

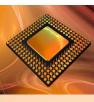


Modern Digital System Design

ECE 2372 / Fall 2018 / Lecture 12

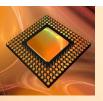
Texas Tech University Dr. Tooraj Nikoubin

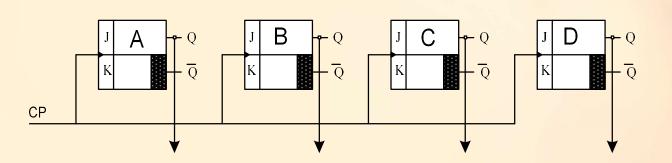
Counters



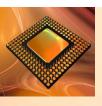


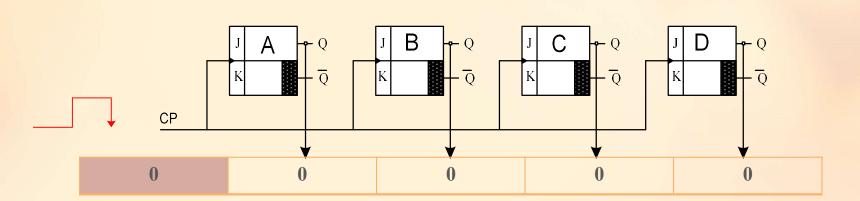
BCD Counter



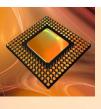






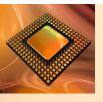


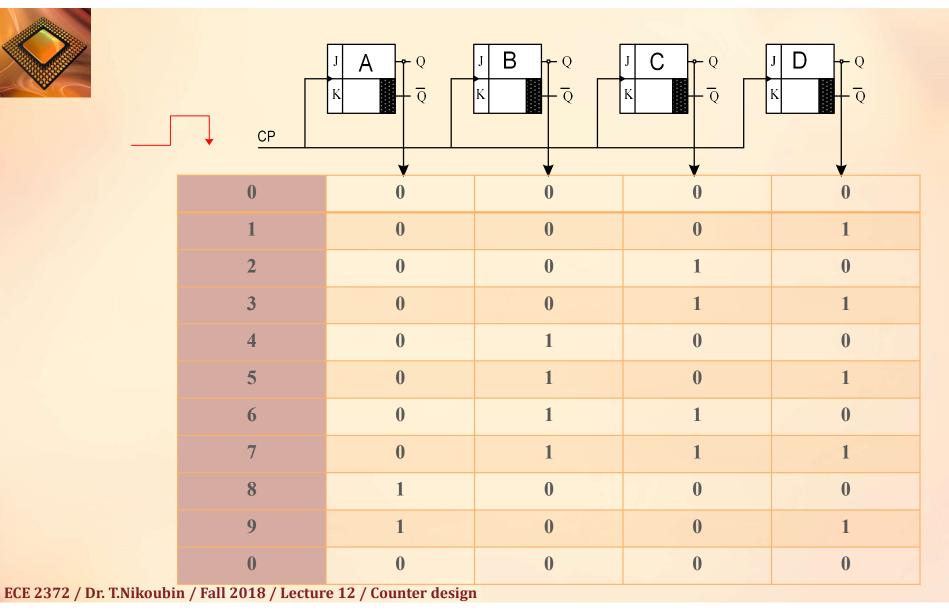


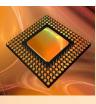




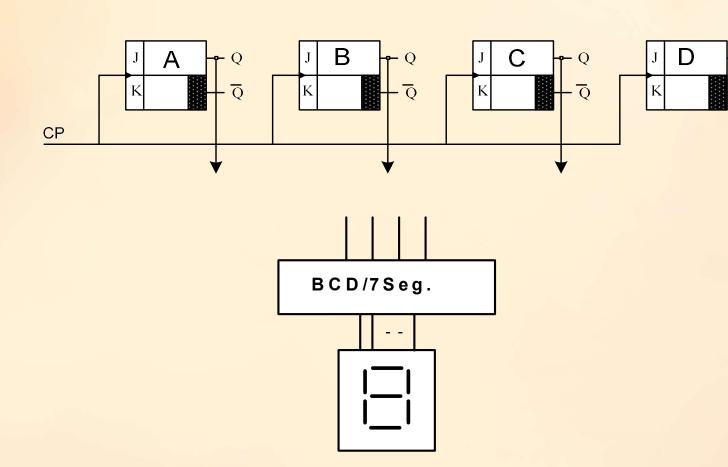
СР		565		J D - Q K - Q
	+	\	\	V
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1

