

Basic concepts – element type

EqualityComparable

A type is EqualityComparable if objects of that type can be compared for equality

We denote this type: TE

- Element Type that can be compared for equality
- has a default value;

Alternative name: TElement

Notation: ε_{TE} – the default element from the set

TE as an ADT:

$\mathcal{D}_{TE} = \{e \mid e \text{ --element}\}$

operations:

Subalg. assignment(e1,e2)

Desc.: assign value from one element to another

Prec.: $e1 \in \mathcal{D}_{TE}$ *here “ \in ” and “=” are the math. signs*

Post.: $e2 = e1$ *with mathematical significance*

Funct. isEqual (e1,e2)

Desc.: test if that 2 values are equal

Prec.: $e1 \in \mathcal{D}_{TE}$, $e2 \in \mathcal{D}_{TE}$

Post.: isEqual = true if $e1=e2$
 false if $e1 \neq e2$

Subalg. initDefault(e)

Desc.: initialize with the default element

Prec.: -

Post.: $e = \varepsilon_{TE}$

Notations:

assignment	operator:	$:=$ or \leftarrow
equalityTest	operator:	$=$

Remarks:

- we consider TE a general (abstract) Type (that can have specialization)
- basic data types are a kind of TE
- Specification of the type of an element:

$e \in \mathcal{D}_{TE}$

e : TE

We can read/print an element by using *read/print* (pseudocode)

LessThanComparable

A type is `LessThanComparable` if it is ordered.

- it must be possible to compare two elements of that type by using operators `<`, `=` and `>`
 - o `<`, `>` - is a partial ordering relation
 - o `=` is a equivalence relation
 - o any 2 elements are in one of the 3 relations: `<`, `=`, `>`

Example:

`<`, `=`, `>` - mathematical relations for numbers

`<`, `=`, `>` - given by the “dictionary” order of strings (of chars)

Remark:

Only operator `<=` is fundamental;

the other inequality operators are essentially syntactic sugar.

We denote this type: TCE (Type: Comparable Element)

It is a kind of TE, that is it has all operations of TE and *some* more

Alternative name: `TLessThanComparable`

TCE as an ADT:

$\mathcal{D}_{\text{TCE}} = \{e \mid e - \text{less than comparable element}\}$

operations:

@all operations of TE

Funct. `compare(e1,e2)`

Desc.: compare 2 elements

Prec.: $e1 \in \mathcal{D}_{\text{TE}}$, $e2 \in \mathcal{D}_{\text{TE}}$

Post.: compare =	-1	if $e1 < e2$
	0	if $e1 = e2$
	1	if $e1 > e2$

Note:

sometimes, we will use operators: `<`, `=`, `>`, `<=`, `>=`
instead of calling function *compare*