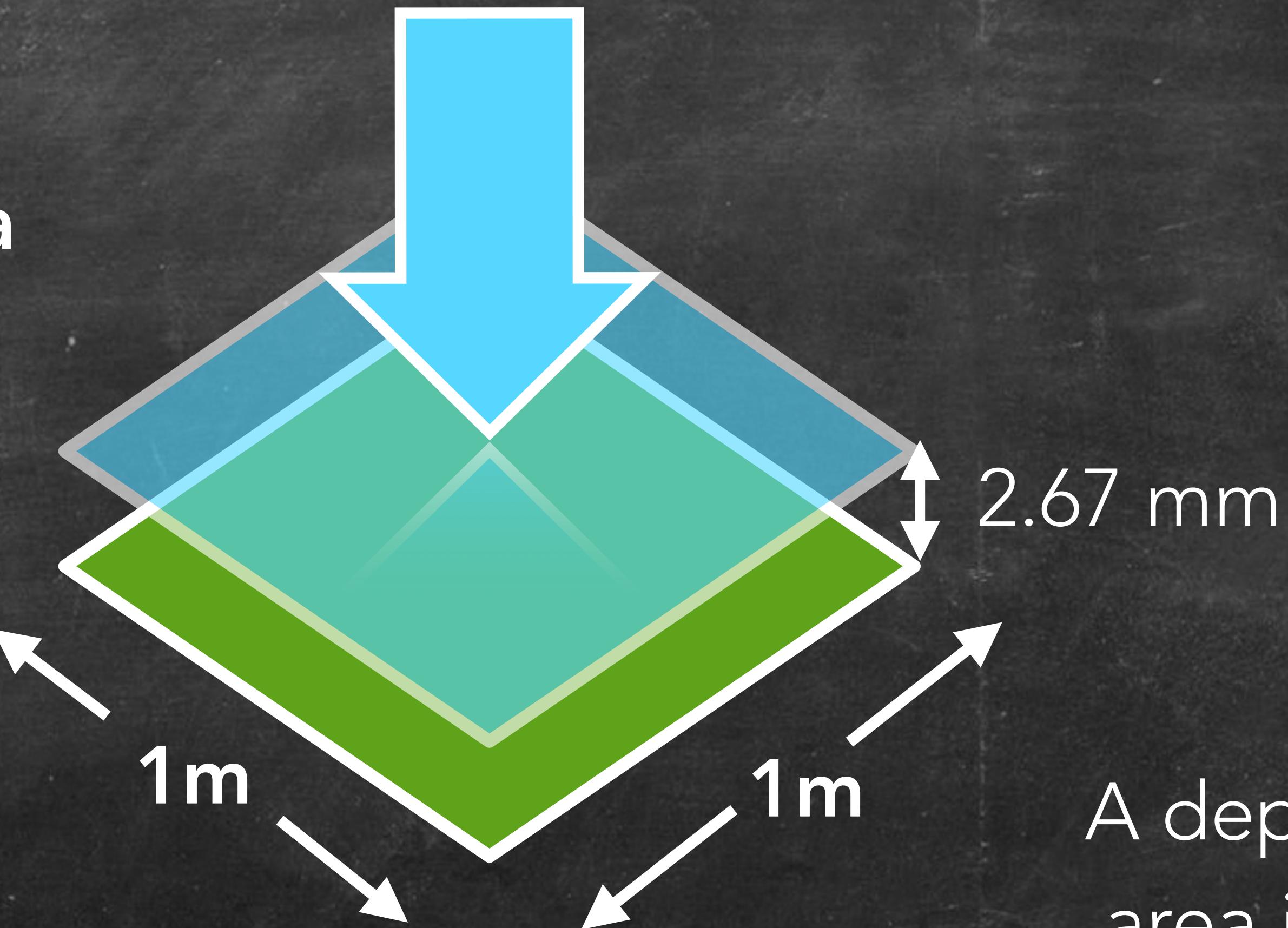
So. Daily rainfall is a  
**depth** per unit area per  
day... right?

