

# **Stellar population synthesis models**

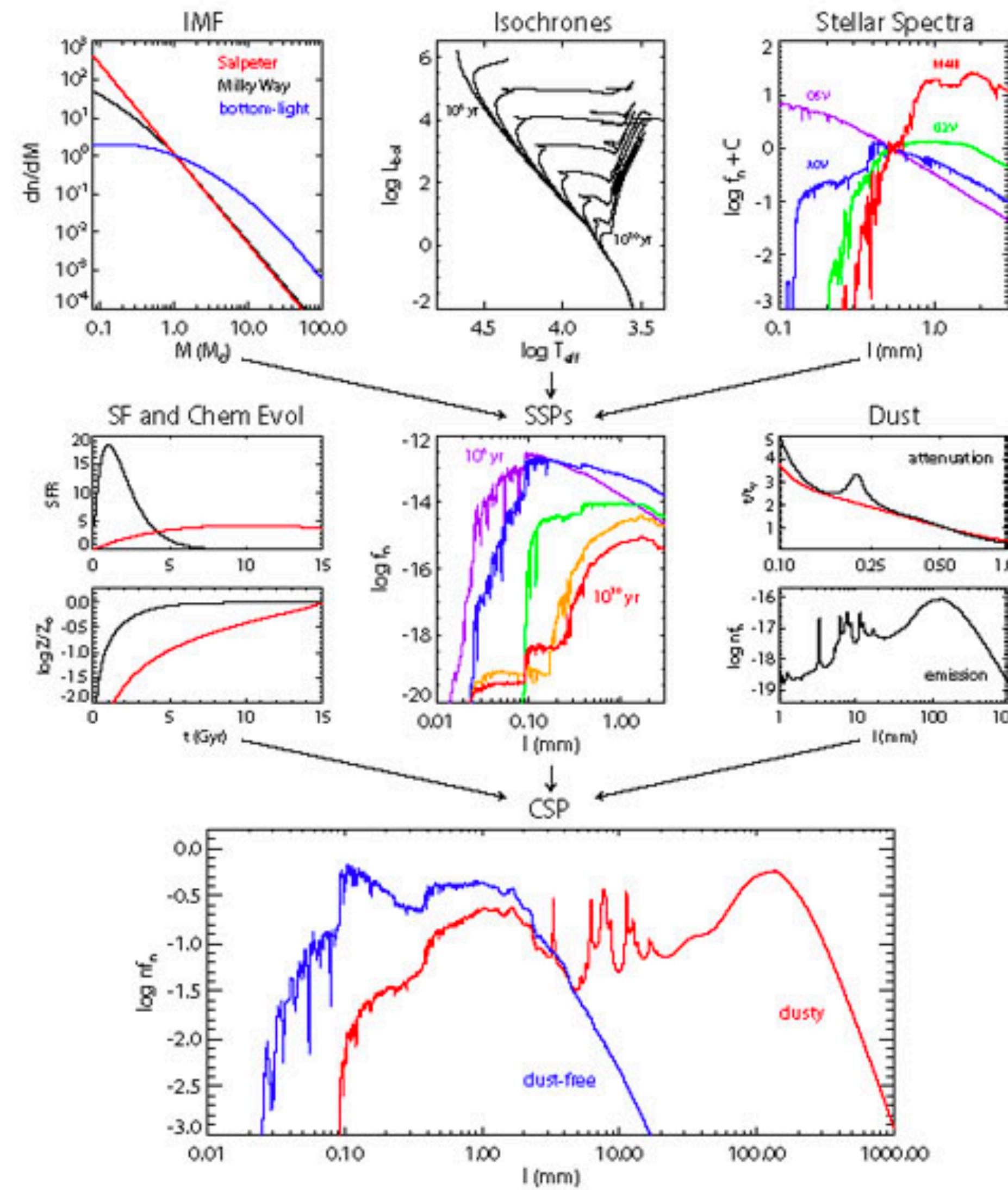
**Lluís Galbany (RyC fellow, ICE-CSIC)**

**Galaxies and extragalactic astrophysics**

# Introduction

- The light coming from a galaxy is the sum of all the contribution to the emission of its **stars** and **gas** content and therefore has the information of its stellar formation history (which and how many stars have been formed and when)
- The stellar Population Synthesis models predict the spectra of galaxies (stellar populations) changing the number of stars that are formed and the time at which they are formed
- Fundamental to interpret galaxy spectra

# Ingredients



IMF, isochrones for a range of ages and metallicities, and stellar spectra spanning a range of  $T_{\text{eff}}$ ,  $L_{\text{bol}}$ , and metallicity.

SFH and chemical evolution, SSPs, and a model for dust attenuation and emission.

final CSPs both before and after a dust model is applied.

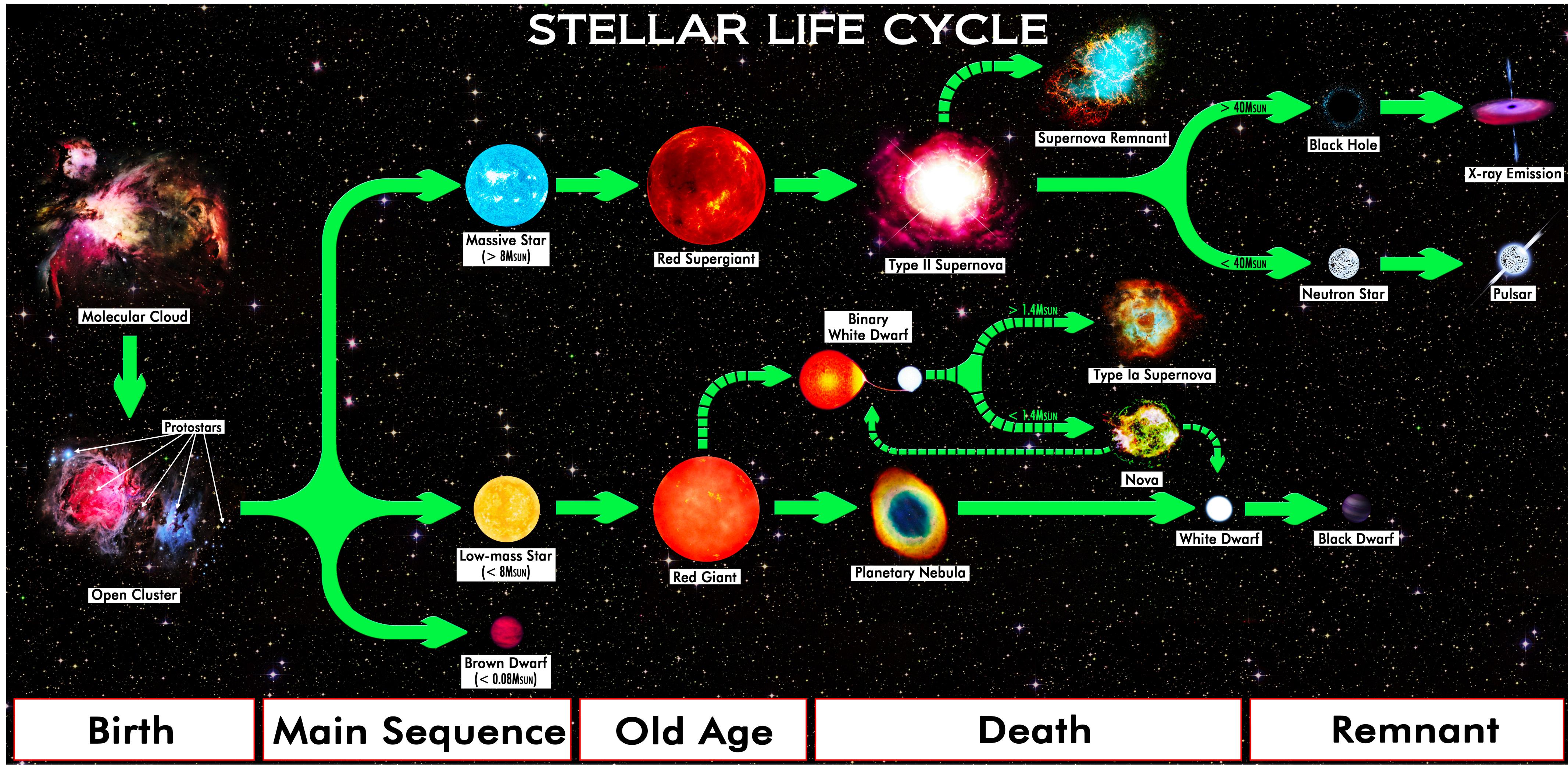
# Ingredients

- Star Formation Rate (SFR): gives the number of stars formed per unit time  
exponential law
- Initial mass function (IMF): gives the number of stars formed as a function of the mass

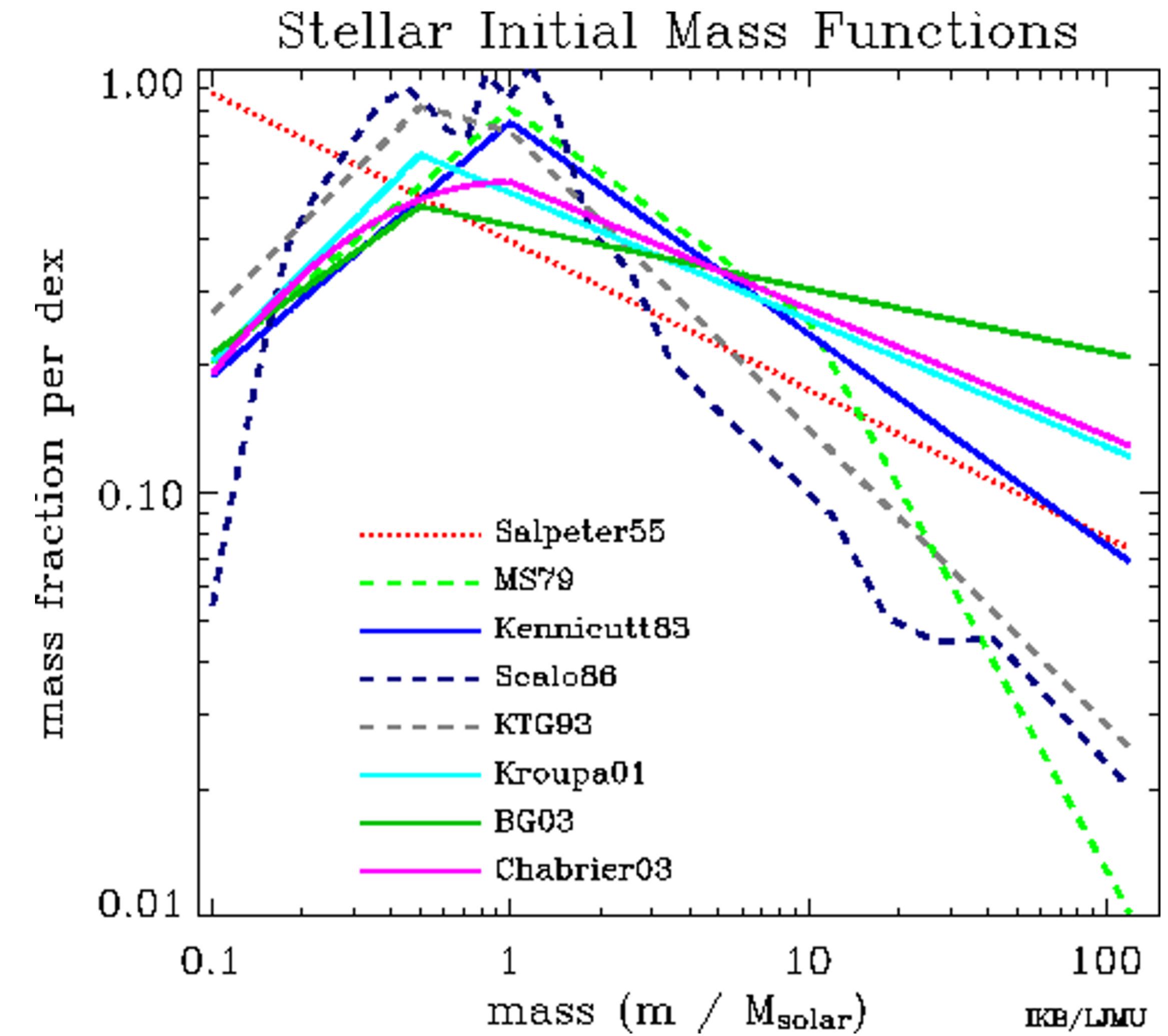
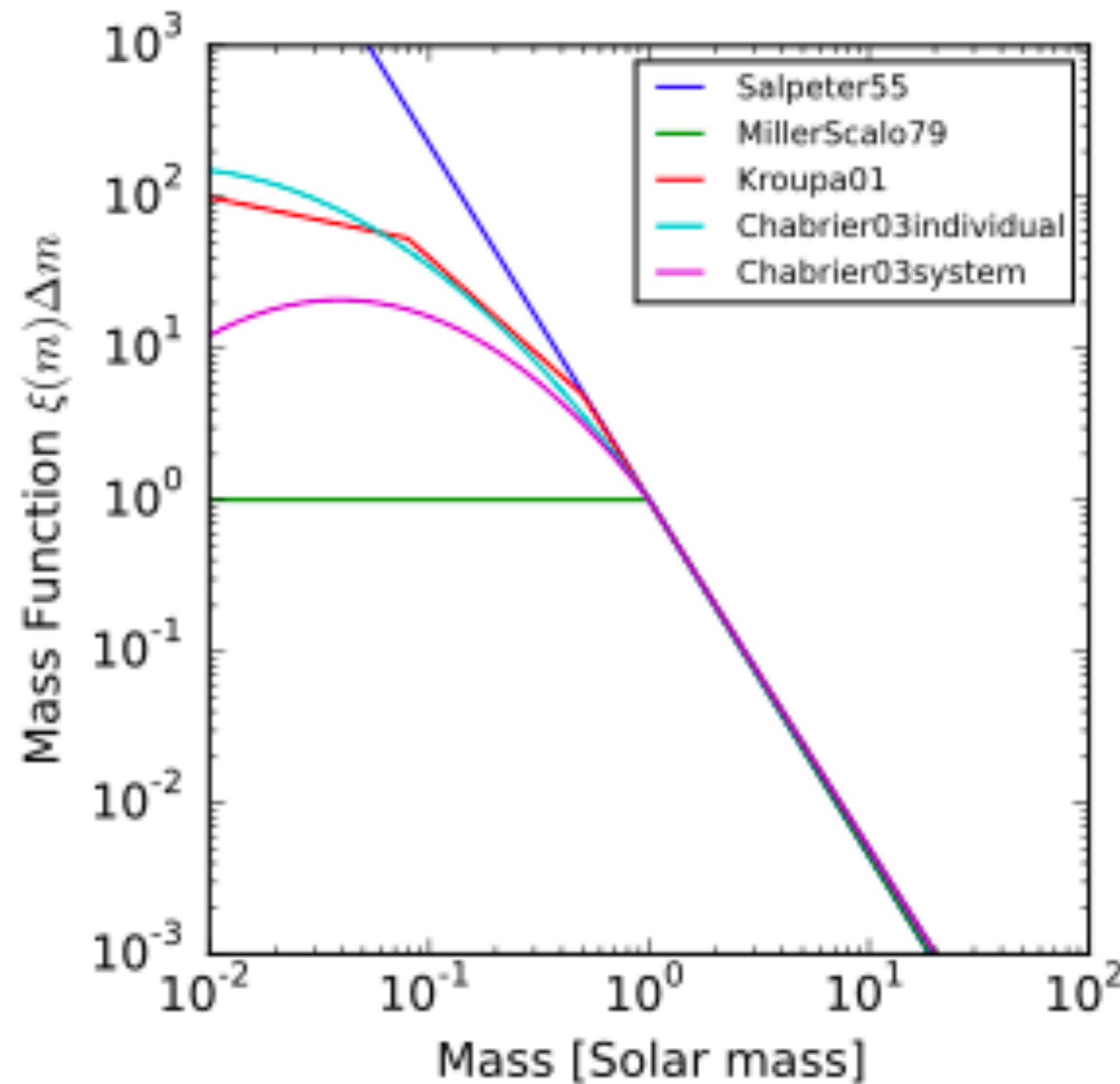
Salpeter:  $\text{IMF}(m) \propto m^{-2.35}$

- Evolutionary tracks: evolution in the HR diagram of stars of a given mass
- Isochrones: position in the HR diagram of stars of different mass at the same evolutionary stage

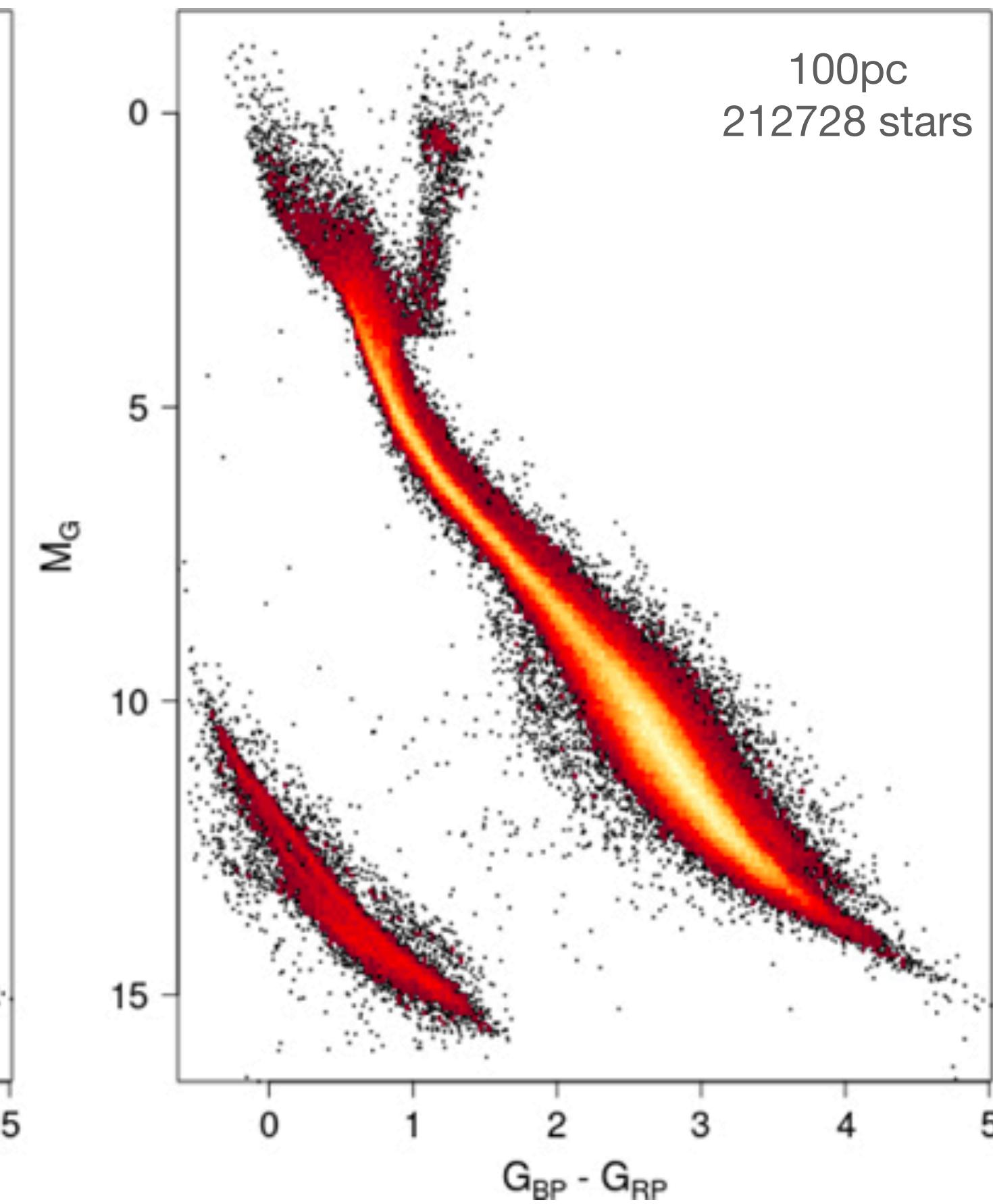
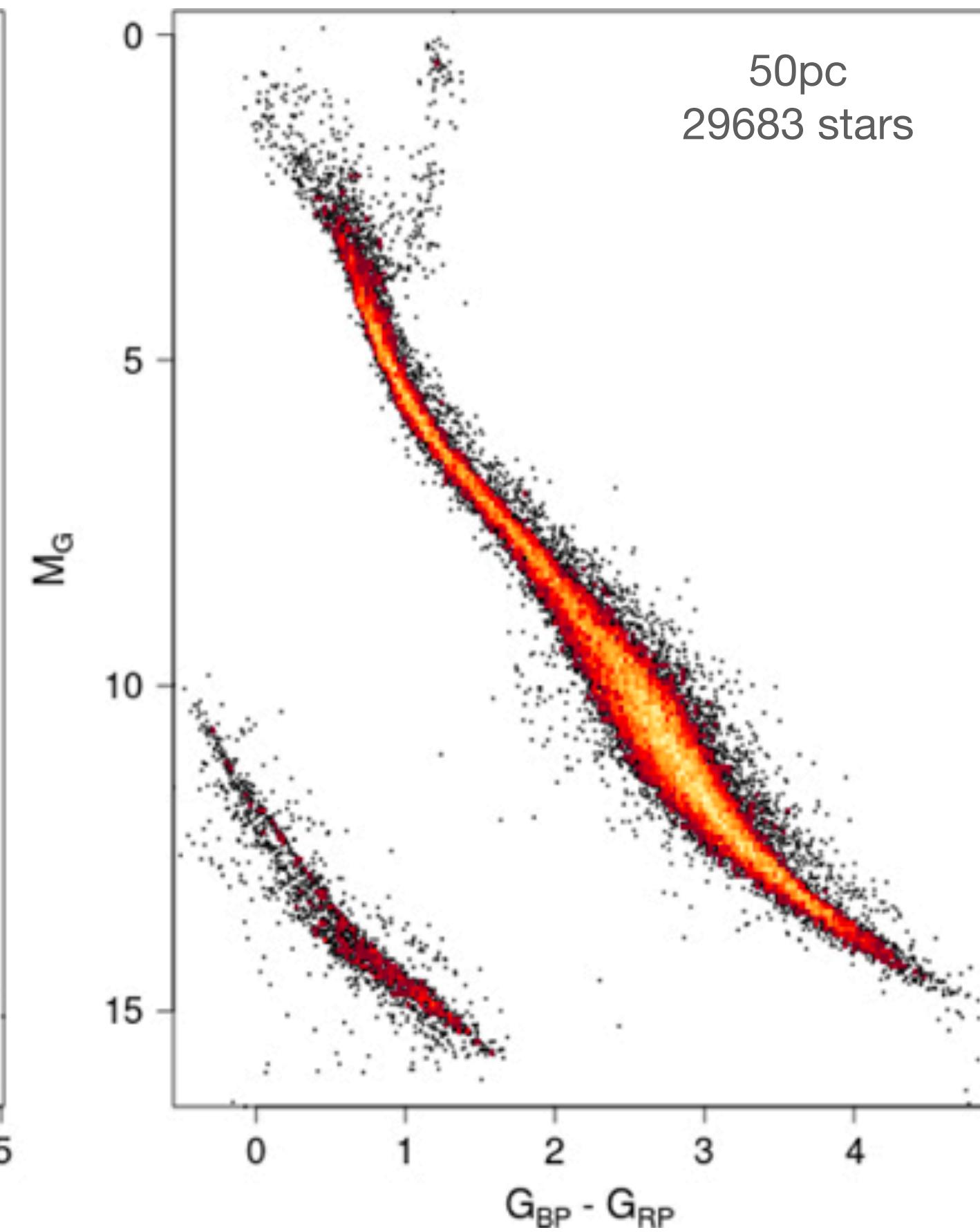
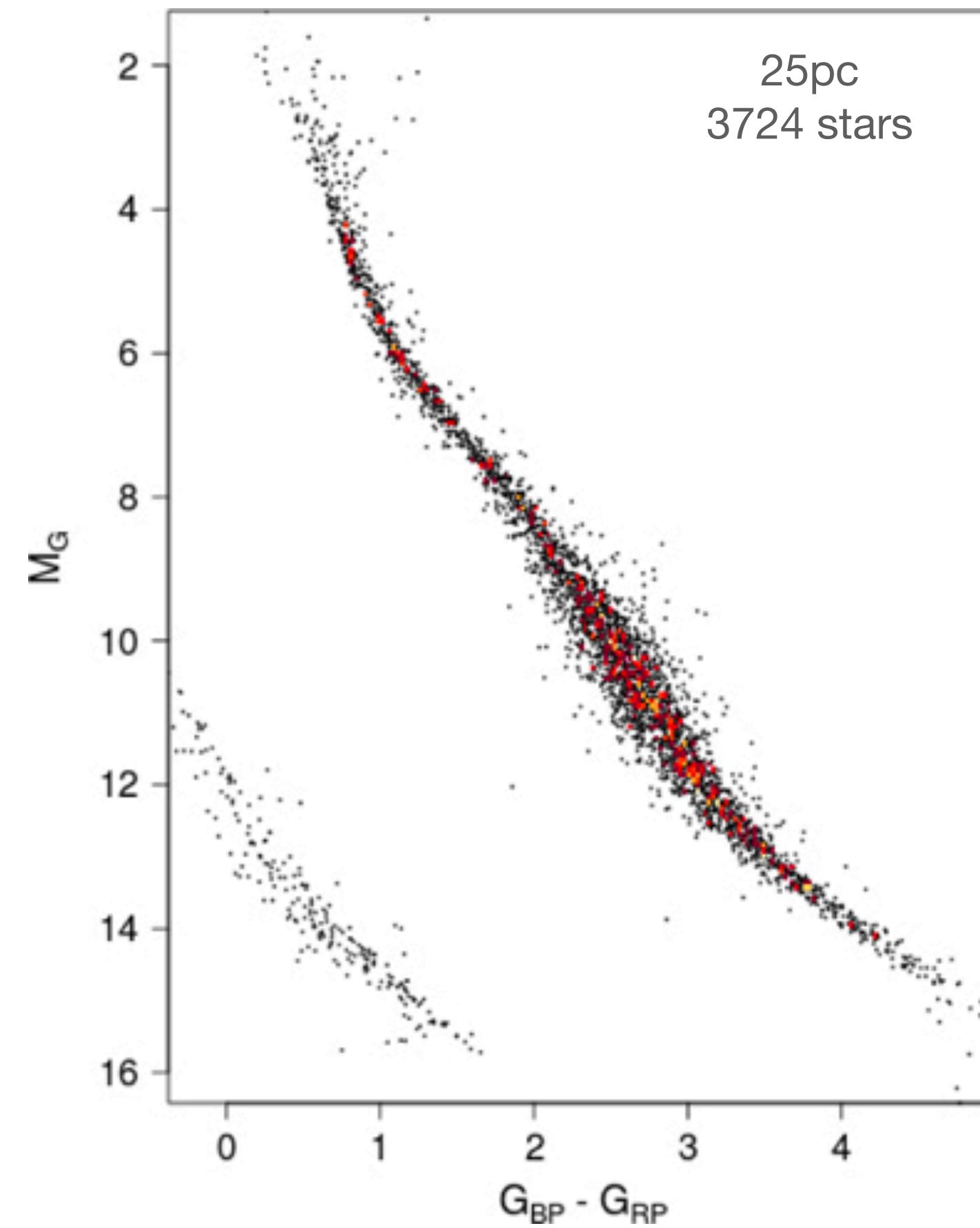
# Initial Mass Function