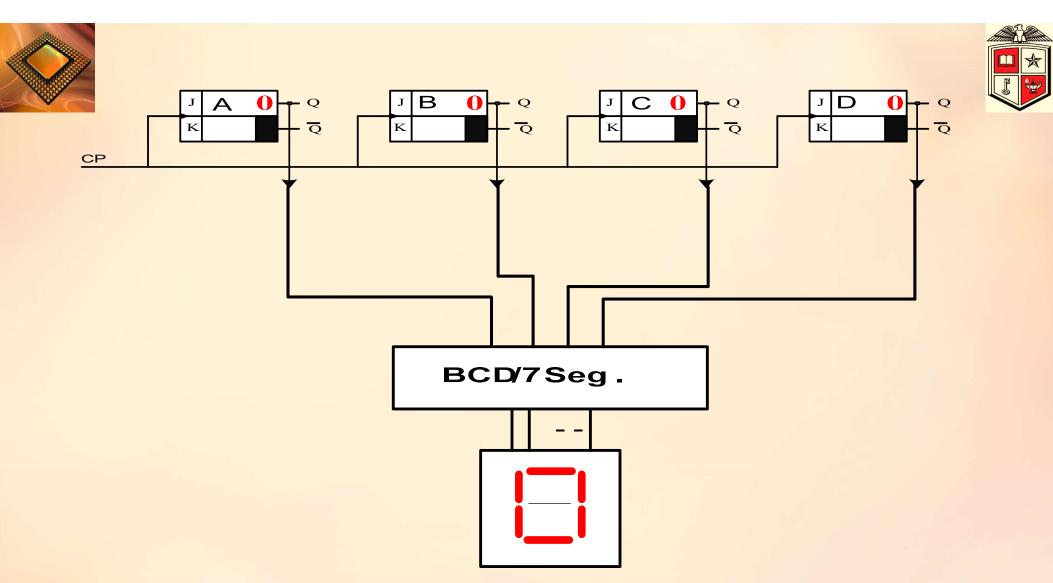


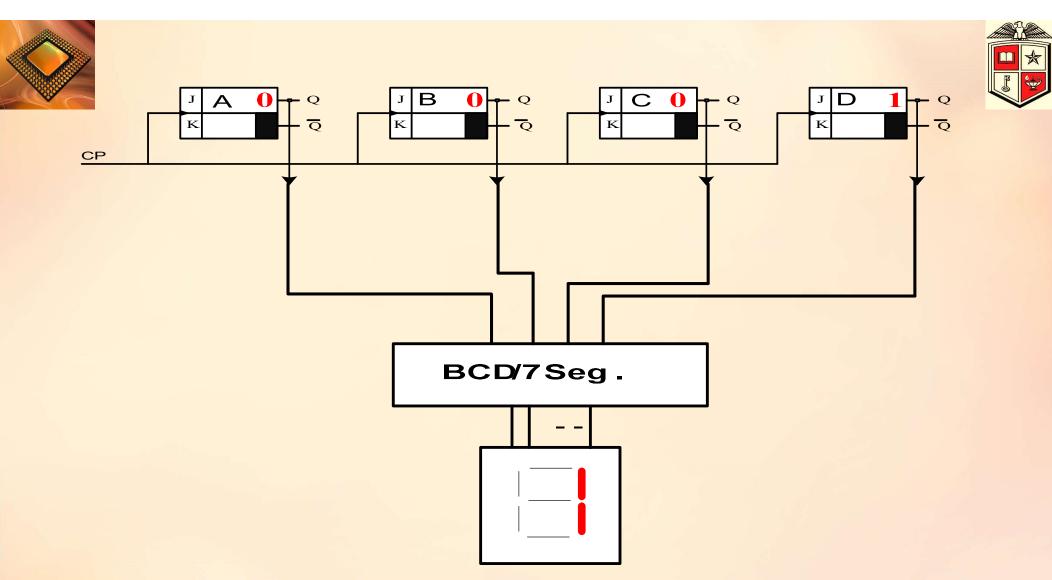


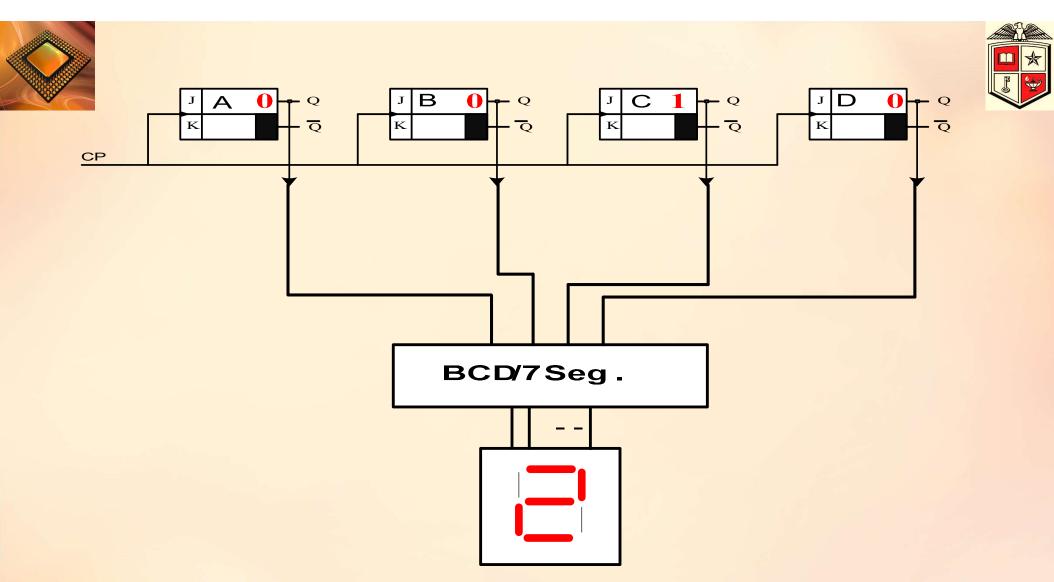


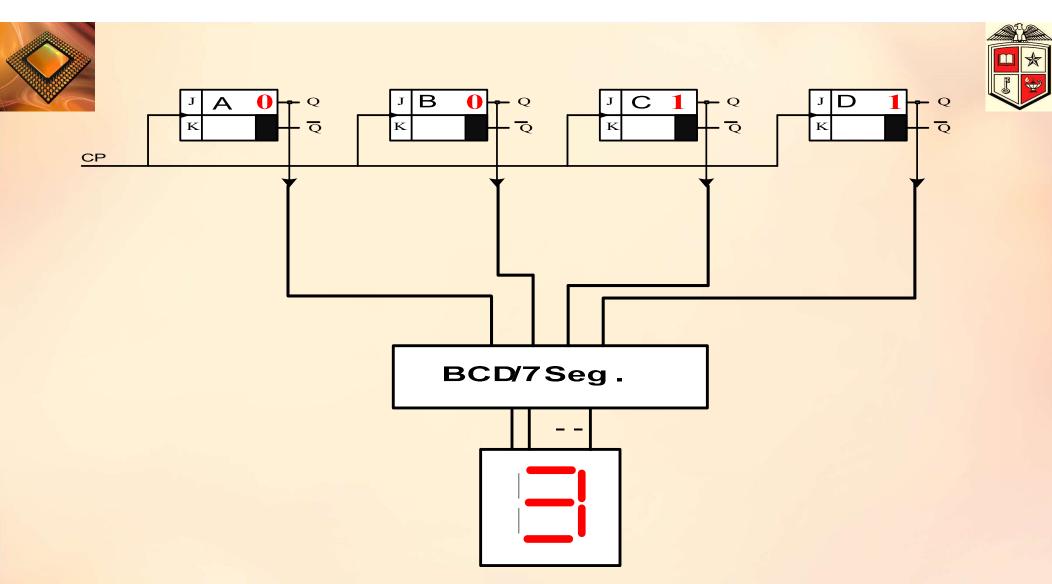


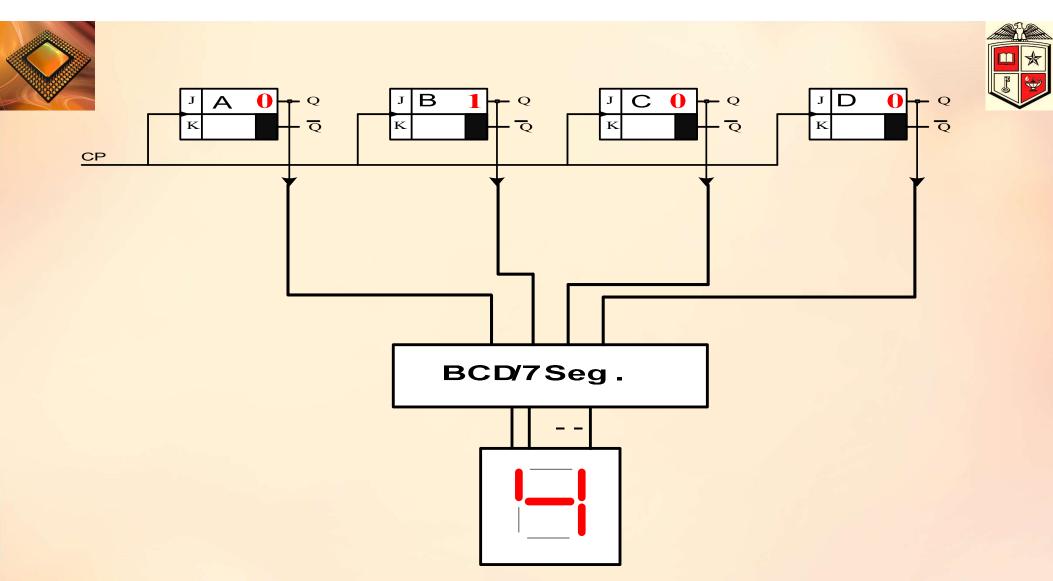


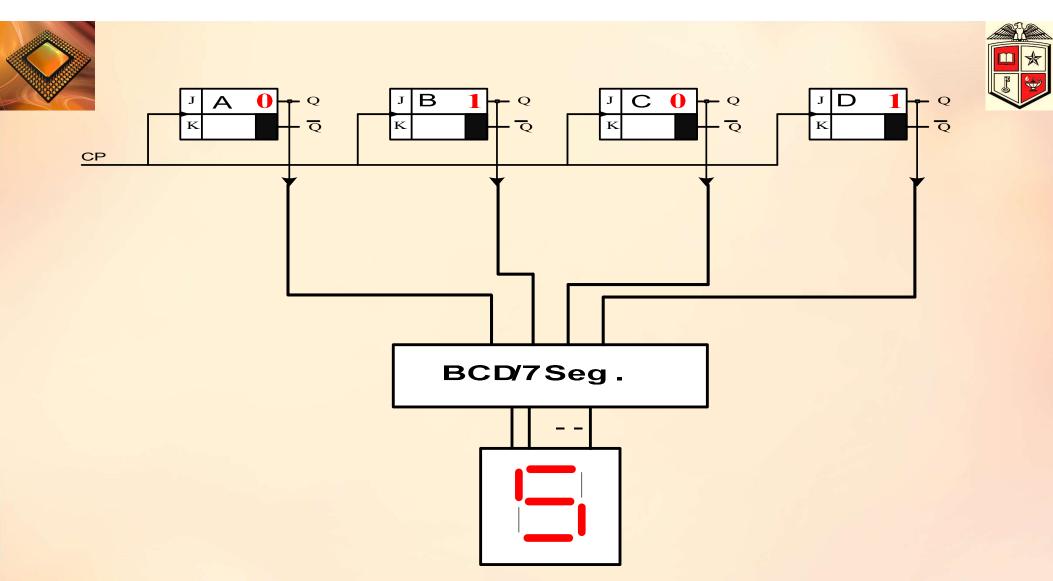


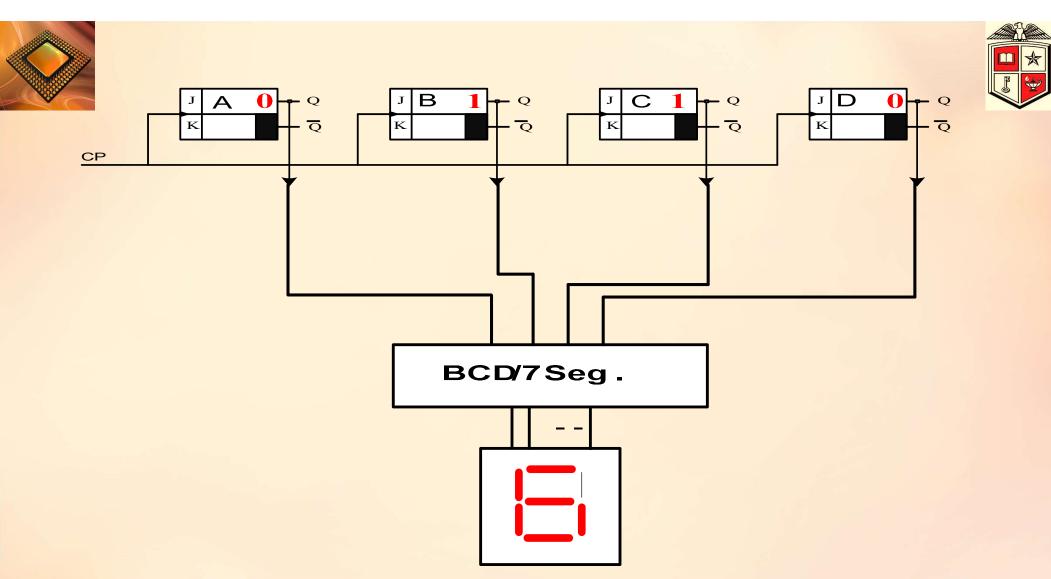


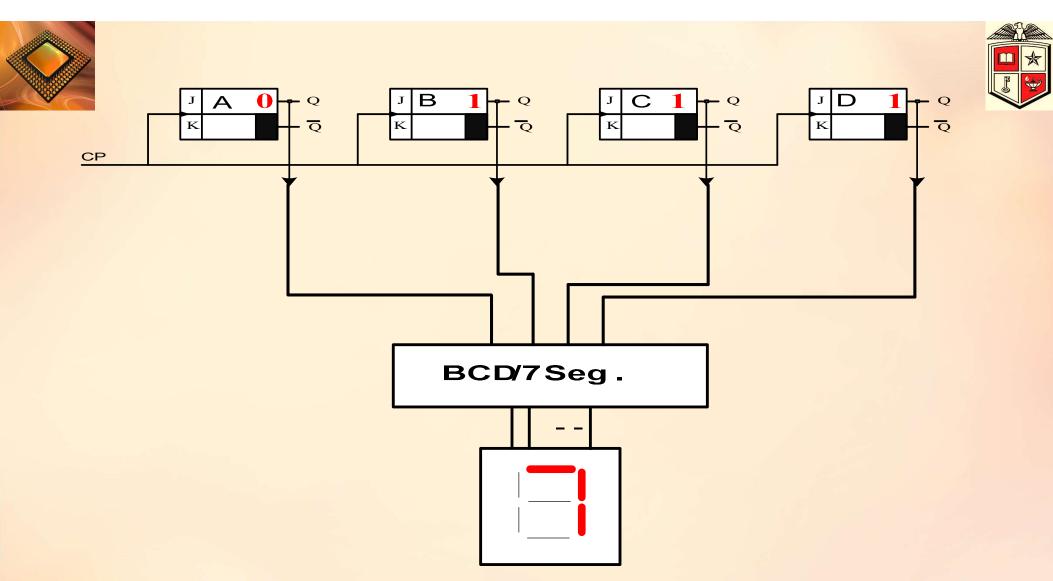


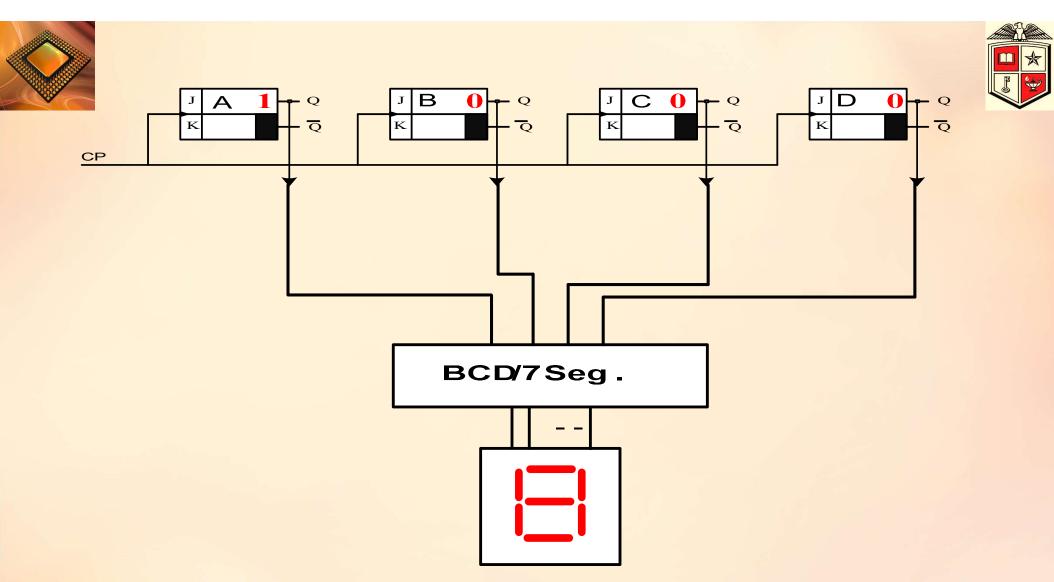


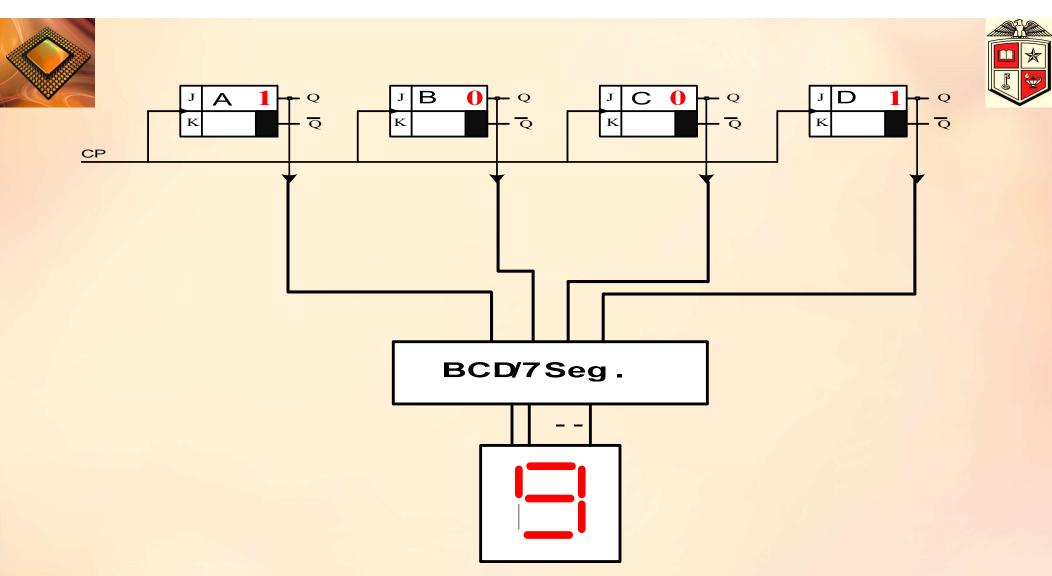


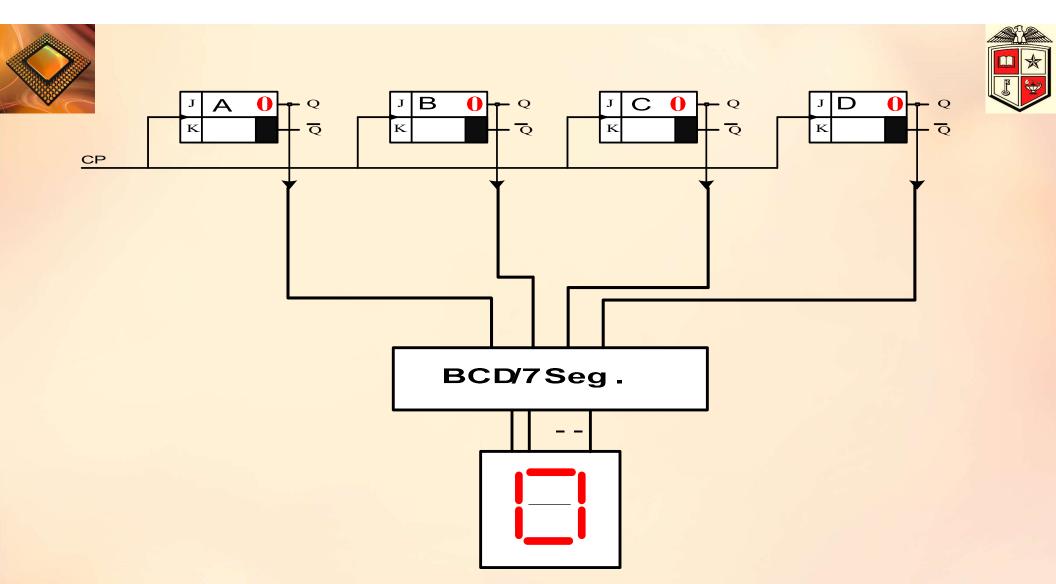


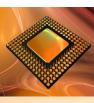






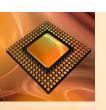








DESIGN OF COUNT UP BCD COUNTER



DESIGN OF COUNT UP BCD COUNTER



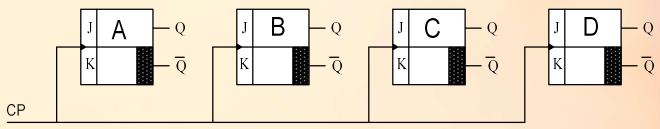
With

- 1- JK-MS-FF
- 2-RS-FF
- 3- D-FF
- 4- T-FF





