



Luis Fauré Navarro

AG3 - Actividad Guiada

https://github.com/lfauren/03MAIR-Algoritmos-de-Optimizacion-2019/tree/master/AG3

```
In [0]: import urllib.request
         file = "swiss42.tsp"
         urllib.request.urlretrieve("http://elib.zib.de/pub/mp-testdata/tsp/tsplib/tsp/swiss42.tsp", fil
         e)
Out[0]: ('swiss42.tsp', <http.client.HTTPMessage at 0x7ff43335e5f8>)
        http://elib.zib.de/pub/mp-testdata/tsp/tsplib/tsp/swiss42.tsp Esta es la dirección del archivo "swiss42.tsp"
In [0]: !pip install tsplib95
        Requirement already satisfied: tsplib95 in /usr/local/lib/python3.6/dist-packages (0.3.2)
        Requirement already satisfied: networkx==2.1 in /usr/local/lib/python3.6/dist-packages (from tsp
        lib95) (2.1)
        Requirement already satisfied: Click>=6.0 in /usr/local/lib/python3.6/dist-packages (from tsplib
        95) (7.0)
        Requirement already satisfied: decorator>=4.1.0 in /usr/local/lib/python3.6/dist-packages (from
         networkx == 2.1 - > tsplib95) (4.3.2)
In [0]: import tsplib95
         import random
         from math import e
         problem = tsplib95.load problem(file)
         #Nodos
         Nodos = list(problem.get nodes())
         #Aristas
         Aristas = list(problem.get edges())
In [0]: print('Nodos', Nodos)
         print('Aristas', Aristas)
```