# Initial Mass Function



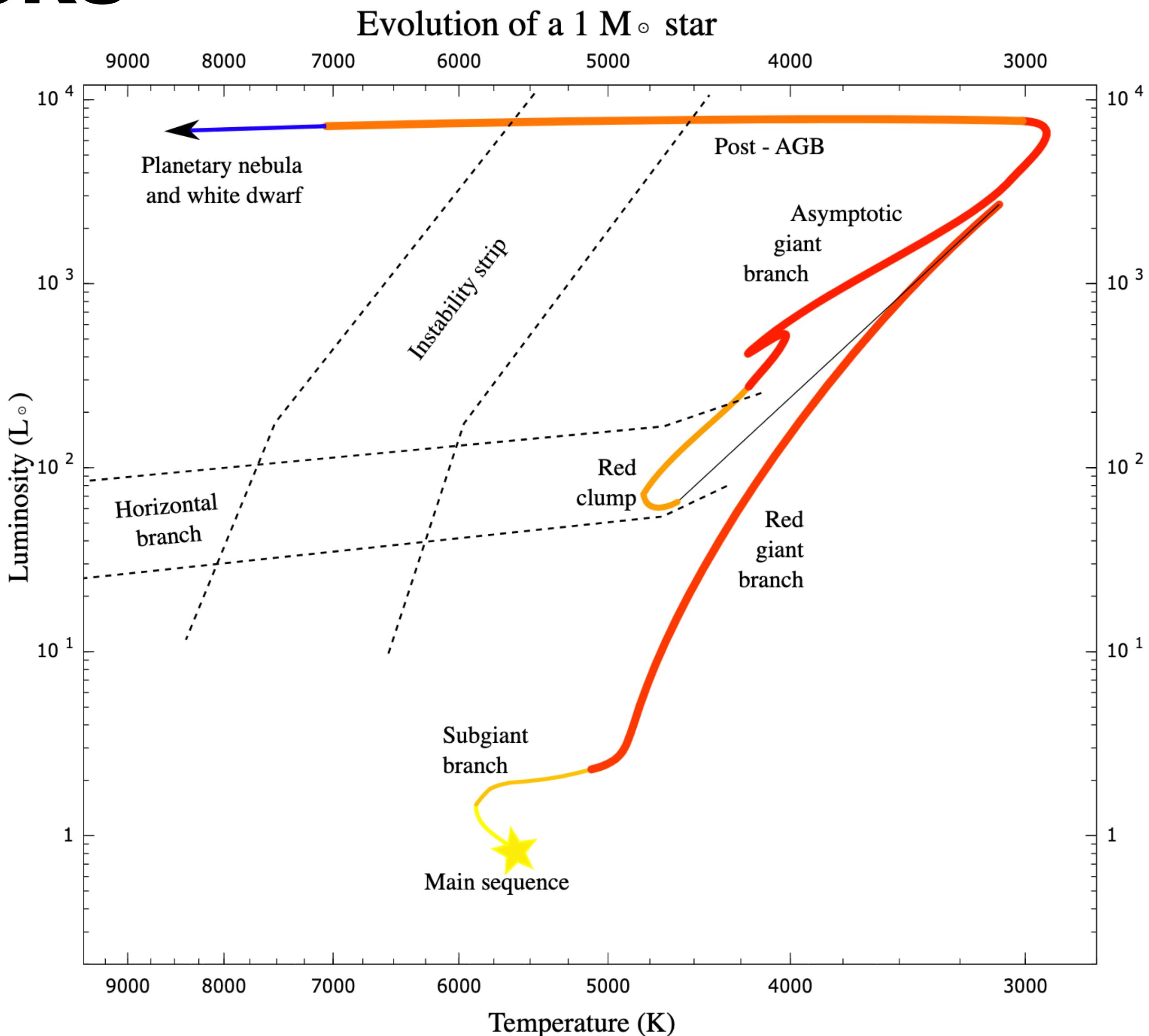
# Gaia Solar neighbourhood HRD



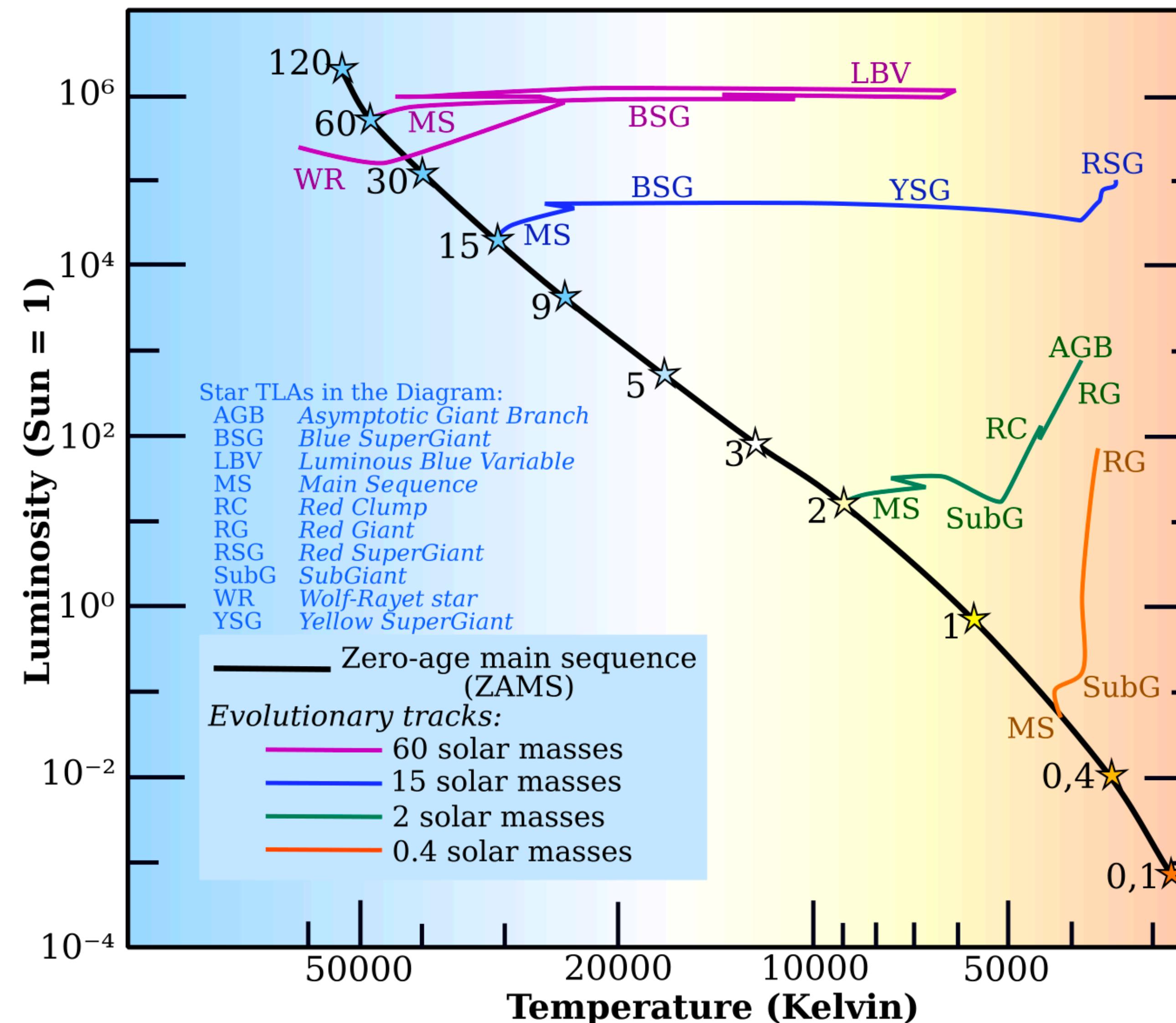
# Evolutionary tracks

Table 5.1 Features in the CM diagram

Feature	Physical significance
Main sequence (MS)	Core H burning
Subgiant branch (SGB)	Transition from core to shell H burning
Red giant branch (RGB)	Shell burning of H
Horizontal branch (HB)	Core He burning
Red clump (RC)	Stubby red HB formed by more metal-rich stars
Asymptotic giant branch (AGB)	Shell He burning
Instability strip	$\text{He}^+$ ionization zone gives rise to regular variables
White-dwarf sequence	Cooling electron-degenerate stars



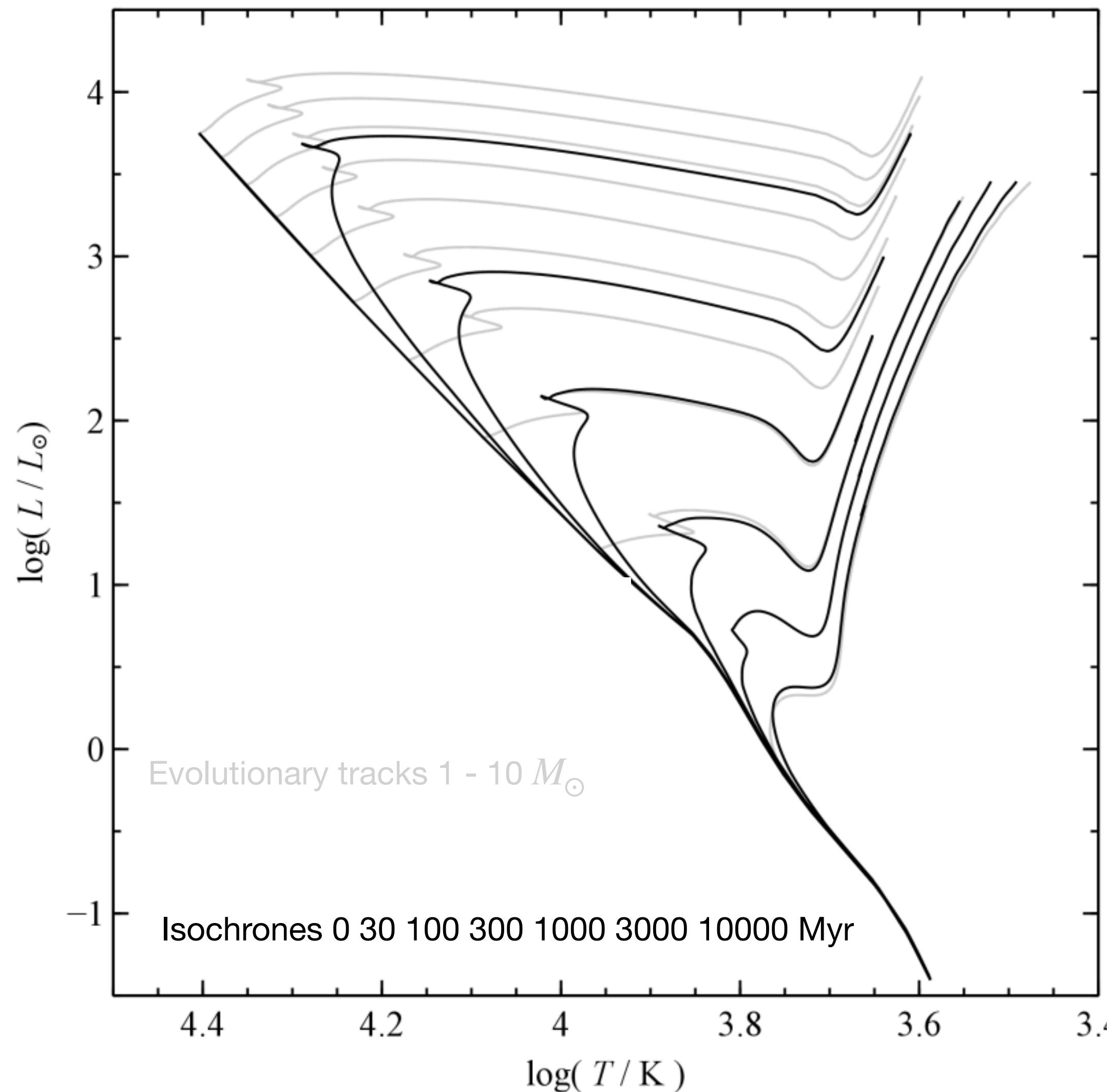
# Evolutionary tracks



HR diagram

Dependence (~shift) on  
metallicity, rotation, binary...

# Isochrones



Isochrones: set of stellar models compute at the **same (iso) age (chrone)**.

use a stellar evolution code to compute evolutionary tracks for a number of stars of different masses, and then they connect all the models of different masses at the **same age**.

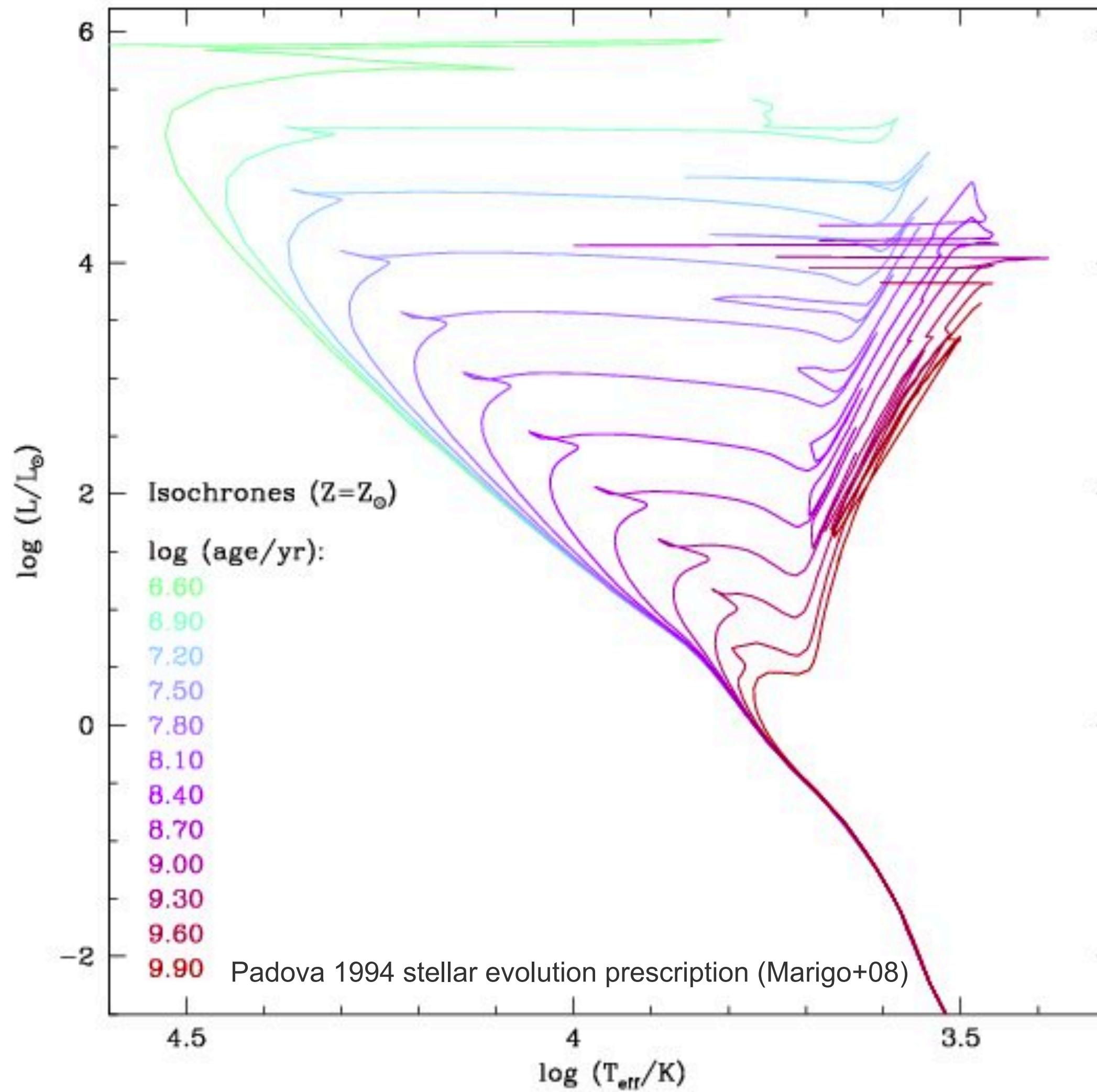
grey lines are evolutionary tracks for stars with masses from 1 to 10 solar masses

they all evolve at different rates

30 Myr: most massive stars have already disappeared  
Stars around 6-7  $M_\odot$  exhausted H in the core,  
lower mass stars have barely budged.

As the isochrones get older, more and more stars "peel away" from the ZAMS. But the very low-mass stars don't budge at all.

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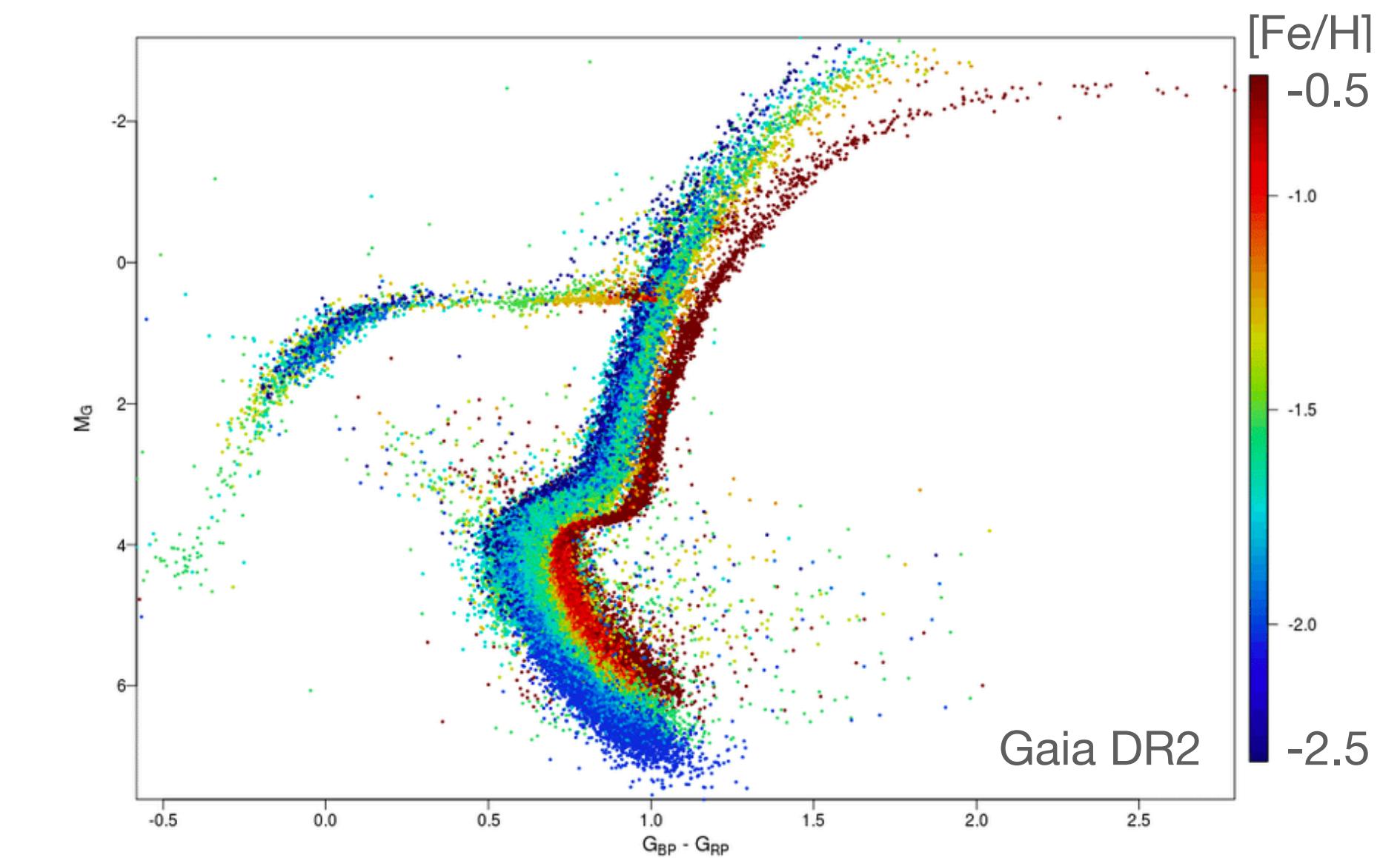
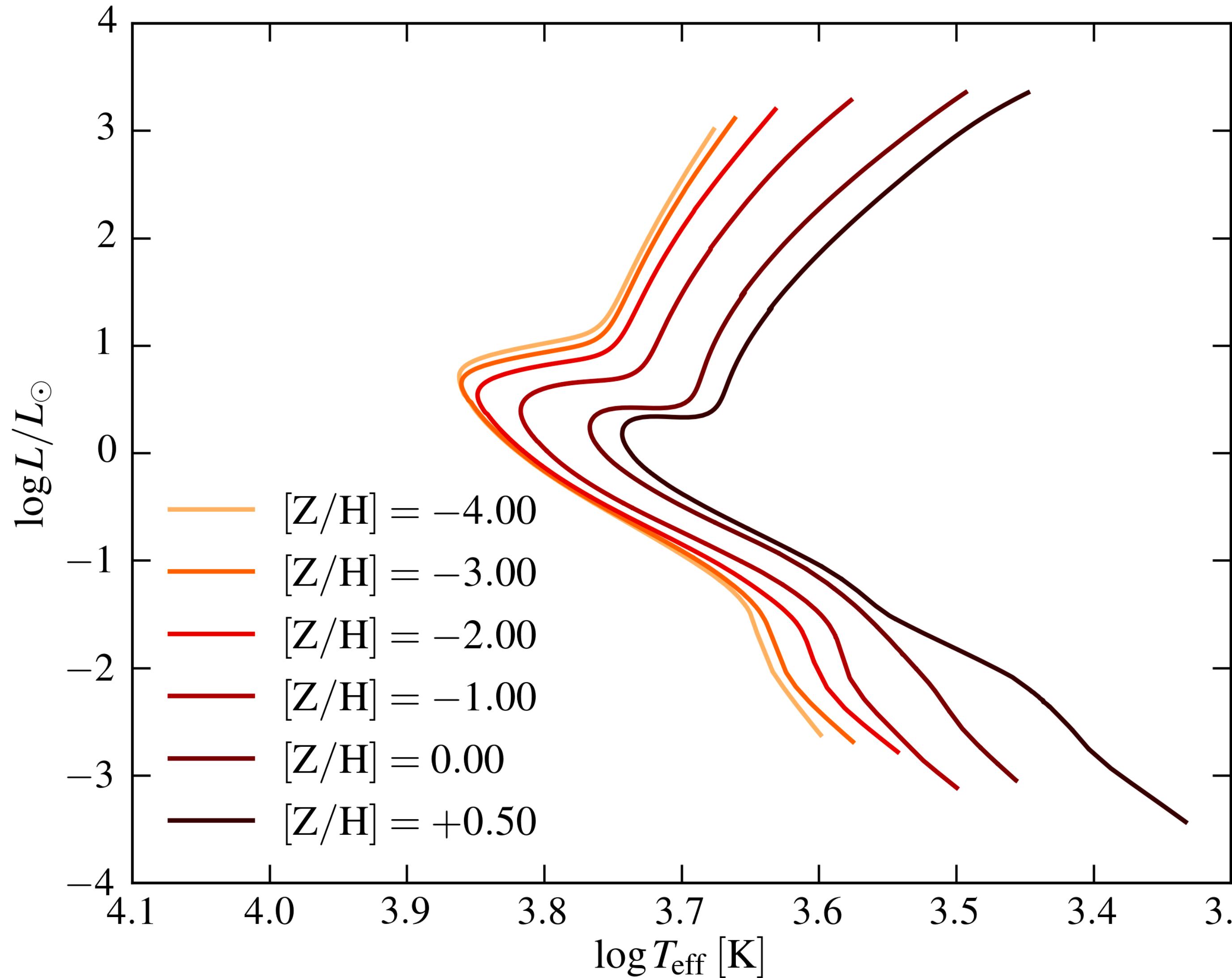
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# Isochrones - dependence on metallicity