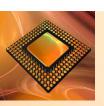
BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		



$$Ji = \sum m(0 \Rightarrow 1)$$

$$Ki = \sum m(1 \Rightarrow 0)$$

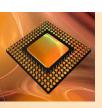
ECE 2372 / Dr. T.Nikoubin / Fall 2018 / Lecture 12 / Counter design





BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		

 $JD = \sum m(0,2,4,6,8)$

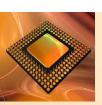




BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		

$$JD=\sum m(0,2,4,6,8)$$

 $KD=\sum m(1,3,5,7,9)$



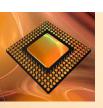


BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		

$$JD = \sum m(0,2,4,6,8)$$

$$KD = \sum m(1,3,5,7,9)$$

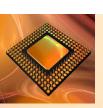
$$JC = \sum m(1,5)$$





BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	• 0	• 0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		

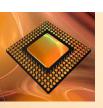
$JD = \sum m(0,2,4,6,8)$	
$KD = \sum m(1,3,5,7,9)$	
$JC = \sum m(1,5)$	
$KC = \sum m(3,7)$	





BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	• 0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		

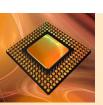
$JD = \sum m(0,2,4,6,8)$
$KD = \sum m(1,3,5,7,9)$
$JC=\sum m(1,5)$
$KC=\sum m(3,7)$
$JB=\sum m(3)$





BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	_1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		

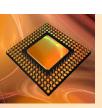
$JD = \sum m(0,2,4,6,8)$
$KD = \sum m(1,3,5,7,9)$
$JC=\sum m(1,5)$
$KC = \sum m(3,7)$