**2.67 mm of rainfall  
on average per  $\text{m}^2$   
each day**



Global Average Rainfall:  $2.67 \frac{\text{mm}}{\text{m}^2}$  per day

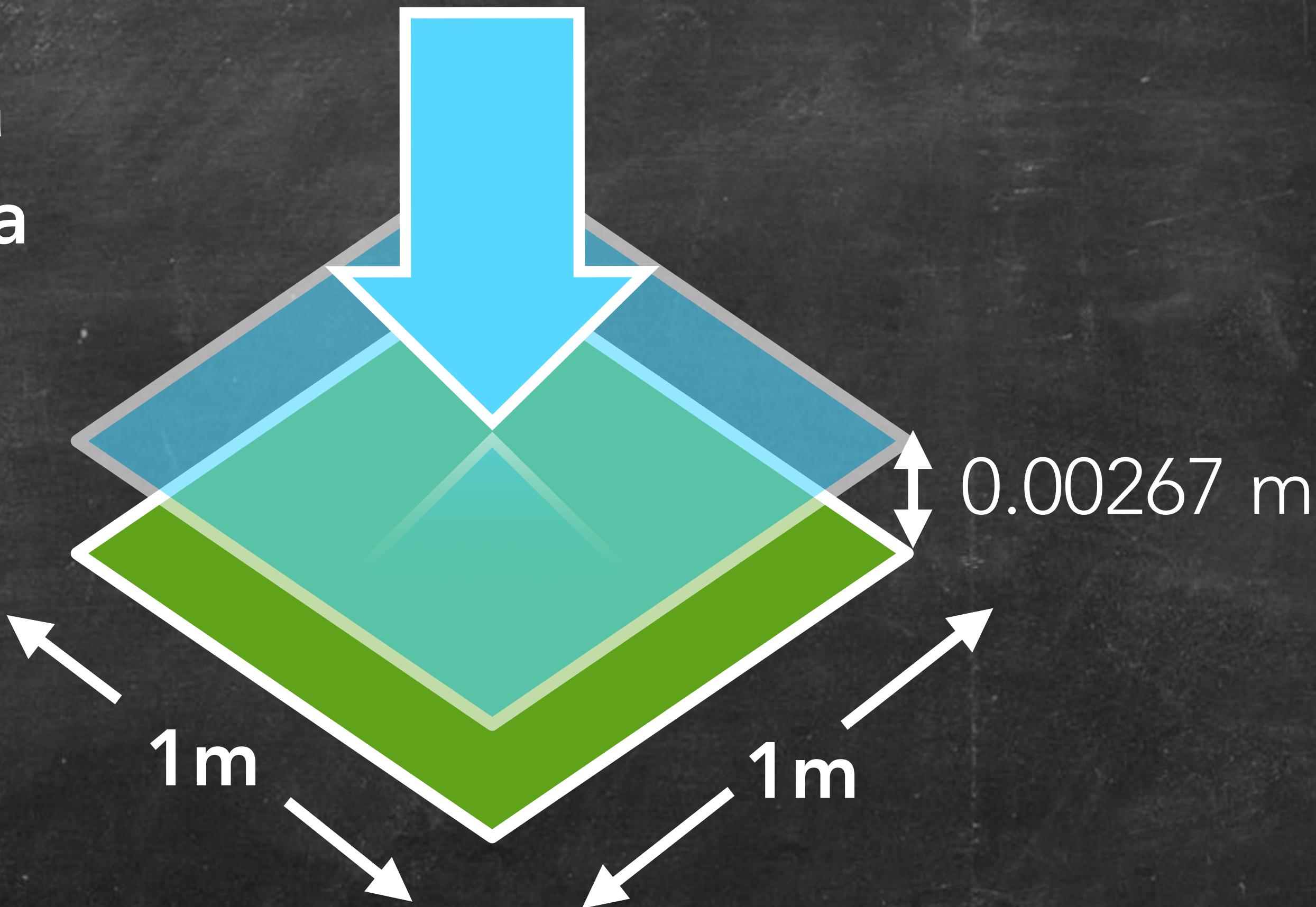
So. Daily rainfall is a  
**depth times an area**  
per unit area.