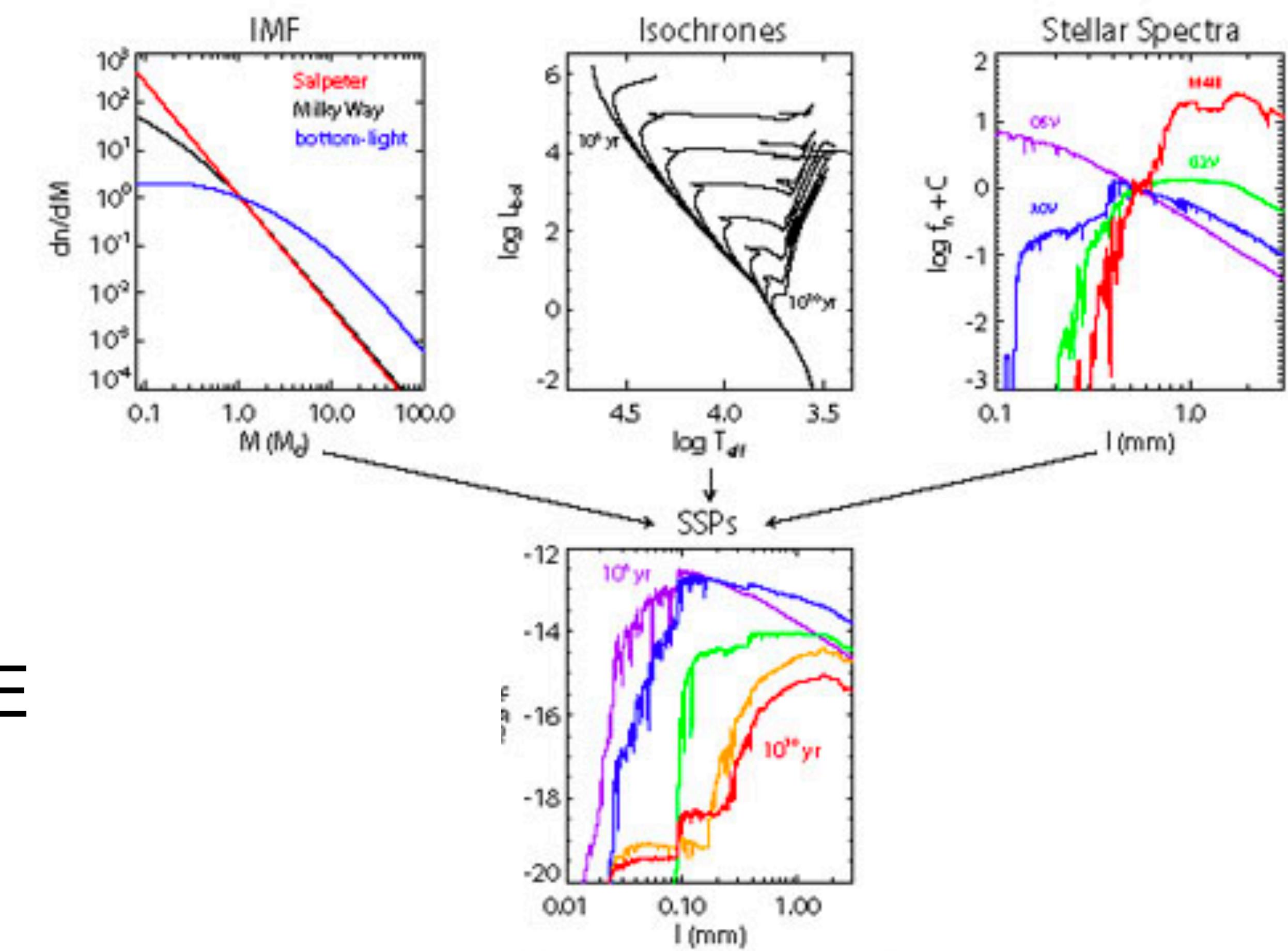
**MESA**  
**Isochrones &**  
**Stellar Tracks**

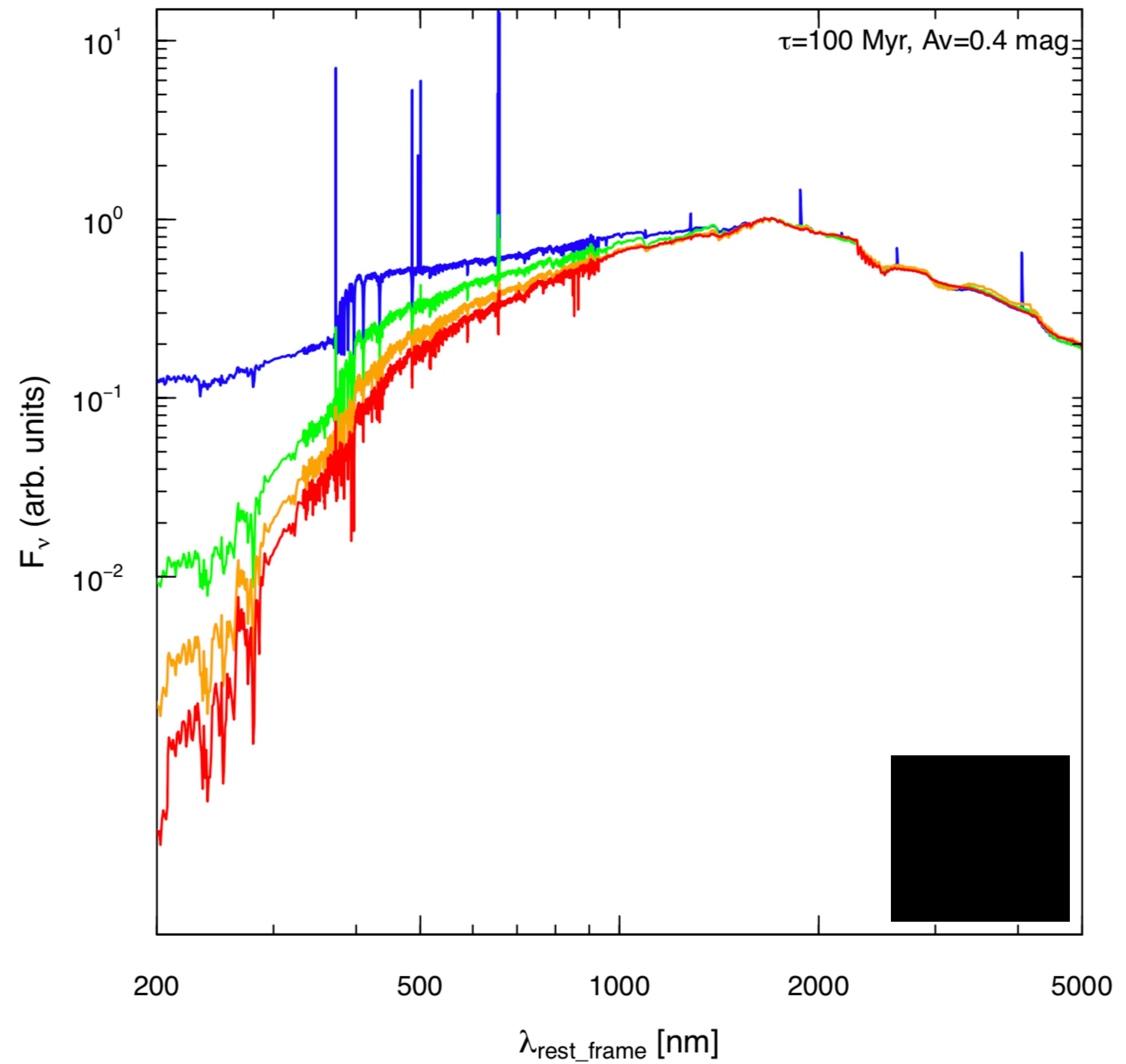
# Ingredients

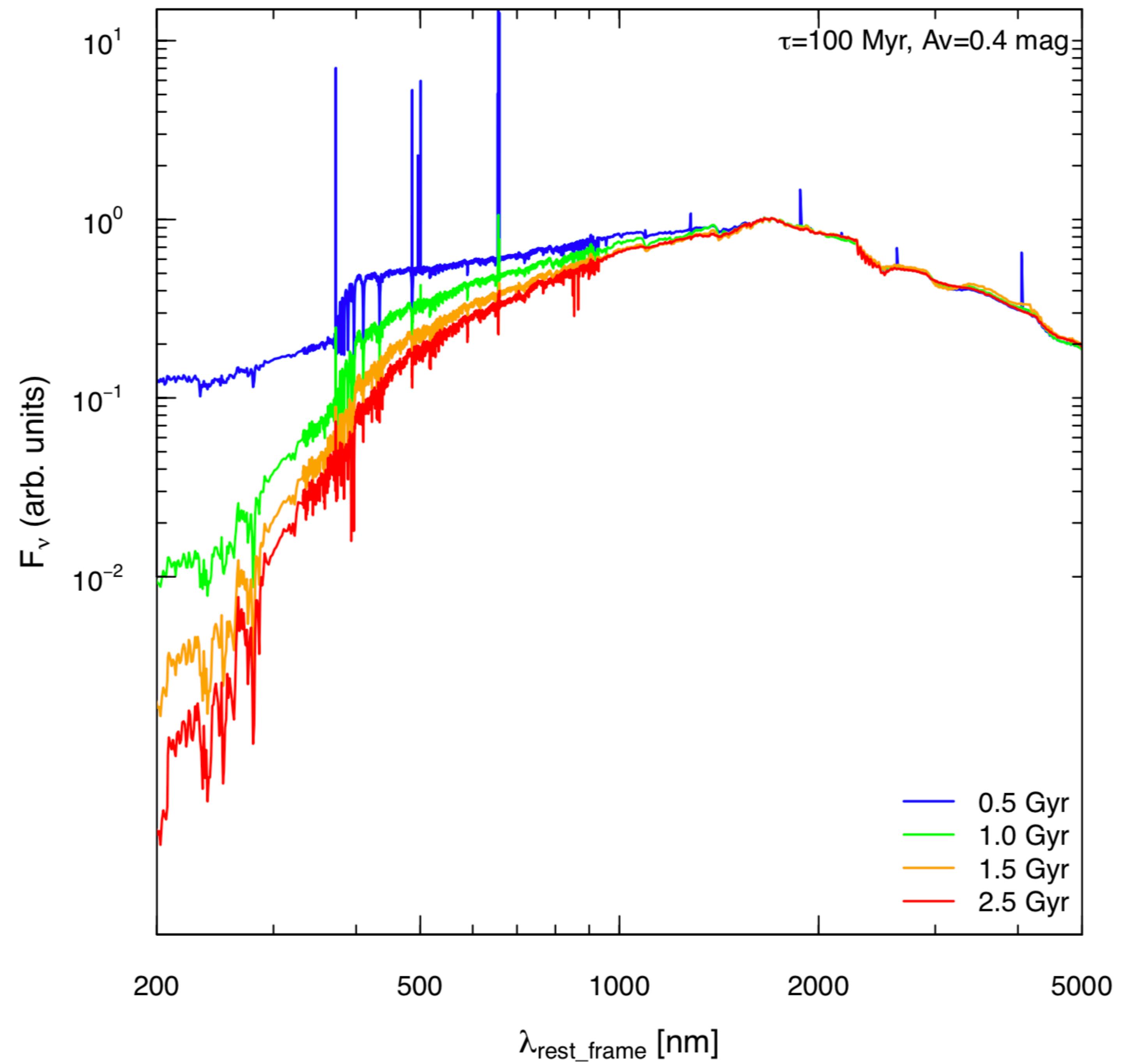
- SFR -> IMF (Salpeter, Kroupa, Chabrier...)
- Evolutionary tracks -> isochrones (Padova, Geneva...)
- Stellar library: spectra that sample parameter space: ( $T$ ,  $g$ ,  $Z$ ) and  $t$ 
  - BaSeL: theoretical synthetic spectra
  - STELIB: observational spectra
  - Kuruc models: theoretical synthetic models
  - MILES: observational spectra
  - ...

# SSP Models

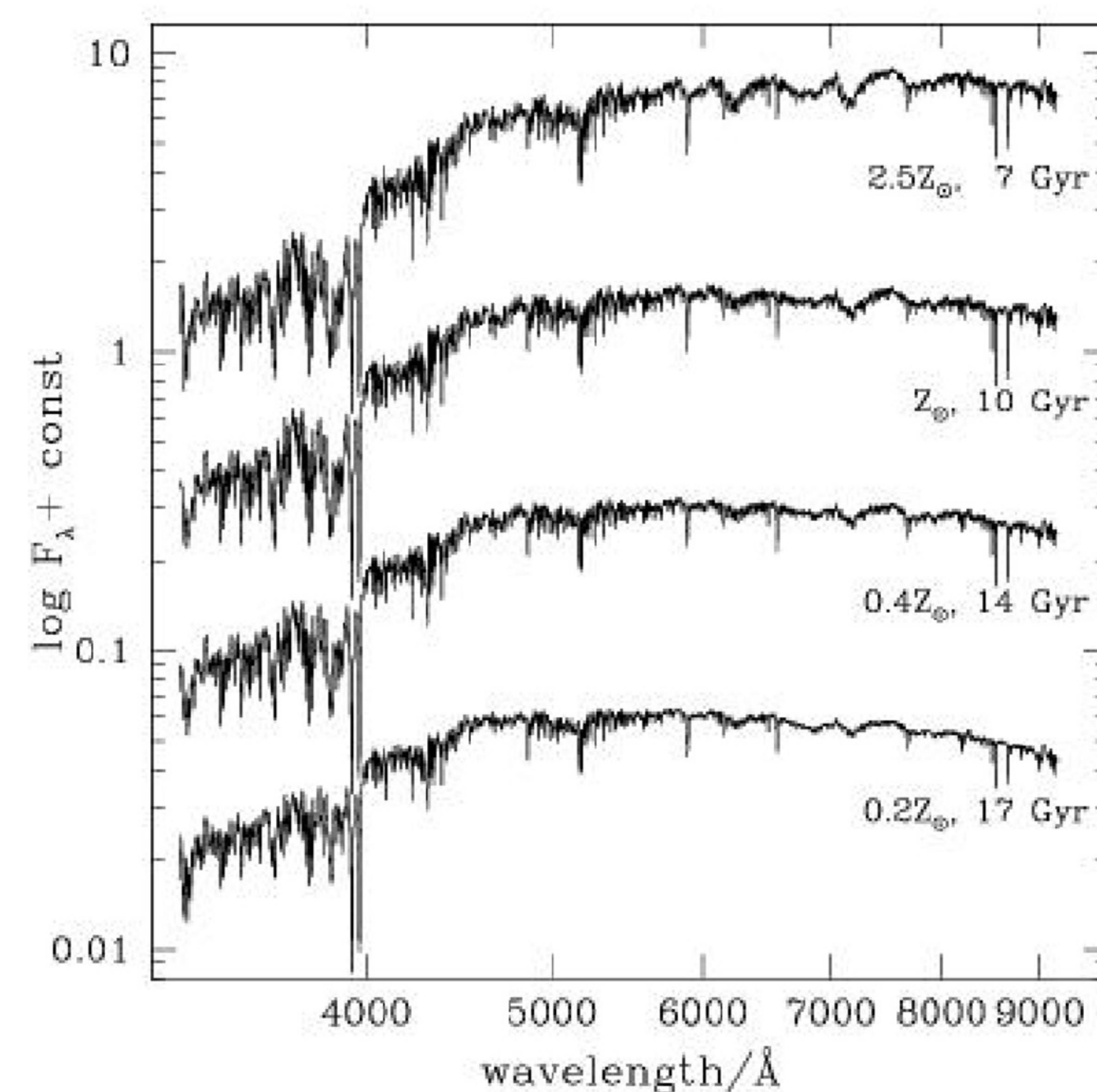
- Goal: reproduce the integrated light of stellar populations adding the contributions of the individual stars forming a galaxy
- Isochrone synthesis or adding of single stellar populations (SSP):
  - Bruzual & Charlot
  - Fioc, Rocca-Volmerange: PEGASE
  - Leitherer et al: STARBURST99
  - Maraston
  - FSPS (Conroy)

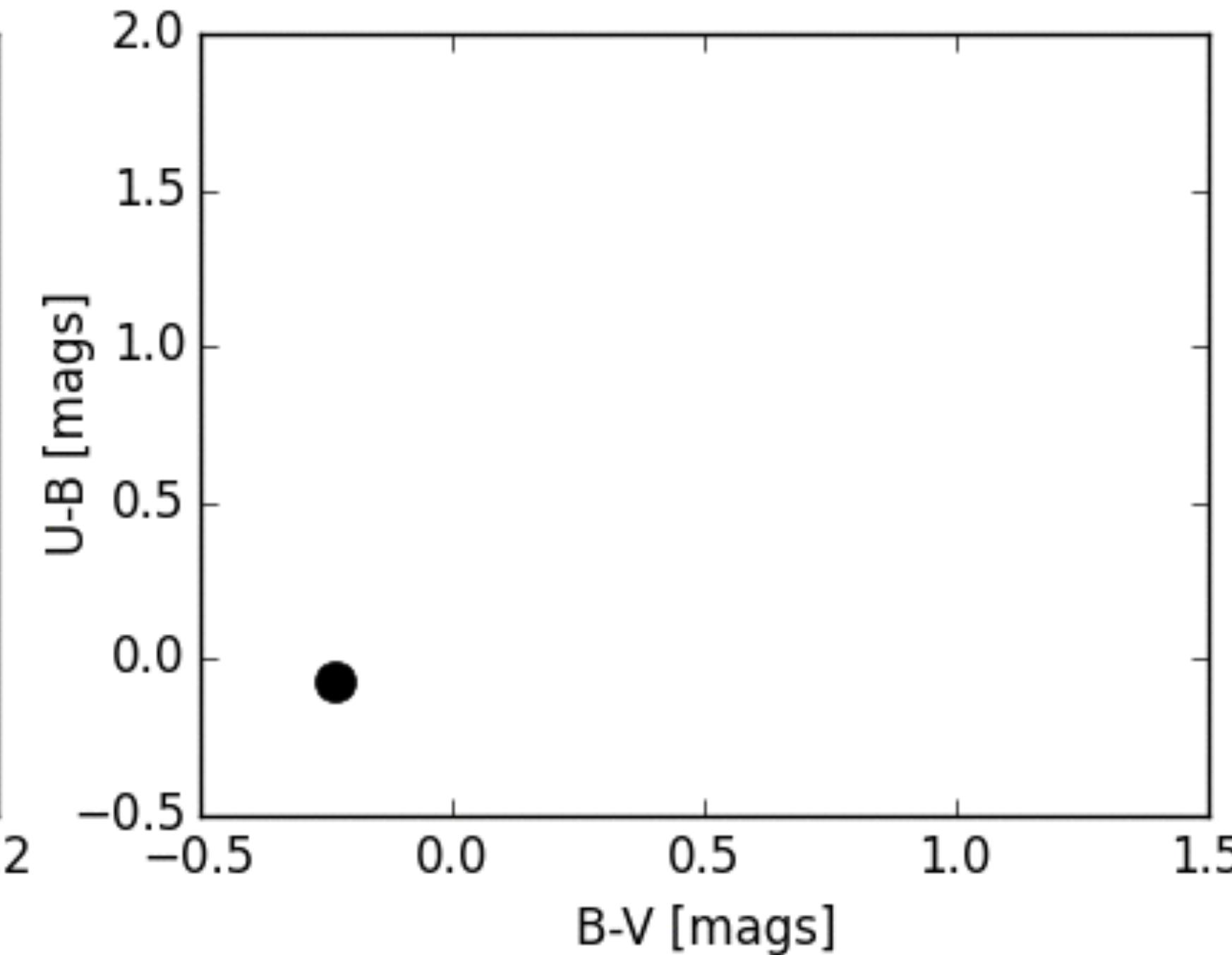
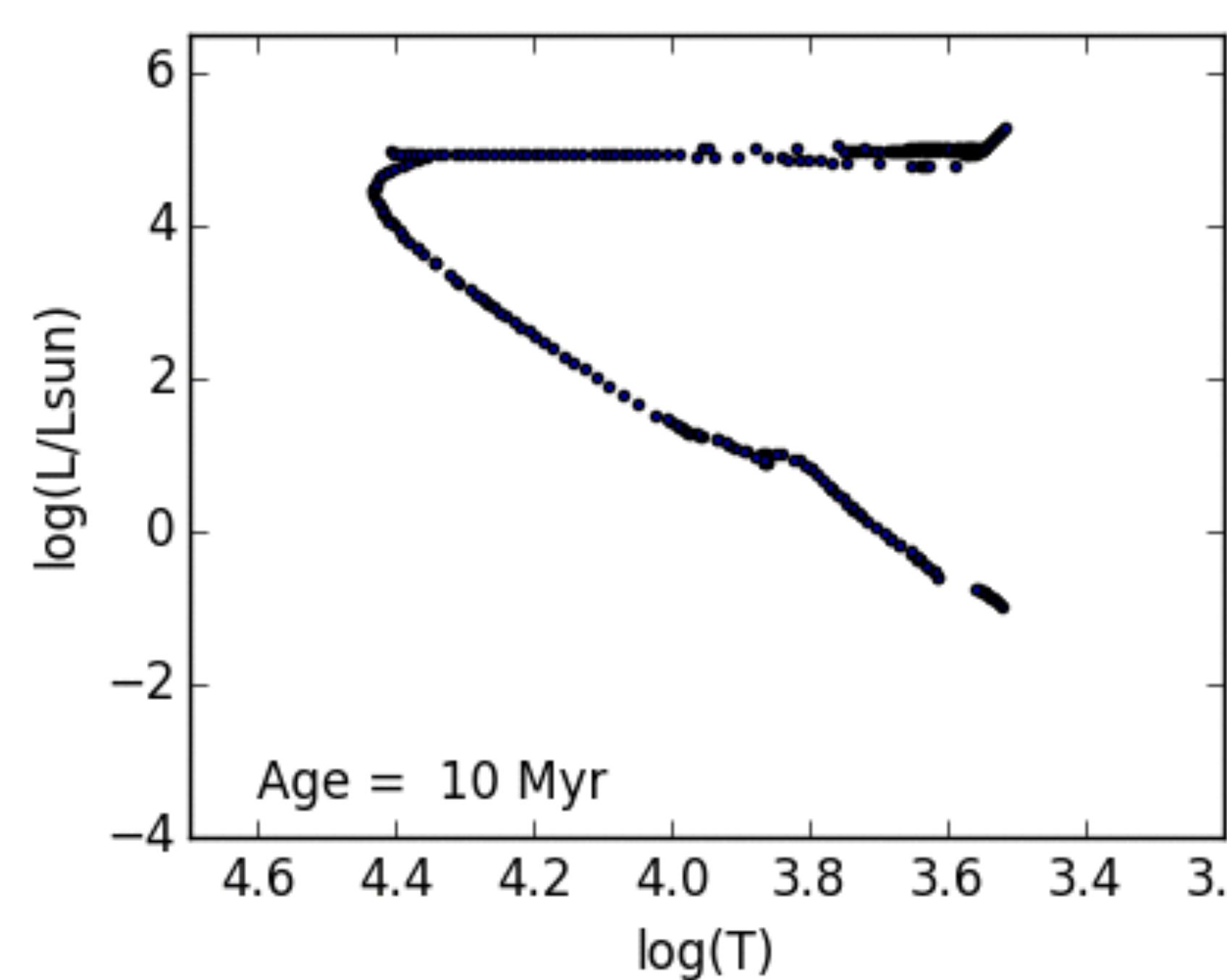
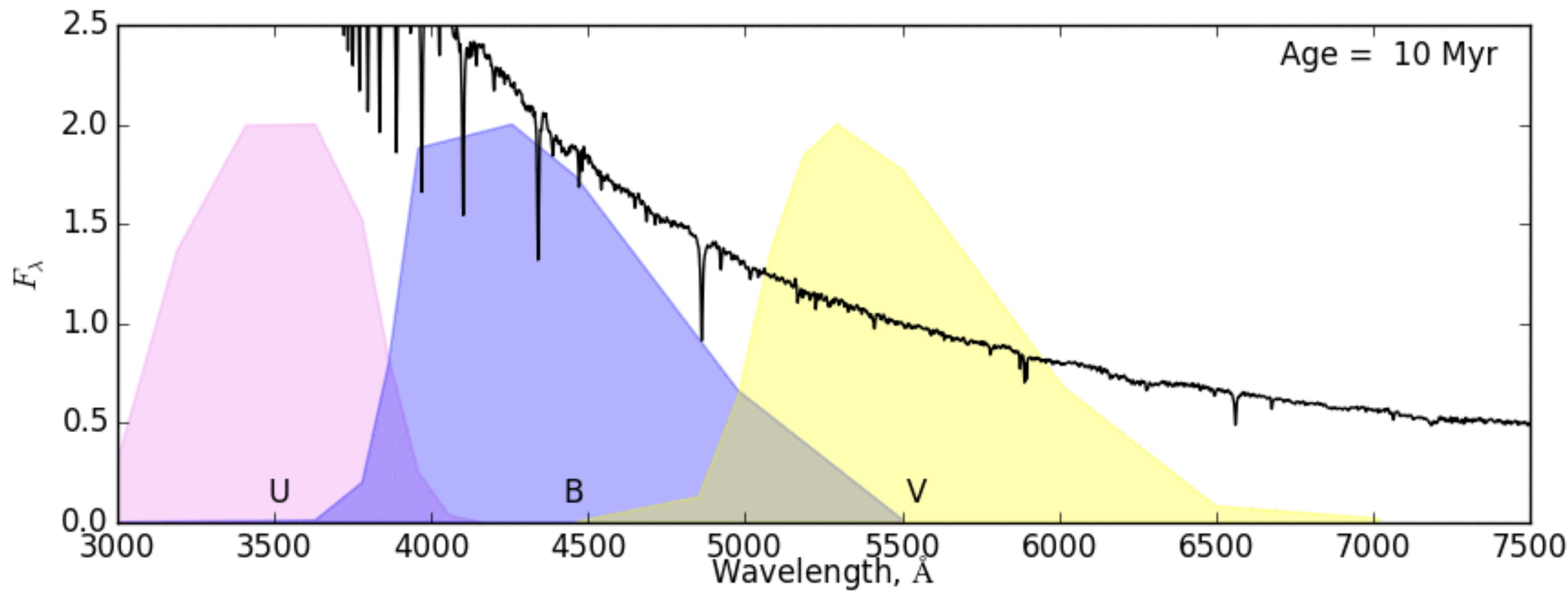