$JB=\sum m(3)$
$KB=\sum m(7)$





BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	• 0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0		
9	1	0	0	1		
0	0	0	0	0		

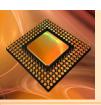
$JD = \sum m(0,2,4,6,8)$
$KD = \sum m(1,3,5,7,9)$
$JC=\sum m(1,5)$
$KC = \sum m(3,7)$
$JB=\sum m(3)$
$KB=\sum m(7)$
$JA = \sum m(7)$





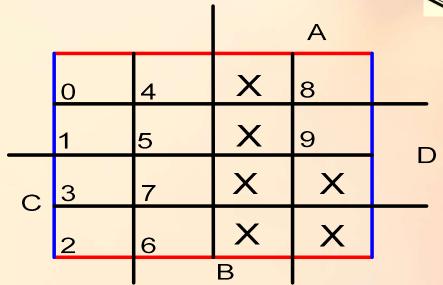
BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	• 0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	• 0	0		
9	_1	0	0	1		
0	0	0	0	0		

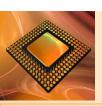
$JD = \sum m(0,2,4,6,8)$	
$KD = \sum m(1,3,5,7,9)$	
$JC = \sum m(1,5)$	
$KC = \sum m(3,7)$	
$JB=\sum m(3)$	
$KB=\sum m(7)$	
$JA=\sum m(7)$	
$KA = \sum m(9)$	





