

DARK ENERGY

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Cosmologia - Gravitació i astropartícules

- Introduction
- Equations
- Candidates

- DE -> Modern & unknown
- Universe expanding
 - Observational evidence from supernovae for an accelerating universe and a cosmological constant (A.Riess et al.) 1998
 - Measurements of omega and lambda from 42 high redshift supernovae. (S. Perlmutter *et al.*) 1999

DE ~ expansion

Beginnings

- Einstein wants a static universe.

GR don't permit it (Matter attracts gravitionally)

He added a term (cosmological constant) to arrange a static UNI

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} - \Lambda g_{\mu\nu} = 8\pi G T_{\mu\nu}$$

- Hubble law -> expansion -> problem!

The standard cosmological model

- Cosmological principle: Universe is isotropic and homogeneous (on large scales)
- Metrics: equation which gives the distance between two points
 - SR -> Minkowsky metric

$$ds^2 = -c^2 dt^2 + dr^2 + r^2 d\Omega^2$$

- GR -> Robertson-Walker metric

$$ds^2 = -c^2 dt^2 + a(t)^2 \left[dr^2 + S_k(r)^2 d\Omega^2 \right]$$

t: cosmic time

r: comoving coordinates

Dynamics: relations between curvature & content ($a(t)$, k , R_0 , $\varepsilon(t)$ & $P(t)$)

- **Friedmann equation.** Rel. between $a(t)$, k , $\varepsilon(t)$ & R_0

$$H(t)^2 = \frac{\dot{a}(t)^2}{a(t)^2} = \frac{8\pi G}{3c^2} \varepsilon(t) - \frac{kc^2}{R_0^2 a(t)^2}$$

- **Fluid equation.** Rel. between $a(t)$, $\varepsilon(t)$ & $P(t)$

$$\dot{\varepsilon} + 3 \frac{\dot{a}}{a} (\varepsilon + P) = 0$$

- **Acceleration equation.** Rel. between $a(t)$, $\varepsilon(t)$ & $P(t)$

$$\frac{\ddot{a}}{a} = - \frac{4\pi G}{3c^2} (\varepsilon + 3P)$$

- **Equation of state.** Rel. between $\varepsilon(t)$ & $P(t)$

$$P = w\varepsilon \quad \text{where } w < 1$$

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$$P = \omega \varepsilon \quad \text{where } w < 1$$

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$$W < -1/3$$

\wedge

$$W = -1$$

Equations with lambda

- **Friedmann equation.** Rel. between $a(t)$, k , $\epsilon(t)$ & R_0

$$H(t)^2 = \frac{\dot{a}(t)^2}{a(t)^2} = \frac{8\pi G}{3c^2} \epsilon(t) - \frac{kc^2}{R_0^2 a(t)^2} + \frac{\Lambda}{3}$$

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$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3c^2} (\epsilon + 3P) + \frac{\Lambda}{3}$$

Einstein wanted to find $H=0$. In a flat Universe

$$\Lambda = -\frac{8\pi G}{c^2} \epsilon$$

“New component”

- $\Lambda \sim \text{fluid}$

$$P_{\Lambda} = -\varepsilon_{\Lambda} = -\frac{c^2}{8\pi G} \Lambda$$

- Λ has a negative effective pressure.
As UNI expands, work is done on Λ fluid.
-> E_{Λ} remains constant

$$W = -\int P dV$$

-> Energy of the empty space (vacuum)

- Classical physics
 - (“Nothing can come from nothing.” King Lear)
- Quantum physics