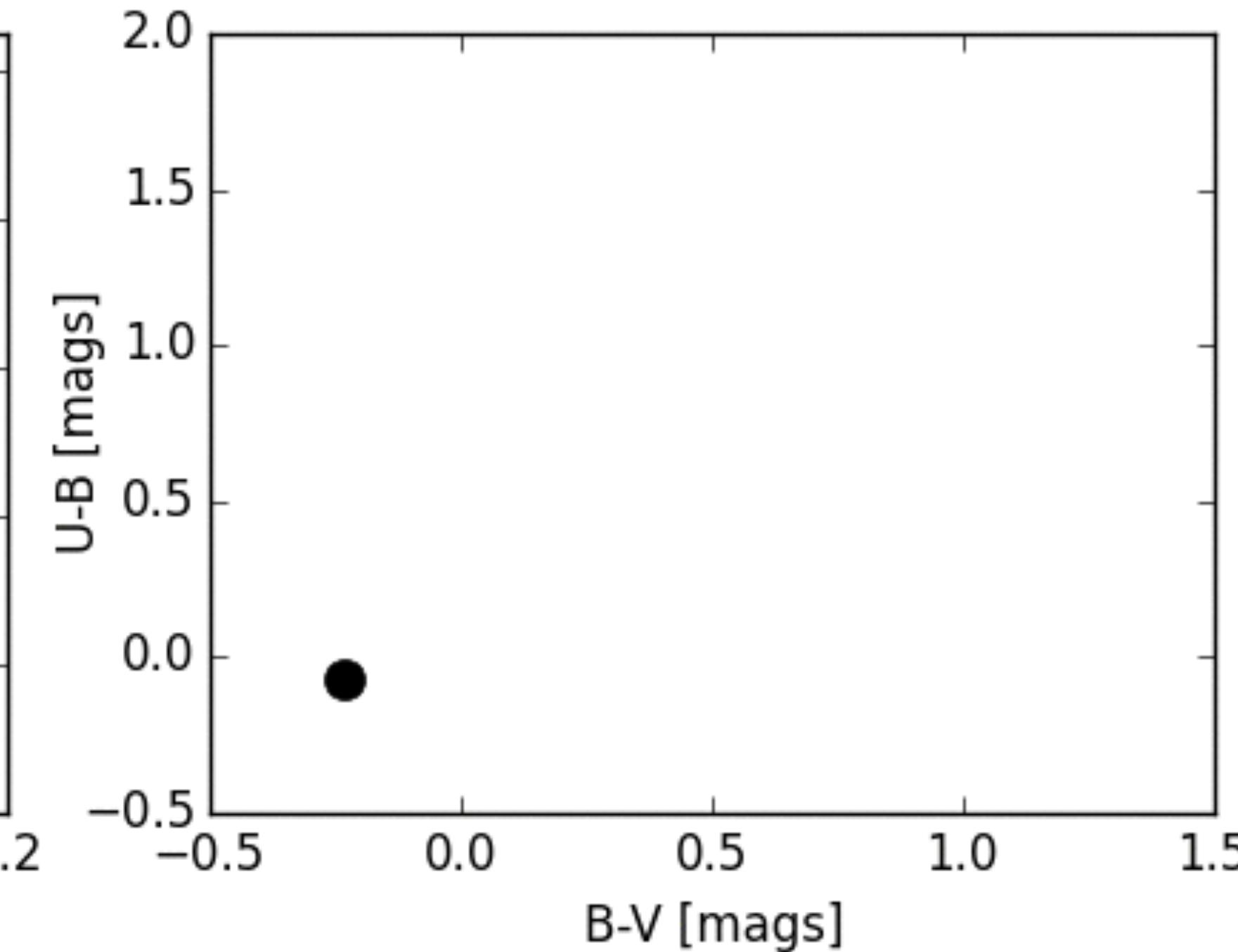
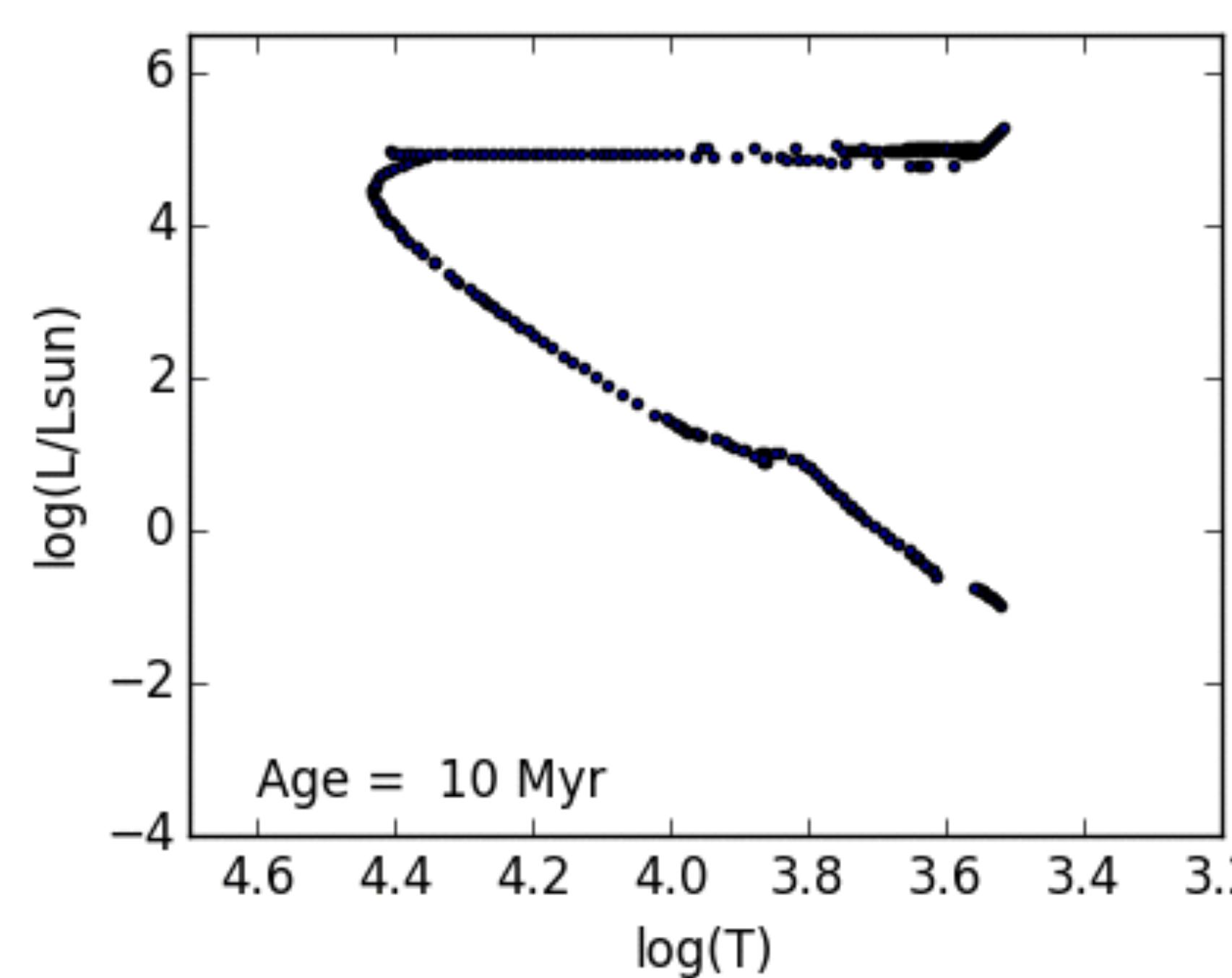
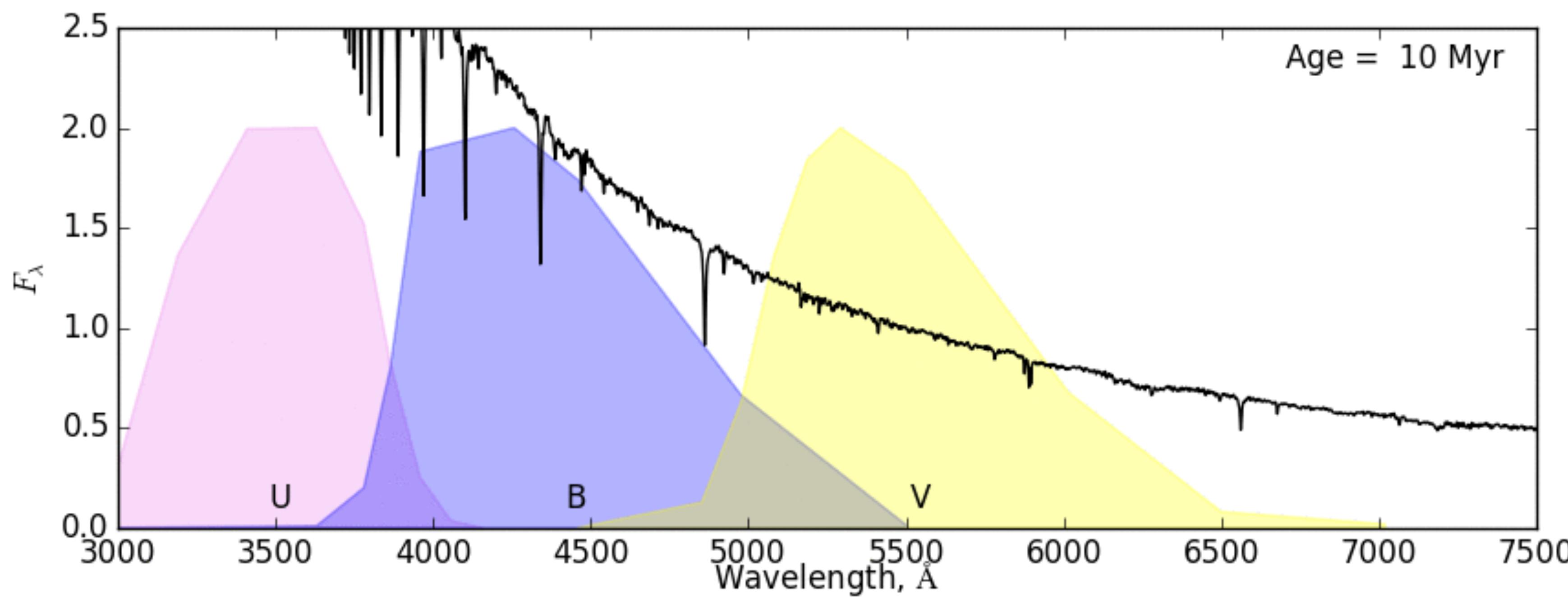


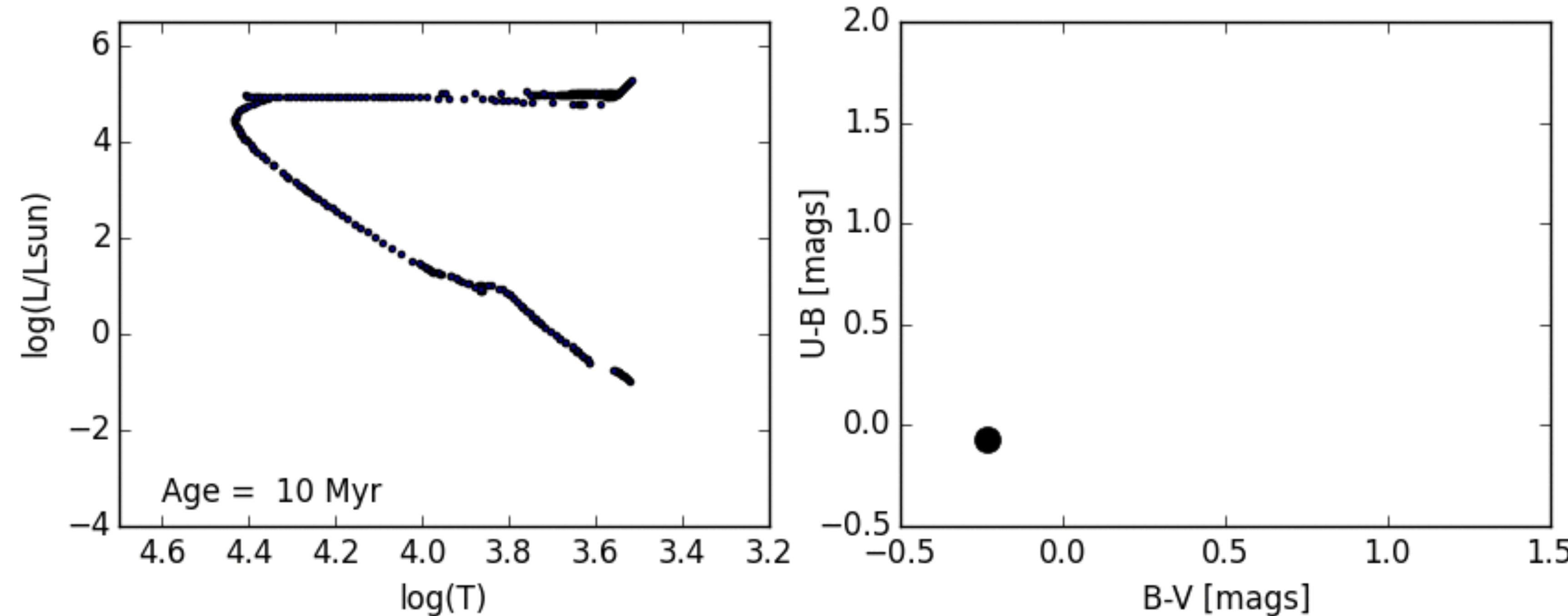
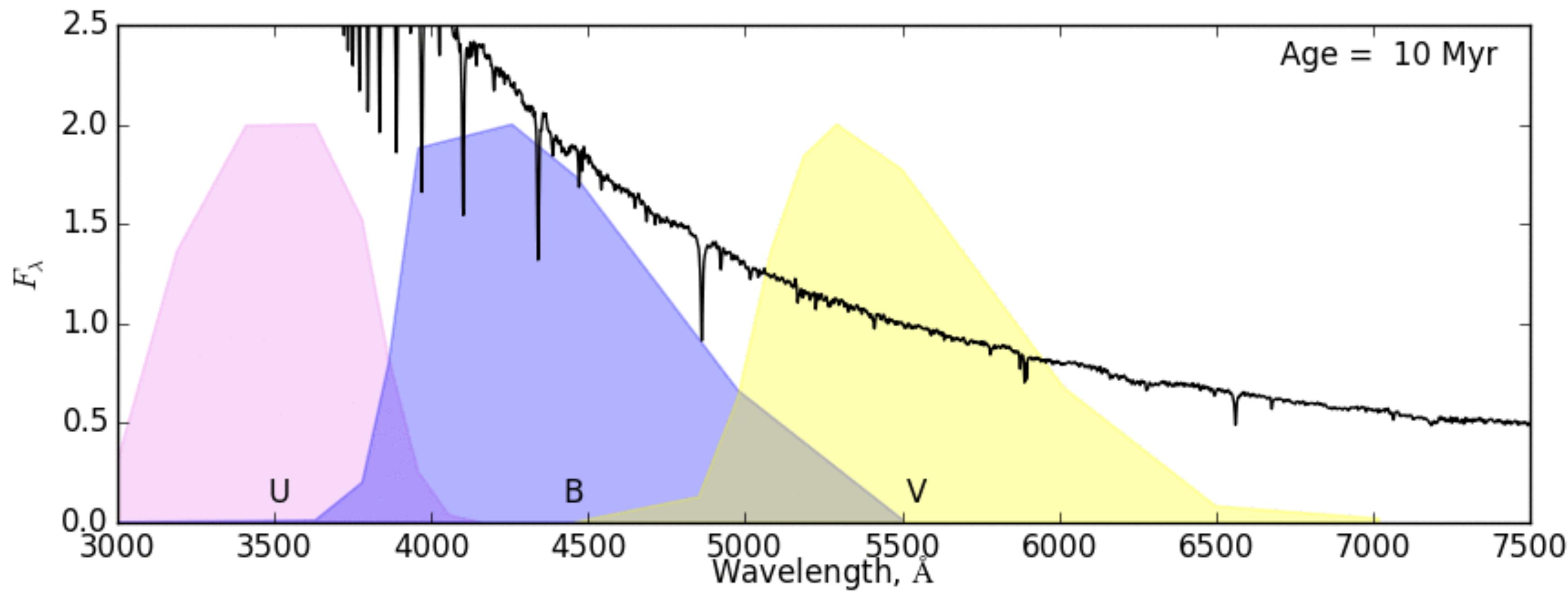