A depth times an  
area is a volume

Global Average Rainfall:  $2.67 \frac{\text{mm}}{\text{m}^2}$  per day

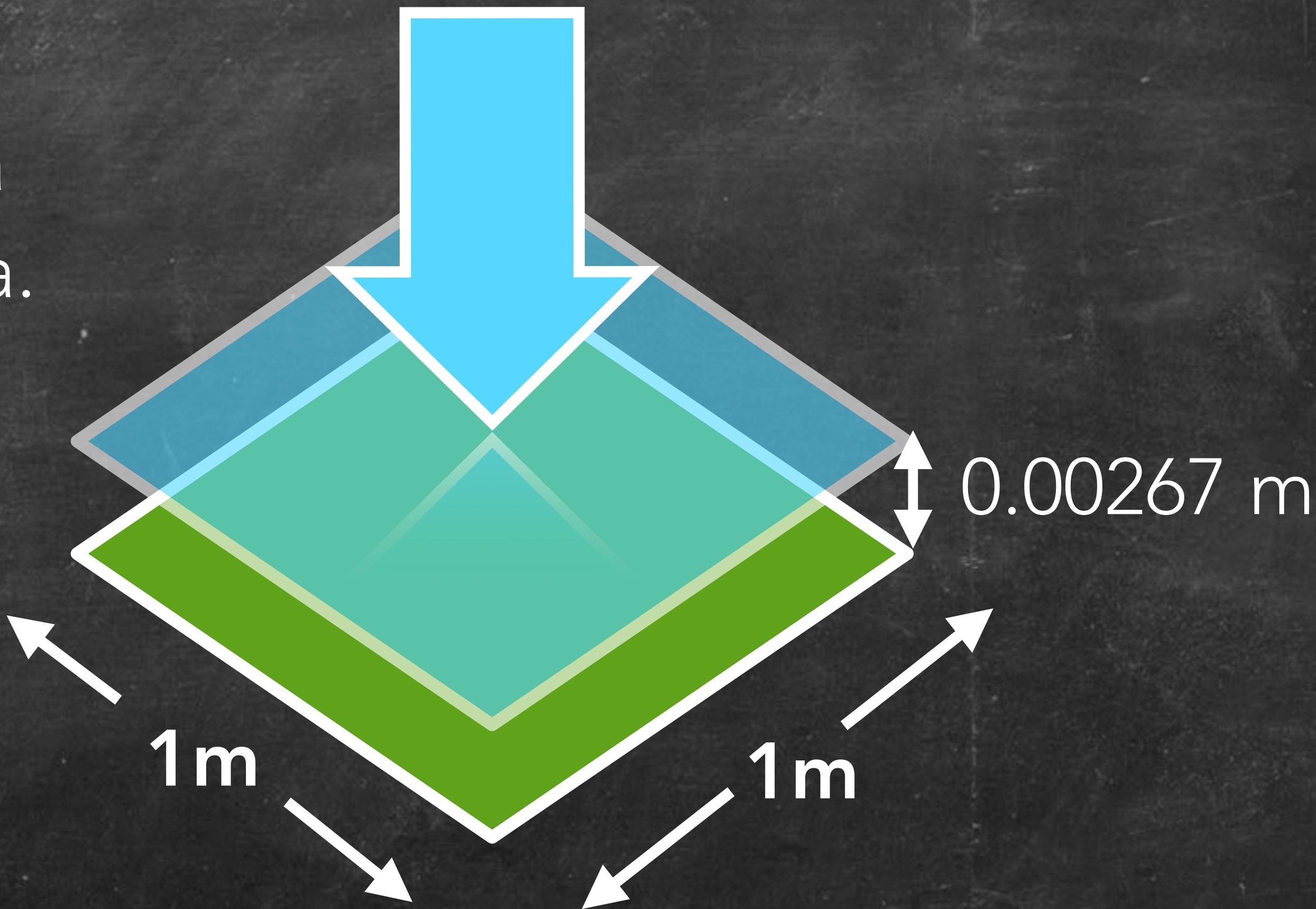
So. Daily rainfall is a  
**depth times an area**  
per unit area.



$$R_v = \left( 2.67 \frac{\text{mm}}{\text{m}^2} \text{ day}^{-1} \times \frac{1 \text{ m}}{1000 \text{ mm}} \right) \times 1 \text{ m}^2 = 0.00267 \frac{\text{m}^3}{\text{m}^2} \text{ day}^{-1}$$

Global Average Rainfall:  $0.00267 \frac{\text{m}^3}{\text{m}^2}$  per day

So. Daily rainfall is a  
**volume** per unit area.



