

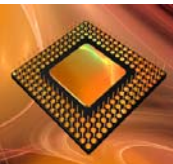


# Modern Digital System Design

ECE 2372 / Fall 2018 / Lecture 6

Texas Tech University  
Dr. Tooraj Nikoubin

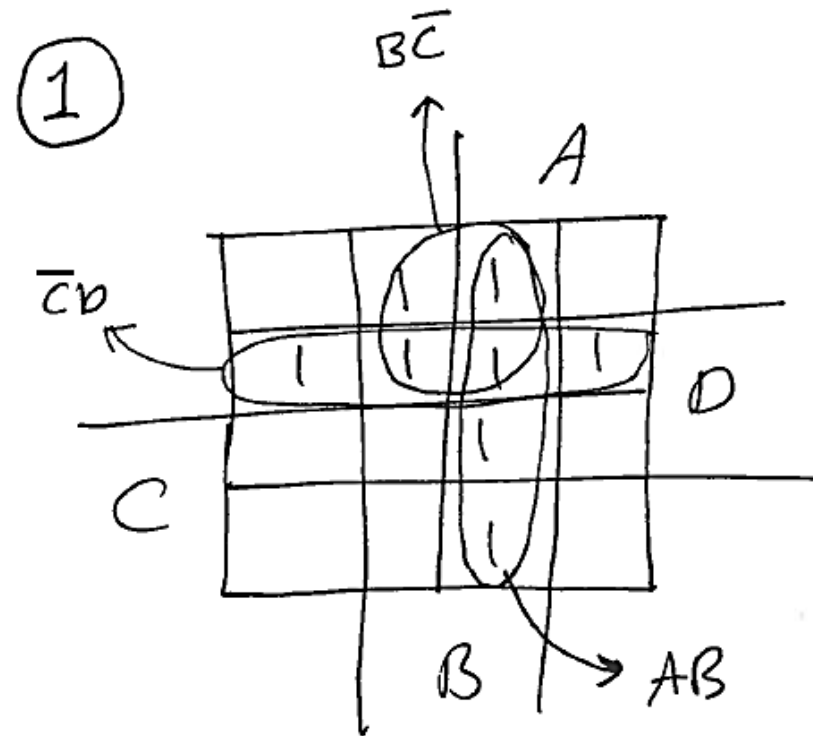
Examples for Karnough map simplification

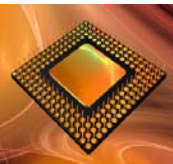


## (SOP) 1

$$Y = \sum m(1, 4, 5, 9, 12, 13, 14, 15)$$

|   |  |   |   |    |    |   |
|---|--|---|---|----|----|---|
|   |  | A |   |    |    |   |
|   |  | 0 | 4 | 12 | 8  |   |
|   |  | 1 | 5 | 13 | 9  |   |
| C |  | 3 | 7 | 15 | 14 | D |
|   |  | 2 | 6 | 14 | 10 |   |
|   |  | B |   |    |    |   |





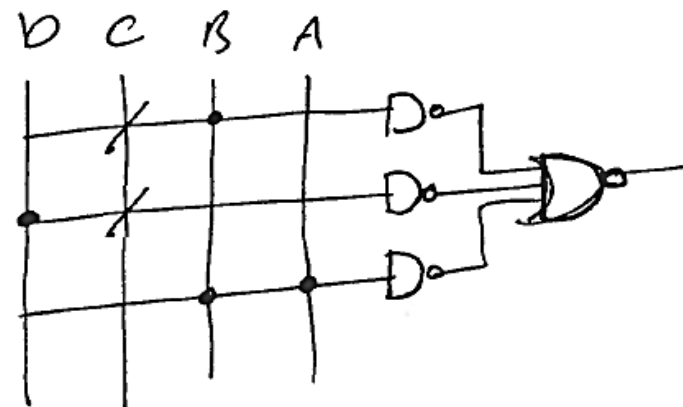
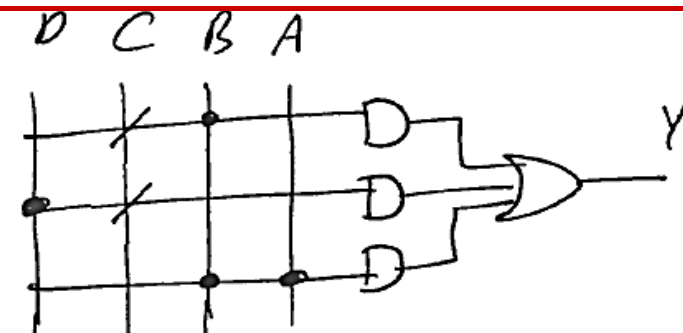
$$Y = B\bar{C} + \bar{C}D + AB$$