Nodos [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41] Aristas [(0, 0), (0, 1), (0, 2), (0, 3), (0, 4), (0, 5), (0, 6), (0, 7), (0, 8), (0, 9), (0, 1)(0), (0, 11), (0, 12), (0, 13), (0, 14), (0, 15), (0, 16), (0, 17), (0, 18), (0, 19), (0, 20), (0, 21), (0, 22), (0, 23), (0, 24), (0, 25), (0, 26), (0, 27), (0, 28), (0, 29), (0, 30), (0, 38)1), (0, 32), (0, 33), (0, 34), (0, 35), (0, 36), (0, 37), (0, 38), (0, 39), (0, 40), (0, 41),(1, 0), (1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (1, 6), (1, 7), (1, 8), (1, 9), (1, 10), (1, 1)1), (1, 12), (1, 13), (1, 14), (1, 15), (1, 16), (1, 17), (1, 18), (1, 19), (1, 20), (1, 21),(1, 22), (1, 23), (1, 24), (1, 25), (1, 26), (1, 27), (1, 28), (1, 29), (1, 30), (1, 31), (1, 3)(1, 33), (1, 34), (1, 35), (1, 36), (1, 37), (1, 38), (1, 39), (1, 40), (1, 41), (2, 0), (2, 38)1), (2, 2), (2, 3), (2, 4), (2, 5), (2, 6), (2, 7), (2, 8), (2, 9), (2, 10), (2, 11), (2, 12),(2, 13), (2, 14), (2, 15), (2, 16), (2, 17), (2, 18), (2, 19), (2, 20), (2, 21), (2, 22), (2, 2)3), (2, 24), (2, 25), (2, 26), (2, 27), (2, 28), (2, 29), (2, 30), (2, 31), (2, 32), (2, 33), (2, 34), (2, 35), (2, 36), (2, 37), (2, 38), (2, 39), (2, 40), (2, 41), (3, 0), (3, 1), (3, 2),(3, 3), (3, 4), (3, 5), (3, 6), (3, 7), (3, 8), (3, 9), (3, 10), (3, 11), (3, 12), (3, 13), (3, 12)14), (3, 15), (3, 16), (3, 17), (3, 18), (3, 19), (3, 20), (3, 21), (3, 22), (3, 23), (3, 24), (3, 25), (3, 26), (3, 27), (3, 28), (3, 29), (3, 30), (3, 31), (3, 32), (3, 33), (3, 34), (3, 38)5), (3, 36), (3, 37), (3, 38), (3, 39), (3, 40), (3, 41), (4, 0), (4, 1), (4, 2), (4, 3), (4, 4), (4, 5), (4, 6), (4, 7), (4, 8), (4, 9), (4, 10), (4, 11), (4, 12), (4, 13), (4, 14), (4, 15), (4, 16), (4, 17), (4, 18), (4, 19), (4, 20), (4, 21), (4, 22), (4, 23), (4, 24), (4, 25), (4, 26), (4, 27), (4, 28), (4, 29), (4, 30), (4, 31), (4, 32), (4, 33), (4, 34), (4, 35), (4, 3(6), (4, 37), (4, 38), (4, 39), (4, 40), (4, 41), (5, 0), (5, 1), (5, 2), (5, 3), (5, 4), (5, 5), (5, 6), (5, 7), (5, 8), (5, 9), (5, 10), (5, 11), (5, 12), (5, 13), (5, 14), (5, 15), (5, 16),(5, 17), (5, 18), (5, 19), (5, 20), (5, 21), (5, 22), (5, 23), (5, 24), (5, 25), (5, 26), (5, 26)7), (5, 28), (5, 29), (5, 30), (5, 31), (5, 32), (5, 33), (5, 34), (5, 35), (5, 36), (5, 37), (5, 38), (5, 39), (5, 40), (5, 41), (6, 0), (6, 1), (6, 2), (6, 3), (6, 4), (6, 5), (6, 6), (6, 6)7), (6, 8), (6, 9), (6, 10), (6, 11), (6, 12), (6, 13), (6, 14), (6, 15), (6, 16), (6, 17), (6, 17), (6, 18)18), (6, 19), (6, 20), (6, 21), (6, 22), (6, 23), (6, 24), (6, 25), (6, 26), (6, 27), (6, 28), (6, 29), (6, 30), (6, 31), (6, 32), (6, 33), (6, 34), (6, 35), (6, 36), (6, 37), (6, 38), (6, 38)9), (6, 40), (6, 41), (7, 0), (7, 1), (7, 2), (7, 3), (7, 4), (7, 5), (7, 6), (7, 7), (7, 8),(7, 9), (7, 10), (7, 11), (7, 12), (7, 13), (7, 14), (7, 15), (7, 16), (7, 17), (7, 18), (7, 18)9), (7, 20), (7, 21), (7, 22), (7, 23), (7, 24), (7, 25), (7, 26), (7, 27), (7, 28), (7, 29), (7, 30), (7, 31), (7, 32), (7, 33), (7, 34), (7, 35), (7, 36), (7, 37), (7, 38), (7, 39), (7, 4)0), (7, 41), (8, 0), (8, 1), (8, 2), (8, 3), (8, 4), (8, 5), (8, 6), (8, 7), (8, 8), (8, 9), (8, 9)10), (8, 11), (8, 12), (8, 13), (8, 14), (8, 15), (8, 16), (8, 17), (8, 18), (8, 19), (8, 20), (8, 21), (8, 22), (8, 23), (8, 24), (8, 25), (8, 26), (8, 27), (8, 28), (8, 29), (8, 30), (8, 38)1), (8, 32), (8, 33), (8, 34), (8, 35), (8, 36), (8, 37), (8, 38), (8, 39), (8, 40), (8, 41), (9, 0), (9, 1), (9, 2), (9, 3), (9, 4), (9, 5), (9, 6), (9, 7), (9, 8), (9, 9), (9, 10), (9, 1)1), (9, 12), (9, 13), (9, 14), (9, 15), (9, 16), (9, 17), (9, 18), (9, 19), (9, 20), (9, 21), (0 25) (0 24) (0 25) (0 26) (0 27) (0 28) (0 20) (0 20) (0 21) (0 2

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In [0]: def factorial(n):
          if n == 0:
             return 1
          else:
             return n*factorial(n-1)
        #Se genera una solucion aleatoria con comienzo en en el nodo 0
        def crear solucion(Nodos):
          solucion = [0]
          for i in range(len(Nodos)-1):
            solucion = solucion + [random.choice(list(set(Nodos) - set({0}) - set(solucion)))]
          return solucion
        #Devuelve la distancia entre dos nodos
        def distancia(a,b, problem):
          return problem.wfunc(a,b)
        #Devuelve la distancia total de una trayectoria/solucion
        def distancia total(solucion, problem):
```

