

1.11 Tabel de integrale nedefinite

Peste tot în acest tabel J este un interval $\subset \mathbb{R}$

1.	$f: \mathbb{R} \rightarrow \mathbb{R}$ $f(x) = x^n; n \in \mathbb{N}$	$\int x^n dx = \frac{x^{n+1}}{n+1} + c.$
2.	$f: J \rightarrow \mathbb{R}; J \subset (0, \infty)$ $f(x) = x^a; a \in \mathbb{R} \setminus \{-1\}$	$\int x^a dx = \frac{x^{a+1}}{a+1} + c.$
3.	$f: \mathbb{R} \rightarrow \mathbb{R}$ $f(x) = a^x; a \in \mathbb{R}_+^* \setminus \{1\}$	$\int a^x dx = \frac{a^x}{\ln a} + c.$
4.	$f: J \rightarrow \mathbb{R}; J \subset \mathbb{R}^*$ $f(x) = \frac{1}{x}$	$\int \frac{1}{x} dx = \ln x + c.$
5.	$f: J \rightarrow \mathbb{R}; J \subset \mathbb{R} \setminus \{-a, a\}$ $f(x) = \frac{1}{x^2 - a^2}, \{a \neq 0\}$	$\int \frac{1}{x^2 - a^2} dx = \frac{1}{2a} \ln \left \frac{x-a}{x+a} \right + c.$
6.	$f: \mathbb{R} \rightarrow \mathbb{R}$ $f(x) = \frac{1}{x^2 + a^2}; a \neq 0$	$\int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \operatorname{arctg} \frac{x}{a} + c.$
7.	$f: \mathbb{R} \rightarrow \mathbb{R}$ $f(x) = \sin x$	$\int \sin x dx = -\cos x + c.$
8.	$f: \mathbb{R} \rightarrow \mathbb{R}$ $f(x) = \cos x$	$\int \cos x dx = \sin x + c.$
9.	$f: J \rightarrow \mathbb{R}; J \subset \mathbb{R} \setminus \left\{ (2k+1) \frac{\pi}{2} \mid k \in \mathbb{Z} \right\}$ $f(x) = \frac{1}{\cos^2 x}$	$\int \frac{1}{\cos^2 x} dx = \operatorname{tg} x + c.$
10.	$f: J \rightarrow \mathbb{R}; J \subset \mathbb{R} \setminus \{k\pi \mid k \in \mathbb{Z}\}$ $f(x) = \frac{1}{\sin^2 x}$	$\int \frac{1}{\sin^2 x} dx = -\operatorname{ctg} x + c.$
11.	$f: J \rightarrow \mathbb{R}; J \subset \mathbb{R} \setminus \left\{ (2k+1) \frac{\pi}{2} \mid k \in \mathbb{Z} \right\}$ $f(x) = \operatorname{tg} x$	$\int \operatorname{tg} x dx = -\ln \cos x + c.$
12.	$f: J \rightarrow \mathbb{R}; J \subset \mathbb{R} \setminus \{k\pi \mid k \in \mathbb{Z}\}$ $f(x) = \operatorname{ctg} x$	$\int \operatorname{ctg} x dx = \ln \sin x + c.$
13.	$f: \mathbb{R} \rightarrow \mathbb{R}$ $f(x) = \frac{1}{\sqrt{x^2 + a^2}}; a \neq 0$	$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln(x + \sqrt{x^2 + a^2}) + c.$
14.	$f: J \rightarrow \mathbb{R} \begin{cases} J \subset (-\infty, -a) \\ \text{sau} \\ J \subset (a, \infty) \end{cases}$ $a > 0$ $f(x) = \frac{1}{\sqrt{x^2 - a^2}}$	$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln x + \sqrt{x^2 - a^2} + c.$
15.	$f: J \rightarrow \mathbb{R}; J \subset (-a, a), a > 0,$ $f(x) = \frac{1}{\sqrt{a^2 - x^2}}$	$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \operatorname{arcsin} \frac{x}{a} + c.$