# Age-metallicity degeneracy

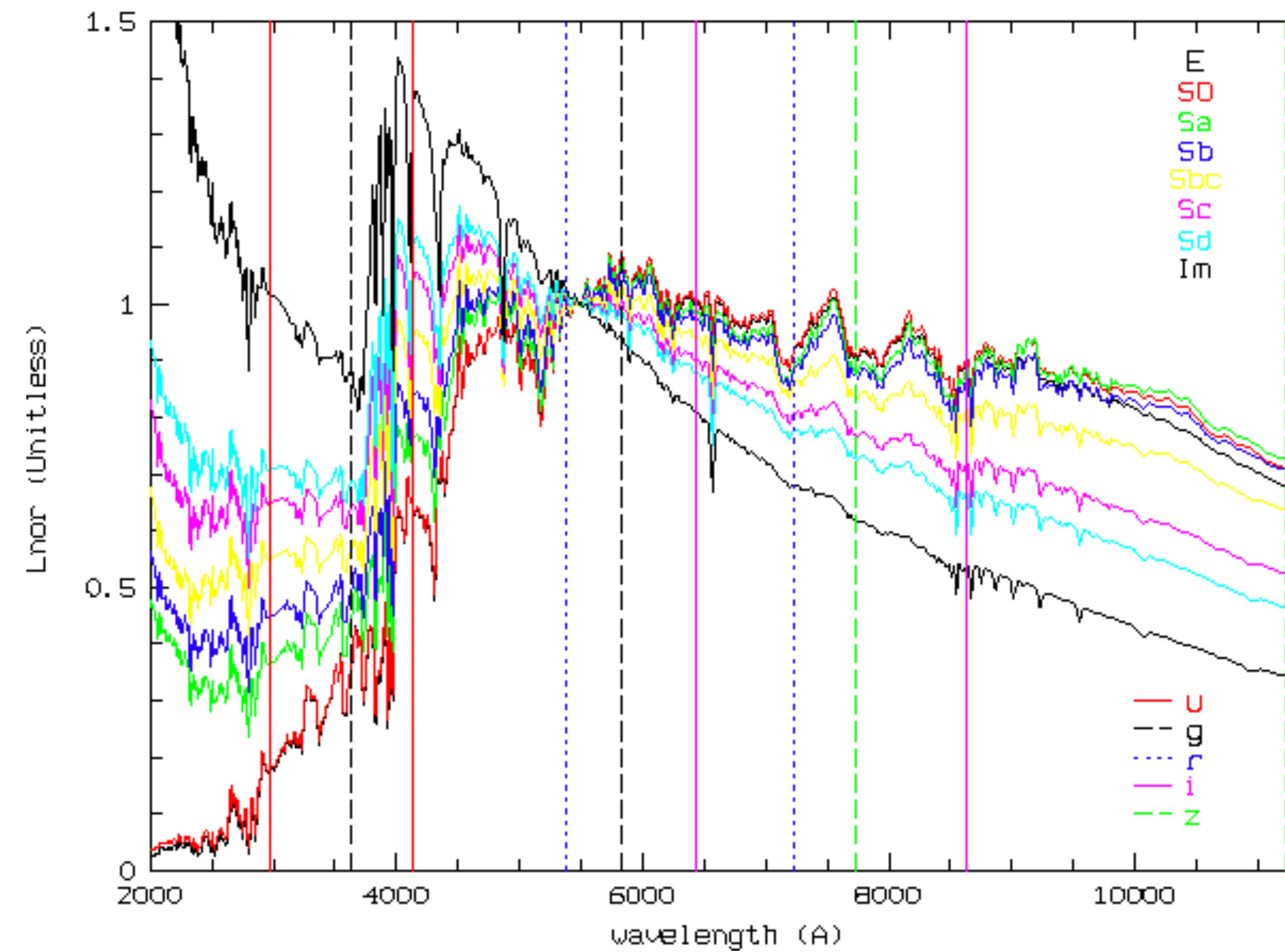




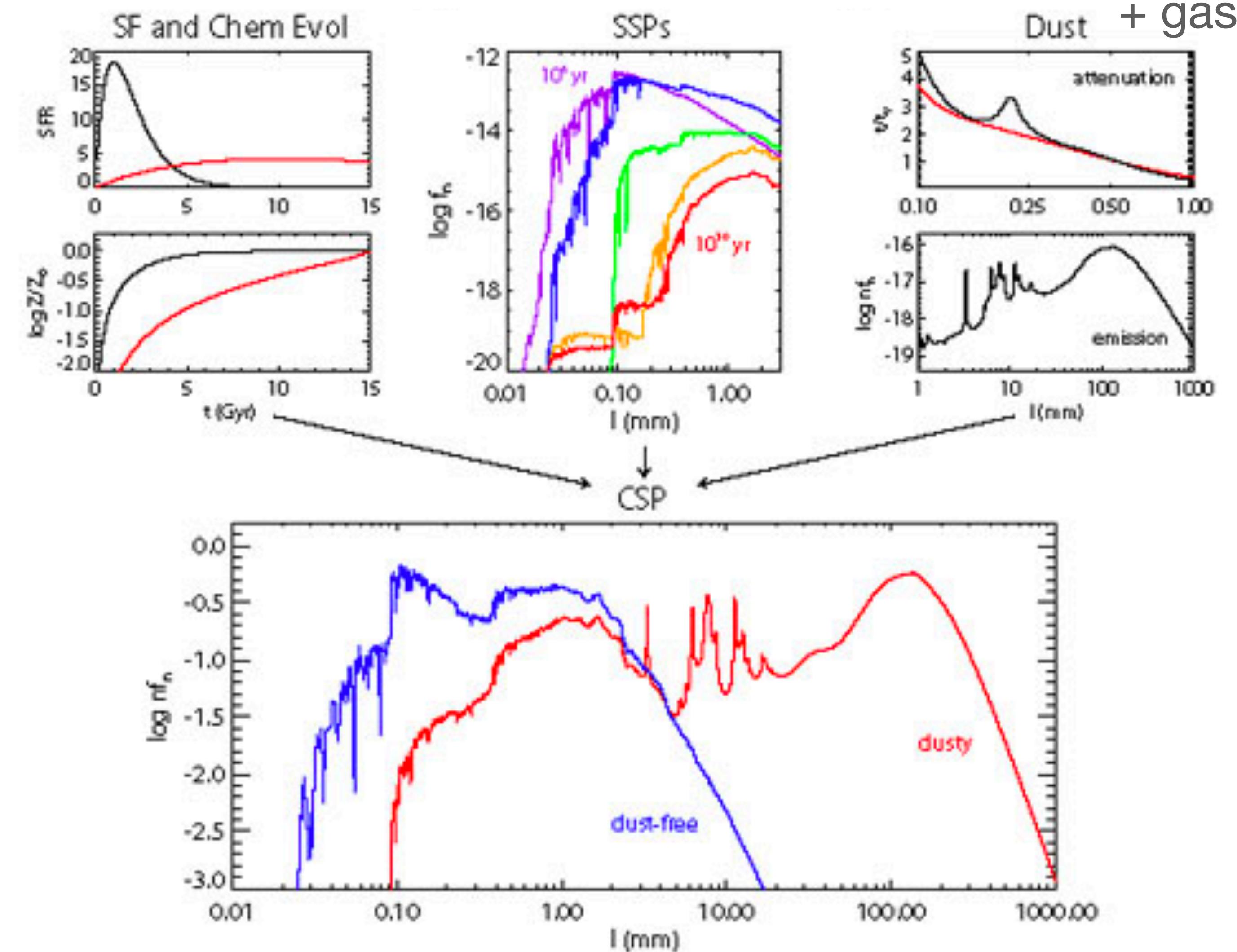




# Morphology



# Composite SP - Ingredients

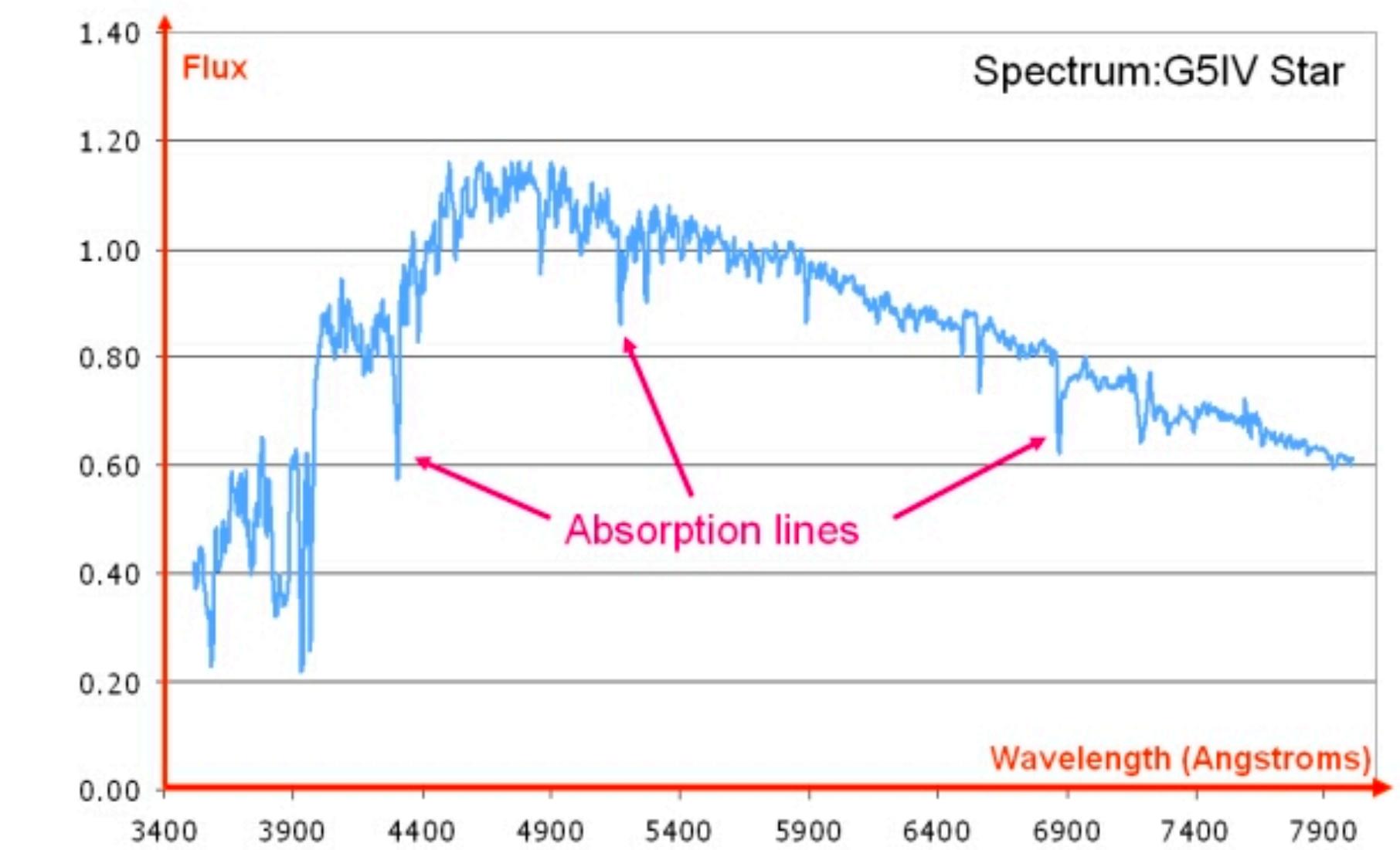
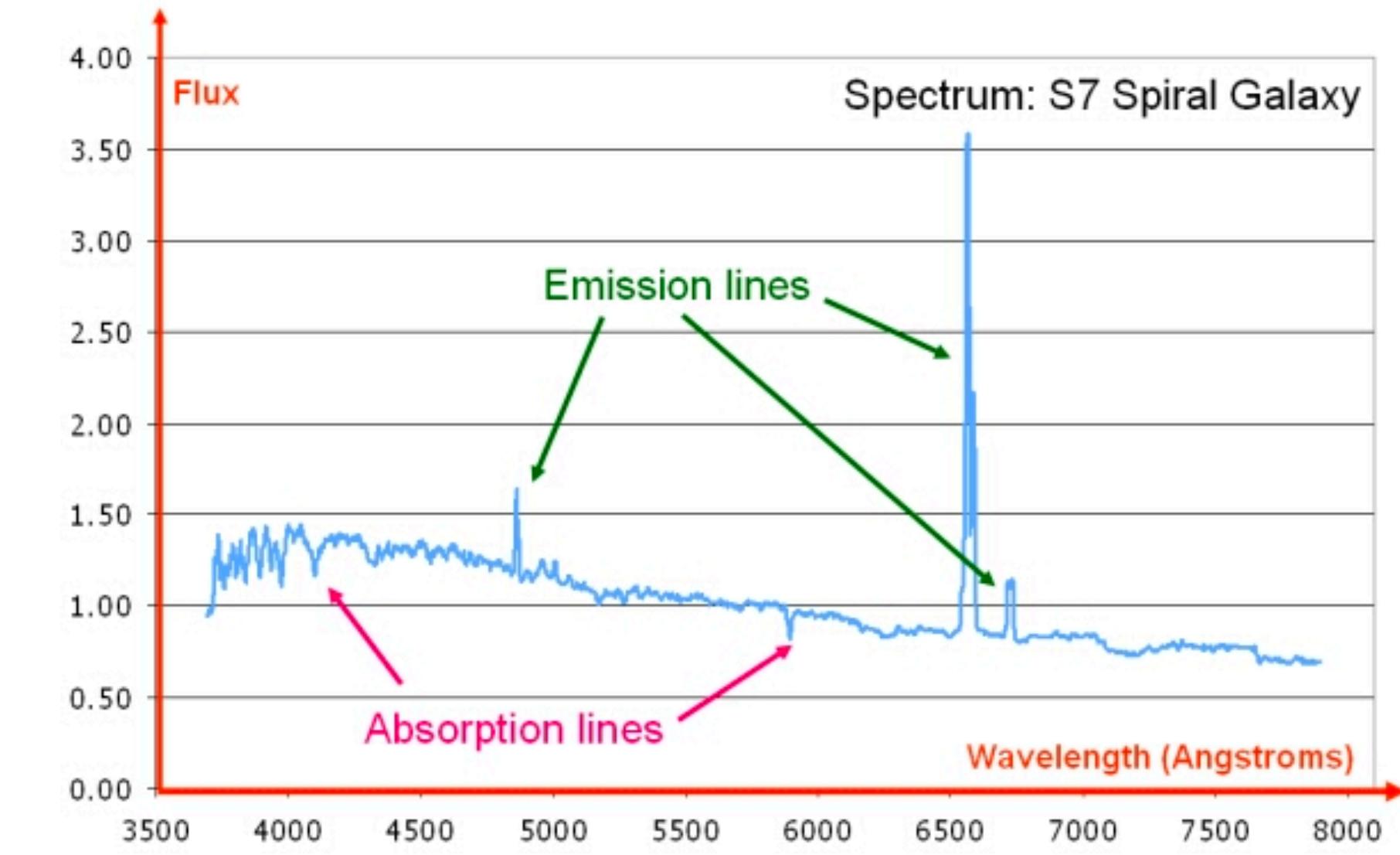
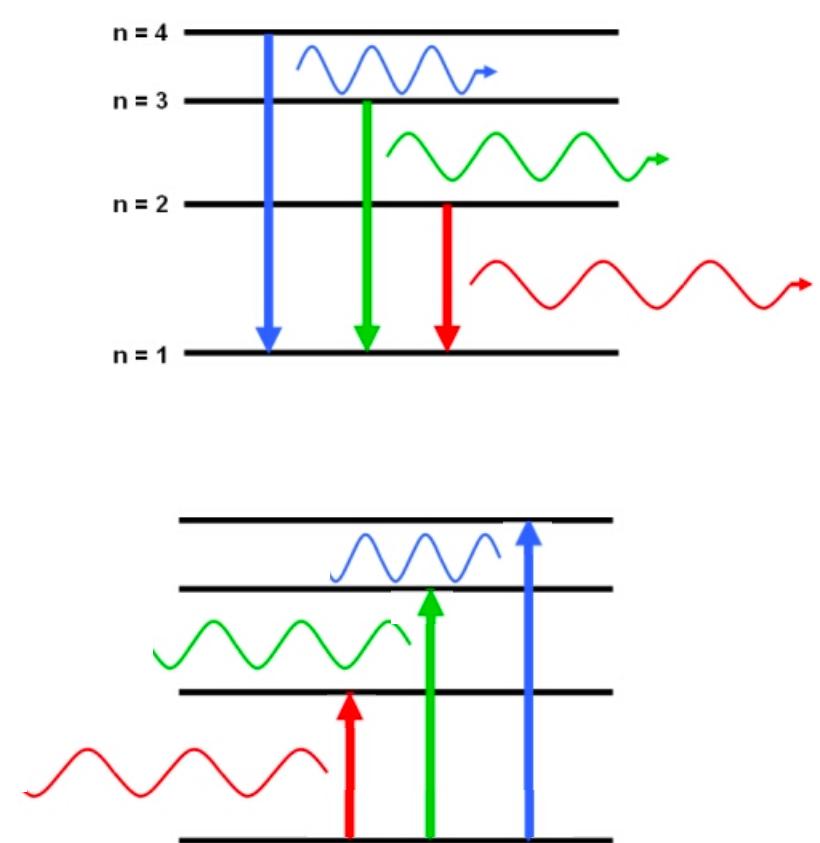
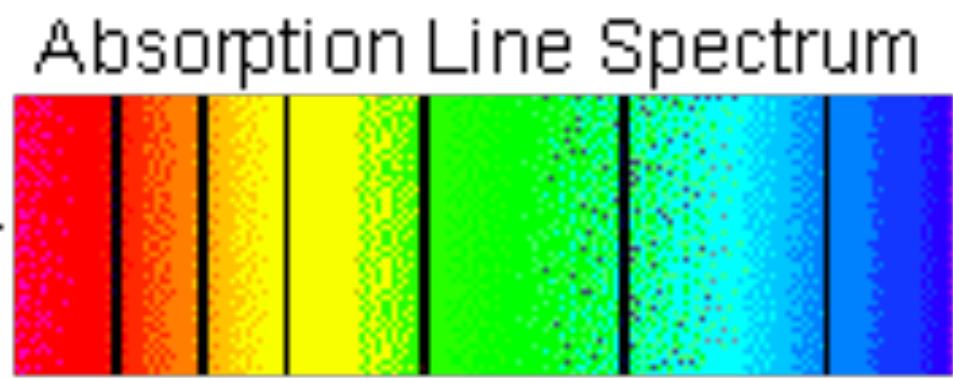
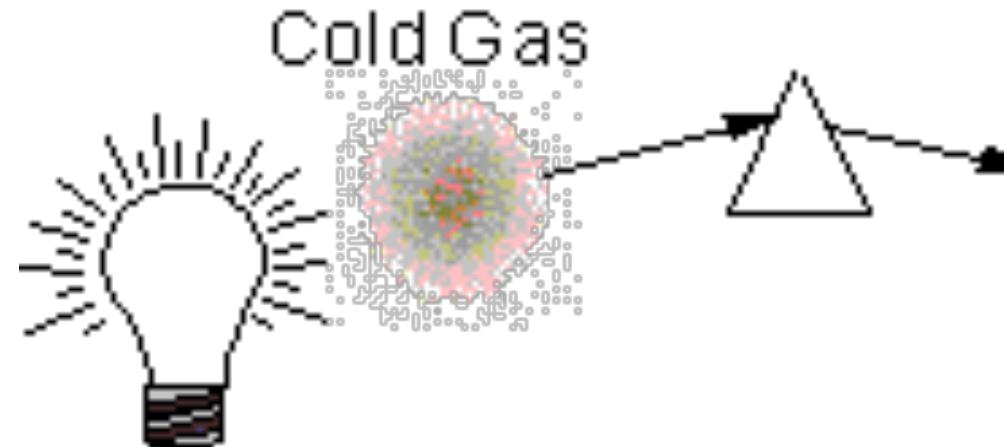
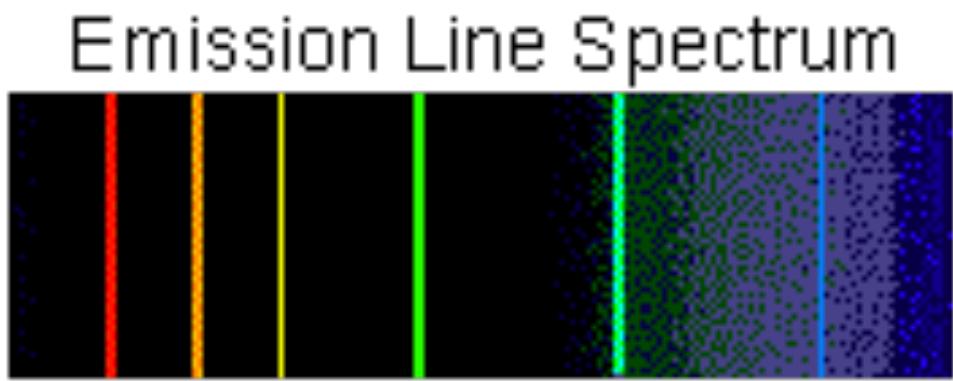
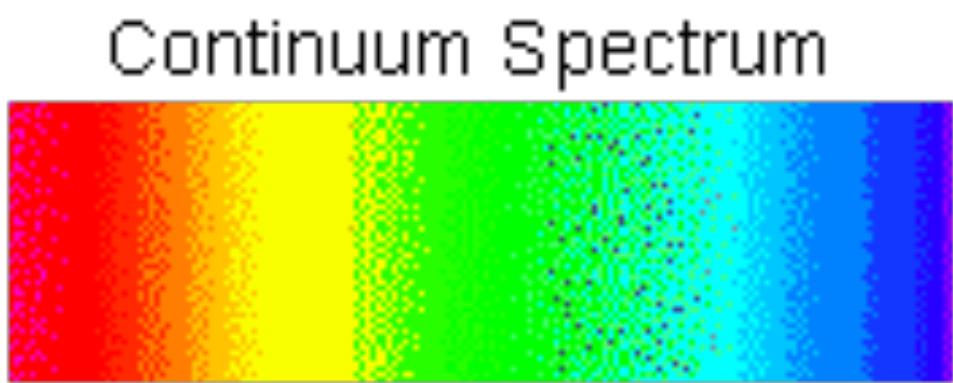
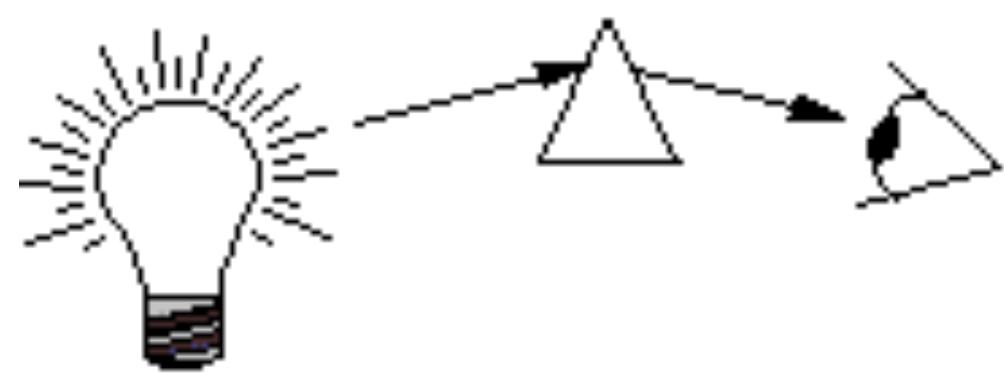


# Ionized gas



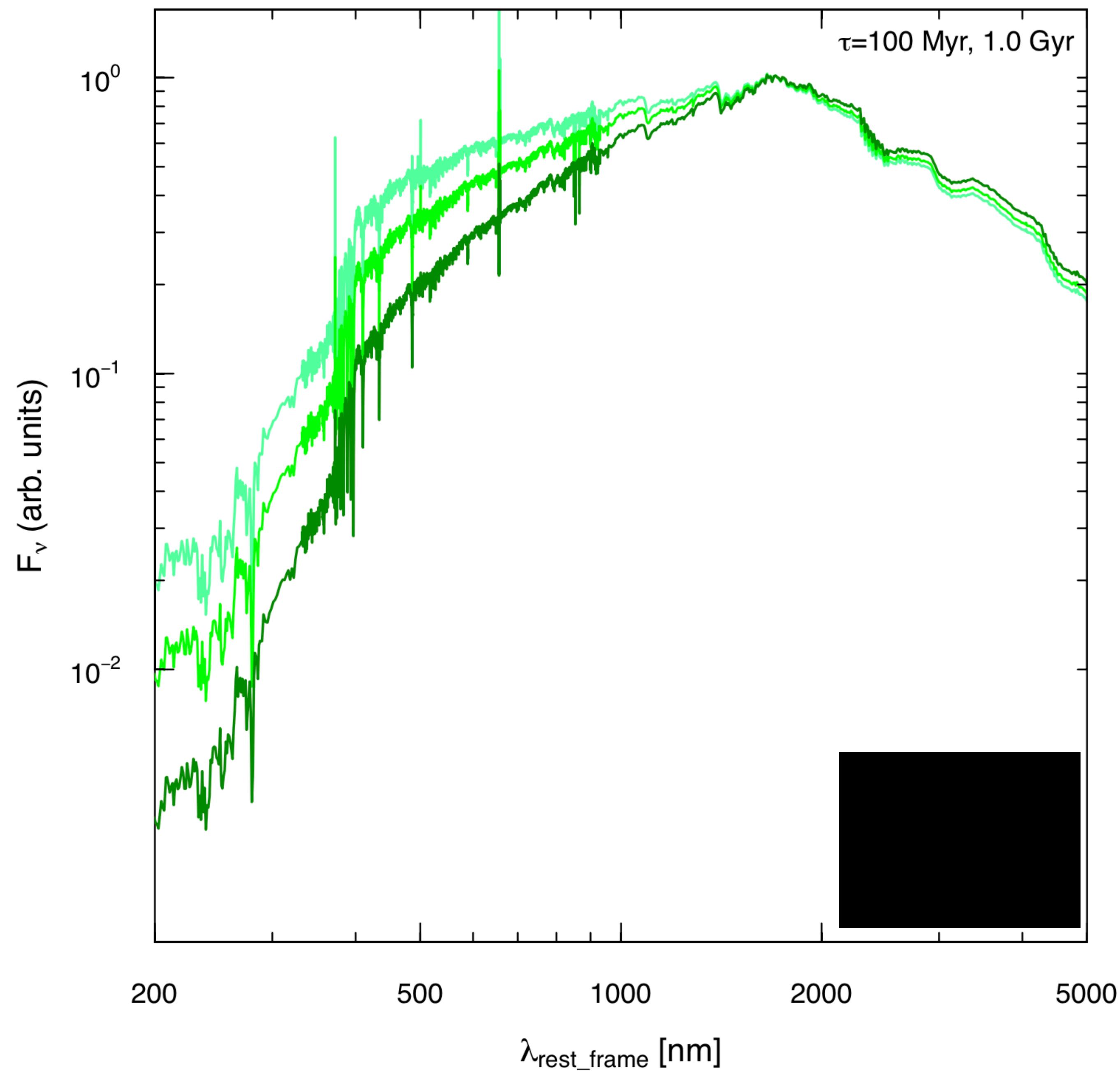
- UV emission: massive young stars are bright in the UV; direct probe of young stellar population
- Nebular lines: zones of ionised gas around young star clusters that still contain OB stars; H $\alpha$  is the brightest
- Far-IR emission: light absorbed by dust and re-emitted at longer wavelengths
- Radio, CO, ...

# Absorption/emission lines



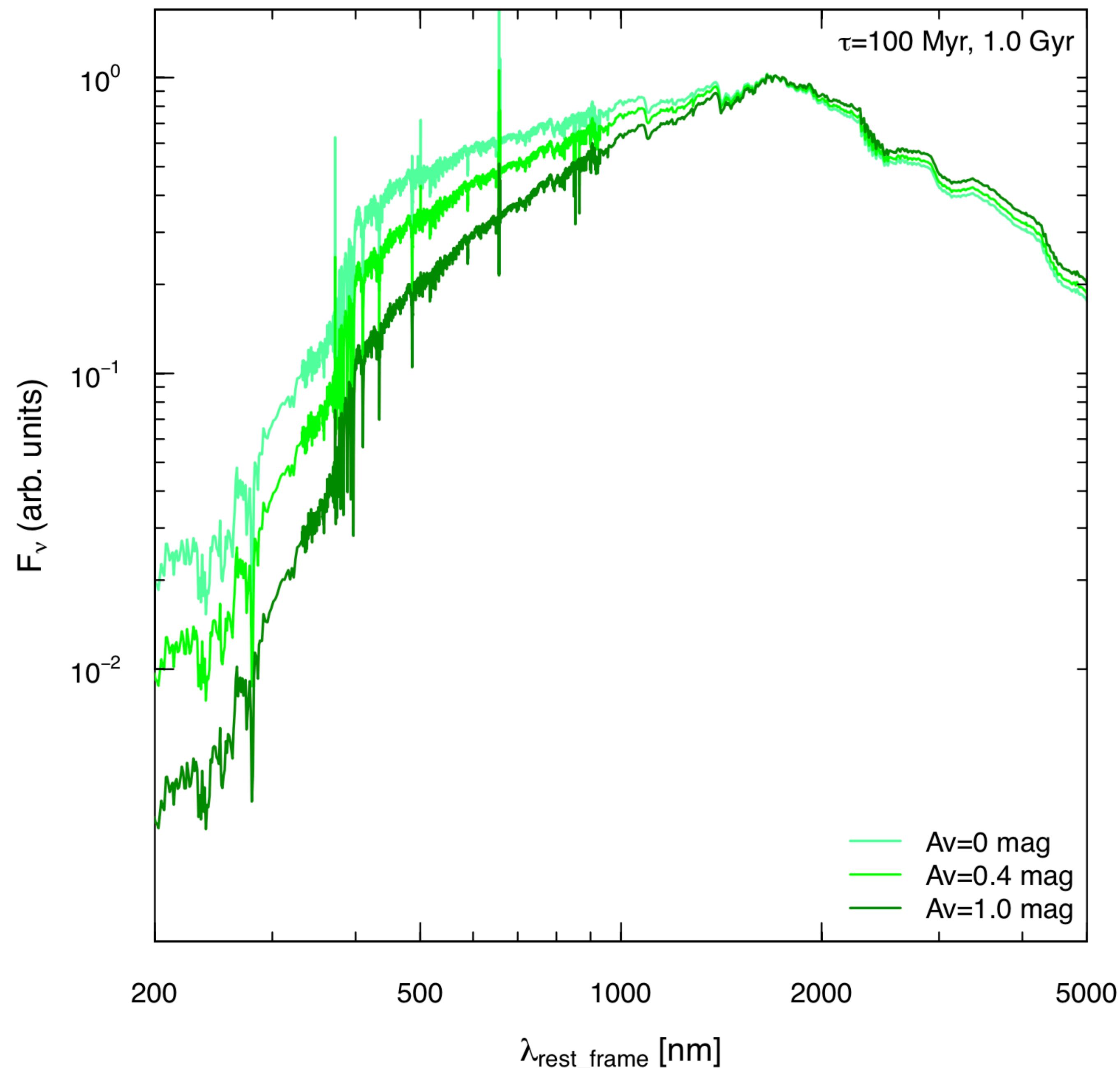
# ...and dust

Absorbs high-energy (blue) light which is reemitted at infrared wavelengths.

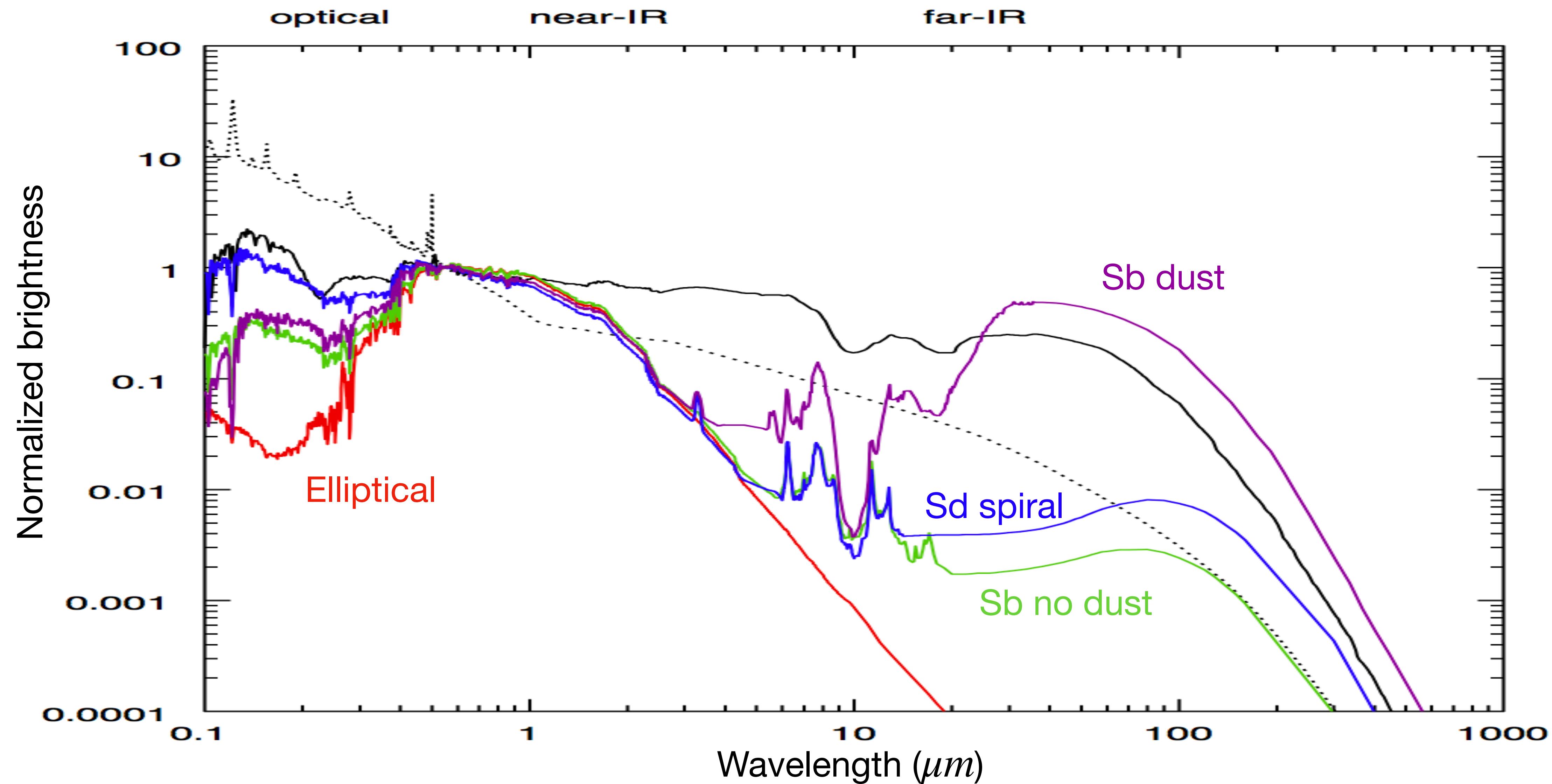


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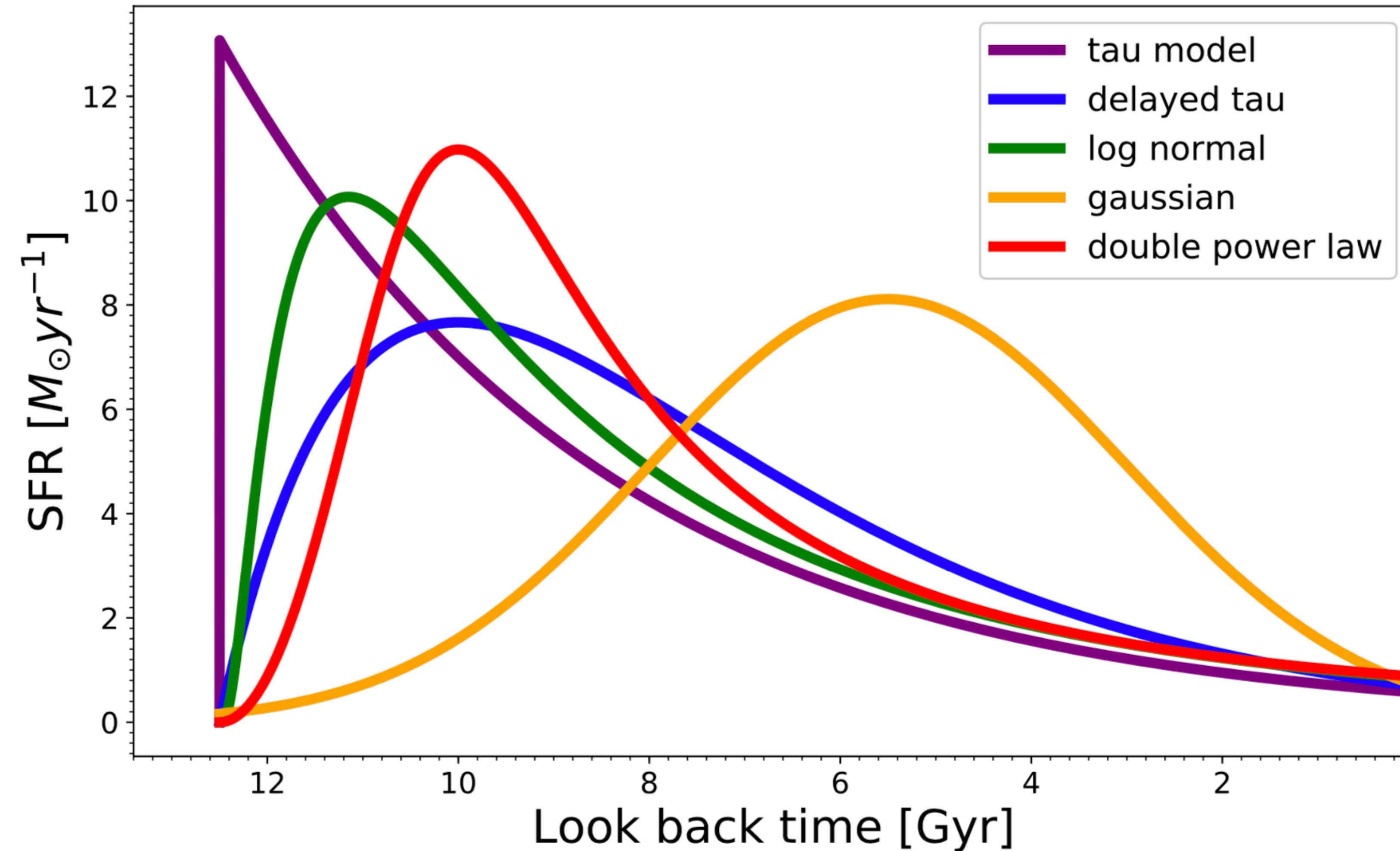


