

# **Virtual Machines**

## **Lecture 5 – Dynamic (or Operational) Semantics and First Assignment**

# Module 2 -Revised Content

It consists of about 6 lectures and covers the following topics:

- **Design an Abstract Syntax Tree for a CoreJava ( a small Object-Oriented) language (1<sup>st</sup> assignment—7% of the final grade)**
- **Implement an interpreter for CoreJava (2<sup>nd</sup> assignment—25% of the final grade)**
- **Implement a Lexer and a Parser for CoreJava(3<sup>rd</sup> assignment—25% of the final grade)**
- **Implement a Type Checker for CoreJava (4<sup>th</sup> assignment—25% of the final grade)**

- **Revised Evaluation:**
  - **Labs activity (85%):**
    - **Group of 2 or 3 students : same project consisting of 4 assignments (82%)**
    - **Oral presentation of your final graduate project (3%)**
  - **Individual Oral Final exam (open book) (15%)**

**Your group assignments, your final graduate project and Individual Oral Final Exam will be in the last two weeks. Each group must reserve one of the following time slots (max 5 groups per time slot):**

- » **11 May 2016, 10-12**
- » **11 May 2016, 14-16**
- » **18 May 2016, 10-12**
- » **18 May 2016, 14-16**

# **Formal Dynamic (or Operational) Semantics of a Language**

# Review

## **Previously in Lecture 4:**

- simple interpreter for expression language:
  - abstract syntax tree (AST)
  - small-step, substitution model of evaluation

## **Today:**

- Formal dynamic/operational semantics:
  - small-step, substitution model
  - large-step, environment model

# Review: Notation

- The interpreter code we've written is one way of *defining* the syntax and semantics of a language
- Programming language designers have another more compact notation that's *independent* of the implementation language of interpreter.

# Review: Abstract syntax

$$e ::= x \mid i \mid e + e \\ \mid \text{let } x = e_1 \text{ in } e_2$$

**e, x, i**: *meta-variables* that stand for pieces of syntax

- **e**: expressions
- **x**: program variables
- **i**: integers

**::=** and **|** are *meta-syntax*: used to describe syntax of language

notation is called *Backus-Naur Form* (BNF) from its use by Backus and Naur in their definition of Algol-60

# Dynamic/Operational semantics

Defined by a *judgement*:

$e \dashrightarrow e'$

Read as  $e$  takes a single step to  $e'$

e.g.,  $(5+2)+0 \dashrightarrow 7+0$

Expressions continue to step until they reach a *value*

e.g.,  $(5+2)+0 \dashrightarrow 7+0 \dashrightarrow 7$

Values are a syntactic subset of expressions:

$v ::= i$



# Dynamic/Operational semantics

Reflexive, transitive closure of  $\rightarrow$  is written  $\rightarrow^*$

$e \rightarrow^* e'$  read as *e multisteps to e'* or *e evaluates to e'*

e.g.,  $(5+2)+0 \rightarrow^* 7$

this style of definition is called a *small-step semantics*: based on taking single small steps

# Dynamic/Operational semantics of expr. lang.

$e1 + e2 \dashrightarrow e1' + e2$

if  $e1 \dashrightarrow e1'$

$v1 + e2 \dashrightarrow v1 + e2'$

if  $e2 \dashrightarrow e2'$

$v1 + v2 \dashrightarrow n$

if  $n$  is the sum of  $v1$  and  $v2$

# Dynamic/Operational semantics of expr. lang.

`let x = e1 in e2 --> let x = e1' in e2`  
`if e1 --> e1'`

`let x = v1 in e2 --> e2{v1/x}`

read `e2{v1/x}` as `e2` with `v1` substituted for `x`  
(as we implemented in `subst`)

so we call this the `substitution model of evaluation`

# Dynamic/Operational semantics of expr. lang.

```
if e1 then e2 else e3
-->  if  e1'      then e2  else e3
      if e1 -->  e1'
```

```
if true then e2 else e3 --> e2
```

```
if false then e2 else e3 --> e3
```

# Dynamic/Operational semantics of expr. lang.

Values and variables do not single step:

**v**     $-/->$

**x**     $-/->$

But they do multistep:

**v**     $-->^* \mathbf{v}$

**x**     $-->^* \mathbf{x}$

because multistep includes 0 steps  
(i.e., it is the *reflexive* transitive closure of  $-->$ )

- values don't step because they're done computing
- variables don't step because they're an error: we should never reach a variable; it should have already been substituted away

# We need Static Semantics

Suppose we add Booleans, conjunction, and `if` expressions to language:

$e ::= \dots \mid b \mid e1 \ \&\& \ e2 \mid \text{if } e1 \text{ then } e2 \text{ else } e3$   
 $v ::= \dots \mid b$

