HW_5_ssingh478

R Markdown

Chapter 10, Exercise 1

Use the prostate data with Ipsa as the response and the other variables as predictors. Implement the following variable selection methods to determine the "best" model.

```
library('faraway')

data(prostate,package='faraway')
lmod<-lm(lpsa~.,data=prostate)
lmod <- update(lmod, . ~ . -gleason)</pre>
```

(a) Backward elimination

First removing 'gleason' predictor->lcp->pgg45->age->lbph.

```
summary(lmod)
```

```
##
## Call:
## lm(formula = lpsa ~ lcavol + lweight + age + lbph + svi + lcp +
##
       pgg45, data = prostate)
##
##
  Residuals:
                      Median
##
       Min
                 10
                                   30
                                           Max
##
  -1.73117 -0.38137 -0.01728 0.43364 1.63513
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.953926
                          0.829439
                                     1.150 0.25319
                          0.086001 6.879 8.07e-10 ***
## lcavol
               0.591615
## lweight
               0.448292
                          0.167771
                                     2.672 0.00897 **
## age
               -0.019336
                          0.011066 -1.747 0.08402 .
## lbph
               0.107671
                          0.058108
                                    1.853 0.06720 .
               0.757734
                          0.241282
                                    3.140 0.00229 **
## svi
## lcp
              -0.104482
                          0.090478 -1.155 0.25127
               0.005318
                          0.003433
                                    1.549 0.12488
## pgg45
## ---
## Signif. codes:
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7048 on 89 degrees of freedom
## Multiple R-squared: 0.6544, Adjusted R-squared: 0.6273
## F-statistic: 24.08 on 7 and 89 DF, p-value: < 2.2e-16
```

```
lmod<-update(lmod,.~.-gleason)
summary(lmod)</pre>
```

```
##
## Call:
## lm(formula = lpsa ~ lcavol + lweight + age + lbph + svi + lcp +
##
      pgg45, data = prostate)
##
## Residuals:
##
       Min
                   Median
                1Q
                                3Q
                                        Max
## -1.73117 -0.38137 -0.01728 0.43364 1.63513
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.953926 0.829439 1.150 0.25319
                        0.086001 6.879 8.07e-10 ***
## lcavol
              0.591615
## lweight
              -0.019336
                        0.011066 -1.747 0.08402 .
## age
## lbph
             0.107671
                        0.058108 1.853 0.06720 .
## svi
              0.757734
                        0.241282 3.140 0.00229 **
## lcp
             -0.104482
                        0.090478 -1.155 0.25127
## pgg45
              0.005318
                        0.003433
                                 1.549 0.12488
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7048 on 89 degrees of freedom
## Multiple R-squared: 0.6544, Adjusted R-squared: 0.6273
## F-statistic: 24.08 on 7 and 89 DF, p-value: < 2.2e-16
```

```
lmod<-update(lmod,.~.-lcp)
summary(lmod)</pre>
```

```
##
## Call:
## lm(formula = lpsa ~ lcavol + lweight + age + lbph + svi + pgg45,
##
       data = prostate)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -1.77711 -0.41708 0.00002 0.40676 1.59681
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.980085
                          0.830665
                                   1.180 0.24116
## lcavol
               0.545770
                          0.076431
                                    7.141 2.31e-10 ***
## lweight
                          0.168078 2.674 0.00890 **
               0.449450
## age
              -0.017470
                          0.010967 -1.593 0.11469
## 1bph
               0.105755
                          0.058191 1.817 0.07249 .
                          0.219757 2.920 0.00442 **
## svi
               0.641666
               0.003528
                          0.003068
                                   1.150 0.25331
## pgg45
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7061 on 90 degrees of freedom
## Multiple R-squared: 0.6493, Adjusted R-squared: 0.6259
## F-statistic: 27.77 on 6 and 90 DF, p-value: < 2.2e-16
```

```
lmod<-update(lmod,.~.-pgg45)
summary(lmod)</pre>
```

```
##
## Call:
## lm(formula = lpsa ~ lcavol + lweight + age + lbph + svi, data = prostate)
##
## Residuals:
##
        Min
                  10
                      Median
                                   30
                                           Max
## -1.83505 -0.39396 0.00414 0.46336 1.57888
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.95100
                          0.83175
                                    1.143 0.255882
## lcavol
                          0.07459
                                    7.583 2.77e-11 ***
               0.56561
## lweight
               0.42369
                          0.16687
                                    2.539 0.012814 *
## age
               -0.01489
                          0.01075 -1.385 0.169528
## lbph
               0.11184
                          0.05805
                                   1.927 0.057160 .
## svi
               0.72095
                          0.20902
                                    3.449 0.000854 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.7073 on 91 degrees of freedom
## Multiple R-squared: 0.6441, Adjusted R-squared: 0.6245
## F-statistic: 32.94 on 5 and 91 DF, p-value: < 2.2e-16
```

```
lmod<-update(lmod,.~.-age)
summary(lmod)</pre>
```

```
##
## Call:
## lm(formula = lpsa ~ lcavol + lweight + lbph + svi, data = prostate)
##
## Residuals:
##
       Min
                      Median
                                   30
                 10
                                           Max
## -1.82653 -0.42270 0.04362 0.47041 1.48530
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                                    0.244 0.80809
## (Intercept) 0.14554
                          0.59747
## lcavol
               0.54960
                          0.07406
                                    7.422 5.64e-11 ***
## lweight
               0.39088
                          0.16600 2.355 0.02067 *
## lbph
               0.09009
                          0.05617
                                    1.604 0.11213
## svi
               0.71174
                          0.20996 3.390 0.00103 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7108 on 92 degrees of freedom
## Multiple R-squared: 0.6366, Adjusted R-squared: 0.6208
## F-statistic: 40.29 on 4 and 92 DF, p-value: < 2.2e-16
```

```
lmod<-update(lmod,.~.-lbph)
summary(lmod)</pre>
```

```
##
## Call:
## lm(formula = lpsa ~ lcavol + lweight + svi, data = prostate)
##
## Residuals:
        Min
                      Median
##
                  1Q
                                   30
                                           Max
## -1.72964 -0.45764 0.02812 0.46403 1.57013
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.26809
                          0.54350 -0.493 0.62298
## lcavol
               0.55164
                          0.07467
                                    7.388 6.3e-11 ***
                                    3.386 0.00104 **
## lweight
               0.50854
                          0.15017
## svi
               0.66616
                          0.20978
                                    3.176 0.00203 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7168 on 93 degrees of freedom
## Multiple R-squared: 0.6264, Adjusted R-squared: 0.6144
## F-statistic: 51.99 on 3 and 93 DF, p-value: < 2.2e-16
```