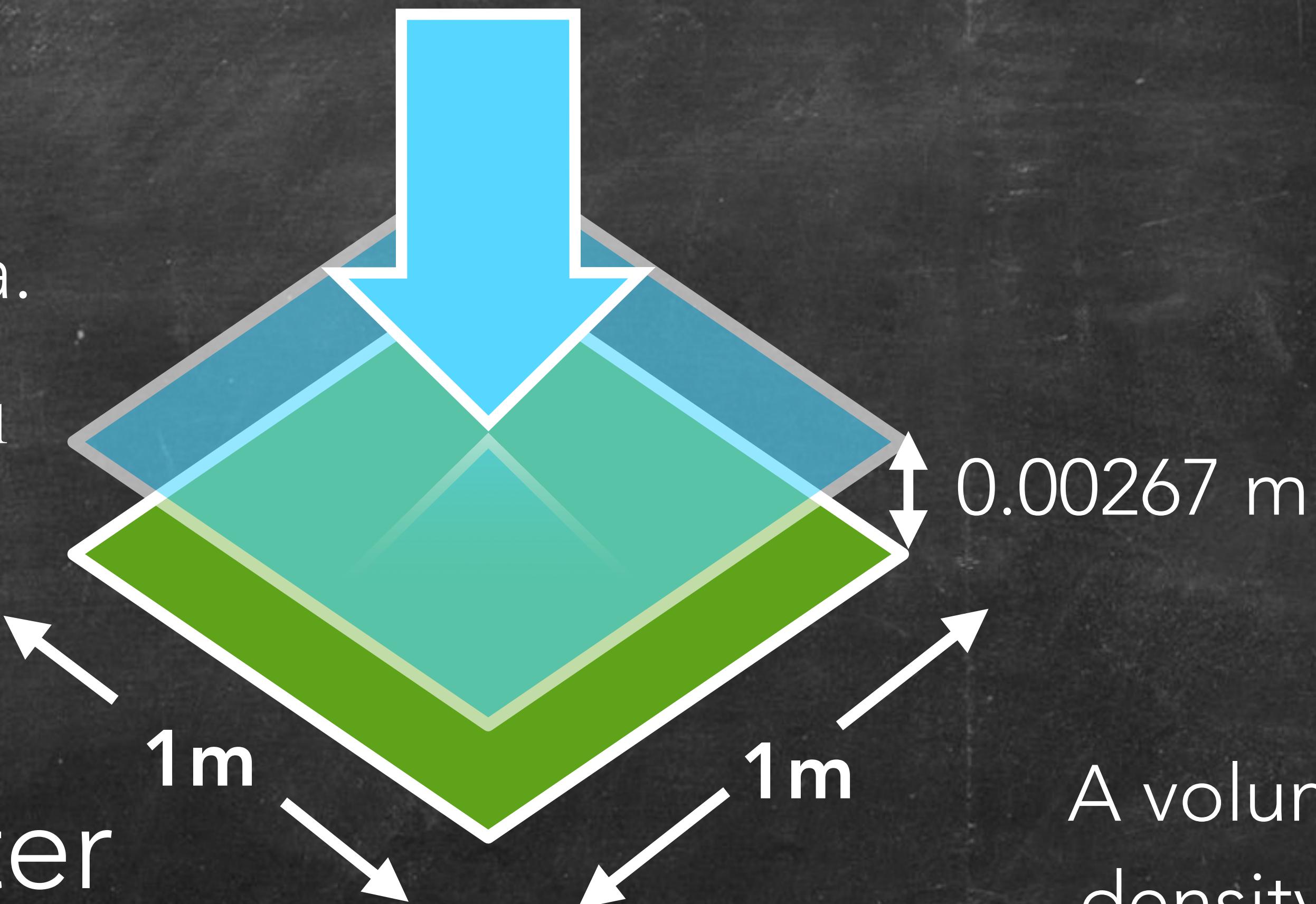
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Global Average Rainfall:  $0.00267 \frac{\text{m}^3}{\text{m}^2}$  per day

So. Daily rainfall is a  
**volume** per unit area.