Now we can have some non-sensical expressions like:

`5 + false`  
`If 5 then true else 0`

These non-sensical expressions must be ruled out at compile time.  
It can be done using a Static Semantic ( a Type Checker) that we will discuss in the near future

# Interpreter for ext. expr. lang.

See `interp3.ml` in code attached for this lecture

# **ANOTHER FORMAL DYNAMIC SEMANTICS**



# Dynamic semantics

Two different models of evaluation:

- **Small-step substitution model:** substitute value for variable in body of `let` expression
  - And in body of function, since `let x = e1 in e2` behaves the same as `(fun x -> e2) e1`
    - What we've done so far; good mental model for evaluation
    - Not really what OCaml does
- **Big-step environment model:** keep a data structure around that binds variables to values
  - What we'll do now; also a good mental model
  - Much closer to what OCaml really does

# Syntax

```
e ::= x | i | b
      | e1 + e2 | e1 && e2
      | let x = e1 in e2
      | if e1 then e2 else e3
v ::= i | b
```

# New evaluation judgement

- *Big-step semantics*: we model just the reduction from the original expression to the final value
- Suppose  $e \rightarrow e' \dots \rightarrow v$
- We'll abstract that fact to  $e \Rightarrow v$ 
  - forget about all the intermediate expressions
  - new notation means  $e$  evaluates (down) to  $v$ , equiv.  
 $e$  takes a big step to  $v$
  - textbooks use down arrows:  $e \Downarrow v$
- **Goal:**  $e \Rightarrow v$  if and only if  $e \rightarrow^* v$

# Values

- Values are already done:
  - Evaluation rule:  $v \implies v$
- Constants are values
  - 42 is a value, so  $42 \implies 42$
  - **true** is a value, so **true**  $\implies$  **true**

# Operator evaluation

`e1 + e2 ==> v`

`if e1 ==> i1`

`and e2 ==> i2`

`and v is the result of the primitive  
operation i1 + i2`

eg.

`true && false ==> false`

`1 + 2 ==> 3`

`1 + (2 + 3) ==> 6`

# Variables

- What does a variable name evaluate to?

**x** ==> ???

- Trick question: we don't have enough information to answer it
- Need to know what value variable was *bound* to

– e.g., **let x = 2 in x + 1**

- It evaluates to **3**, but we reach a point where we need to know binding of **x**

Until now, *we've never needed this*, because we always **substituted** before we ever get to a variable name

# Variables

OCaml doesn't actually do substitution

```
(fun x -> 42) 0
```

waste of runtime resources to do substitution inside 42

Instead, OCaml lazily substitutes by maintaining  
*dynamic environment*

# Dynamic environment

- Dictionary of bindings of all current variables
- Changes throughout evaluation:

– No bindings at \$:

```
$ let x = 42 in let y = false in e
```

– One binding **[x=42]** at \$:

```
let x = 42 in  
$ let y = false in e
```

– Two bindings **[x=42, y=false]** at \$:

```
let x = 42 in let y = false in  
$ e
```



# Variable evaluation

**To evaluate  $x$  in environment**

**env Look up** value  $v$  of  $x$  in

**env Return  $v$**

Type checking **guarantees that variable is bound**, so we can't ever fail to find a binding in dynamic environment

# Evaluation judgement

Extended notation:

$$\langle \mathbf{env}, \mathbf{e} \rangle \Rightarrow \mathbf{v}$$

Meaning: in dynamic environment **env**, expression **e** takes a big step to value **v**

$\langle \mathbf{env}, \mathbf{e} \rangle$  is called a *machine configuration*

# Variable evaluation

$\langle \text{env}, x \rangle \Rightarrow v$

if =

$v \quad \text{env}(x)$

**env(x) :**

- meaning: the value to which **env** binds **x**
- think of it as looking up **x** in dictionary **env**

# Redo: evaluation with environment

$\langle \text{env}, v \rangle \Rightarrow v$

$\langle \text{env}, e1 + e2 \rangle \Rightarrow v$

if  $\langle \text{env}, e1 \rangle \Rightarrow i1$

and  $\langle \text{env}, e2 \rangle \Rightarrow i2$

and  $v$  is the result of  
primitive operation  $i1+i2$

# Let expressions

**To evaluate** **let  $x = e1$  in  $e2$**  in environment **env**

**Evaluate** the binding expression  **$e1$**  to a value  **$v1$**  in environment **env**

**$\langle env, e1 \rangle \Rightarrow v1$**

**Extend** the environment to bind  **$x$**  to  **$v1$**

**$env' = env[x \rightarrow v1]$**  *new notation*

**Evaluate** the body expression  **$e2$**  to a value  **$v2$**  in extended environment **env'**

**$\langle env', e2 \rangle \Rightarrow v2$**

**Return  $v2$**

# Let expression evaluation rule

$\langle \text{env}, \text{let } x=e1 \text{ in } e2 \rangle \Rightarrow v2$   
if  $\langle \text{env}, e1 \rangle \Rightarrow v1$   
and  $\langle \text{env}[x \rightarrow v1], e2 \rangle \Rightarrow v2$

Example (let [] be the empty environment)

:  $\langle [], \text{let } x = 42 \text{ in } x \rangle \Rightarrow 42$

Because...

