# What If We Encoded Words as Matrices and Used Matrix Multiplication as Composition Function?

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Extended abstract of: F Mai, L Galke, A Scherp: CBOW Is Not All You Need: Combining CBOW with the Compositional Matrix Space Model, ICLR 2019.

#### **Motivation**

- Word embeddings (Collobert & Weston, ICML 2008; Mikolov et al., NeurIPS 2013)
  - Learn once from unlabelled text, re-use often
- Drawback of aggregated word embeddings
  - Compositions are not order-aware

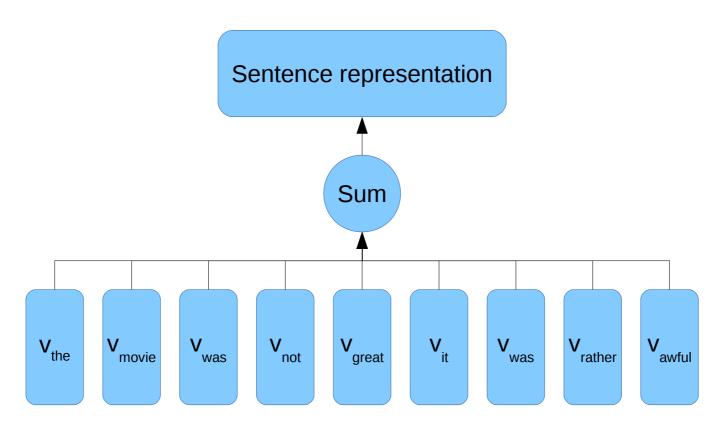
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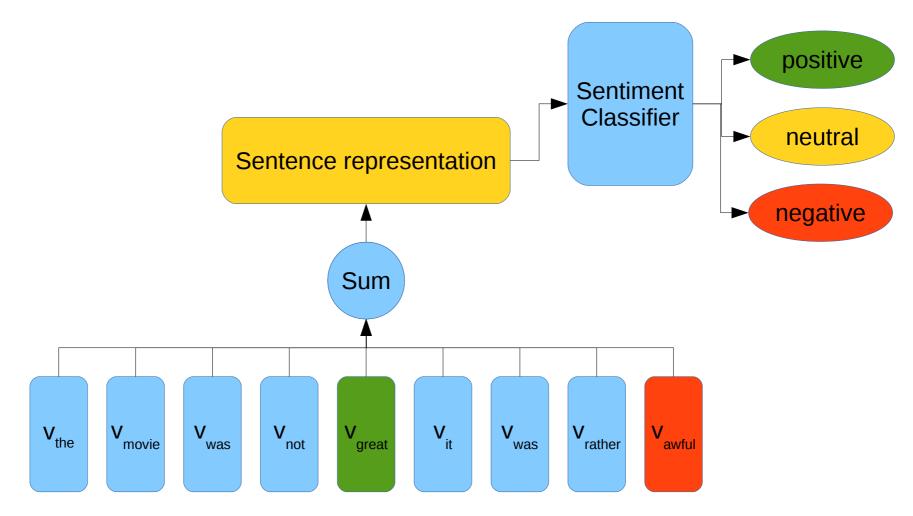
The movie was not great, it was rather awful.

The movie was not awful, it was rather great.