$$R_v = 0.00267 \frac{\text{m}^3}{\text{m}^2} \text{ day}^{-1}$$

$$R_m = R_v \times \rho_{\text{water}}$$



A volume times a  
density is a mass

$$\rho_{\text{water}} = \frac{1000 \text{ kg}}{\text{m}^3}$$

Global Average Rainfall:  $0.00267 \frac{\text{m}^3}{\text{m}^2}$  per day

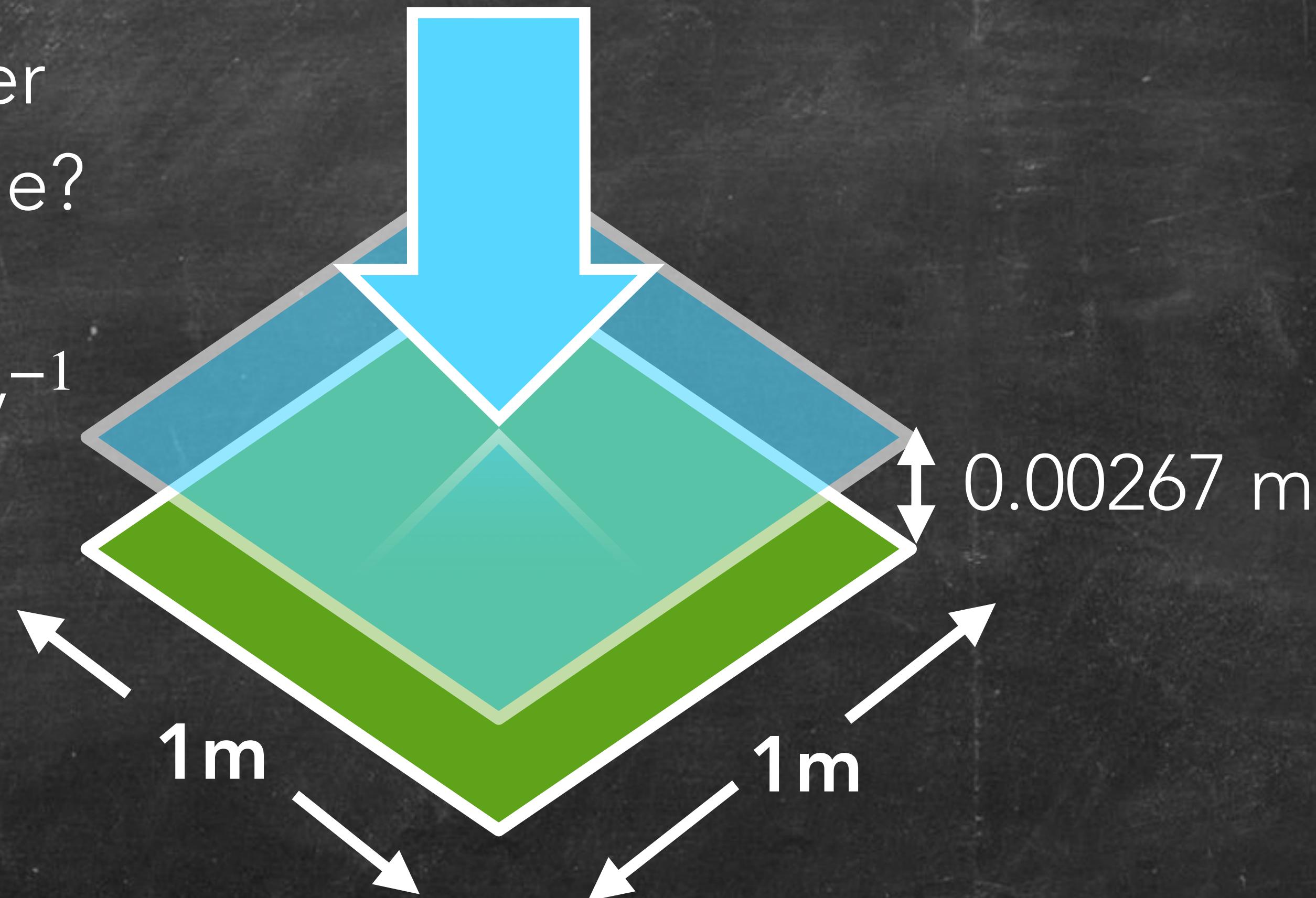
Rainfall is a **mass** per unit area per unit time?

