# Supplementary Materials of "A Relation-and-Regression-assisted Evolutionary Algorithm for Expensive Constrained Multi-objective Optimization"

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### I. GENERAL FRAMEWORK OF RCMOEA

RCMOEA adopts the two-stage strategy for handling expensive CMOPs, for it accelerates the convergence and promotes the diversity of the population with only a few generations [1] [2]. As illustrated in Fig. 1, in the beginning, RCMOEA initializes the solution population P and an empty archive A that stores solutions evaluated by expensive objectives and constraints. After evaluating solutions in P, a CMOP without considering constraints is optimized in the first stage, and the original CMOP is optimized in the second stage. The switching strategy from one stage to the other in RCMOEA is identical to the one in MGSAEA, where the switch is triggered by the maximum change rate  $\gamma$  of ideal points during the past  $\Delta t$  generations. It is calculated in (1):

$$\gamma = \max_{i=1,2,\dots,m} \left\{ \frac{|f_i^t - f_i^{t-\Delta t}|}{\max\{|f_i^{t-\Delta t}|, \delta\}} \right\}$$
(1)

where  $f_i^t$  is the i-th objective value of ideal points in P at the t-th generation, and  $\delta$  is a constant to ensure that the denominator is not zero. The values of  $\Delta$  and  $\delta$  are identical to the ones in MGSAEA, which are 20 and 1e-6, respectively. RCMOEA switches to the second stage if  $\gamma$  is below the threshold  $\lambda$ . The two-stage surrogate-assisted evolutionary search iterates for many generations until the termination condition is met. The optimal solutions in A are the final solutions of RCMOEA.

# II. PERFORMANCE COMPARISON AMONG ALGORITHMS

To gain insight into the optimization results, Fig. 2 visualizes the populations with median IGD obtained by the five compared algorithms on CF2 and LIR-CMOP9 test problem, respectively. In CF2, the CPF shares disconnected

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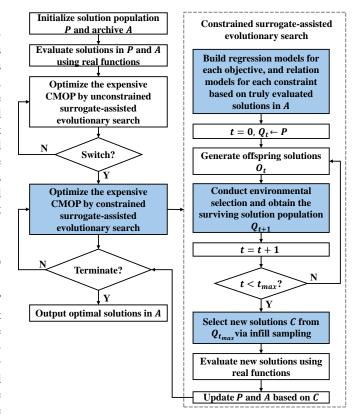


Fig. 1: A general overview of the proposed RCMOEA framework. The blue shaded boxes indicate the steps where this work makes contributions.

segments with UPF. It can be seen that MultiObjectiveEGO and ASA-MOEA/D cannot approach the CPF. Though KTS and MGSAEA find subsets of CPF, RCMOEA can locate the CPF precisely. That's because RCMOEA prefers solutions with more HVC, which are more likely to drive the solution population toward UPF.

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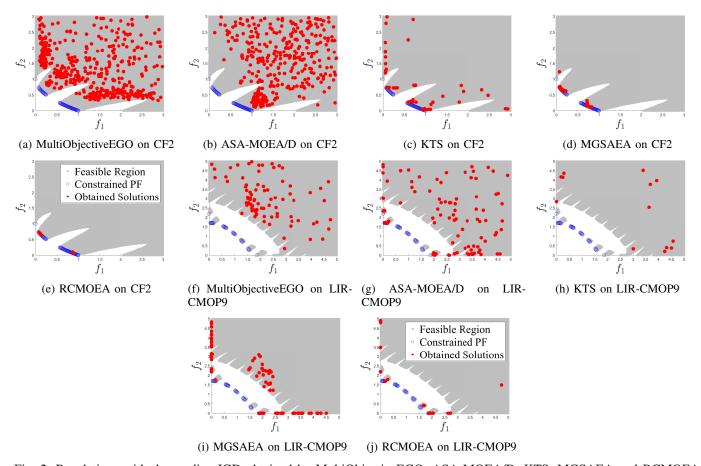


Fig. 2: Populations with the median IGD obtained by MultiObjectiveEGO, ASA-MOEA/D, KTS, MGSAEA and RCMOEA on CF2 and LIR-CMOP9 test problem.

In LIR-CMOP9, the CPF is located in the disjoint and tiny feasible regions obstructed by large infeasible barriers. Hence, to cover CPF, both convergence and diversity should be emphasized during the search. According to Fig. 2, MultiObjectiveEGO and KTS cannot pass through infeasible regions. ASA-MOEA/D and MGSAEA only capture a few subsets of CPF. By contrast, MGSAEA can obtain more solutions on CPF. On the one hand, RCMOEA adopts the two-stage evolutionary search. Since the optimization does not consider constraints in the first stage, the solution population can cross infeasible regions to approach UPF. On the other hand, the proposed RCPD in selecting candidate solutions maintains the diversity of the solution population. Therefore, RCMOEA can cover the disconnected CPF.

## REFERENCES

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