# Absorption, reddening, and reemission



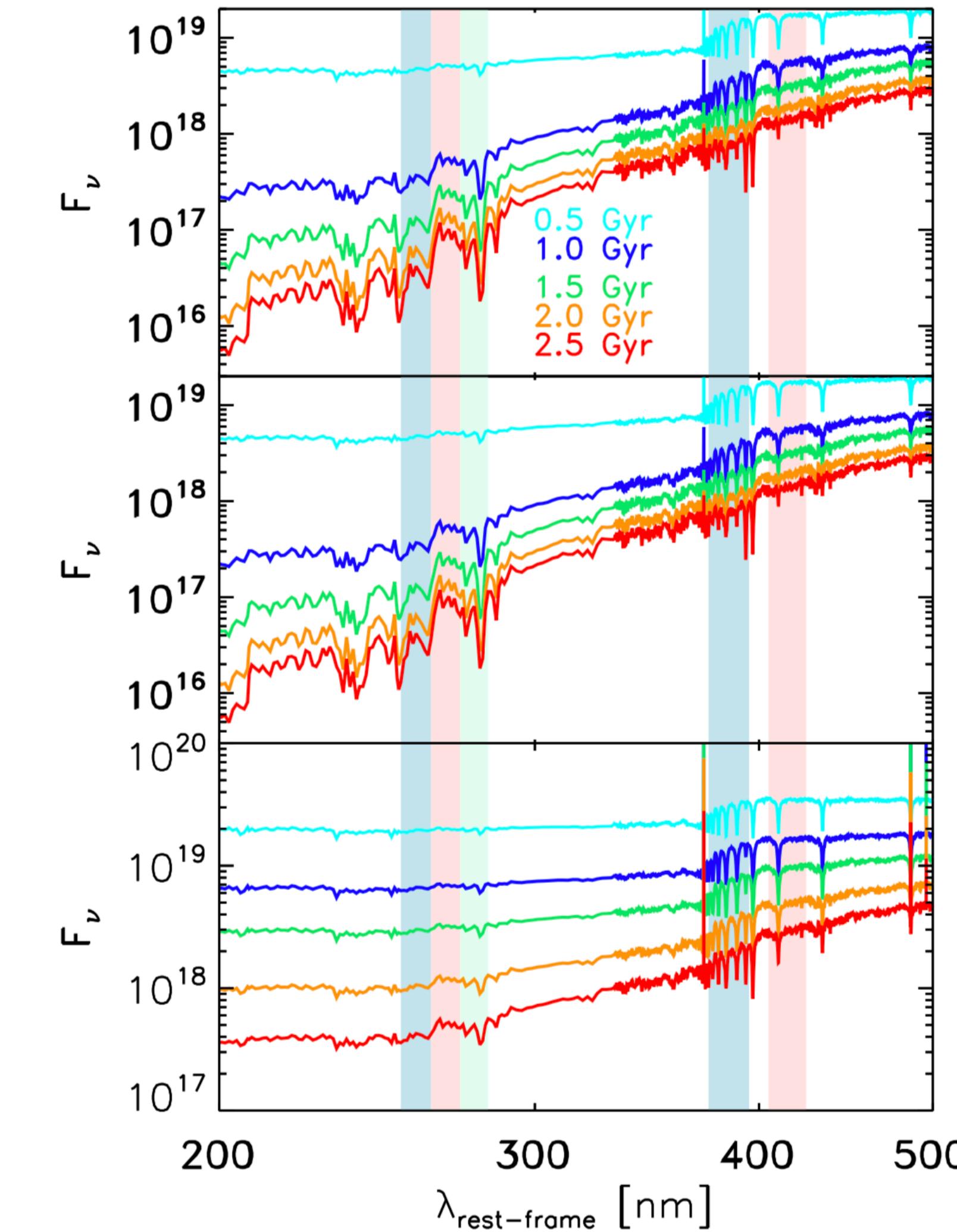
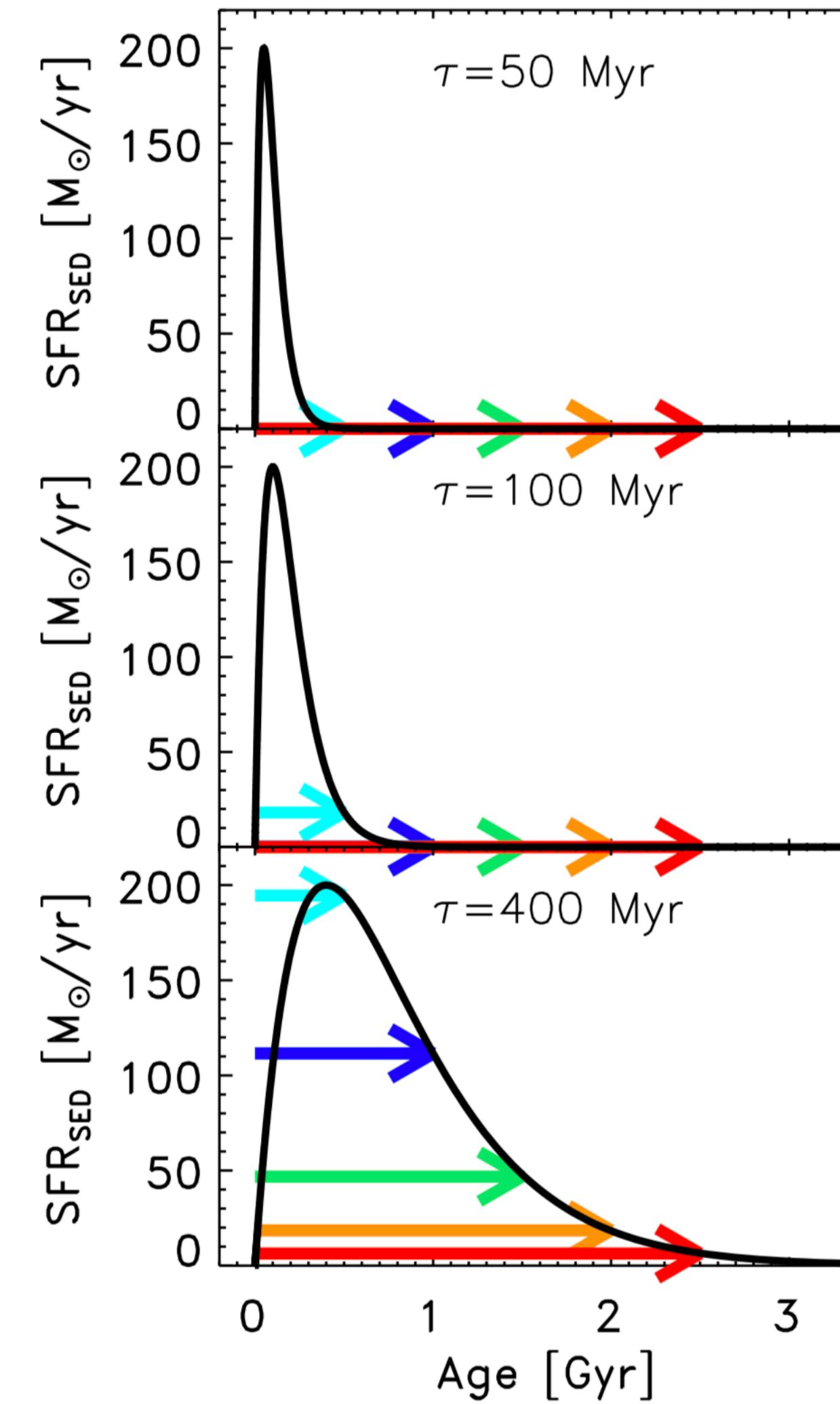
# Star formation histories

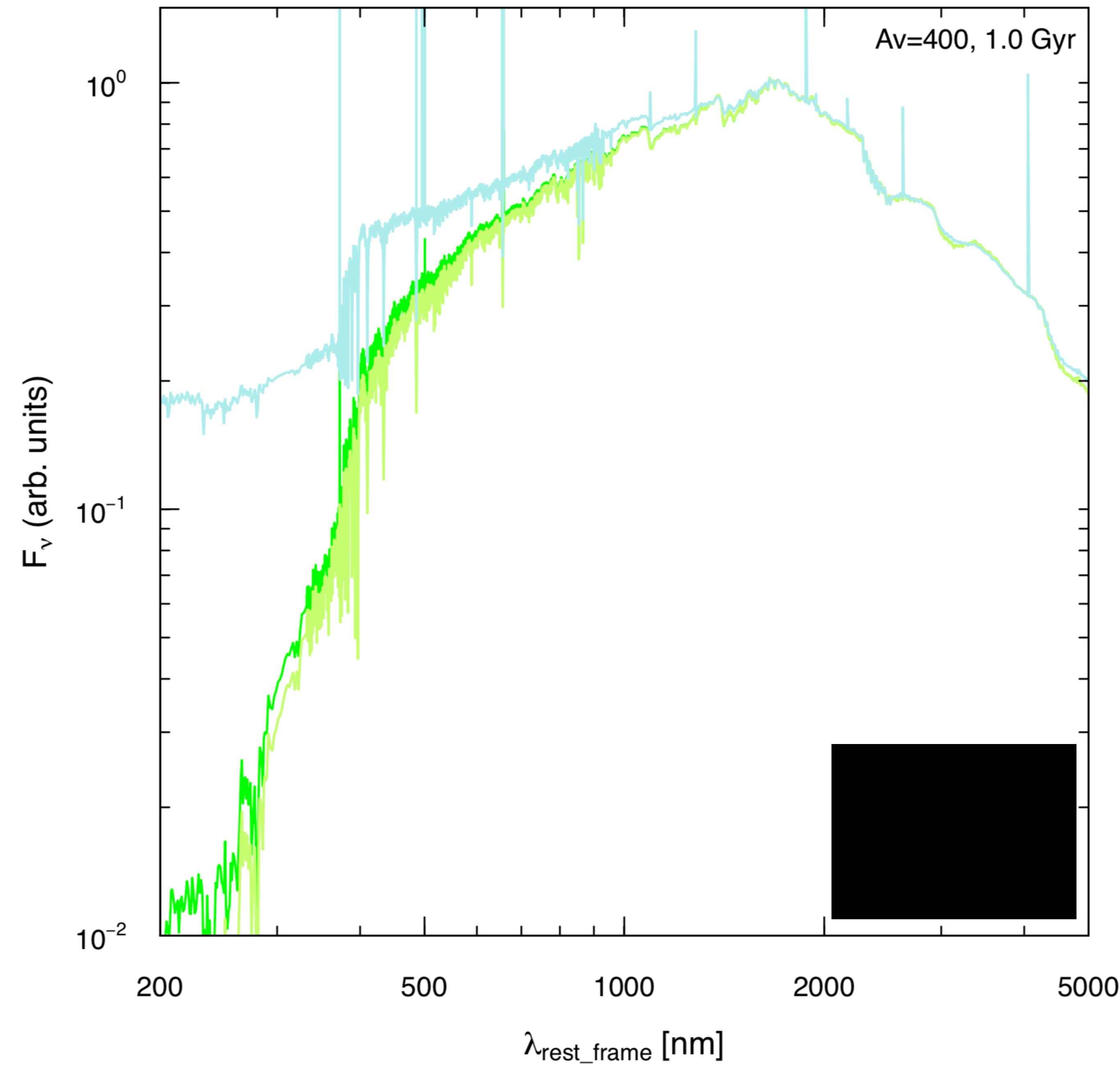
$$SFR(t) \approx t \exp(-t/\tau)$$

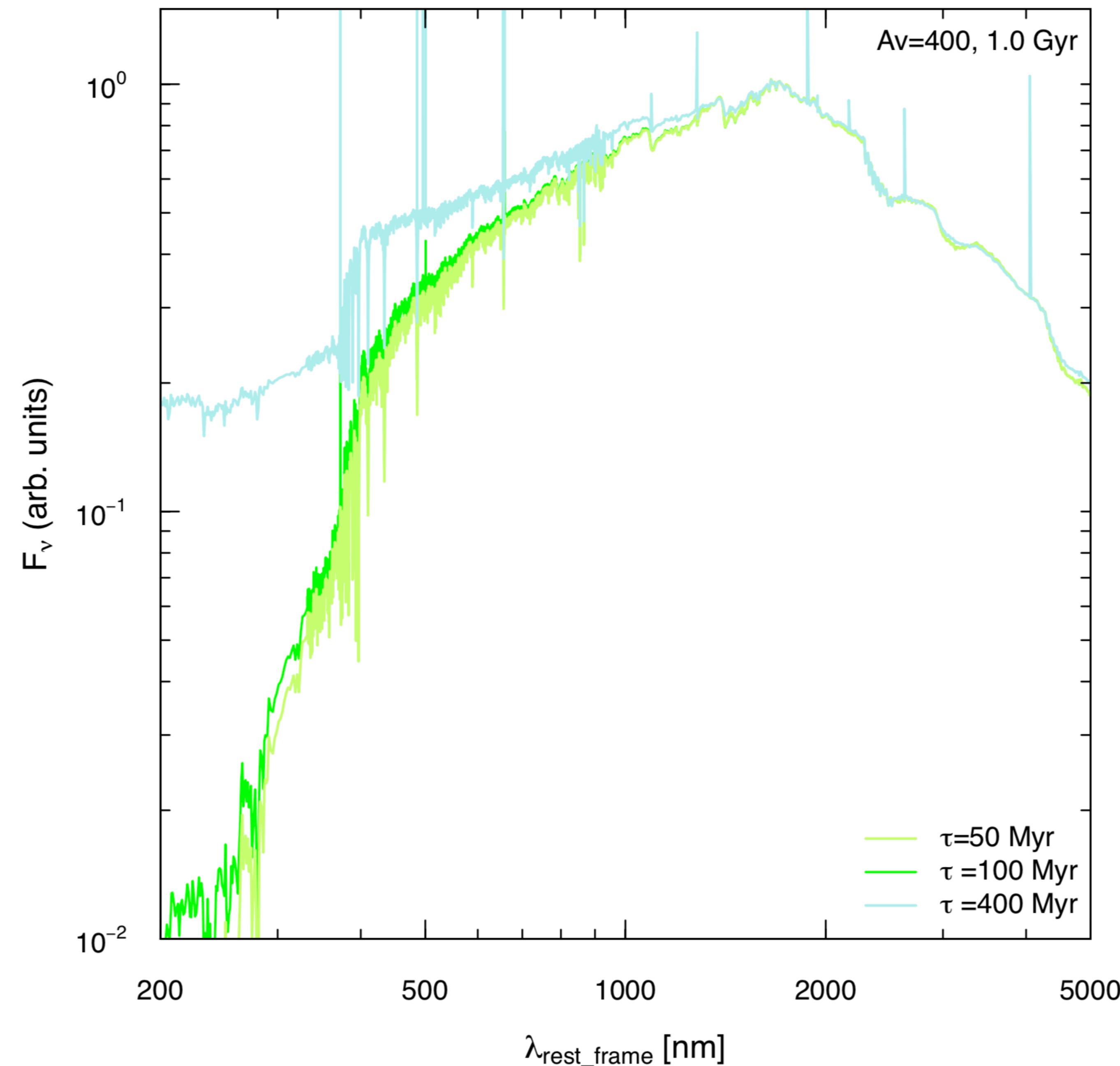


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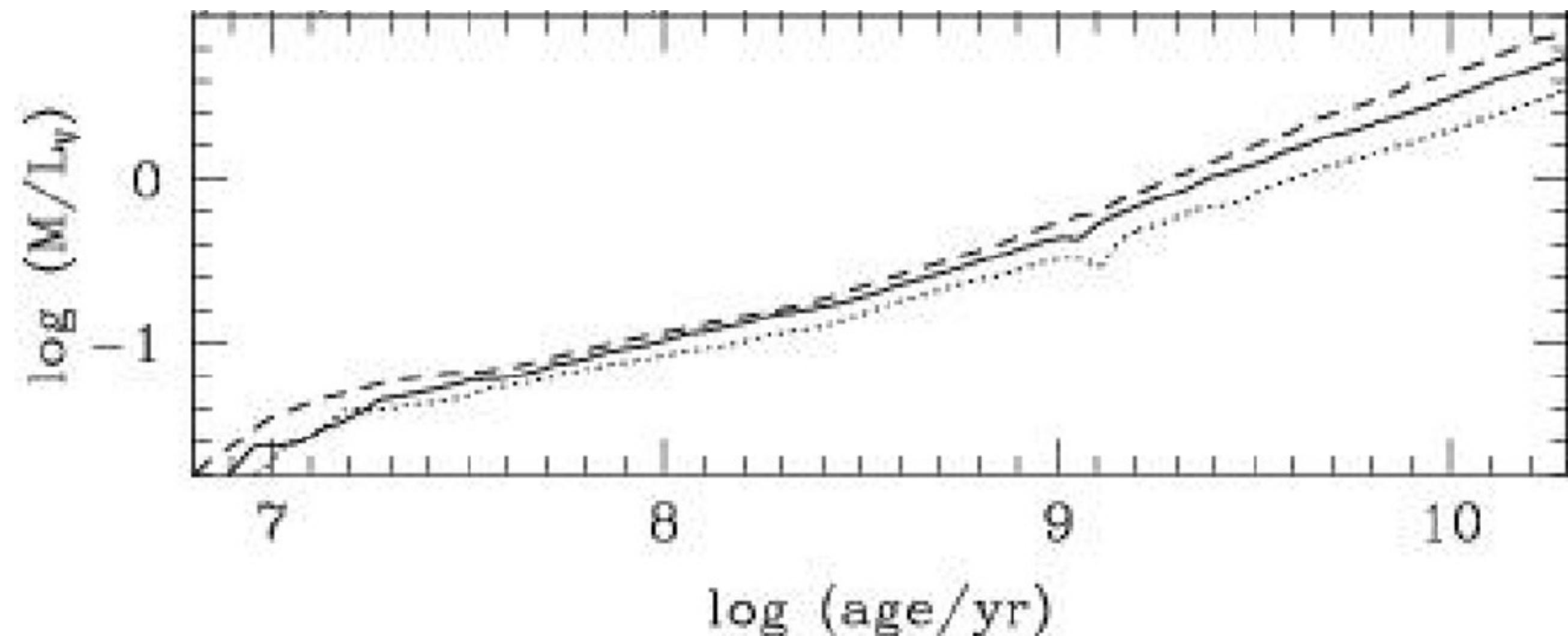