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Global Average Rainfall:  $2.67 \frac{\text{kg}}{\text{m}^2}$  per day

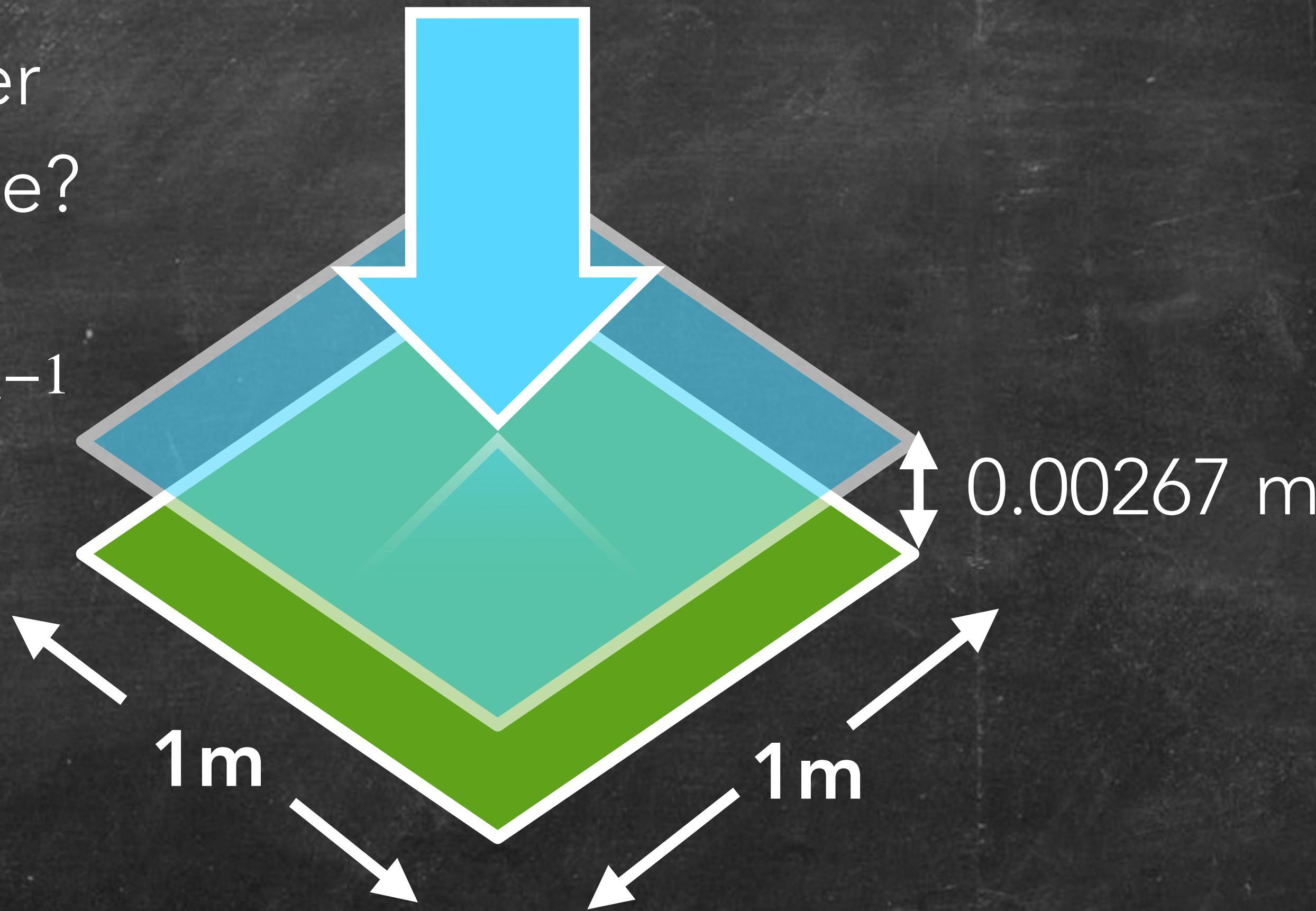