5

6

7

8

TRUE

TRUE

TRUE

TRUE

TRUE

TRUE

TRUE

TRUE

TRUE TRUE

TRUE

TRUE

TRUE

TRUE TRUE TRUE FALSE

TRUE

TRUE TRUE TRUE TRUE TRUE

(b) AIC:

AIC is minimized by a choice of four parameters, namely lcavol, lweight and svi as determined by the logical matrix.

```
require(leaps)
## Loading required package: leaps
b<-regsubsets(lpsa~.,data=prostate)</pre>
rs<-summary(b)
rs$which
     (Intercept) lcavol lweight
##
                                  age lbph
                                              svi
                                                    1cp gleason pgg45
## 1
            TRUE
                   TRUE
                          FALSE FALSE FALSE FALSE
                                                          FALSE FALSE
## 2
            TRUE
                   TRUE
                           TRUE FALSE FALSE FALSE
                                                          FALSE FALSE
            TRUE
## 3
                   TRUE
                           TRUE FALSE FALSE TRUE FALSE
                                                          FALSE FALSE
            TRUE
                   TRUE
## 4
                           TRUE FALSE TRUE TRUE FALSE
                                                          FALSE FALSE
```

```
AIC <- nrow(prostate)*log(rs$rss/nrow(prostate)) + (2:9)*2
plot(AIC ~ I(1:8), ylab="AIC", xlab="Number of Predictors")
```