$$\Delta E \Delta t \geq h$$

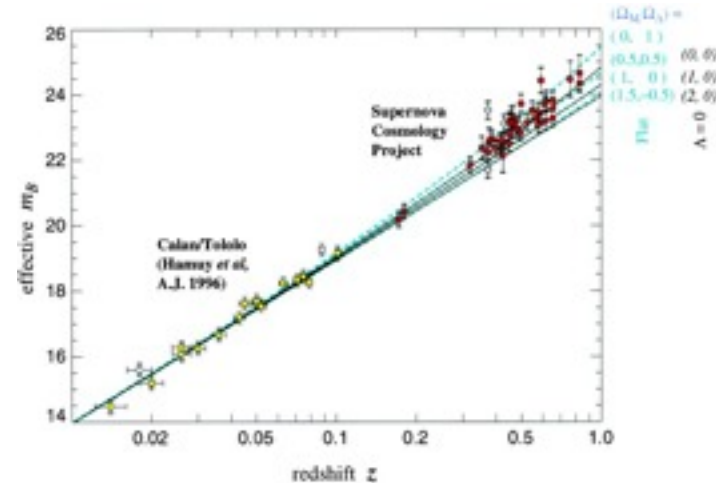
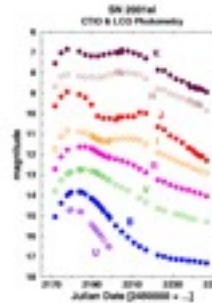
$$\epsilon_{VAC} \sim \frac{E_P}{l_P^3} \approx 3 \times 10^{133} \text{ eV} \times m^{-3} \sim 10^{124} \rho_{critical}$$

Theory and
observations
don't match

Evidences

- Observation of SNIa

Standardized standard candles



$$m - M \approx 43.17 - 5 \log_{10} \left(\frac{H_0}{70 \text{ km s}^{-1} \text{ Mpc}^{-1}} \right) + 5 \log_{10} z + 1.086(1 - q_0)z$$

– The best model is

$$\Omega_M \approx 0.3$$

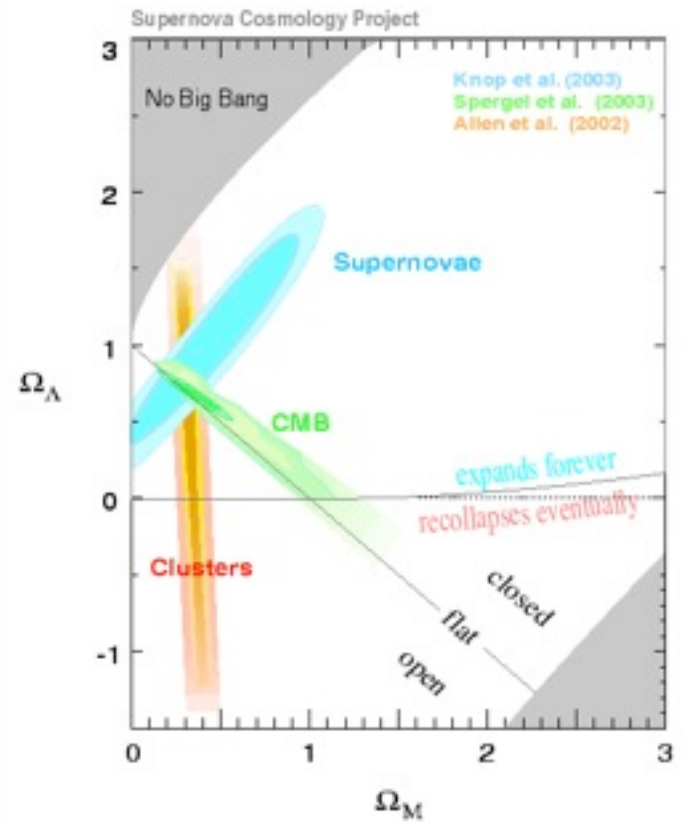
$$\Omega_\Lambda \approx 0.7$$

- Universe only with Λ (or Λ -dominated)

Friedmann equation $\dot{a}^2 = \frac{8\pi G \epsilon_{\Lambda}}{3c^2} a^2 \longrightarrow a(t) = e^{H_0(t-t_0)}$

