

# Software Systems Verification and Validation

## Lecture 10 - Model checking

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- Linear-Time Properties

# System verification

- Information and Communication Technology (ICT)
- Correct ICT systems
  - It is all about money.
  - It is all about safety.
- The **reliability** of the ICT systems is a key issue in the system design process [KB08].
- System verification techniques

## Schematic view of an posteriori system verification

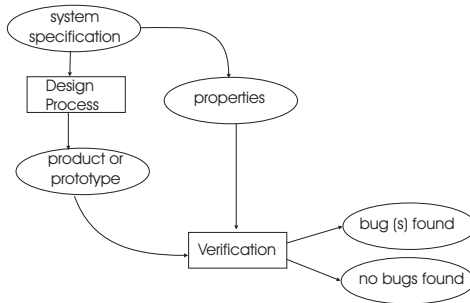
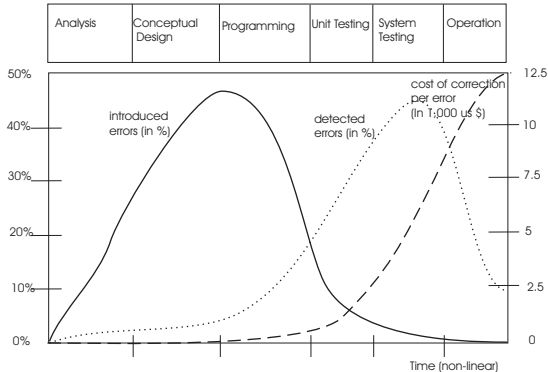


Figure: Schematic view of an posteriori system verification

## Software verification techniques

- Non-formal verification techniques (used in practice): peer reviewing (SSVV Lecture 01) and testing (SSVV Lecture 2-3).
  - Peer review (static technique)
  - Software testing (Dynamic technique)
- Formal verification techniques.
  - Formal methods
  - Model-based simulation
  - Model checking( SSVV Lecture 10- today)
  - Model-based testing
  - Theorem proving (SSVV Lecture 06 and 07)

# Catching software bugs: the sooner, the better [KB08]



## Formal methods

- More time and effort spend on verification than on construction - in software/hardware design of complex systems.
- The role of formal methods:
  - To establish system correctness with mathematical rigor.
  - To facilitate the early detection of defects.
- Brands of verification technique:
  - **deductive methods** - the correctness of system is determined by properties in a mathematical theory, using tools as theorem provers and proof checkers
  - **model-based techniques**: model checking (exhaustive exploration), simulation (restrictive set of scenarios in the model), model-based testings, etc
- Any verification using **model-based techniques** is only as good as the model of the system.

# Model checking

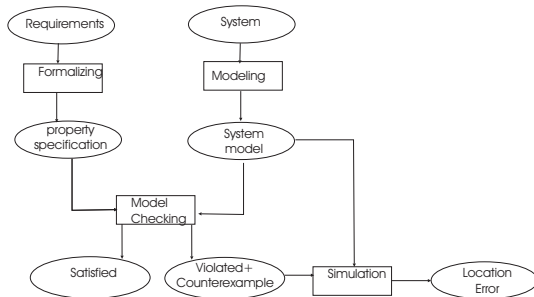


Figure: Schematic view of the model checking approach [KB08]



## Characteristics of Model Checking

- Model checking is an automated technique that, given a finite-state model of a system and a formal property, systematically checks whether this property holds for (a given state in) that model.
- The model checking process
  - Modeling phase
    - model the system under consideration
    - formalize the property to be checked.
  - Running phase
  - Analysis phase
    - property satisfied?
    - property violated?