TRUE FALSE

TRUE TRUE

FALSE FALSE

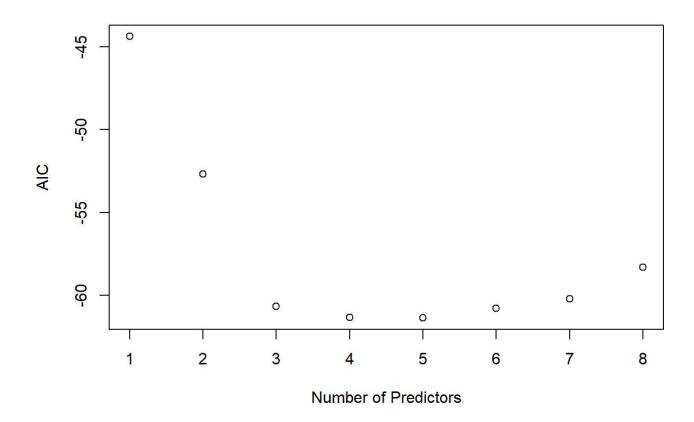
FALSE TRUE

TRUE TRUE

TRUE

FALSE

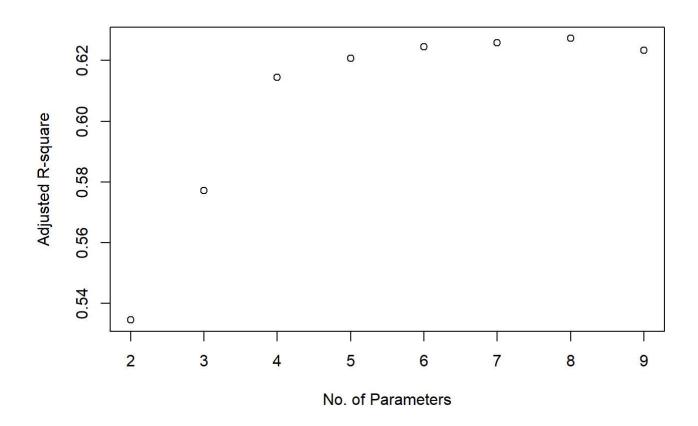
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(c) Adjusted R2

The 7 parameter model with parameters, Icavol, Iweight, age, Ibph, svi and pgg45 as predictors is the clear winner as it is the smallest model that lies below the Cp=p line.

plot(2:9,rs\$adjr2,xlab="No. of Parameters",ylab="Adjusted R-square")



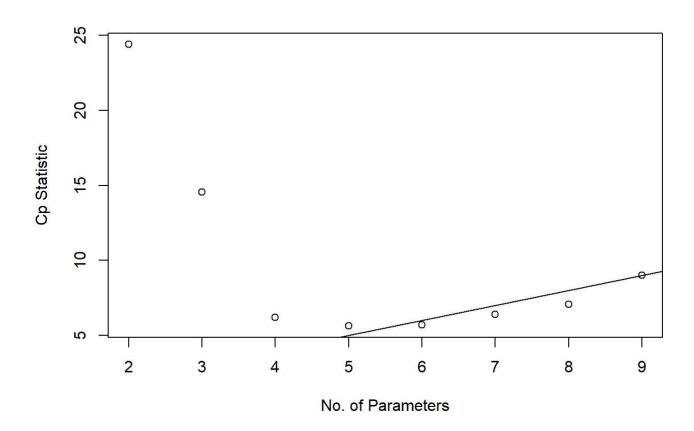
which.max(rs\$adjr2)

[1] 7

(d) Mallows Cp

The 6 parameter model with parameters, Icavol, Iweight, age, Ibph and svi as predictors is the clear winner as it is the smallest model that lies below the Cp=p line.