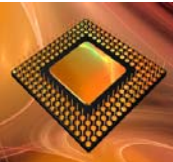
AND-OR

$$Y = B\bar{C} + \bar{C}D + AB$$

$$Y = \overline{\overline{B\bar{C}} \cdot \overline{\bar{C}D} \cdot \overline{AB}}$$

NAND-NAND

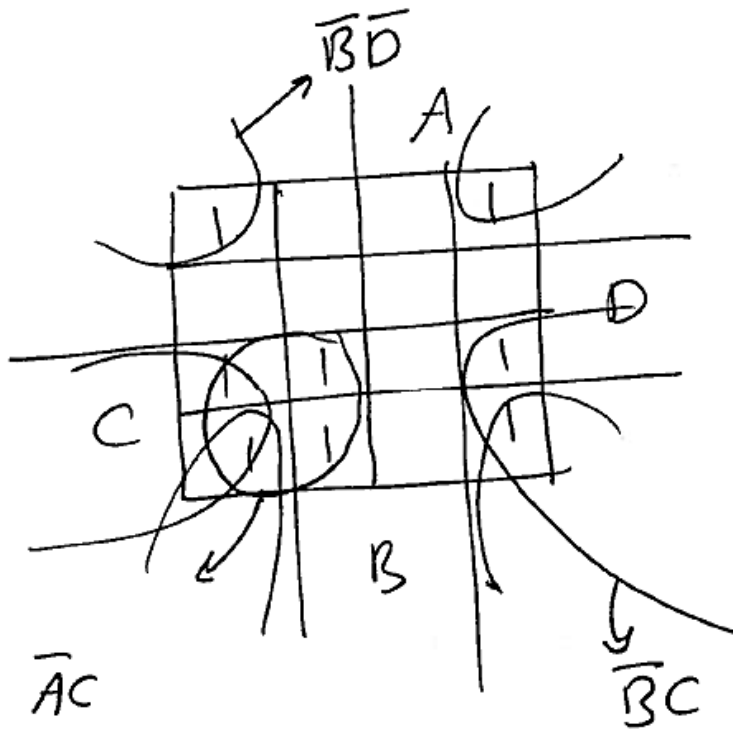




## (SOP) 2

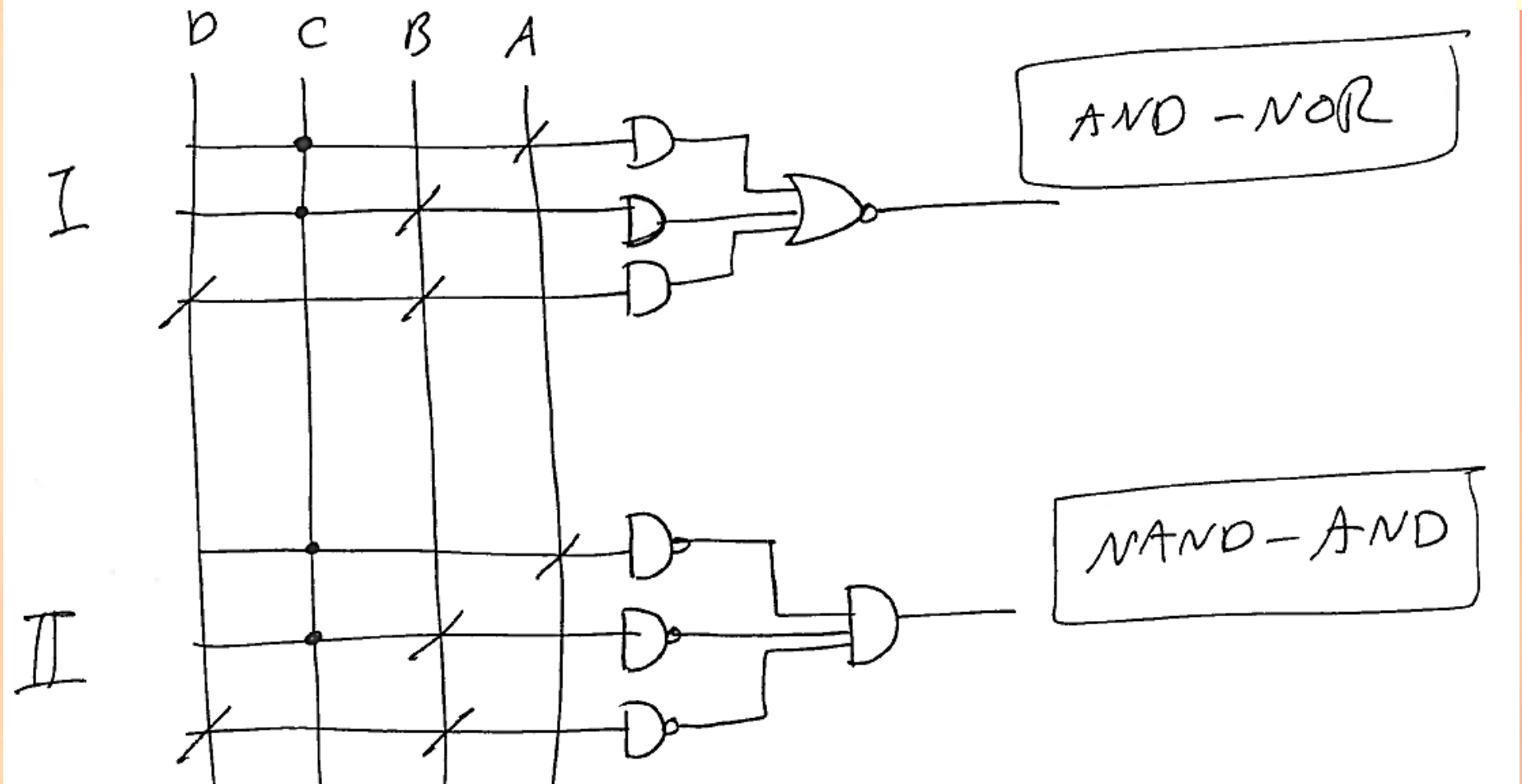
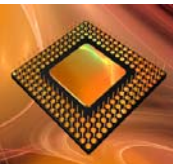


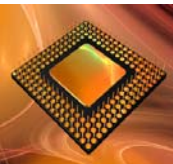
$$Y = \sum m(1, 4, 5, 9, 12, 13, 14, 15)$$



$$Y = \overline{A}C + \overline{B}C + \overline{B}\overline{D} \quad \text{I}$$

$$Y = \overline{A}C \cdot \overline{B}C \cdot \overline{B}\overline{D} \quad \text{II}$$