## Strengths and Weaknesses of model checking [KB08]

### Strengths

- General verification approach
- Supports partial verification
- Provides diagnostic information
- Potential “push-button” technology
- Increasing interest by industry
- Easily integrated in existing development cycles

### Weaknesses

- Appropriate to control-intensive applications
- Its applicability is subject to decidability issues
- It verifies a system model
- Checks only stated requirements
- Suffers from the state-space explosion problem
- Requires some expertise

# Transition system

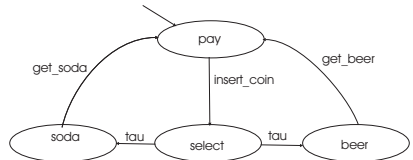
- Transition systems - used in computer science as models to describe the behavior of the systems.
- Transition systems - directed graphs:
  - Nodes - represent states;
  - Edges - model transitions, i. e. state changes.
- A Transition System (TS) is tuple  $(S, \text{Act}, \rightarrow, I, \text{Ap}, L)$ , where
  - $S$  is a set of states,
  - $\text{Act}$  is a set of actions,
  - $\rightarrow \subseteq S \times \text{Act} \times S$  is a transition relation,
  - $I \subseteq S$  is a set of initial states,
  - $\text{AP}$  is a set of atomic propositions, and
  - $L : S \rightarrow 2^{\text{AP}}$  is a labeling function.
- TS is called finite if  $S$ ,  $\text{Act}$  and  $\text{AP}$  are finite.

## Transition system - remarks

- Intuitive behavior of a transition system
  - Initial state  $s_0 \in I$
  - Using the transition relation  $\rightarrow$  the system evolves
  - Current state  $s$ , a transition  $s \xrightarrow{\alpha} s'$  is selected  
*nondeterministically*
  - The selection procedure is repeated and finishes once a state is encountered that has no outgoing transitions.
- The labeling function  $L$  relates a set  $L(s) \in 2^{AP}$  at atomic propositions to any state  $s$ .  $L(s)$  intuitively stands for exactly those atomic propositions  $a \in AP$  which are satisfied by state  $s$ .
- Given that  $\phi$  is a propositional logic formula, then  $s$  satisfies the formula  $\phi$  if the evaluation induced by  $L(s)$  makes the formula  $\phi$  true,

## Beverage Vending Machine

- $S = \{pay, select, soda, beer\}, I = \{pay\}$
- $Act = \{insert\_coin, get\_soda, get\_beer, \tau\}$
- Example transitions:  $pay \xrightarrow{insert\_coin} select$ ,  
 $select \xrightarrow{get\_beer} beer$ ,  
 $pay \xrightarrow{get\_soda} soda$
- Atomic propositions depends on the properties under consideration. A simple choice - to let the state names act as atomic propositions, i. e.  $L(s) = \{s\}$ .  
 "The vending machine only delivers a drink after providing a coin,"  
 $AP = \{paid, drink\}$ ,  
 $I(pay) = \emptyset, I(soda) = I(beer) =$



# Linear-Time Properties

- Deadlock
- Safety properties = “nothing bad should happen”.
  - The number of inserted coins is always at least the number of dispensed drinks.
- Liveness properties = “ something good will happen in the future” .

# Temporal Logic

- Propositional temporal logics [KB08], [Fre10]- extensions of propositional logic by temporal modalities.
- The elementary temporal modalities that are present in most temporal logics include the operators
  - “eventually” (eventually in the future) -  $\Diamond$
  - “always” (now and forever in the future) -  $\Box$
- The nature of time in temporal logics can be either linear or branching.
- The adjective “temporal”
  - specification of the relative order of events;
  - does not support any means to refer to the precise timing of events.