plot(2:9,rs\$cp,xlab="No. of Parameters",ylab="Cp Statistic")
abline(0,1)



Chapter 11: Exercise 4

Take the fat data, and use the percentage of body fat, siri, as the response and the other variables, except brozek and density as potential predictors. Remove every tenth observation from the data for use as a test sample. Use the remaining data as a training sample building the following models: (a) Linear regression with all predictors (b) Linear regression with variables selected using AIC (c) Principal component regression (d) Partial least squares (e) Ridge regression (f) LASSO regression Use the models you find to predict the response in the test sample. Make a report on the performances of the models

```
data(fat,package='faraway')
fat<-data.frame(fat)
ind <- seq(10, nrow(fat), by=10)
drops <- c("brozek","density")
train_data=fat[-ind,!(names(fat) %in% drops)]
#train_data=train_data[,-(!(names(train_data) %in% drops))]
test_data=fat[ind,!(names(fat) %in% drops)]
#test_data=test_data[,-(!(names(test_data) %in% drops))]</pre>
```

a. Linear regression with all predictors

```
lmod3<-lm(siri~.,data=test_data)
summary(lmod3)</pre>
```

```
##
## Call:
## lm(formula = siri ~ ., data = test_data)
##
## Residuals:
                    Median
##
       Min
                10
                                 3Q
                                        Max
## -0.91300 -0.33943 0.06558 0.28091 0.74021
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -150.28386 53.69480 -2.799
                                           0.0208 *
## age
               -0.01585
                          0.03507 -0.452
                                         0.6619
## weight
                0.03936
                          0.16746
                                  0.235
                                           0.8194
## height
                          0.72677 2.976
                                         0.0155 *
                2.16312
## adipos
                2.21152
                          0.95912 2.306
                                          0.0466 *
## free
               ## neck
               -0.09268
                          0.17480 -0.530
                                         0.6088
## chest
                0.14160
                          0.11043 1.282
                                          0.2318
## abdom
                0.10218
                          0.07521 1.359
                                         0.2074
## hip
               -0.03646
                          0.13089 -0.279
                                           0.7869
## thigh
               -0.01546
                          0.13606 -0.114
                                          0.9120
## knee
               -0.14962
                          0.25385 -0.589
                                          0.5701
## ankle
                0.10486
                          0.37143 0.282
                                          0.7841
                0.47382
## biceps
                          0.16961 2.794
                                           0.0209 *
## forearm
               -0.17431
                          0.24492 -0.712
                                          0.4947
## wrist
                0.75940
                          0.51383 1.478
                                          0.1736
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7632 on 9 degrees of freedom
## Multiple R-squared: 0.9953, Adjusted R-squared: 0.9876
## F-statistic: 128.2 on 15 and 9 DF, p-value: 1.278e-08
```

```
rmse <- function(x,y) sqrt(mean((x-y)^2))
rmse(predict(1mod3), test_data$siri)</pre>
```

```
## [1] 0.4578904
```