- $\langle [], 42 \rangle \Rightarrow 42$
- and  $\langle [][x \rightarrow 42], x \rangle \Rightarrow 42$ 
  - Because  $[x=42](x)=42$

# Group Project – First Assignment

7% of the final grade

# First Assignment

Design in Ocaml the Abstract Syntax Tree for a small object-oriented language called CoreJava.

The syntax of CoreJava is described in the following.



# Syntax of CoreJava

A CoreJava program  $P$  consists of a list of class declarations as follows:

$P ::= \text{def}^+$

$\text{def}^+ ::= \text{def} \mid \text{def1}; \text{def2}; \dots; \text{defn}$

The program contains at least one class declaration.

The last class declaration must contain a method called “**main**” which is the starting execution point for the CoreJava program.

# Syntax of CoreJava

A class declaration def consists of the following:

**def ::= class cn1 extends cn2 { field\* # meth\* }**

where cn1 is the current class name and cn2 is the name of the parent class

The body of the class consists of a list of fields declarations followed by a list of methods declarations. The fields list is separated by “#” from the methods list. **The fields list is either empty or field+ ::= field1;field2;...;fieldn. The methods list is either empty or meth+ ::= meth1;meth2;...;methn.**

# Syntax of CoreJava

A field declaration consists of the following:

$\text{field} ::= \text{typ fn}$

where  $\text{typ}$  is the type of the field and  $\text{fn}$  is the name of the field

A type  $\text{typ}$  can be either a primitive type, or a class name or the bottom (the type of null).

$\text{typ} ::= \text{prim} \mid \text{cn} \mid \_ \mid \_$

$\text{prim} ::= \text{int} \mid \text{float} \mid \text{bool} \mid \text{void}$

# Syntax of CoreJava

A method declaration consists of the following:

$\text{meth} ::= \text{typ1 mn}((\text{typ pn})^*) \{e\}$

where  $\text{typ1}$  is the type of the method result,  $\text{mn}$  is the method name,  $(\text{typ pn})^*$  is the list of method parameters.

The list of method parameters can be either empty or  $(\text{typ pn})^+ ::= \text{typ1 pn1, typ2 pn2, ..., typn pnn}$

The body of the method is given by the expression  $e$ .

# Syntax of CoreJava

An expression is defined as follows:

<code>e ::= null</code>	(null value)
<code>  kint</code>	(a constant value)
<code>  kfloat</code>	
<code>  true   false</code>	
<code>  ()</code>	( a value of type void)
<code>  v</code>	(a variable name)
<code>  v.f</code>	( a field f of an object denoted by v)

# Syntax of CoreJava

An expression is defined as follows:

$e ::= \dots$

|  $v = e$  (variable assignment)

|  $v.f = e$  (object field assignment)

|  $\{ \text{typ } v \} e_1$  (local variable declaration such that  $v$  has type  $\text{typ}$  and its scope is the expression  $e_1$ )

|  $e_1; e_2$  ( a sequence such that  $e_2$  is executed only after  $e_1$  is executed)

|  $\text{if } v \text{ then } \{e_1\} \text{ else } \{e_2\}$  (conditional where the condition is a variable)

# Syntax of CoreJava

An expression is defined as follows:

$e ::= \dots$

$| e1 \text{ opint } e2$  (arithmetic expressions for ints  
where  $\text{opint} ::= +|-|*|/$ )

$| e1 \text{ opfloat } e2$  (arithmetic expressions for floats  
where  $\text{opfloat} ::= +.|-.|*|/|.$ )

$| e1 \ \&\& \ e2$  (logical expressions)

$| e1 \ || \ e2$

$| !e$  (negation)

# Syntax of CoreJava

An expression is defined as follows:

$e ::= \dots$

|  $\text{new } cn(v^*)$  (creation of an instance object of the class  $cn$ . The fields of the new object are initialized by the list of variables  $v^*$ . The fields are initialized in the order defined in the declaration of class  $cn$ )

|  $v.mn(v^*)$  (method call where  $v$  is the method receiver and the list of variables  $v^*$  are the current arguments initializing the method parameters)

|  $\text{while } v \{e\}$  (loop where the condition is a variable)



# Operational Semantics of CoreJava

We'll discuss it Next Lecture ...

when you will also get the second assignment, the interpreter implementation