

## HW#2 Solutions-572

**3.6** Give a complete problem formulation for each of the following. Choose a formulation that is precise enough to be implemented.

a. Using only four colors, you have to color a planar map in such a way that no two adjacent regions have the same color.

**Solution:**

**Initial state:** No regions colored.

**Goal test:** All regions colored, and no two adjacent regions have the same color.

**Successor function:** Assign a color to a region.

**Cost function:** Number of assignments.

d. You have three jugs, measuring 12 gallons, 8 gallons, and 3 gallons, and a water faucet. You can fill the jugs up or empty them out from one to another or onto the ground. You need to measure out exactly one gallon.

**Solution:**

**Initial state:** jugs have values  $[0, 0, 0]$ .

**Goal test:** If any of the following states:  $[1, y, z], [x, 1, z], [x, y, 1]$

**Successor function:** given values  $[x, y, z]$ , generate  $[12, y, z]$ ,  $[x, 8, z]$ ,  $[x, y, 3]$  (by filling);  $[0, y, z]$ ,  $[x, 0, z]$ ,  $[x, y, 0]$  (by emptying); or for any two jugs with current values  $x$  and  $y$  pour  $y$  into  $x$ ; this changes the jug with  $x$  to the minimum of  $x + y$  and the capacity of the jug, and decrements the jug with  $y$  by the amount gained by the first jug.

**Cost function:** Number of actions.