(b)Linear regression with variables selected using AIC

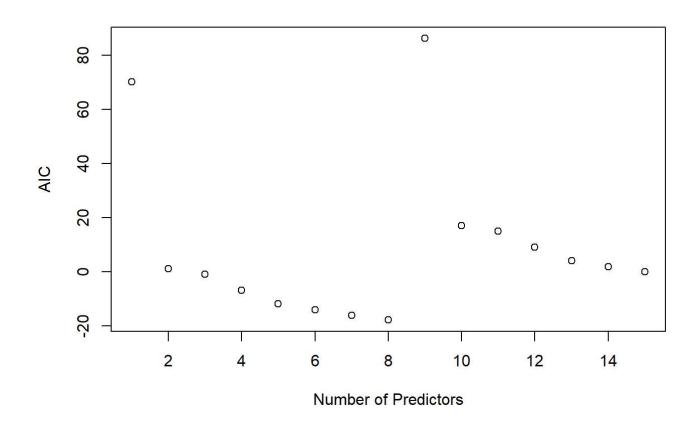
```
require(leaps)
b<-regsubsets(siri~.,data=test_data)
rs1<-summary(b)
rs1$which</pre>
```

```
age weight height adipos free neck chest abdom
##
     (Intercept)
                      FALSE
                                     TRUE FALSE FALSE FALSE FALSE
## 1
           TRUE FALSE
                              FALSE
## 2
           TRUE FALSE
                        TRUE
                              FALSE FALSE TRUE FALSE FALSE FALSE
## 3
           TRUE FALSE
                        TRUE
                              FALSE
                                    FALSE TRUE FALSE FALSE FALSE
## 4
           TRUE FALSE
                      FALSE
                              TRUE
                                     TRUE TRUE FALSE FALSE FALSE
## 5
           TRUE FALSE
                      FALSE
                               TRUE
                                     TRUE TRUE FALSE FALSE TRUE FALSE
## 6
           TRUE FALSE FALSE
                               TRUE
                                     TRUE TRUE FALSE TRUE TRUE FALSE
## 7
           TRUE FALSE FALSE
                               TRUE
                                     TRUE TRUE FALSE TRUE FALSE FALSE
## 8
           TRUE FALSE FALSE
                               TRUE
                                     TRUE TRUE FALSE TRUE TRUE FALSE
##
    thigh knee ankle biceps forearm wrist
## 1 FALSE FALSE FALSE
                       FALSE
                               FALSE FALSE
## 2 FALSE FALSE FALSE
                       FALSE
                               FALSE FALSE
## 3 FALSE FALSE FALSE
                      FALSE
                               FALSE TRUE
## 4 FALSE FALSE FALSE
                               FALSE FALSE
                        TRUE
## 5 FALSE FALSE FALSE
                        TRUE
                               FALSE FALSE
## 6 FALSE FALSE FALSE
                        TRUE
                               FALSE FALSE
## 7 FALSE FALSE FALSE
                        TRUE
                                TRUE TRUE
## 8 FALSE FALSE FALSE
                        TRUE
                                TRUE TRUE
```

```
AIC <- nrow(test_data)*log(rs1$rss/nrow(test_data)) + (2:16)*2
```

```
## Warning in nrow(test_data) * log(rs1$rss/nrow(test_data)) + (2:16) * 2:
## longer object length is not a multiple of shorter object length
```

```
plot(AIC ~ I(1:15), ylab="AIC", xlab="Number of Predictors")
```



#No. of Parameters=8 :Intercept,height, adipos, free, chest, biceps, forearm, wrist

lmodAIC=lm(siri~height+adipos+free+chest+biceps+forearm+wrist,data=train_data)

rmse(predict(lmodAIC), test_data\$siri)

Warning in x - y: longer object length is not a multiple of shorter object ## length

[1] 10.39814

c. Principal component regression

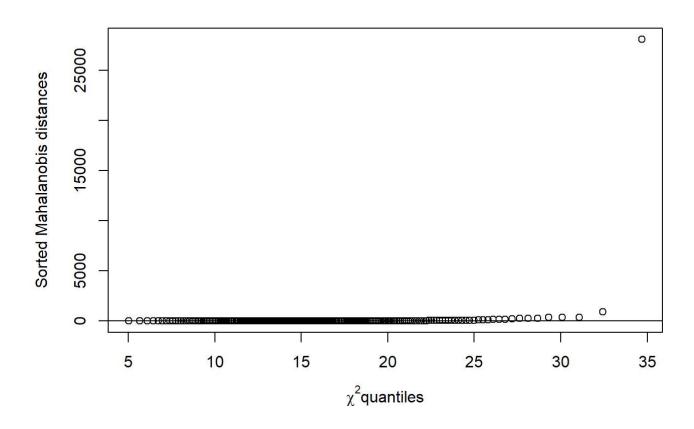
prfatc <- prcomp(train_data)
summary(prfatc)</pre>

```
## Importance of components:
                              PC1
##
                                      PC2
                                               PC3
                                                       PC4
                                                              PC5
                                                                      PC6
## Standard deviation
                          37.3563 15.5618 10.31319 3.78465 3.4687 2.59870
## Proportion of Variance 0.7766 0.1348 0.05919 0.00797 0.0067 0.00376
## Cumulative Proportion
                           0.7766 0.9114 0.97056 0.97853 0.9852 0.98898
##
                              PC7
                                      PC8
                                              PC9
                                                     PC10
                                                             PC11
                                                                     PC12
## Standard deviation
                          2.21857 1.85400 1.59104 1.48755 1.32575 1.31106
## Proportion of Variance 0.00274 0.00191 0.00141 0.00123 0.00098 0.00096
## Cumulative Proportion 0.99172 0.99364 0.99505 0.99628 0.99725 0.99821
##
                             PC13
                                     PC14
                                             PC15
                                                     PC16
## Standard deviation
                          1.14090 1.03327 0.77727 0.49028
## Proportion of Variance 0.00072 0.00059 0.00034 0.00013
## Cumulative Proportion 0.99894 0.99953 0.99987 1.00000
```