## **Continuous Bag of Words (CBOW)**



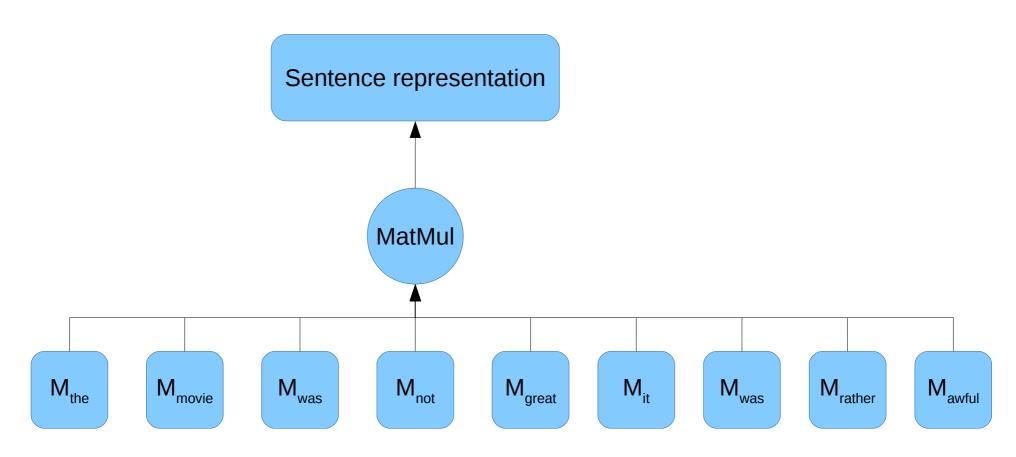
#### **Classification with CBOW**



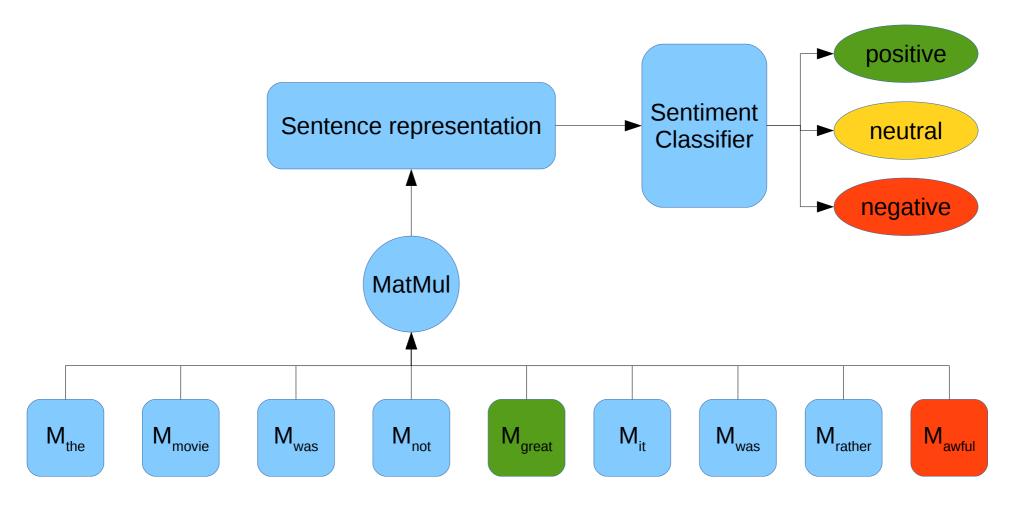
# **Key Idea**

Use matrix multiplication as composition function.

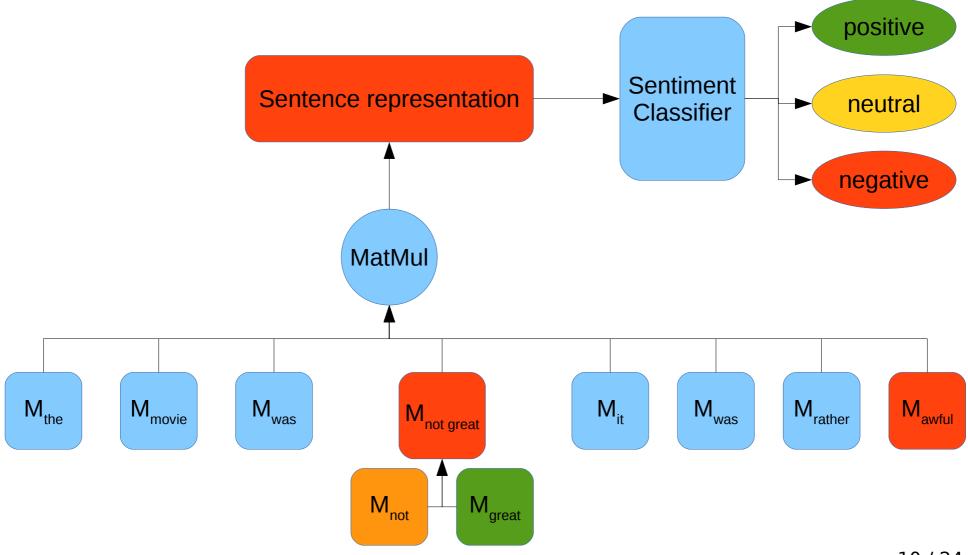
# Continual Matrix Multiplication (CMOW)



