Z3-Noodler - An Automata based String Solver

Theory and Practice of SMT Solving

Luís Felipe Ramos Ferreira

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  - *Stabilization-based procedure*
  - Heavy usage of *non deterministic automata*

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  - Union, concatenation, intersection, etc
- Very efficient and optimized

Architecture

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- Parser, rewriter and LIA solver

Architecture

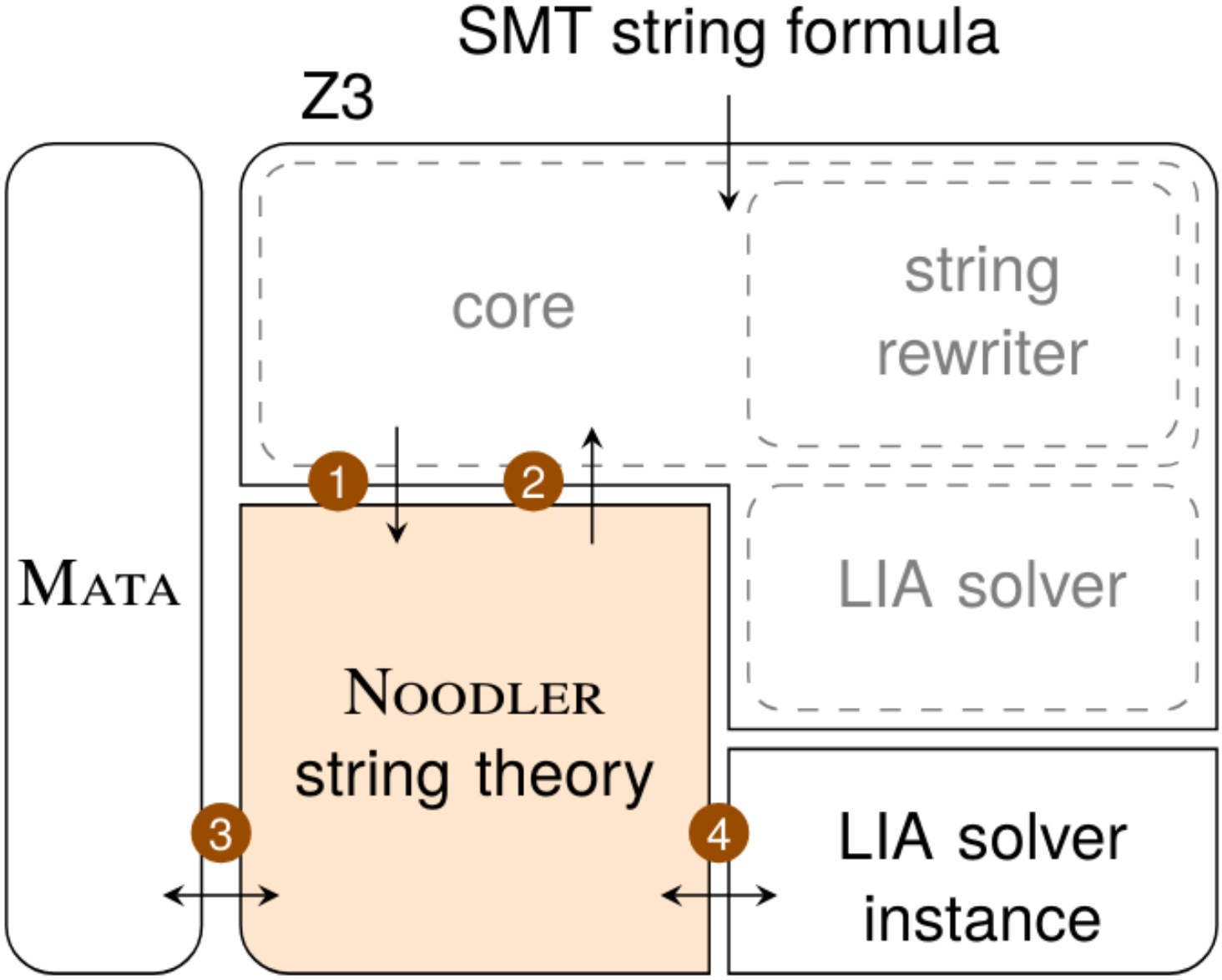

Figure 1: Z3-Noodler architecture

String Theory Core

- Axiom Saturation

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- Decision Procedures

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- $t_1 = t_2 \implies len(t_1) = len(t_2)$

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- $\neg \mathit{contains}(s, "abc")$ becomes $s \notin \Sigma^* abc \Sigma^*$

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- After stability, length constraints are added and fed to the LIA solver

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- Regular constraints enforce *UNSAT*

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- $xy = zw \wedge len(x) = len(z) \implies y = w$

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- Z3-Noodler is complete for the chain-free fragment with unbounded disequations, regular constraints and quadratic equations
- Outside of this, the theory is sound but not complete

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- The same happens in the *Equations* group
- cvc5 is the best one in *Predicates Small*, while Z3-Noodler performed poorly
- Z3-Noodler could, however, be further improved by proper axiom saturation for predicates or lazy predicate evaluation

The end

- Thanks!