require(MASS)

```
## Loading required package: MASS
```

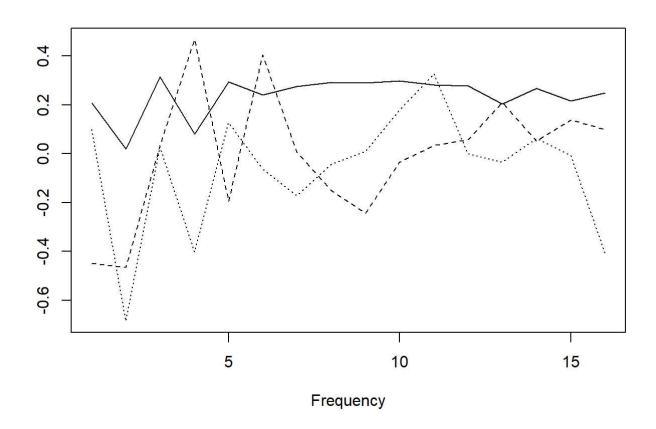
```
robfat <- cov.rob(train_data)
md <- mahalanobis(train_data, center=robfat$center, cov=robfat$cov)
n <- nrow(train_data);p <- ncol(train_data)
plot(qchisq(1:n/(n+1),p), sort(md), xlab=expression(paste(chi^2,"
quantiles")), ylab="Sorted Mahalanobis distances")
abline(0,1)</pre>
```



train_pca <- prcomp((train_data),scale=TRUE)
round(train_pca\$sdev,3)</pre>

[1] 3.135 1.364 1.048 0.829 0.803 0.723 0.574 0.522 0.480 0.428 0.361 ## [12] 0.280 0.234 0.198 0.179 0.077

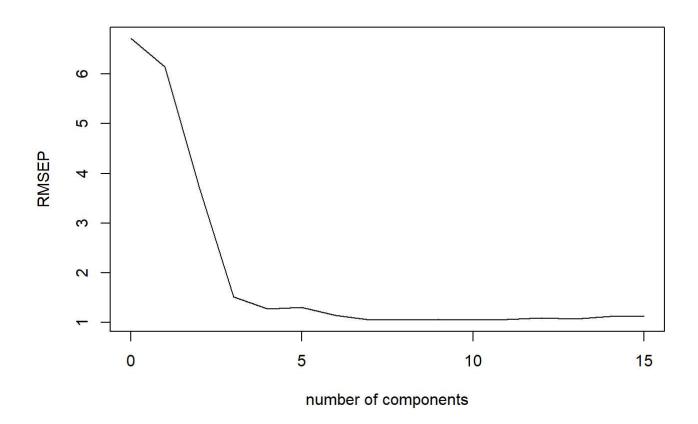
matplot(1:16, train_pca\$rot[,1:3], type="l", xlab="Frequency", ylab
="", col=1)



```
## Warning in x - y: longer object length is not a multiple of shorter object ## length
```

```
## [1] 10.88871
```

```
pcrmse <- RMSEP(pcrmod, newdata=test_data)
plot(pcrmse,main="")</pre>
```



which.min(pcrmse\$val)