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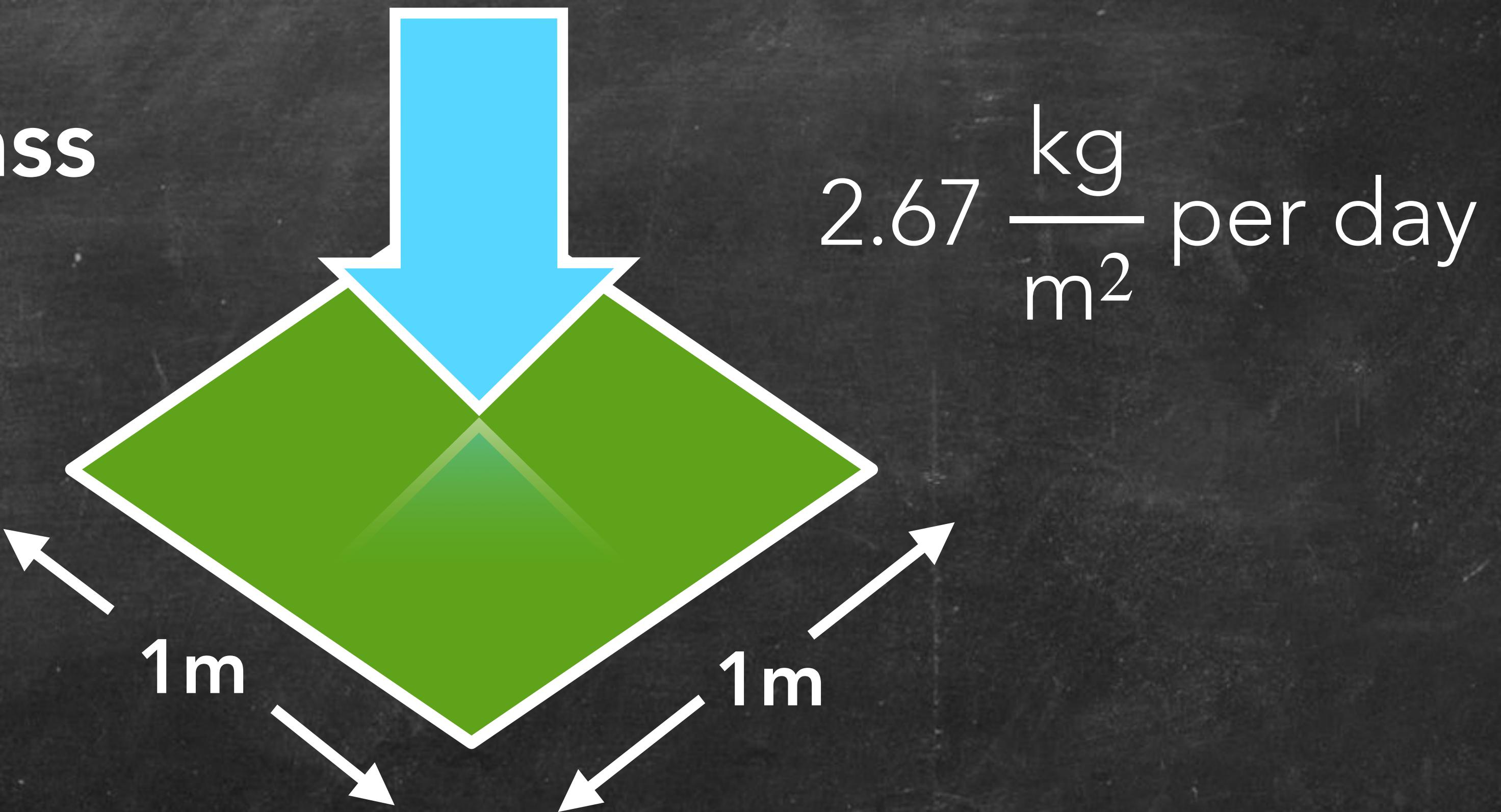
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Global Average Rainfall:  $2.67 \frac{\text{kg}}{\text{m}^2}$  per day