```
distancia total = 0
          for i in range(len(solucion)-1):
            distancia total += distancia(solucion[i] ,solucion[i+1] , problem)
          return distancia total + distancia(solucion[len(solucion)-1] ,solucion[0], problem)
        solucion = crear solucion(Nodos)
        distancia total(solucion, problem)
Out[0]: 4584
In [0]: def busqueda aleatoria(problem, N):
          Nodos = list(problem.get nodes())
          mejor solucion = []
          meior distancia = 10e100
          for i in range(N):
            solucion = crear solucion(Nodos)
            distancia = distancia total(solucion, problem)
            if distancia < mejor distancia:</pre>
              mejor solucion = solucion
              mejor distancia = distancia
          print("Mejor solución:" , mejor_solucion)
                              :" , mejor distancia)
          print("Distancia
          return mejor solucion
        sol = busqueda aleatoria(problem, 50000)
        Mejor solución: [0, 14, 17, 20, 34, 40, 41, 16, 37, 22, 29, 3, 18, 4, 19, 5, 1, 24, 21, 38, 30,
        9, 23, 32, 36, 7, 31, 8, 10, 25, 11, 28, 12, 13, 26, 33, 35, 39, 2, 15, 6, 27]
        Distancia
                      : 3606
In [0]: def genera vecina(solucion):
          #Generador de soluciones vecinas: 2-opt (intercambiar 2 nodos) Si hay N nodos se generan (N-
        1)x(N-2)/2 soluciones
          #print(solucion)
          mejor solucion = []
          mejor distancia = 10e100
          for i in range(1,len(solucion)-1):
            for j in range(i+1, len(solucion)):
              vecina = solucion[:i] + [solucion[j]] + solucion[i+1:j] + [solucion[i]] + solucion[j+1:]
              distancia vecina = distancia total(vecina, problem)
```

```
if distancia vecina <= mejor distancia:</pre>
                mejor distancia = distancia vecina
                mejor solucion = vecina
          return mejor solucion
        solucion = crear solucion(Nodos)
        print(solucion)
        nueva solucion = genera vecina(solucion)
        print(nueva solucion)
        [0, 11, 26, 18, 29, 9, 31, 16, 34, 41, 15, 6, 10, 33, 39, 3, 21, 7, 32, 30, 17, 12, 25, 1, 19,
        5, 35, 28, 20, 8, 40, 23, 13, 27, 38, 4, 2, 24, 37, 14, 22, 36]
        [0, 11, 26, 18, 29, 9, 31, 16, 34, 41, 15, 6, 10, 33, 39, 24, 21, 7, 32, 30, 17, 12, 25, 1, 19,
        5, 35, 28, 20, 8, 40, 23, 13, 27, 38, 4, 2, 3, 37, 14, 22, 36]
In [0]: def busqueda local(problem, N):
          mejor solucion = []
          mejor distancia = 10e100
          Nodos = list(problem.get nodes())
          solucion referencia = crear solucion(Nodos)
          for i in range(N):
            vecina = genera vecina(solucion referencia)
            distancia vecina = distancia total(vecina, problem)
            if distancia vecina < mejor distancia:</pre>
              mejor solucion = vecina
              mejor distancia = distancia vecina
            solucion referencia = vecina
          print("Mejor solución:" , mejor_solucion)
          print("Distancia :" , mejor distancia)
          return mejor solucion
        sol = busqueda local(problem, 100)
        Mejor solución: [0, 32, 30, 38, 34, 33, 20, 15, 16, 14, 19, 13, 5, 8, 23, 41, 25, 11, 26, 6, 31,
        35, 36, 17, 37, 7, 1, 3, 4, 18, 12, 10, 2, 28, 29, 22, 39, 21, 24, 40, 9, 27]
        Distancia
                      : 1838
In [0]: def genera vecina aleatorio(solucion):
          #Generador de 1 solucion vecina 2-opt (intercambiar 2 nodos)
          #Se puede mejorar haciendo que la elección no se uniforme sino entre las que estén más proxim
```