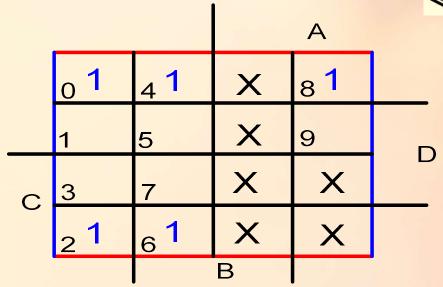
$$JD = \sum m(0,2,4,6,8) =$$

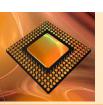






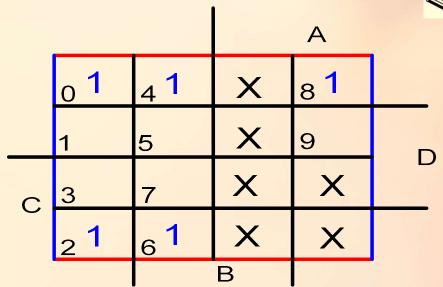
$$JD = \sum m(0,2,4,6,8) =$$

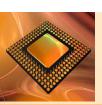






$$JD = \sum m(0,2,4,6,8) = D'$$



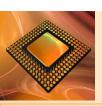




$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) =$$

				Α	
	0	4	X	8	
	₁ 1	₅ 1	X	91	D
С	₃ 1	₇ 1	X	X	
	2	6	X	X	
			В		

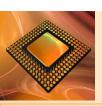




$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

				Α	
	0	4	X	8	
	₁ 1	₅ 1	X	91	D
С	₃ 1	₇ 1	X	X	
J	2	6	X	X	
			В		



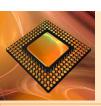


$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC = \sum m(1,5) =$$

				Α	
	0	4	X	8	
	1 1	₅ 1	X	9	D
С	3	7	X	X	
	2	6	X	X	
			В		



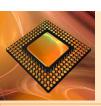


$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

		1	1		
				Α	
	0	4	X	8	
	1 1	₅ 1	X	9	D
С	3	7	X	X	
J	2	6	X	X	
			В		





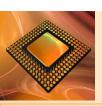
$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) =$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	₃ 1	₇ 1	X	X	
	2	6	X	X	
			В		





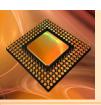
$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	₃ 1	₇ 1	X	X	
	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

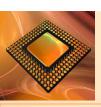
$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

$$JB=\sum m(3)=$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	₃ 1	7	X	X	
J	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

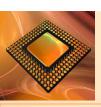
$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

$$JB = \sum m(3) = B'CD$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	₃ 1	7	X	X	
	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

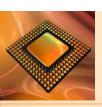
$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

$$JB = \sum m(3) = B'CD$$

$$KB = \sum m(7) =$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	3	₇ 1	X	X	
	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

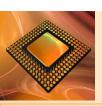
$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

$$JB = \sum m(3) = B'CD$$

$$KB = \sum m(7) = BCD$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	3	7 1	X	X	
	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

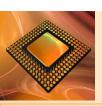
$$KC = \sum m(3,7) = CD$$

$$JB = \sum m(3) = B'CD$$

$$KB = \sum m(7) = BCD$$

$$JA = \sum m(7) =$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	3	₇ 1	X	X	
)	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

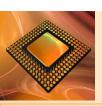
$$KC = \sum m(3,7) = CD$$

$$JB = \sum m(3) = B'CD$$

$$KB = \sum m(7) = BCD$$

$$JA = \sum m(7) = BCD$$

				Α	
	0	4	X	8	
	1	5	X	9	D
С	3	7 1	X	X	
O	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

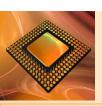
$$JB = \sum m(3) = B'CD$$

$$KB = \sum m(7) = BCD$$

$$JA = \sum m(7) = BCD$$

$$KA = \sum m(9) =$$

				Α	
	0	4	X	8	
	1	5	X	₉ 1	D
С	3	7	X	X	
	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