Rainfall is a **mass** flux!



# Flows vs. Fluxes

DESCRIPTION	MASS EXAMPLE	MASS UNITS	ENERGY EXAMPLE	ENERGY UNITS
Flow	A <b>quantity</b> per unit time	Streamflow	$\frac{\text{kg}}{\text{s}}$	Heat Flow $\frac{\text{J}}{\text{s}}$
Flux	A <b>quantity</b> per unit time per unit area	Evaporation	$\frac{\text{kg}}{\text{m}^2\text{s}}$	Evaporation $\frac{\text{J}}{\text{m}^2\text{s}}$ or $\frac{\text{W}}{\text{m}^2}$

# EXTENSIVE VS. INTENSIVE

## Extensive Measures

Extensive measures are properties that depend on the size or extent of a system

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Intensive measures are properties that do not depend on the size or extent of a system

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## Extensive Measures

Extensive measures are properties that depend on the size or extent of a system

- Heat content (J)
- Mass (kg)
- Volume ( $m^3$ )
- Area ( $m^2$ )
- Flow (kg/s)

## Intensive Measures

Intensive measures are properties that do not depend on the size or extent of a system

- Mass density ( $kg/m^3$ )
- Temperature
- Soil Moisture ( $kg/m^3$ )
- Flux ( $kg/m^2/s$ )

# Catchment Water Balance

$P$ : Precipitation

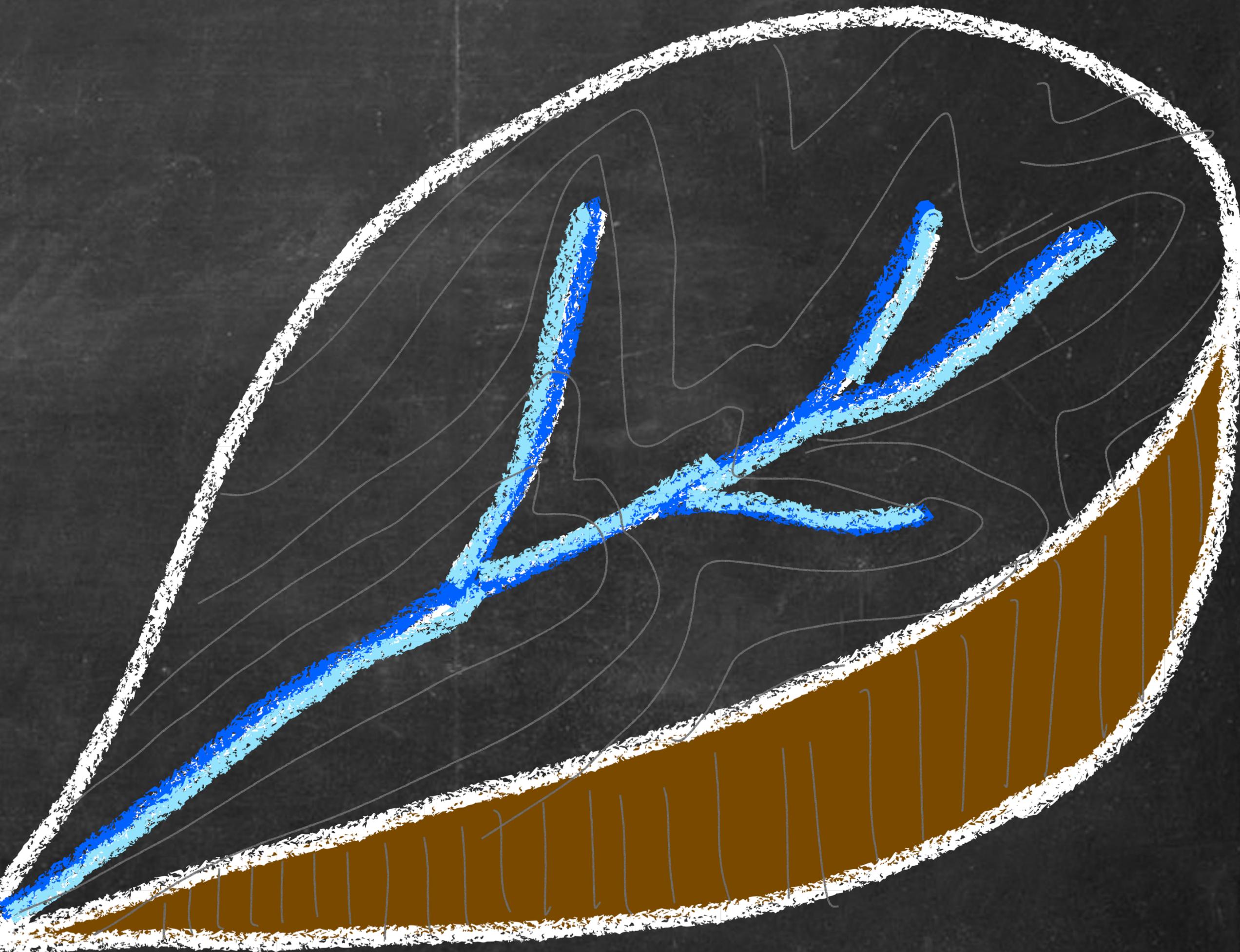
$ET$ : Evapotranspiration

$Q$ : Streamflow

$S$ : Soil Water Storage

$R_c$ : Runoff Coefficient =  $\frac{Q}{P}$

Assumes no groundwater  
flows between basins



$$\frac{dS}{dt} = P - ET - Q$$