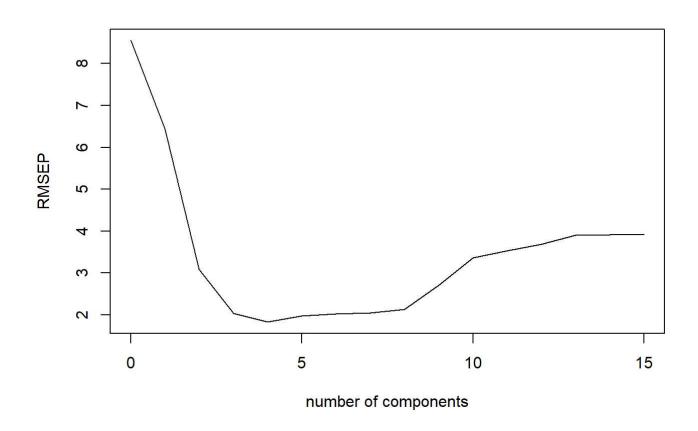
[1] 8

#Optimum no. of components=11
pcrmse\$val[11]

[1] 1.049483

d)Partial Least Squares

```
set.seed(123)
plsmod <- plsr(siri ~ ., data=train_data, ncomp=15, validation
="CV")
plsCV <- RMSEP(plsmod, estimate="CV")
plot(plsCV,main="")</pre>
```



ypred <- predict(plsmod,ncomp=5)
rmse(ypred, train_data\$siri)</pre>

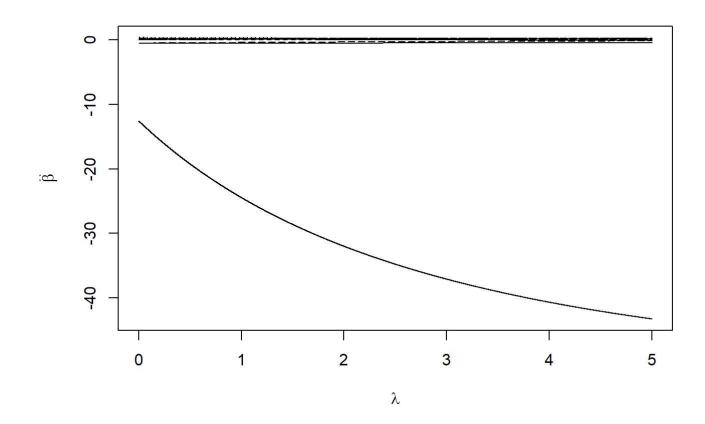
[1] 1.549977

ytpred <- predict(plsmod, test_data, ncomp=5)
rmse(ytpred, test_data\$siri)</pre>

[1] 1.049793

e. Ridge Regression

```
require(MASS)
rgmod <- lm.ridge(siri ~ ., data.frame((train_data)), lambda = seq(0, 5, len=10000))
matplot(rgmod$lambda, coef(rgmod), type="l", xlab=expression(lambda)
,ylab=expression(hat(beta)),col=1)</pre>
```



which.min(rgmod\$GCV)

0.04650465 ## 94

ypred <- cbind(1,as.matrix(train_data[,-1])) %*% coef(rgmod)[94,]
rmse(ypred, train_data\$siri)</pre>

[1] 1.494422

#which is comparable to the above, but for the test sample we find:
ypred <- cbind(1,as.matrix(test_data[,-1])) %*% coef(rgmod)[94,]
rmse(ypred, test_data\$siri)</pre>