## Linear-Time Logic

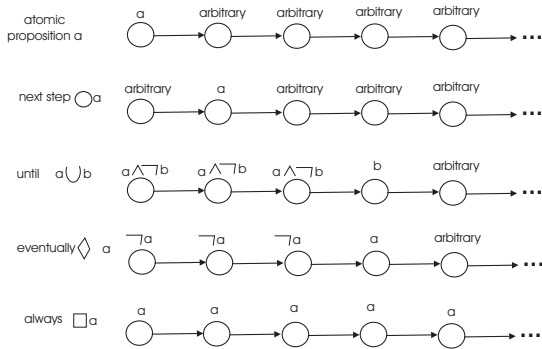
- Construction of LTL formulae in LTL - ingredients:
  - atomic propositions  $a \in AP$ , (stands for the state label  $a$  in a transition system)
  - boolean connectors like conjunction  $\wedge$  and negation  $\neg$ ,
  - basic temporal modalities “next”  $\bigcirc$  and “until”  $\bigcup$ .
- LTL formulae over the set  $AP$  of atomic proposition are formed according to the following grammar:  
$$\varphi ::= \text{true} \mid a \mid \varphi_1 \wedge \varphi_2 \mid \neg \varphi \mid \bigcirc \varphi \mid \varphi_1 \bigcup \varphi_2, \text{ where } a \in AP.$$



## LTL temporal modalities

- The until operator allows to derive the temporal modalities  $\Diamond$  (“eventually”, sometimes in the future) and  $\Box$  (“always”, from now on forever) as follows:
  - $\Diamond\varphi = \text{true} \cup \varphi$ .
  - $\Box\varphi = \neg\Diamond\neg\varphi$ .
- By combining the temporal modalities  $\Diamond$  and  $\Box$ , new temporal modalities are obtained:
  - $\Box\Diamond\varphi$  - “infinitely often  $\varphi$ .”  
at any moment  $j$  there is a moment  $i$   $i \geq j$  at which an  $a$  state is visited
  - $\Diamond\Box\varphi$  - “eventually forever  $\varphi$ .”  
from some moment  $j$  on, only  $a$ -states are visited.

# Intuitive semantics of temporal modalities



**Figure:** Intuitive semantics of temporal modalities



# CTL

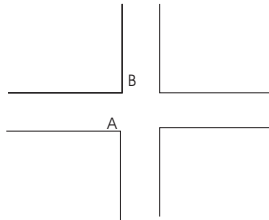
- Construction of CTL formulae:
  - as in LTL by the next-step and until operators,
  - must be not combined with boolean connectives
  - no nesting of temporal modalities is allowed.
- CTL formulae over the set  $AP$  of atomic proposition are formed according to the following grammar:  
 $\phi ::= \text{true} \mid a \mid \phi_1 \wedge \phi_2 \mid \neg\phi \mid \exists\phi \mid \forall\phi$ , where  $a \in AP$  and  $\varphi$  is a path formula.
- CTL path formulae are formed according to the following grammar:  
 $\varphi ::= \bigcirc\phi \mid \phi_1 \bigcup \phi_2$ , where  $\phi, \phi_1$  and  $\phi_2$  are state formulae.

# CTL

- CTL distinguishes between state formulae and path formulae:
  - State formulae express a property of a state.
  - Path formulae express a property of a path, i.e. an infinite sequence of states.
- Temporal PATH operators  $\bigcirc$  and  $\bigcup$ 
  - $\bigcirc\phi$  holds for a path if  $\phi$  holds in the next state of the path;
  - $\phi\bigcup\psi$  holds for a path if there is some state along the path for which  $\psi$  holds, and  $\phi$  holds in all states prior to that state.
- Path formulae  $\Rightarrow$  state formulae by prefixing them with
  - path quantifier  $\exists$  (pronounced “for some path”);  
 $\exists\phi$  - holds in a state if there exists some path satisfying  $\phi$  that starts in that state.
  - path quantifier  $\forall$  (pronounced “for all paths”)

## Semaphore example

- $\forall \Box (B = \text{yellow} \rightarrow \forall \bigcirc (B = \text{red}))$ .
  - If B is yellow, it will become (sometime in the future) red.



Outline  
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Transition system  
Linear-Time Properties  
Temporal Logic  
Linear-Time Logic  
Computation Tree Logic  
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Questions  
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Next lecture

## Next lecture

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