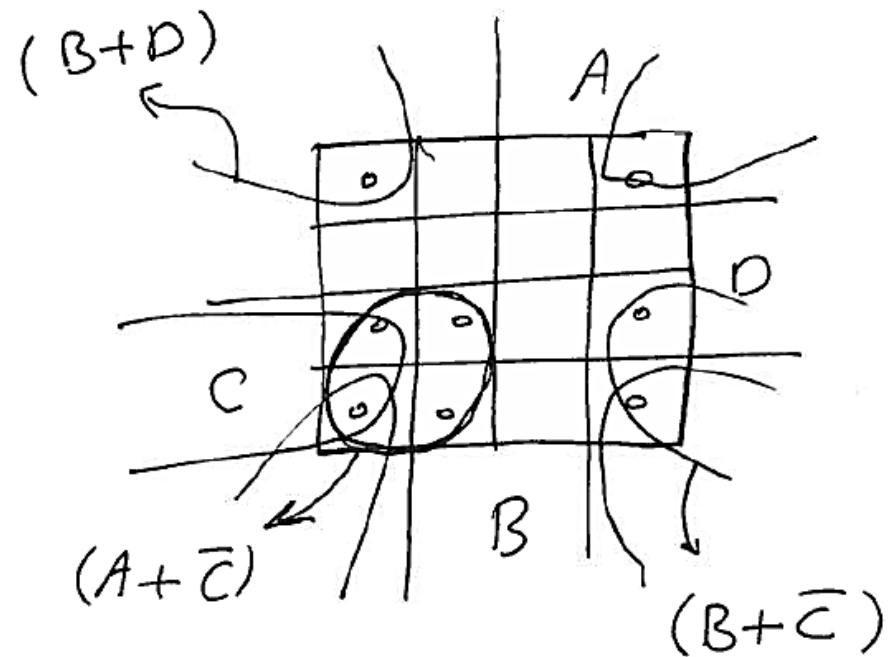


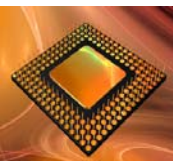
## (POS) 1



$$Y = \sum_m (1, 4, 5, 9, 12, 13, 14, 15)$$

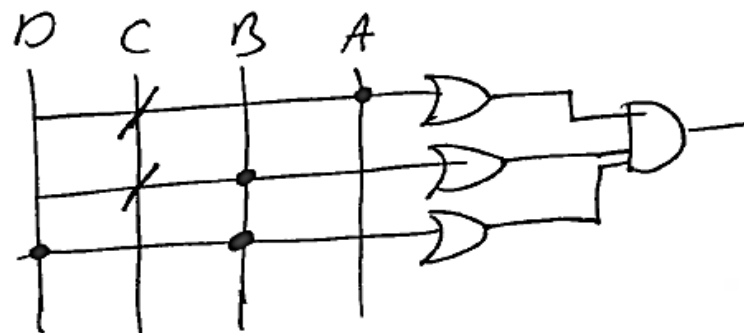
|   | A |   |    |    |   |
|---|---|---|----|----|---|
|   | 0 | 4 | 12 | 8  |   |
|   | 1 | 5 | 13 | 9  |   |
|   | 3 | 7 | 15 | 11 | D |
| C | 2 | 6 | 14 | 10 |   |
|   | B |   |    |    |   |





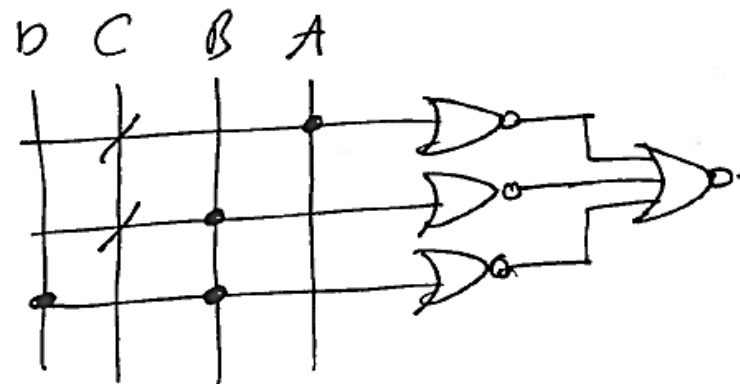
$$Y = (A + \bar{C})(B + \bar{C})(B + D)$$