Universe exponentially expanding

Infinitely old, infinite horizon distance

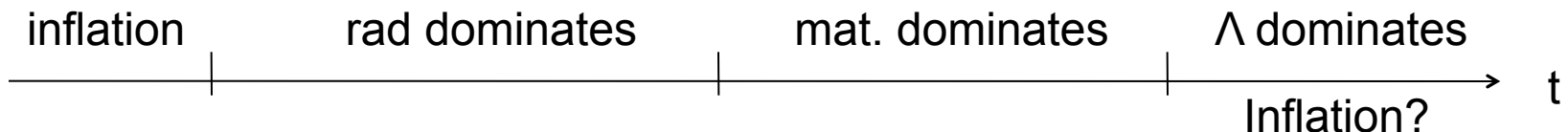


Inflation

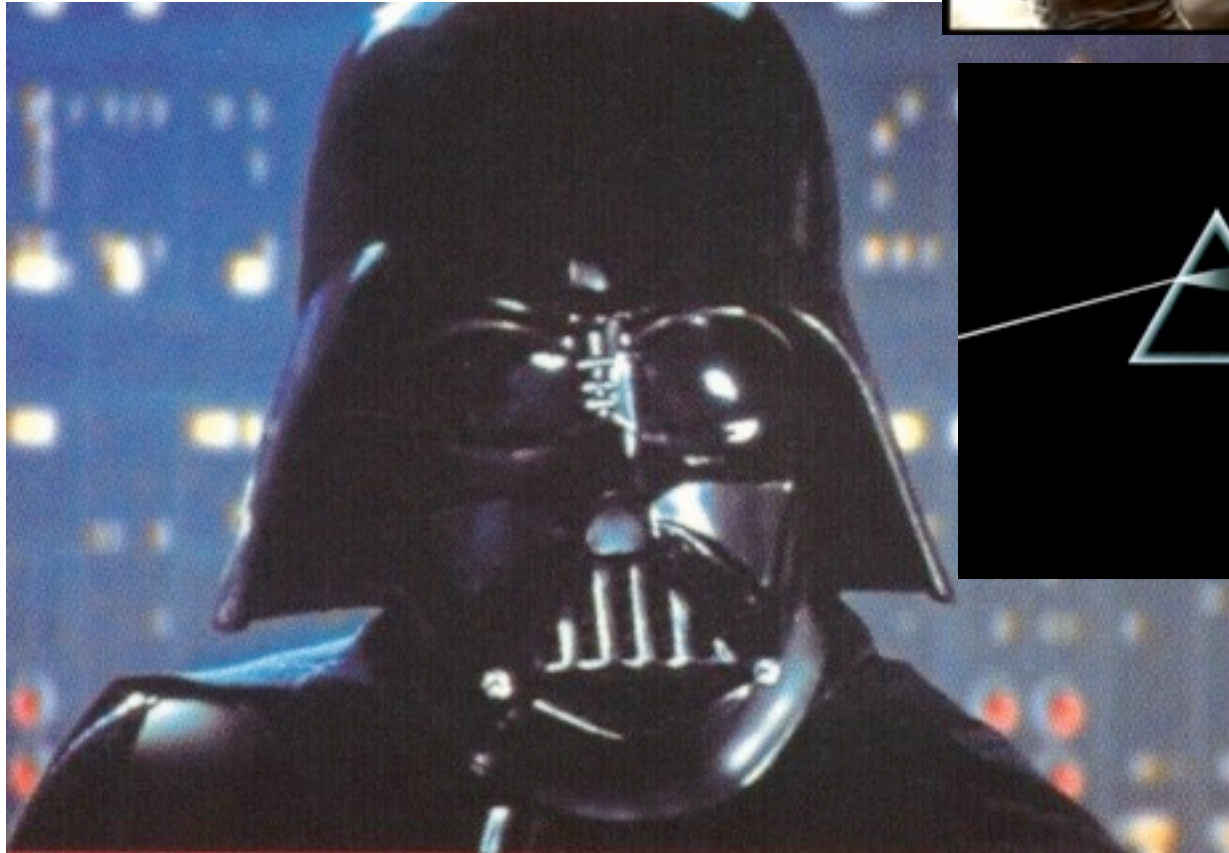
- DE is fundamental in inflation (Guth 1981)