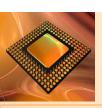
$$JB = \sum m(3) = B'CD$$

$$KB = \sum m(7) = BCD$$

$$JA = \sum m(7) = BCD$$

$$KA = \sum m(9) = AD$$

				Α	
	0	4	X	8	
	1	5	X	₉ 1	D
С	3	7	X	X	
	2	6	X	X	
			В		





$$JD = \sum m(0,2,4,6,8) = D'$$

$$KD = \sum m(1,3,5,7,9) = D$$

$$JC=\sum m(1,5)=A'C'D$$

$$KC = \sum m(3,7) = CD$$

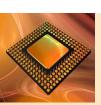
$$JB = \sum m(3) = B'CD$$

$$KB = \sum m(7) = BCD$$

$$JA = \sum m(7) = BCD$$

$$KA = \sum m(9) = AD$$

Without Simplification JK-MS-FF





$$JD = \sum m(0,2,4,6,8) = D' = 1$$

$$KD = \sum m(1,3,5,7,9) = D = 1$$

$$JC = \sum m(1,5) = A'C'D = A'D$$

$$KC = \sum m(3,7) = 2D = D$$

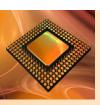
$$JB = \sum m(3) = B'CD = CD$$

$$KB = \sum m(7) = BCD = CD$$

$$JA = \sum m(7) = BCD$$

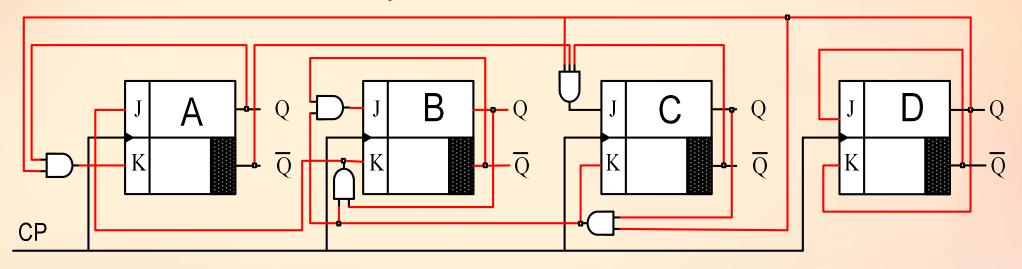
$$KA = \sum m(9) = AD = D$$

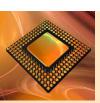
With simplification JK-MS_FF





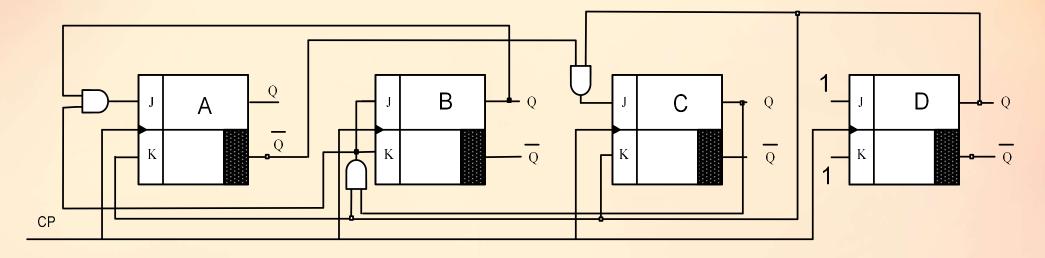
Without Simplification JK_MS_FF

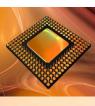




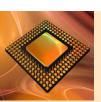


With simplification JK-MS-FF



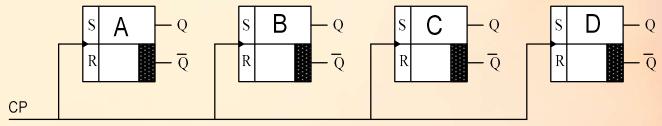






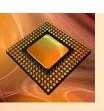


BCD							
	A	В	C	D			
0	0	0	0	0			
1	0	0	0	1			
2	0	0	1	0			
3	0	0	1	1			
4	0	1	0	0			
5	0	1	0	1			
6	0	1	1	0			
7	0	1	1	1			
8	1	0	0	0			
9	1	0	0	1			
0	0	0	0	0			



$$Si = \sum m(0 \Rightarrow 1)$$

$$Ri = \sum m(1 \Rightarrow 0)$$





$$S_D = \sum m(0,2,4,6,8) =$$

$$R_D = \sum m(1,3,5,7,9) =$$

$$Sc = \sum m(1,5) =$$

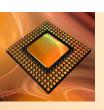
$$Rc = \sum m(3,7) =$$

$$S_B = \sum m(3) =$$

$$R_B = \sum m(7) =$$

$$S_A = \sum m(7) =$$

$$R_A = \sum m(9) =$$





$$S_D = \sum m(0,2,4,6,8) = D'$$

$$R_D = \sum m(1,3,5,7,9) = D$$

$$Sc = \sum m(1,5) = A'C'D$$

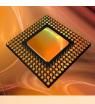
$$Rc = \sum m(3,7) = CD$$

$$S_B = \sum m(3) = B'CD$$

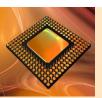
$$R_B = \sum m(7) = BCD$$

$$S_A = \sum m(7) = BCD$$

$$R_A = \sum m(9) = AD$$

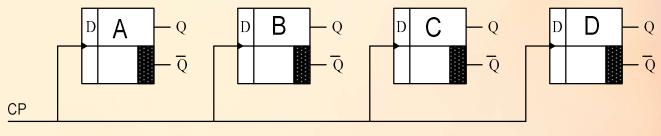




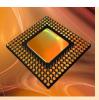




BCD							
	A	В	C	D			
0	0	0	0	0			
1	0	0	0	1			
2	0	0	1	0			
3	0	0	1	1			
4	0	1	0	0			
5	0	1	0	1			
6	0	1	1	0			
7	0	1	1	1			
8	1	0	0	0			
9	1	0	0	1			
0	0	0	0	0			



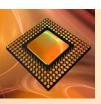
$$Di = \sum m(0 \Rightarrow 1 \& 1 \Rightarrow 1)$$





BCD					
	A	В	C	D	
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0	0	0	0	0	

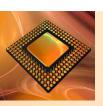
 $D_D = \sum m(0,2,4,6,8)$





BCD					
	A	В	C	D	
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0 ECE 2272	0	0	0	0 ture 12: / C	

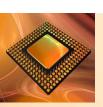
$D_D = \sum m($	0,2,4,6,8)
$D_{C}=\sum m($	1,2,5,6)





BCD					
	A	В	C	D	
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0	0	0	0	0	

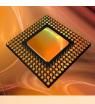
$D_D = \sum m($	0,2,4,6,8)
$D_{C}=\sum m($	1,2,5,6)
$D_B = \sum m($	3,4,5,6)





BCD					
	A	В	C	D	
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0	0	0	0	0	

$D_D = \sum m($	0,2,4,6,8)
$Dc = \sum m($	1,2,5,6)
$D_B = \sum m($	3,4,5,6)
$D_A = \sum m($	7,8)

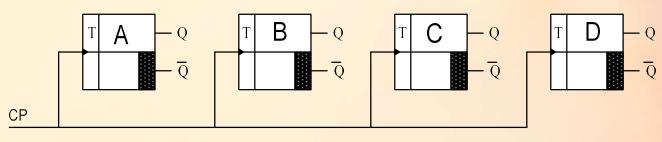








BCD					
	A	В	C	D	
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0	0	0	0	0	



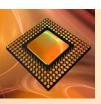
$$Ti = \sum m(0 \Rightarrow 1 \& 1 \Rightarrow 0)$$





BCD					
	A	В	C	D	
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0 <	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0	0	0	0	0	

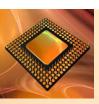
$$T_D = \sum m(0,1,2,3,4,5,6,7,8,9)$$





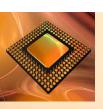
	BCD					
	A	В	C	D	$T_D=$	
0	0	0	0	0	$T_{c}=$	
1	0	0	0	1		
2	0	0	1	0		
3	0	0	1	1		
4	0	1	0	0		
5	0	1	0	1		
6	0	1	1	0		
7	0	1	1	1		
8	1	0	0	0 <		
9	1	0	0	1		
0 ECE 2272	0 / Dr. T.Nilz	0 oubin / Fal	0	0 cture 12 /	Counter desig	

$$T_D = \sum m(0,1,2,3,4,5,6,7,8,9)$$
 $T_C = \sum m(1,3,5,7)$





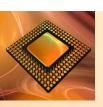
BCD					
	A	В	C	D	
0	0	0	0	0	
1	0	0	0	1	
2	0	0	1	0 🗲	
3	0	0	1	1	
4	0	1	0	0 🗲	
5	0	1	0	1	
6	0	1	1	0 🗲	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0	0	0	0	0	