[1] 1.128102

f. LASSO

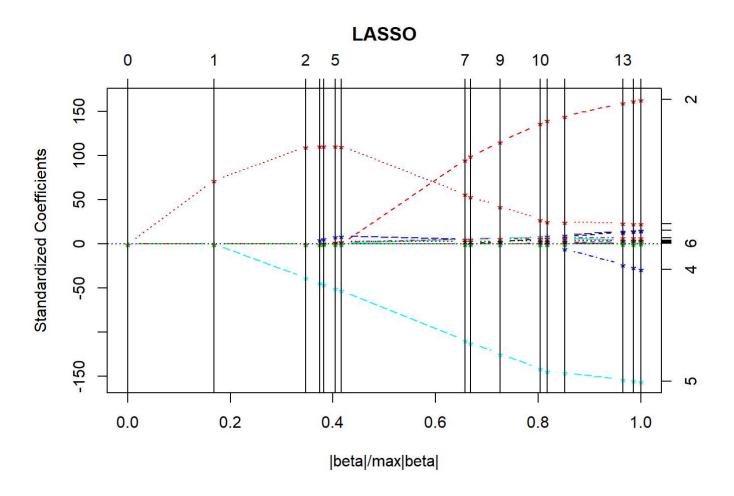
require(lars)

Loading required package: lars

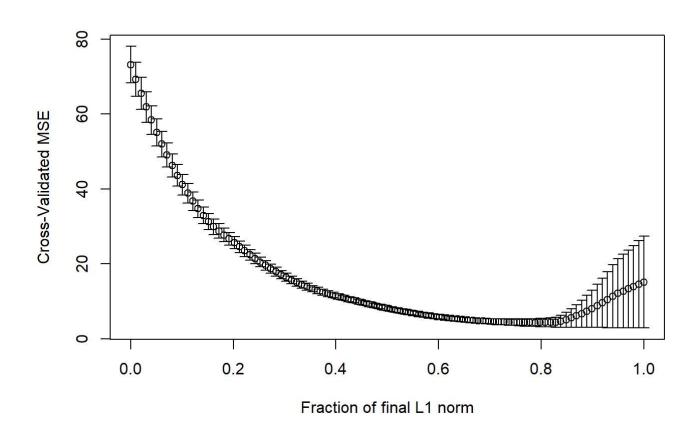
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```
## Loaded lars 1.2
```

```
trainy <- train_data$siri
trainx <- as.matrix(train_data[,-1])
lassomod <- lars(trainx,trainy)
plot(lassomod)</pre>
```



#We now compute the crossvalidation choice of t:
set.seed(123)
cvout <- cv.lars(trainx,trainy)



cvout\$index[which.min(cvout\$cv)]

[1] 0.7878788

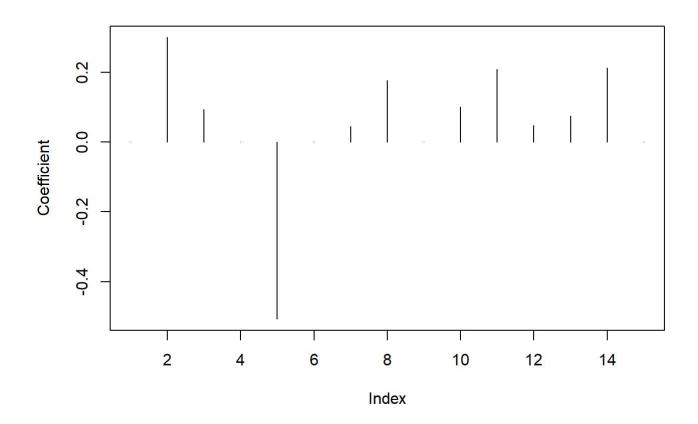
#0.7979798
#For this choice of t, we compute the predicted values for the test data:

testx <- as.matrix(test_data[,-1])
predlars <- predict(lassomod,testx,s=0.7979798,mode="fraction")
#The RMSE may now be computed:
rmse(test_data\$siri, predlars\$fit)</pre>

[1] 1.093538

predlars <- predict(lassomod, s=0.7979798, type="coef", mode="fraction")
plot(predlars\$coef,type="h",ylab="Coefficient")</pre>

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sum(predlars\$coef != 0)

[1] 10