Early period in the history of the Universe,
when the expansion was accelerating
outward

$$\ddot{a} > 0$$

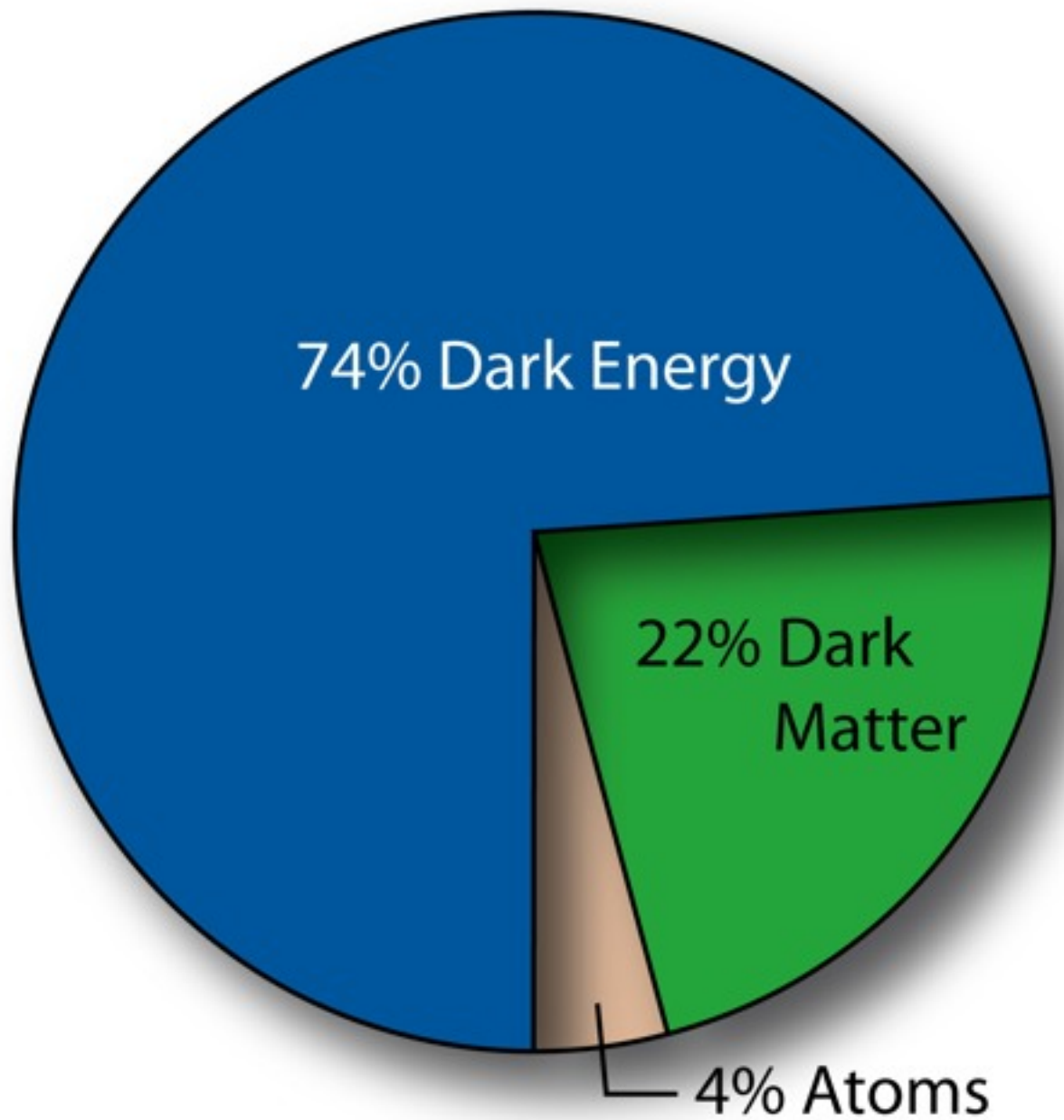


DE is not...



What can be DE?

- Transient phenomenon, which will disappear in the future
- Cosmological constant (Λ CDM model)
- Scalar field (quintessence). Λ is not constant, exhibits slow variation
- Modified gravity (Gauss-Bonnet: extradimensions)



LOS ESCAÑOS TOTAL ESCAÑOS 135 MAYORÍA ABSOLUTA 68

ESCRUTADO: 100%



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100



DARK MATTER

30



ATOMS

5