BCD						
	A	В	C	D		
0	0	0	0	0		
1	0	0	0	1		
2	0	0	1	0 🗲		
3	0	0	1	1		
4	0	1	0	0 🗲		
5	0	1	0	1		
6	0	1	1	0 🗲		
7	0	1	1	1		
8	1	0	0	0 🗲		
9	1	0	0	1		
0	O TAN	0	0	oture 12 / C		

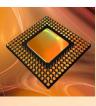
$T_D = \sum m(0,1,2,3,4,5,6,7,8,9)$
$T_{c}=\sum m(1,3,5,7)$
$T_{B}=\sum m(3,7)$
$T_A = \sum m(7,9)$





BCD					
	A	В	С	D	$T_D = \sum_{i=1}^{n} T_i $
0	0	0	0	0	$T_{c}=$
1	0	0	0	1	T ₂ -1
2	0	0	1	0	1 B-7
3	0	0	1	1	$T_A = 1$
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0 ECE 2372	/ Dr. T.Nik	0 oubin / Fal	0 l 2018 / Le	0 cture 12 /	Counter design

$T_D = \sum m(0,1,2,3,4,5,6,7,8,9)$
$T_c = \sum m(1,3,5,7)$
$T_{\rm B}=\sum m(3,7)$
$T_A = \sum m(7,9)$

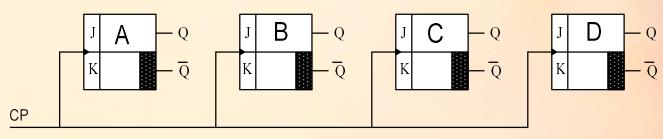








BCD						
	A	В	C	D		
9	1	0	0	1		
8	1	0	0	0		
7	0	1	1	1		
6	0	1	1	0		
5	0	1	0	1		
4	0	1	0	0		
3	0	0	1	1		
2	0	0	1	0		
1	0	0	0	1		
0	0	0	0	0		
9	1	0	0	1		

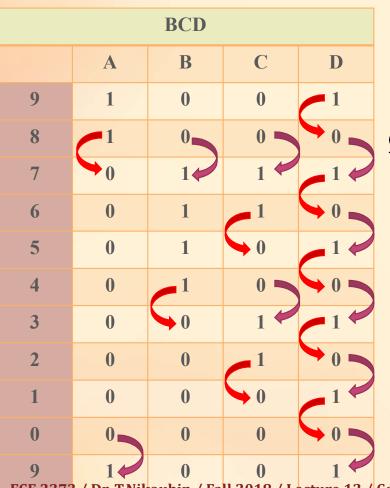


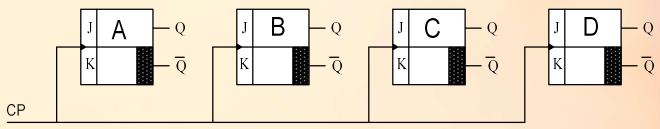
$$Ji = \sum m(0 \Rightarrow 1)$$

$$Ki = \sum m(1 \Rightarrow 0)$$





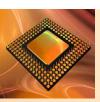




$$Ji = \sum m(0 \Rightarrow 1)$$

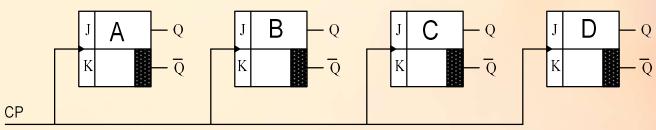
$$Ki = \sum m(1 \Rightarrow 0)$$

70



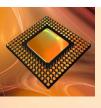


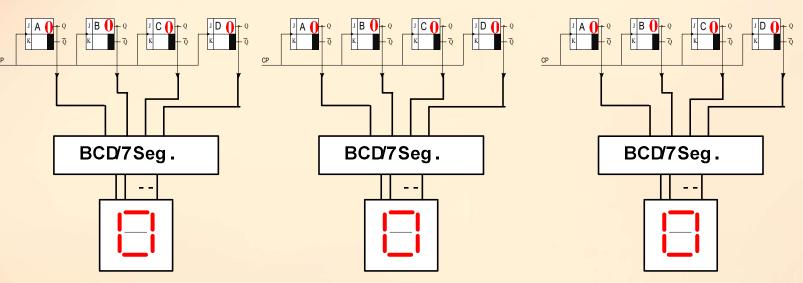
BCD							
	A	В	С	D			
9	1	0	0	1			
8	_1	0	0	0			
7	0	1	1	1			
6	0	1	1	0			
5	0	1	0	1			
4	0	1	0	0			
3	0	0	1	1			
2	0	0	1	0			
1	0	0	• 0	1			
0	0	0	0	0			
9 ECE 2272	Dr. TNSk	0	0	1 cture 12 / C			



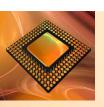
$$Ji = \sum m(0 \Rightarrow 1)$$

$$Ki = \sum m(1 \Rightarrow 0)$$



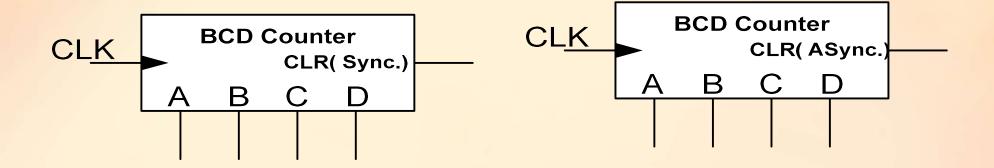


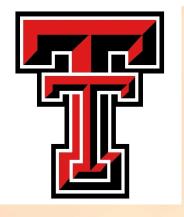
BCD					
	A	В			
0	0	0	0		
1	0	0	0	1	
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	
5	0	1	0	1	
6	0	1	1	0	
7	0	1	1	1	
8	1	0	0	0	
9	1	0	0	1	
0	0	0	0	0	

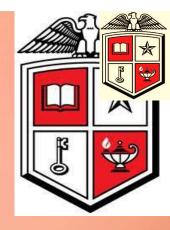


Design of frequency dividers with BCD Counters Design of other counters with BCD Counters









Thank You