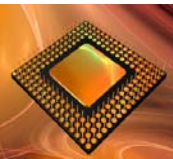
OR-AND



$$Y = \overline{\overline{(A + \bar{C})(B + \bar{C})(B + D)}}$$

$$Y = \overline{(A + \bar{C}) + (B + \bar{C}) + (B + D)}$$

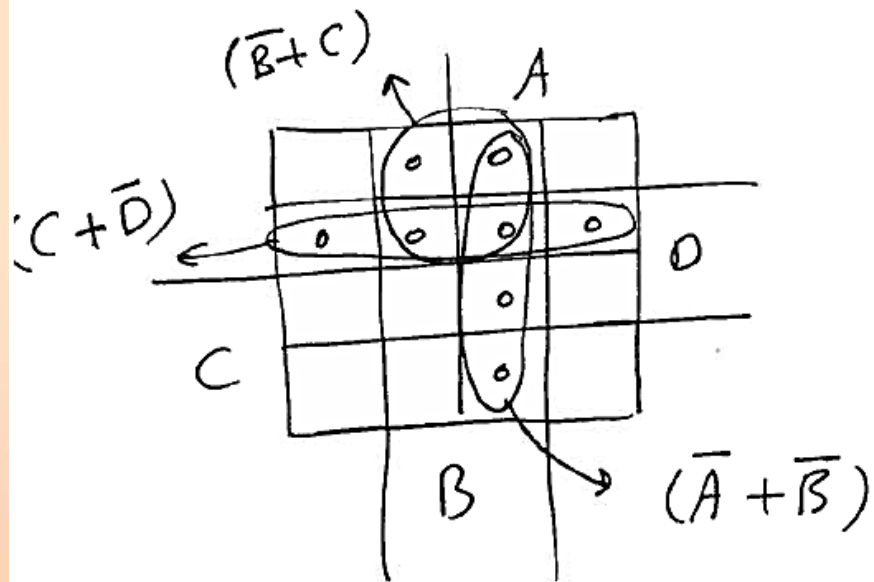




## (POS) 2



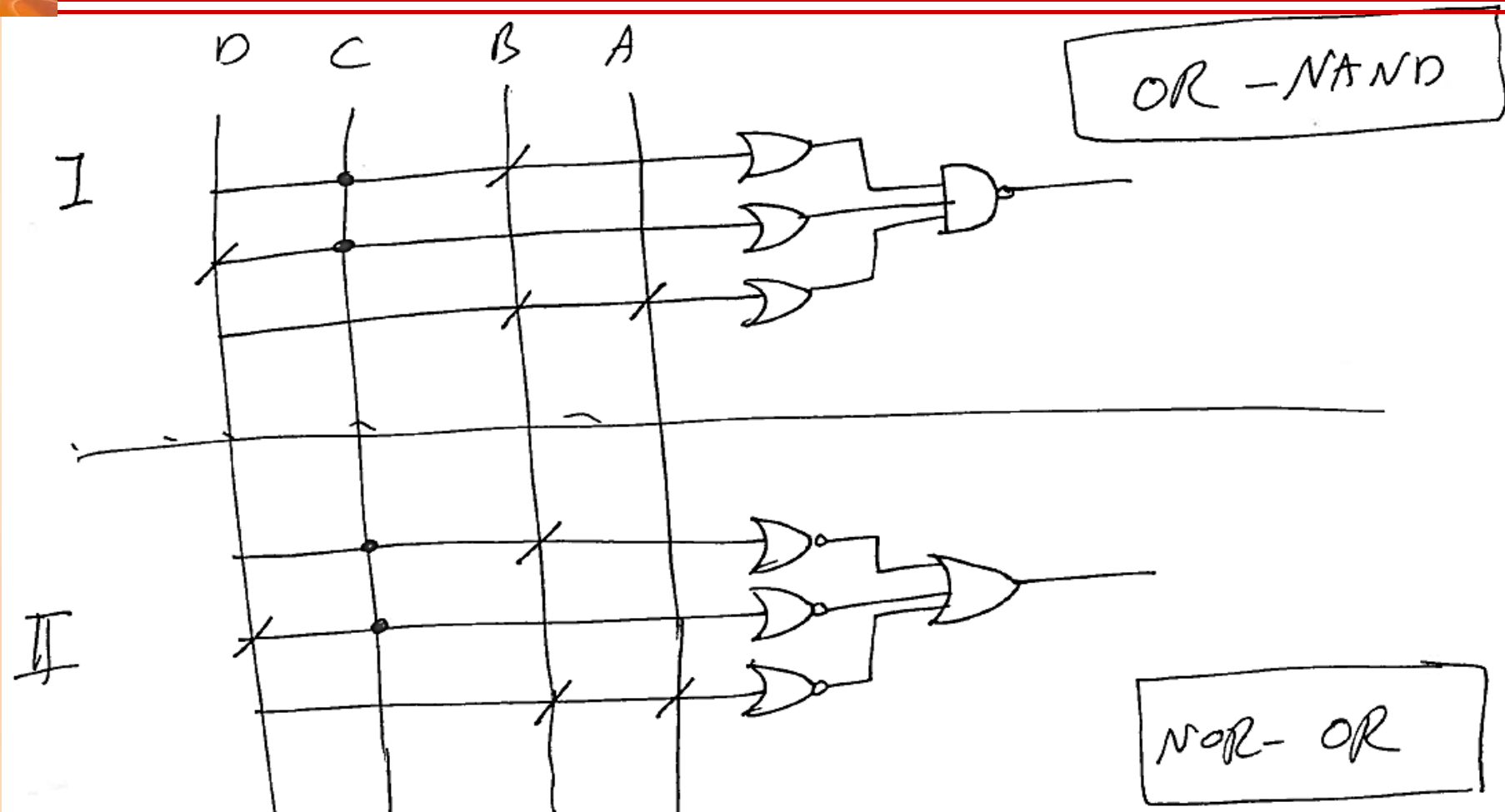
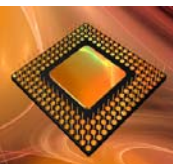
$$Y = \sum_m (1, 4, 5, 9, 12, 13, 14, 15)$$



$$Y = \overline{(B+C)}(C+\overline{D})(\overline{A}+\overline{B}) \quad \text{I}$$

$$Y = \overline{(\overline{B}+C)} + \overline{(C+\overline{D})} + \overline{(\overline{A}+\overline{B})} \quad \text{II}$$







**Thank You**