

第 3-11 讲: 旅行问题

姓名: 林凡琪 学号: 211240042

评分: _____ 评阅: _____

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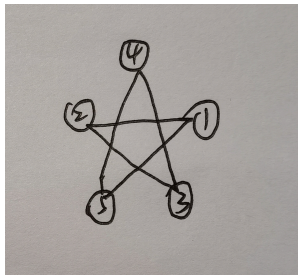
请独立完成作业, 不得抄袭。
若得到他人帮助, 请致谢。
若参考了其它资料, 请给出引用。
鼓励讨论, 但需独立书写解题过程。

1 作业 (必做部分)

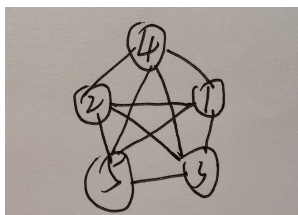
题目 1 (CZ 6.4)

解答:

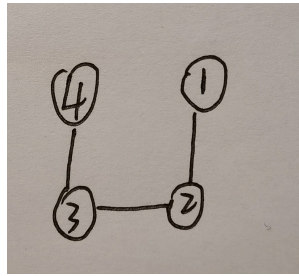
(a)



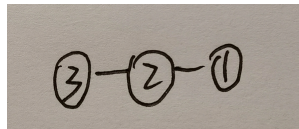
(b)



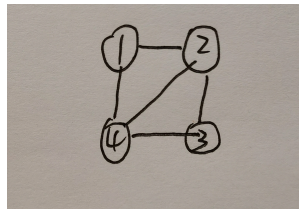
(c)



(d)



(e)



题目 2 (CZ 6.6)**解答:**

If n is connected to k regular graph G is not a Euler chart, it is known that k is odd, and it can be known that n can only be even.

Then in \overline{G} , the degree of each point is $n - k - 1$, which is an even number.

Therefore, if \overline{G} is connected, it is a regular graph.

题目 3 (CZ 6.10)**解答:**

(i) When G is Hamiltonian:

$$\forall x, y \in V(G) \wedge (x, y) \notin E(G)$$

$$\rightarrow \deg(x) + \deg(y) \geq 6 + 6 = 12 \geq 10$$

(ii) When $G-v$ is Hamiltonian:

$$\forall x, y \in V(G-v) \wedge (x, y) \notin E(G-v)$$

$$\rightarrow \deg(x) + \deg(y) \geq 5 + 5 = 10 \geq 9$$

(iii) When $G-v-u$ is Hamiltonian:

$$\begin{aligned} & \forall x, y \in V(G - v - u) \wedge (x, y) \notin E(G - v - u) \\ & \rightarrow \deg(x) + \deg(y) \geq 4 + 4 \geq 8 \end{aligned}$$

题目 4 (CZ 6.12)

解答:

(a) The nodes in $G + H$, if originally in G , is 14 in the new figure; If it was originally in H , it is 16 in the new figure; So it is *Eulerian*

(b) For any two nonadjacent nodes u, v in $G + H$, there is $\deg(u) + \deg(v) \geq 14 + 14 \geq 23$. Hence it is *Hamiltonian*

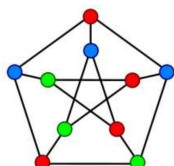
题目 5 (CZ 6.20)

解答:

(a) Proof by contradiction.

Suppose there is a secant point S in G , and from the inscription, we can see that there is a Hamiltonian path starting with S , let the path be S, x_1, x_2, \dots, T . Then after deleting S , there is still a path x_1, x_2, \dots, T , so that the remaining points are connected. Therefore, S is not a cut point, which contradicts the assumption.

(b) A counterexample



2 Open Topics

Open Topics 1 (竞赛图)

底图是完全图的有向图称为竞赛图。请证明: 竞赛图一定含有有向哈密尔顿通路

Open Topics 2 (循环赛排名)

请你给出一种合理的循环赛排名方法

3 反馈