# Real galaxy spectra

<http://skyserver.sdss.org/dr16/en/tools/chart/list.aspx>

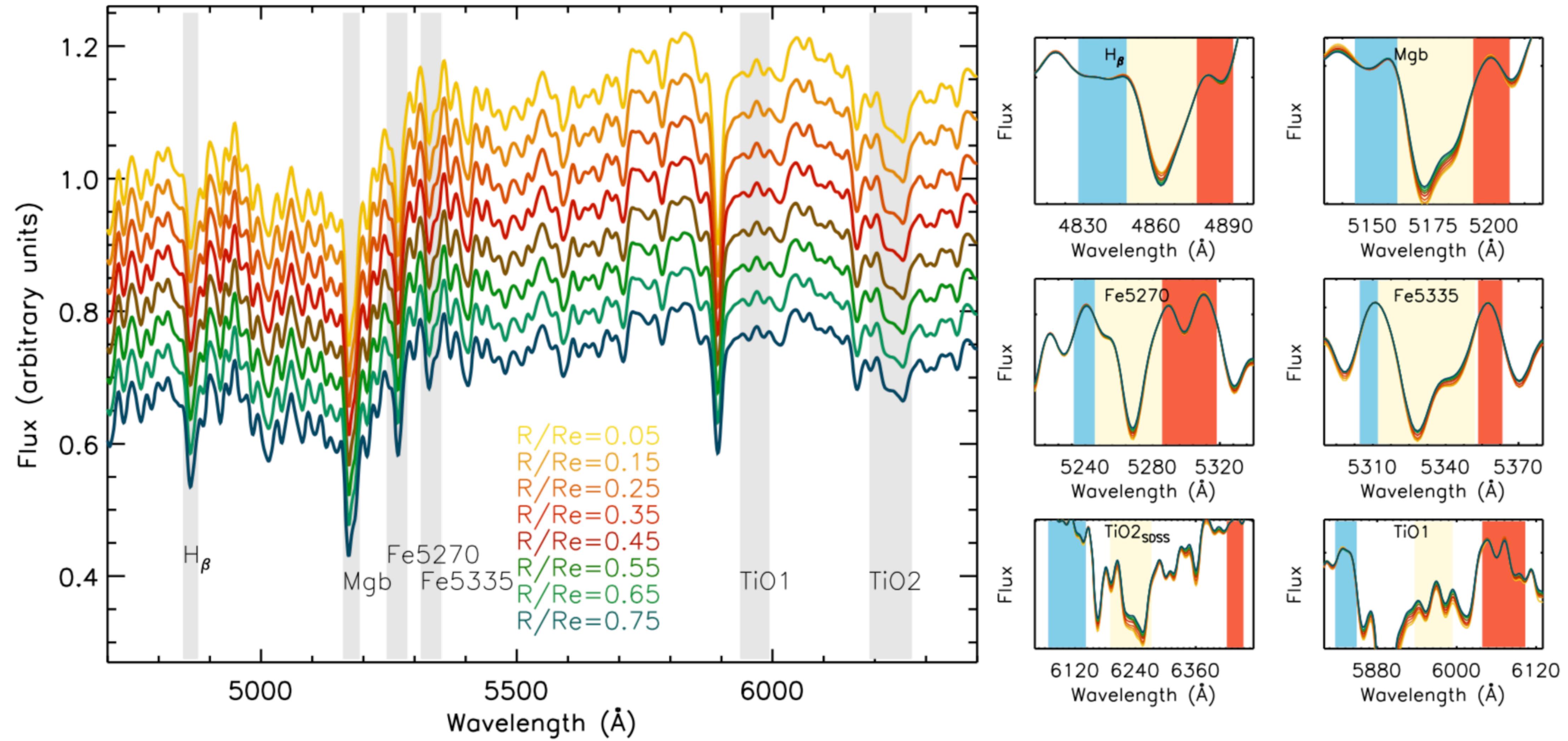
# Mass-to-light ratio

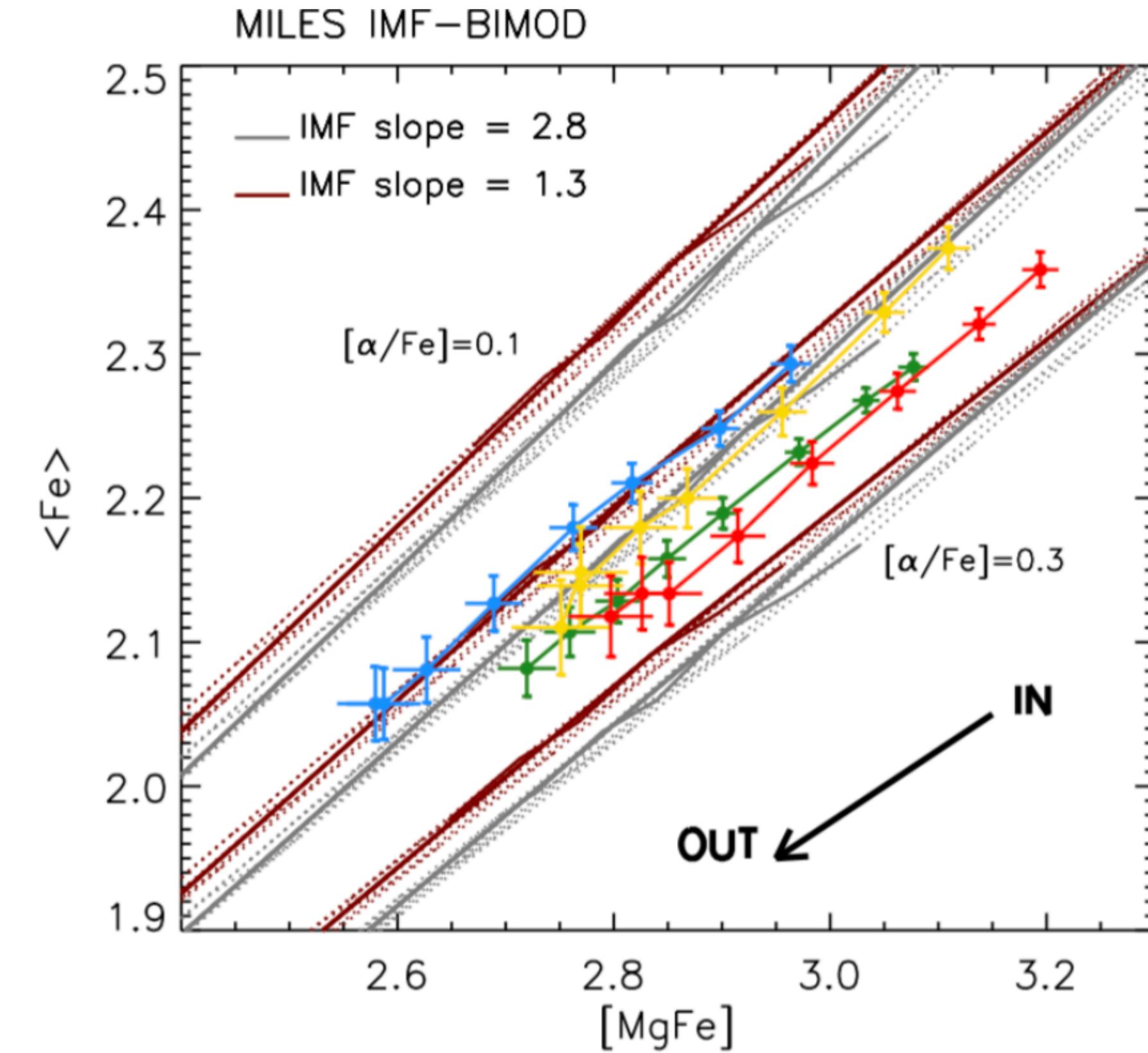
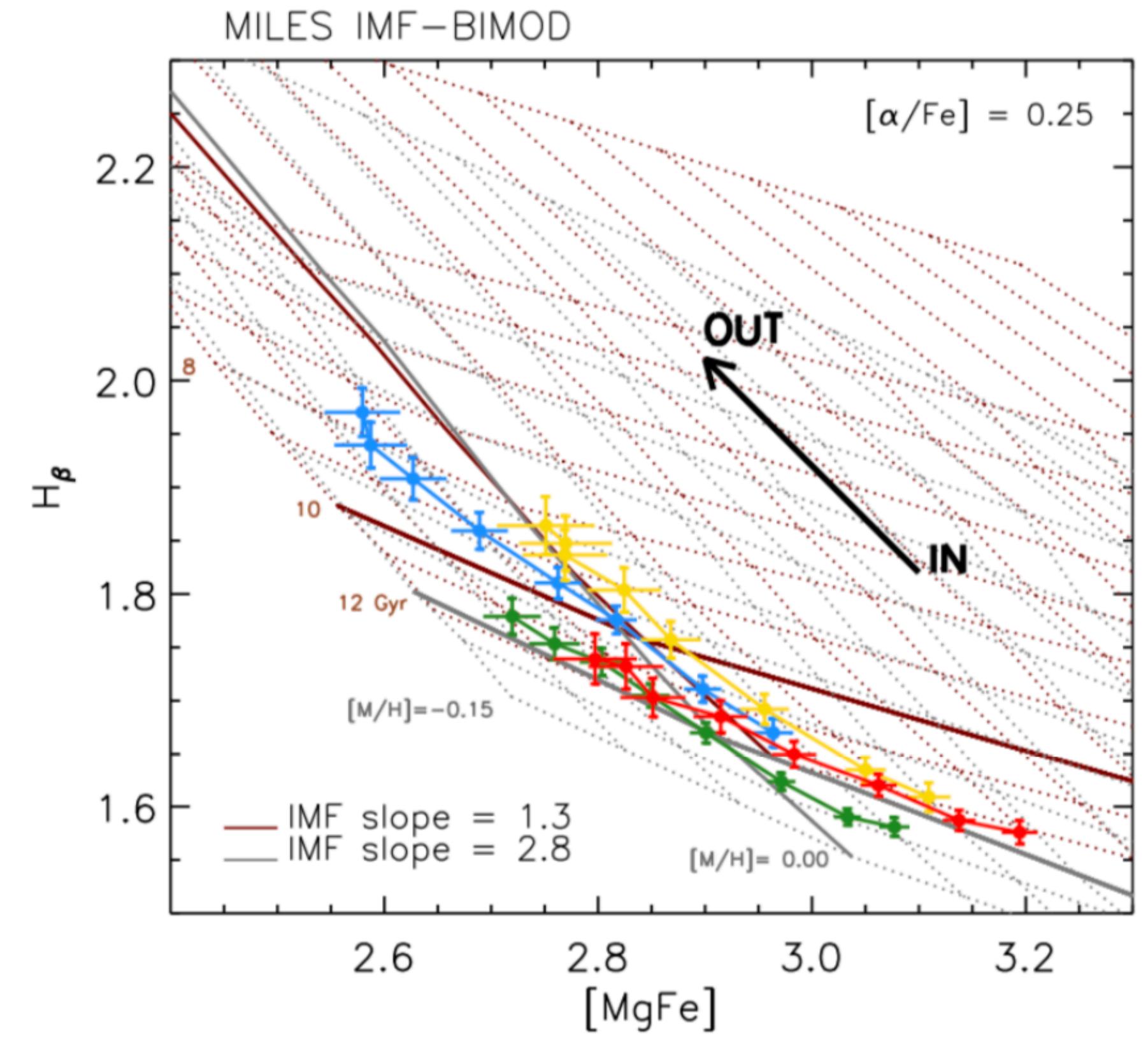
- If we understand the properties of SP, we can use L to infer M in stars by invoking M/L
- It has units of  $M_{\odot}/L_{\odot}$ , so the Sun has M/L=1
  - An A-type MS star with  $L = 12L_{\odot}$  and  $M = 2M_{\odot}$ , it has  $(M/L) = 0.17M_{\odot}/L_{\odot}$
  - A K-type MS star with  $L = 0.3L_{\odot}$  and  $M = 0.75M_{\odot}$ , has  $(M/L) = 2.5M_{\odot}/L_{\odot}$



- Q: Does the M/L increase or decrease with time for a SSP?

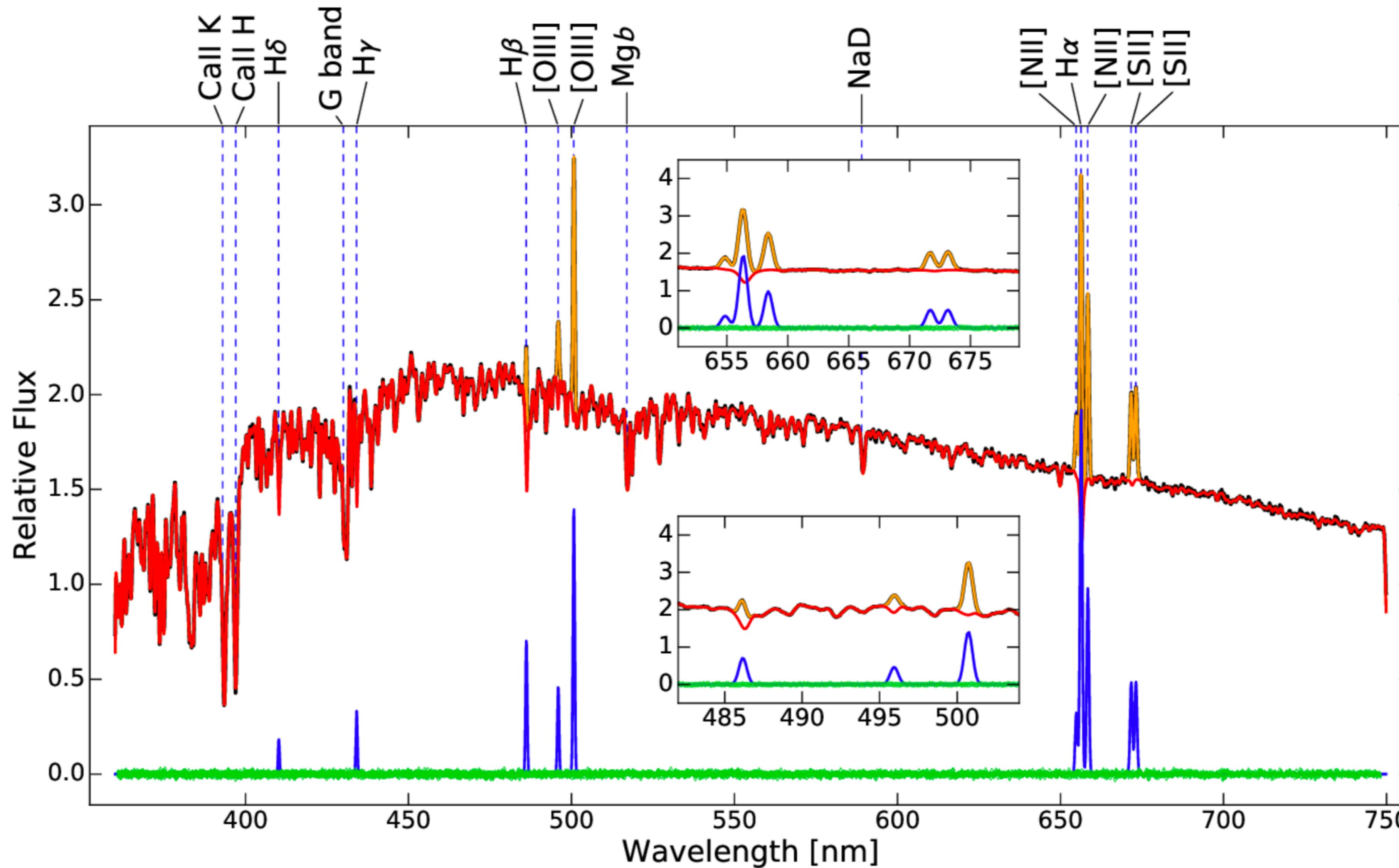
# Lick indices





- Lick indices are measured on observed spectra and compared to the predictions of theoretical models.
- Hb-MgFe good indicator of age-metallicity.
- $\langle Fe \rangle$ -MgFe good alpha-enhancement indicator.
- TiO<sub>2</sub> good IMF indicator.

# Spectral synthesis



- FIREFLY
- PPXF
- Starlight
- Prospector
- ...
- Q: What are the ‘output’ parameters of a spectral fitting?

# → SFH(t,Z): 2 approaches

$$\text{SFH} \rightarrow L_{\text{gal}}(\lambda)$$

*Given a SFH, what  
is the resulting  
galaxy spectrum?*



Evolutionary  
Population Synthesis

$$L_{\text{gal}}(\lambda) \rightarrow \text{SFH}$$

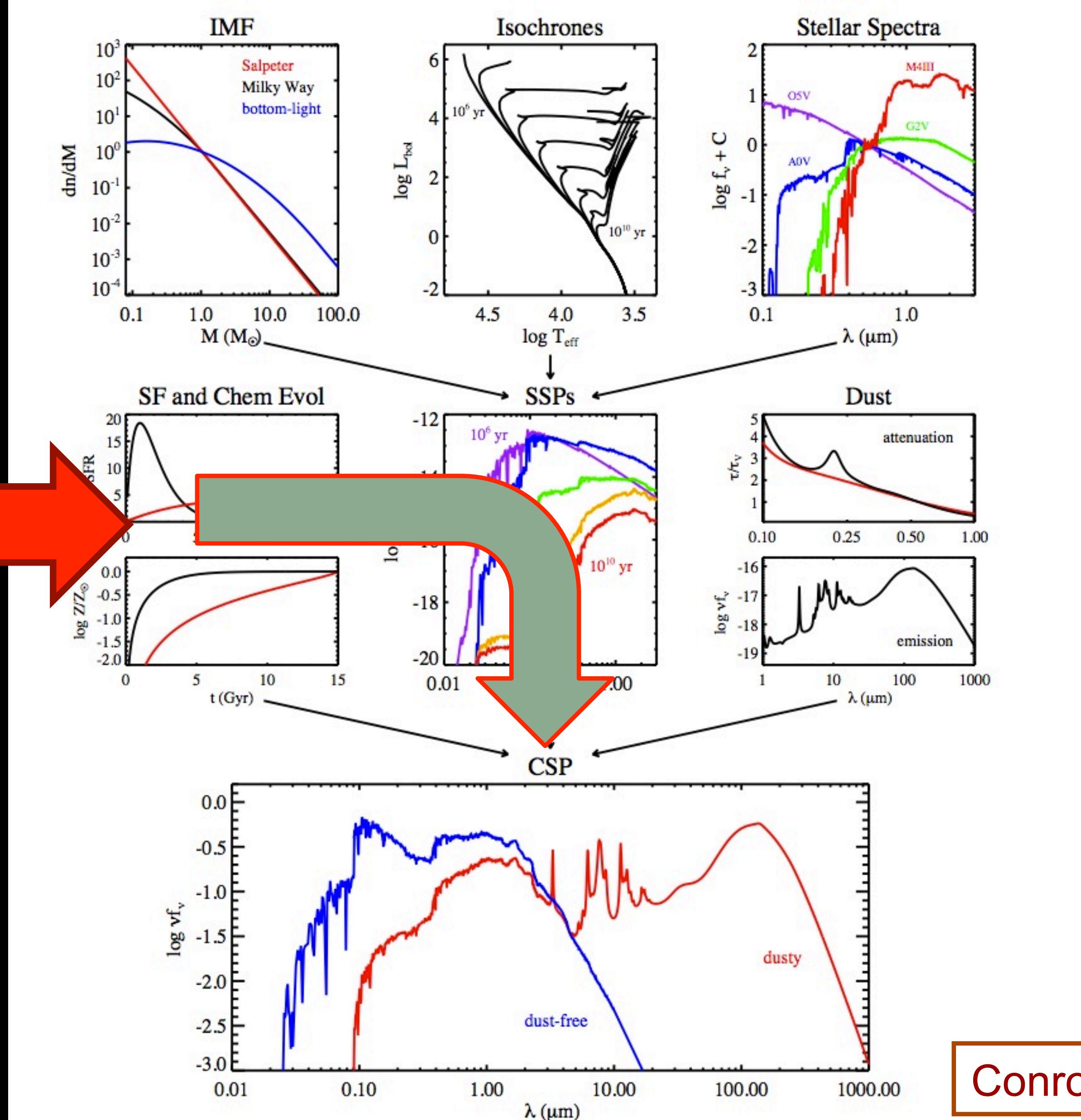
*Given a galaxy  
spectrum, what is  
the SFH?*



Inverse  
Population Synthesis

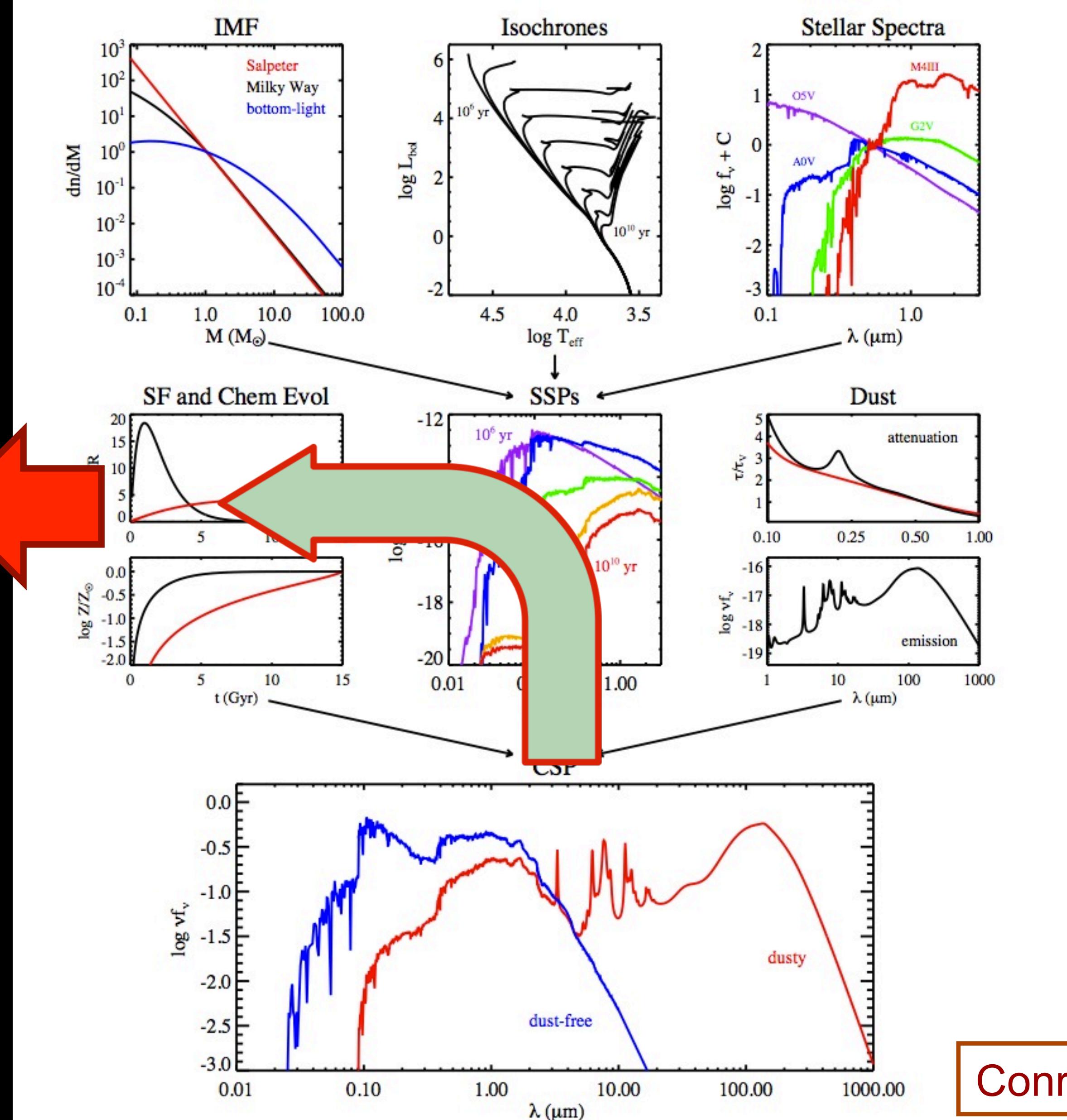
# Forward spectral synthesis

**ASSUME**  
Star  
Formation  
History



# Inverse spectral synthesis

**DERIVE**  
Star  
Formation  
History



# → SFH( $t, Z$ ): 2 approaches

## Evolutionary Pop Synthesis

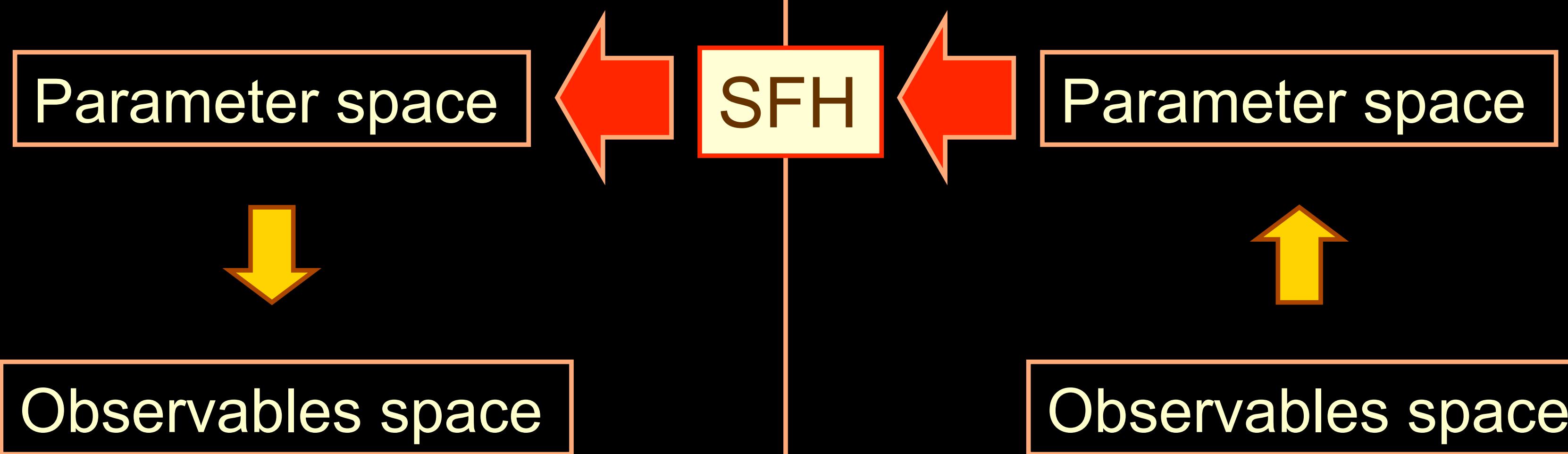
= Forward Modeling  
Predict spectra( $t, Z, \dots$ )  
*Ab initio* calculation of