```
i = random.choice(range(1, len(solucion)) )
          j = random.choice(list(set(range(1, len(solucion))) - {i}))
          vecina = solucion[:i] + [solucion[i]] + solucion[i+1:i] + [solucion[i]] + solucion[i+1:]
           return vecina
        def probabilidad(T,d):
           r=random.random():
          if(r \le (e^{**}(-1^*d)/(T^*1.0))):
             return True
          else:
             return False
        def bajar temperatura(T):
           return T-1
In [0]: def recocido simulado(problem, TEMPERATURA):
          #problem = datos del problema
          #T = Temperatura
          solucion referencia = crear solucion(Nodos)
          distancia referencia = distancia total(solucion referencia, problem)
          mejor solucion = []
          mejor distancia = 10e100
           while TEMPERATURA > 0:
            #Genera una solución vecina(aleatoria)
            vecina = genera vecina(solucion referencia)
            #Calcula su valor(distancia)
            distancia vecina = distancia total(vecina, problem)
            #Si es la mejor solución de todas se guarda
            if distancia vecina < mejor distancia:</pre>
                 mejor solucion = vecina
                 mejor distancia = distancia vecina
            #Si la nueva vecina es mejor se cambia y si es peor se cambia según una probabilidad depend
        iente de T y de | distancia referencia - distancia vecina |
             if distancia vecina < distancia referencia or probabilidad(TEMPERATURA, abs(distancia refer</pre>
        encia - distancia vecina) ) :
               solucion referencia = vecina
               distancia referencia = distancia vecina
            TEMPERATURA = bajar temperatura(TEMPERATURA)
          print("La mejor solución encontrada es " , end="")
```

```
print(mejor solucion)
          print("con una distancia total de " , end="")
          print(mejor distancia)
          return mejor solucion
        sol = recocido simulado(problem, 100)
        La mejor solución encontrada es [0, 31, 17, 36, 35, 20, 33, 34, 32, 30, 29, 9, 40, 24, 21, 39, 2
        2, 38, 23, 41, 25, 11, 12, 4, 3, 6, 5, 14, 15, 16, 19, 13, 26, 18, 10, 8, 28, 2, 27, 1, 37, 7]
        con una distancia total de 1632
In [0]: def Add Nodo(problem, H ,T ) :
          #Establecer una una funcion de probabilidad para
          # añadir un nuevo nodo dependiendo de los nodos mas cercanos y de las feromonas depositadas
          Nodos = list(problem.get nodes())
          return random.choice( list(set(range(1,len(Nodos))) - set(H) ) )
        def Incrementa Feromona(problem, T, H ) :
          #Incrementar segun la calidad de la solución. Añadir una cantidad inversamente proporcional a
         la distancia total
          for i in range(len(H)-1):
            T[H[i]][H[i+1]] += 1000/distancia total(H, problem)
          return T
        def Evaporar Feromonas(T ):
          #Podemos elegir diferentes funciones de evaporación dependiendo de la cantidad actual y de la
         suma total de feromonas depositadas,...
          #Evapora 0.3 el valor de la feromona, sin que baje de 1
          T = [[max(T[i][i] - 0.3, 1) for i in range(len(Nodos))] for i in range(len(Nodos))]
          return T
In [0]: def hormigas(problem, N) :
          #problem = datos del problema
          #N = Número de agentes(hormigas)
          #Nodos
          Nodos = list(problem.get nodes())
            #Aristas
          Aristas = list(problem.get edges())
          #Inicializa las aristas con una cantidad inicial de feromonas:1
          T - [[ 1 for in range(len(Nodos)) ] for in range(len(Nodos))]
```

```
I — [[ I IVI _ III | alige(tell(NOUOS))] | IVI _ III | lalige(tell(NOUOS))]
          #Se generan los agentes(hormigas) que serán estructuras de caminos desde 0
          Hormiga = [[0] for in range(N)]
          #Recorre cada agente construyendo la solución
          for h in range(N):
            #print("\nAgente:", h)
            #Para cada agente se construye un camino
            for i in range(len(Nodos)-1) :
              #Elige el siguiente nodo
              Nuevo Nodo = Add Nodo(problem, Hormiga[h] ,T )
              Hormiga[h].append(Nuevo Nodo)
            #Incrementa feromonas en esa arista
            T = Incrementa Feromona(problem, T, Hormiga[h])
            #print("Feromonas(1)", T)
            #Evapora Feromonas
            T = Evaporar Feromonas(T)
            #print("Feromonas(2)", T)
          #Seleccionamos el mejor agente
          mejor solucion = []
          mejor distancia = 10e100
          for h in range(N) :
            distancia actual = distancia total(Hormiga[h], problem)
            if distancia actual < mejor_distancia:</pre>
              mejor solucion = Hormiga[h]
              mejor distancia =distancia actual
          print(mejor solucion)
          print(mejor distancia)
        hormigas(problem, 1000)
        [0, 18, 9, 13, 32, 11, 15, 36, 20, 29, 30, 35, 34, 1, 27, 2, 41, 16, 31, 19, 26, 14, 7, 28, 12,
        10, 25, 4, 5, 6, 40, 8, 23, 22, 38, 17, 37, 33, 3, 24, 21, 39]
        3763
In [0]:
```