$$L_{\text{gal}}(\lambda | \text{SFH parameters})$$

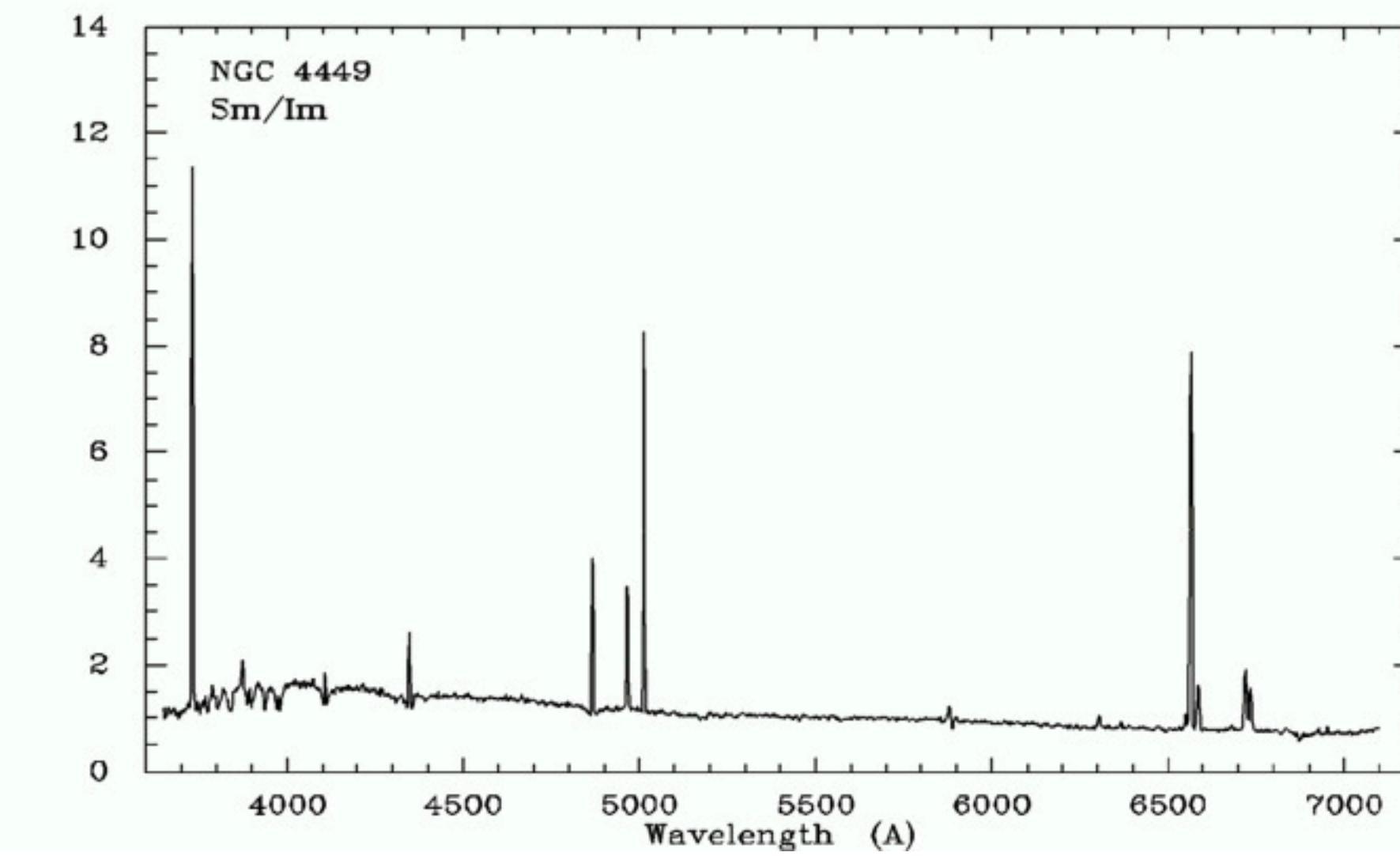
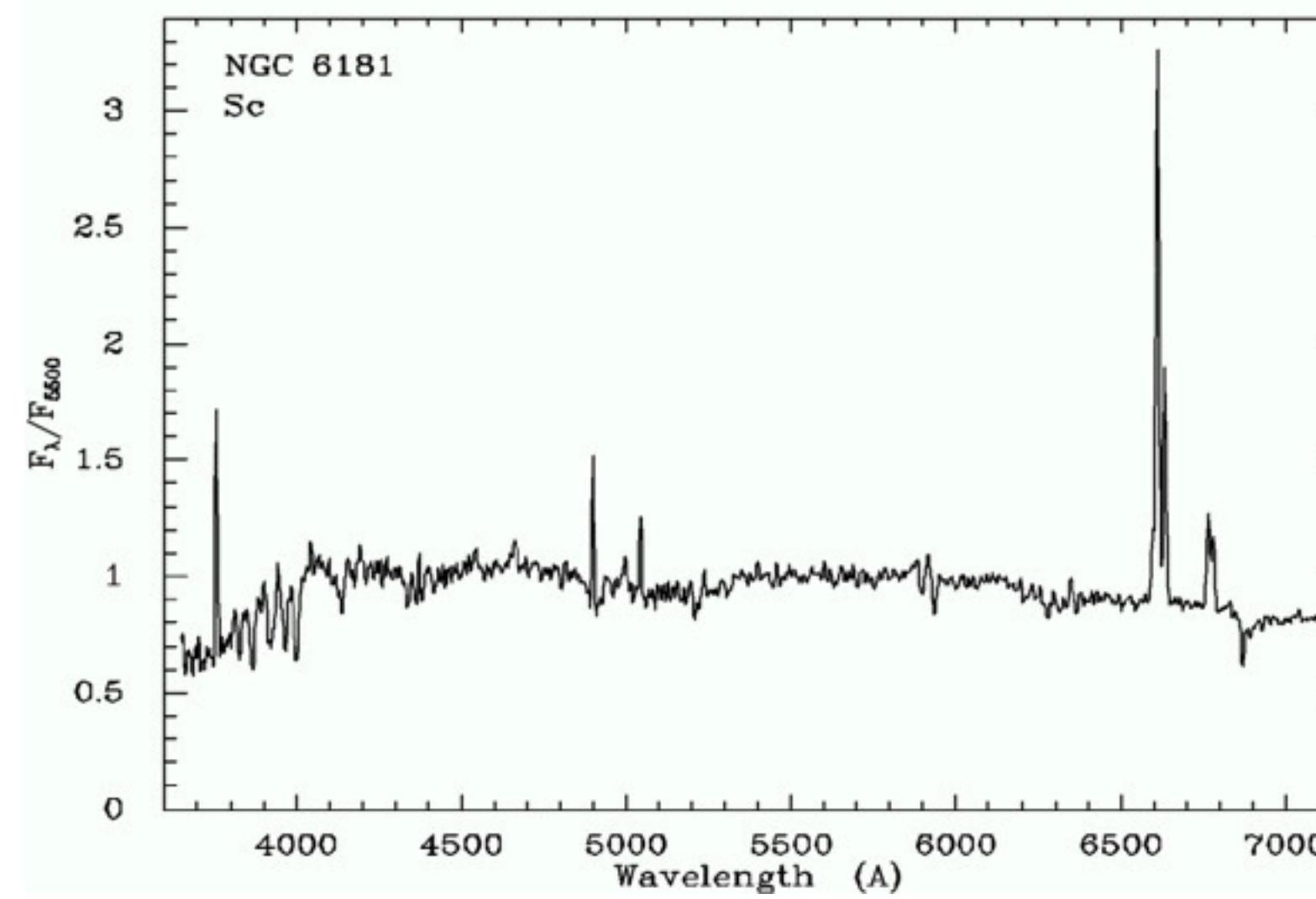
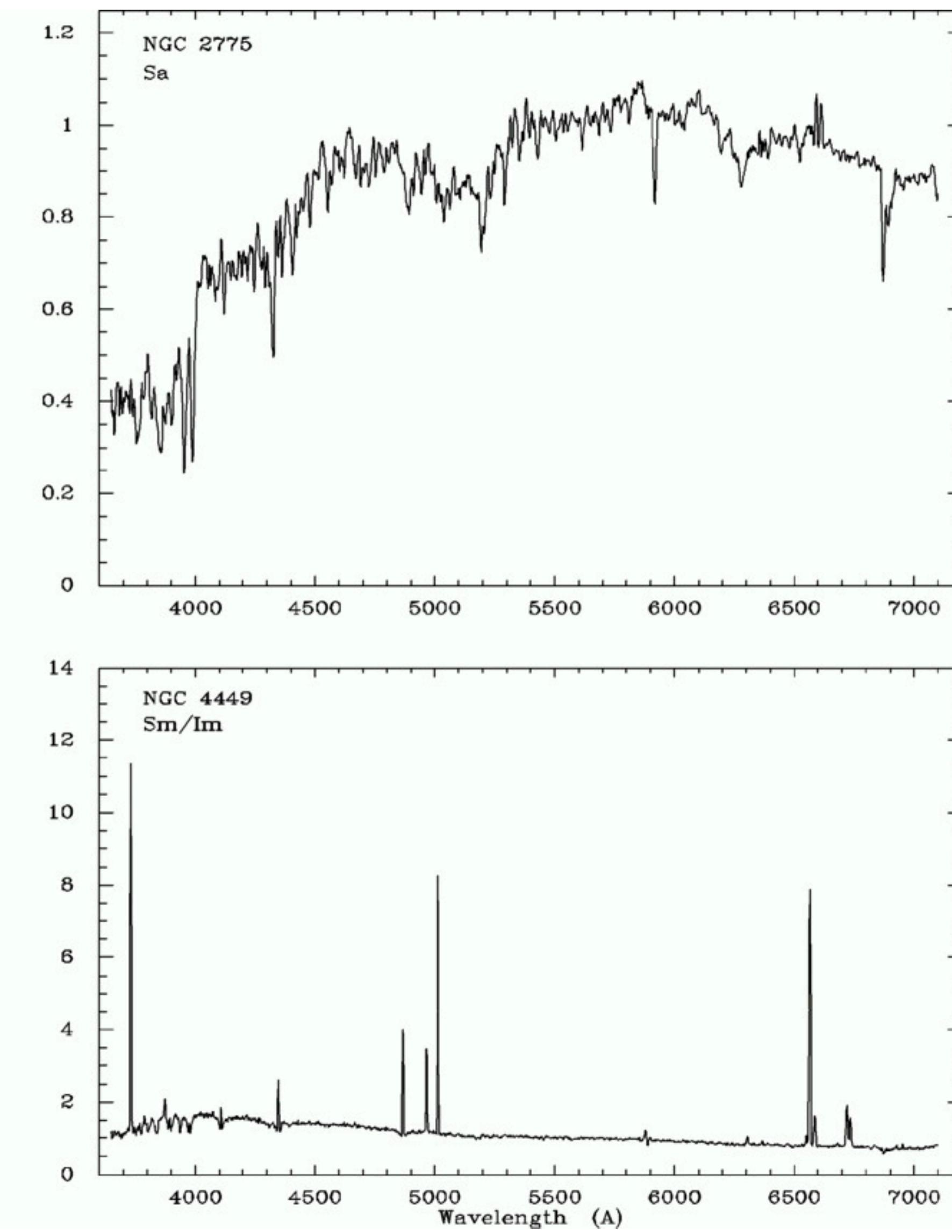
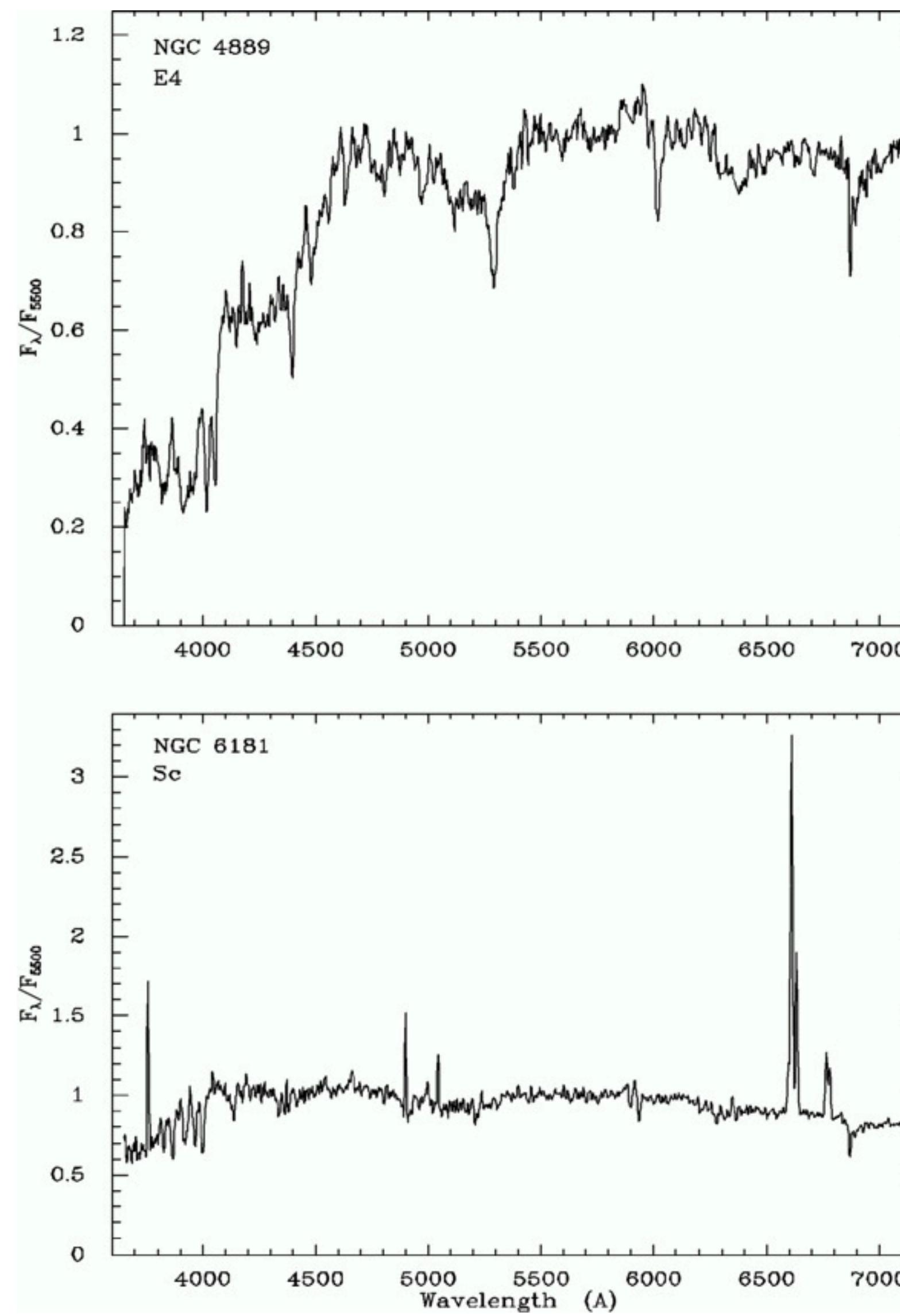
## Inverse Pop Synthesis

= “Paleontology”  
“Reverse engineering”  
“Fossil Method”

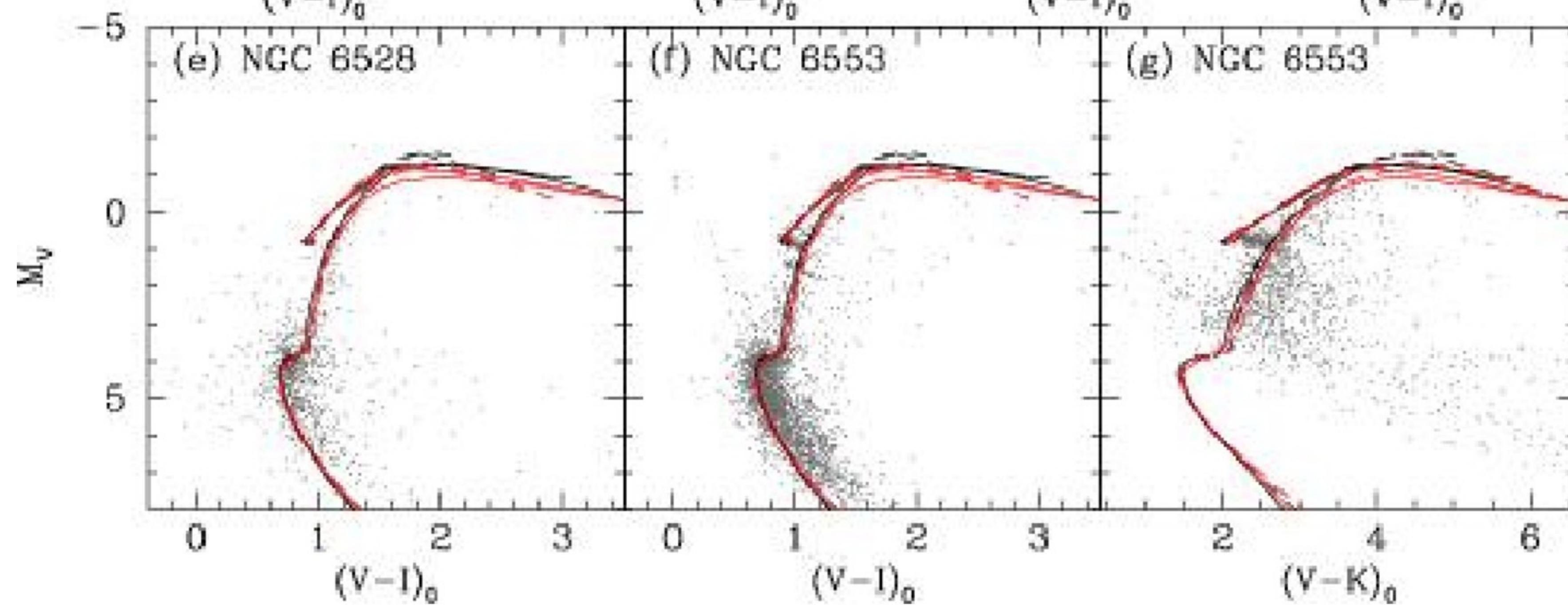
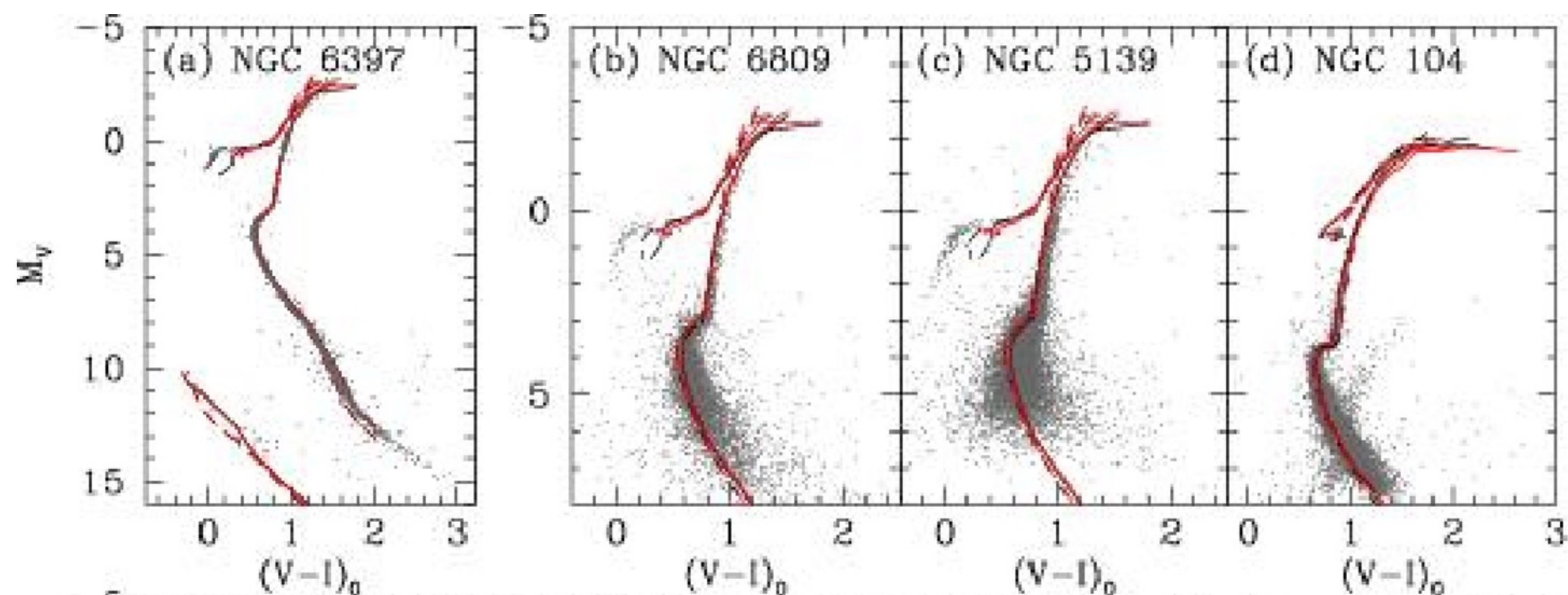
Infer population parameters  
from an **observed**  $L_{\text{gal}}(\lambda)$

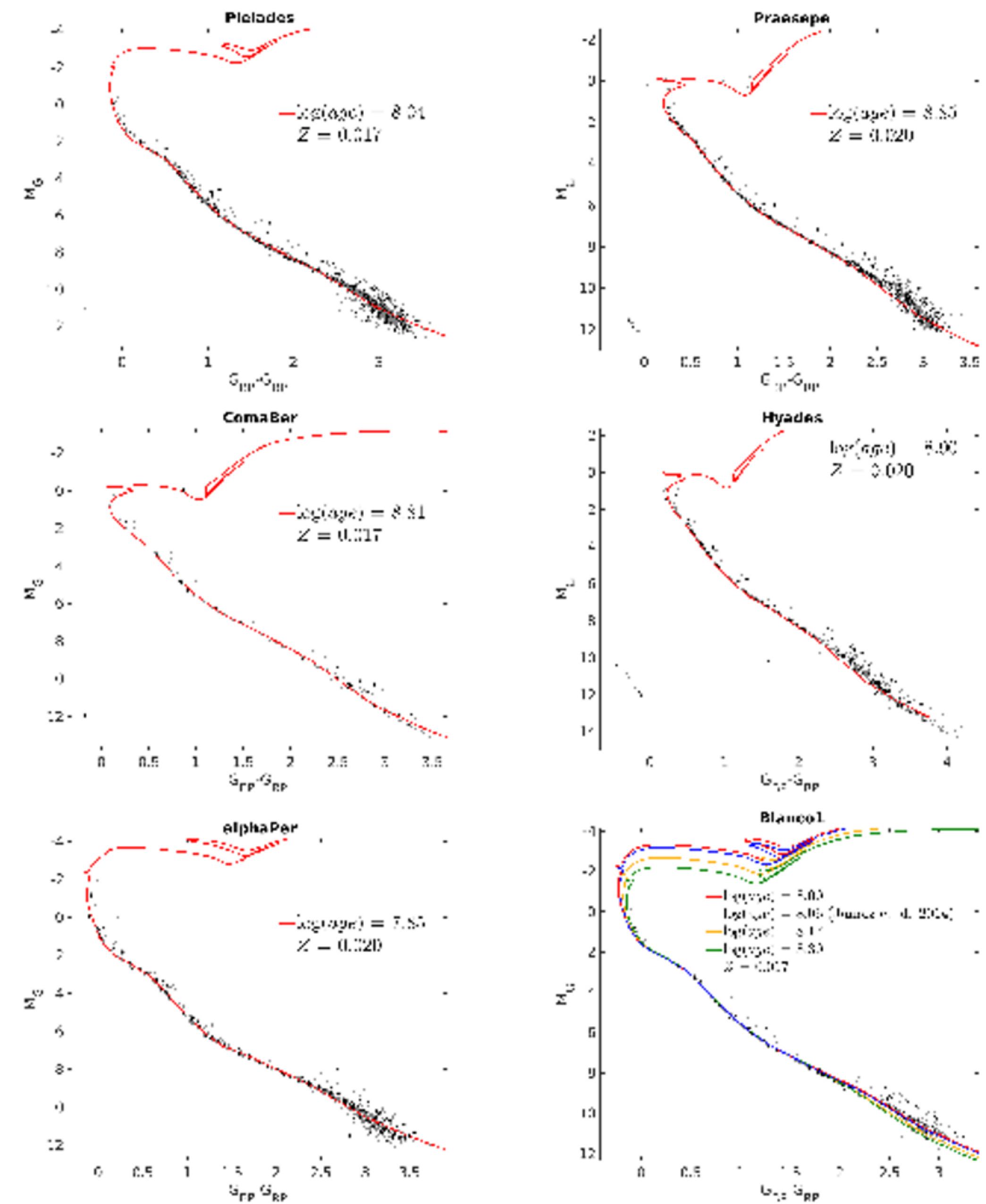


Q: : Which morphological class corresponds to each spectra?

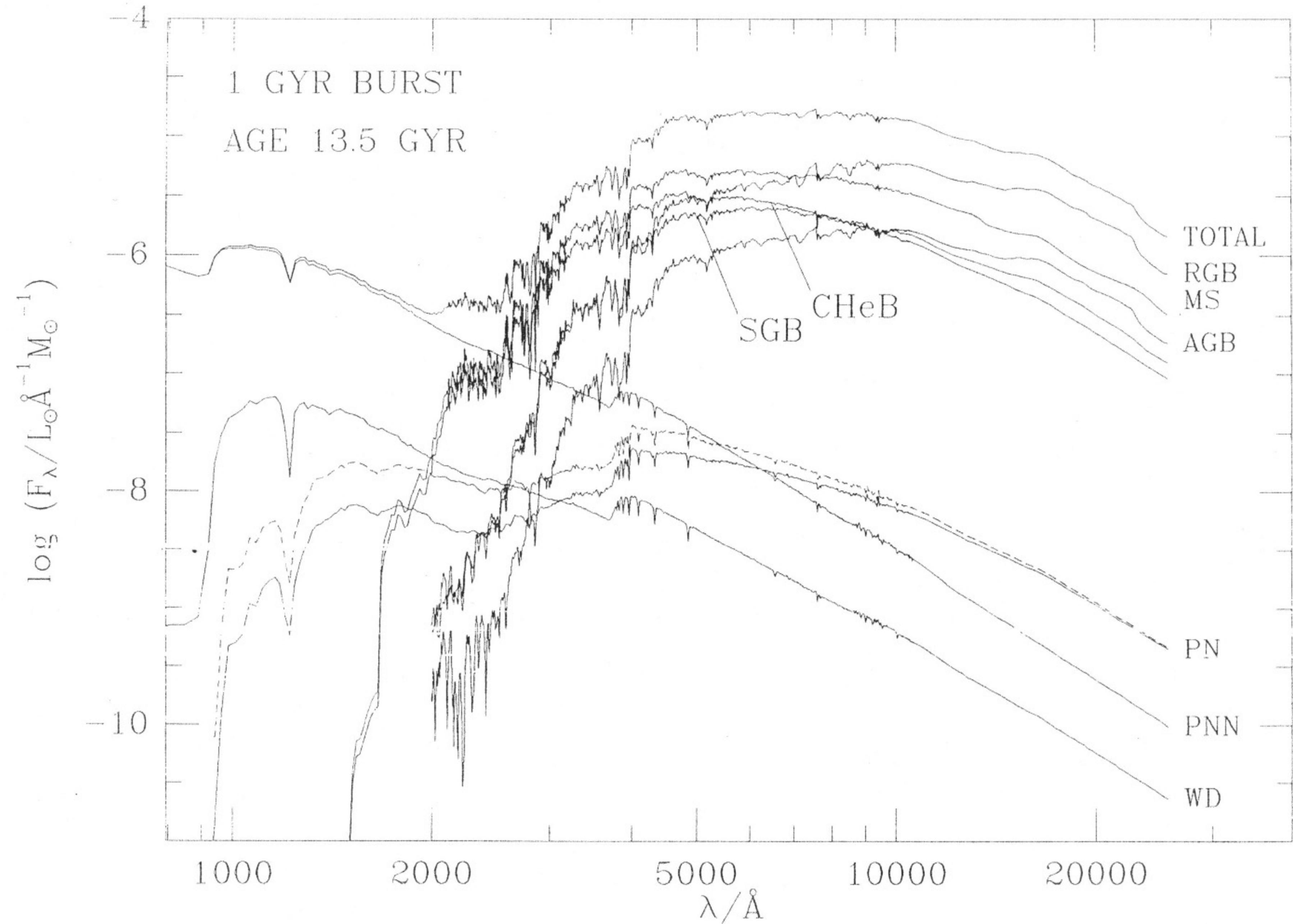


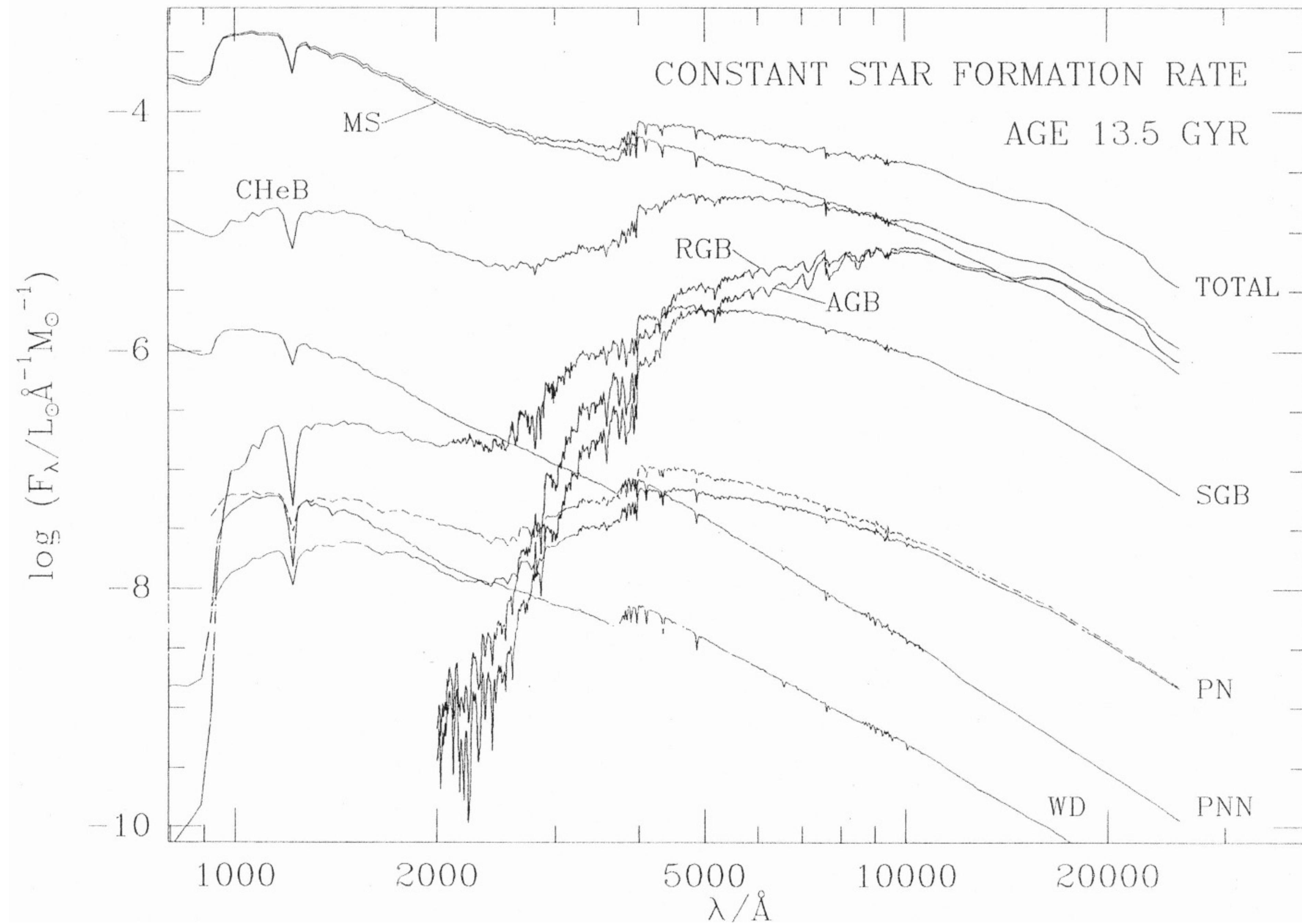
# Backup





**Fig. 17.** HRDs of nearby clusters compared with PARSEC isochrones (see text for details) of the Pleiades (*panel a*), Praesepe (*panel b*), Coma Ber (*panel c*), Hyades (*panel d*), Alpha Per (*panel e*), and Blanco 1 (*panel f*). Praesepe, Hyades, and Alpha Per are fitted with  $Z = 0.02$ , while the others are reproduced using  $Z = 0.017$ .





models, with ages indicated on the top right corner.  
Figure adapted from Bruzual & Charlot (2003).