### Classification with CMOW



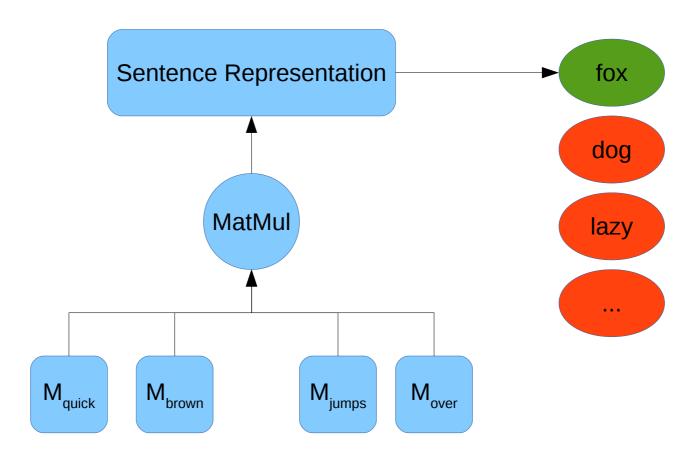
### Classification with CMOW



# **Unsupervised Training**

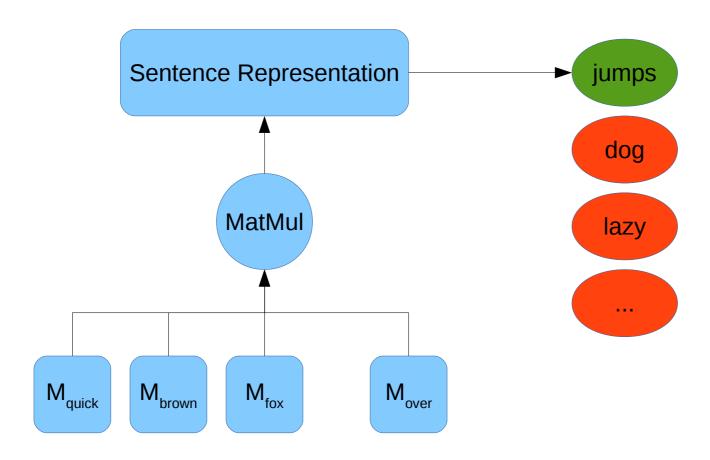
- Training as in Word2Vec (Mikolov et al, NeurIPS 2013)
- Matrix multiplication as composition function
- Initialization close to identity matrix
  - Such that values don't vanish or explode
- Randomize target word
  - To alleviate bias regarding center words

# **Unsupervised Training**



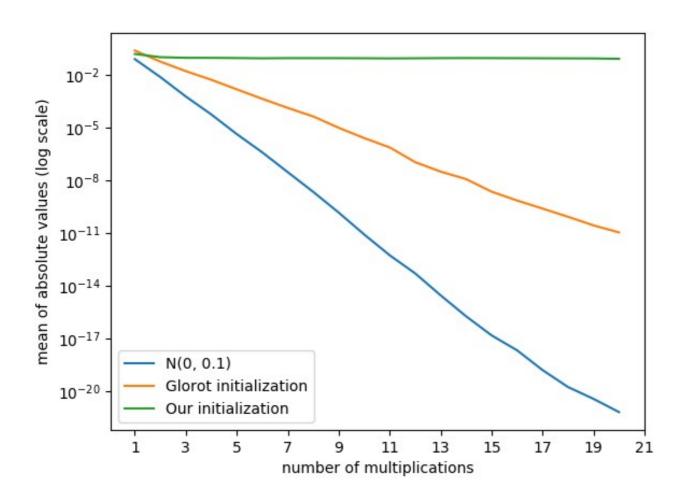
The quick brown \_\_\_ jumps over the lazy dog.

# **Training: Randomize Target Word**



The quick brown fox \_\_\_ over the lazy dog.

# **Initialize Close to Identity Matrix**



Ours: Initialize word matrices as  $I_n + N(0, 0.1)$ 

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#### **Fair Evaluation**

- Same training data: 3B tokens
- Same vocabulary size: 30k
- Same number of parameters
- 10 linguistic probing tasks
- 16 downstream tasks

### **Results: CBOW vs CMOW**

#### **Linguistic Probing Tasks**

Method	Depth	BShift	SubjNum	Tense	Coord Inv	Length	Obj Num	TopConst	SOMO	WordContent
CBOW	33.0	49.6	79.3	78.4	53.6	74.5	78.6	72.0	49.6	89.5
CMOW	35.1	70.8	82.0	80.2	61.8	82.8	79.7	74.2	50.7	72.9

#### **Supervised Downstream Tasks**

Method	SUBJ	CR	MR	MPQA	MRPC	TREC	SICK-E	SST2	SST5	STS-B	SICK-R
CBOW	90.0	79.2	74.0	87.1	71.6	85.6	78.9	78.5	42.1	61.0	78.1
CMOW	87.5	73.4	70.6	87.3	69.6	88.0	77.2	74.7	37.9	56.5	76.2

#### **Unsupervised Downstream Tasks**

Method	STS12	STS13	STS14	STS15	STS16
CBOW	43.5	50.0	57.7	63.2	61.0
CMOW	39.2	31.9	38.7	49.7	52.2

### **Results: CBOW vs CMOW**

#### **Linguistic Probing Tasks**

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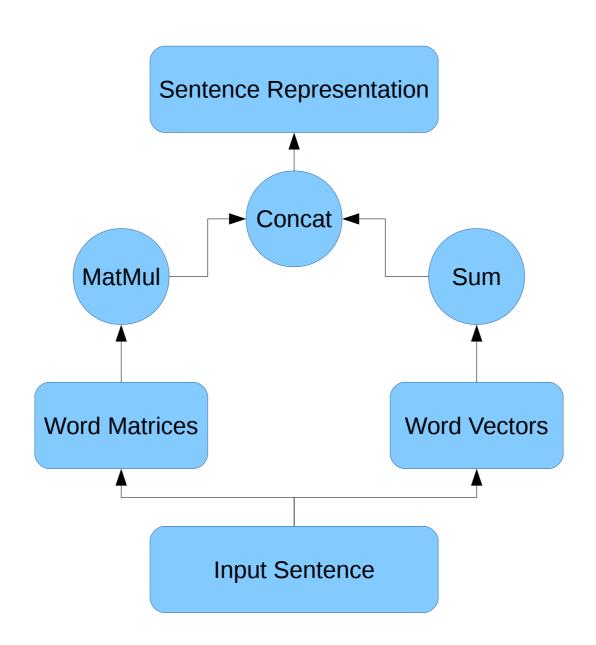
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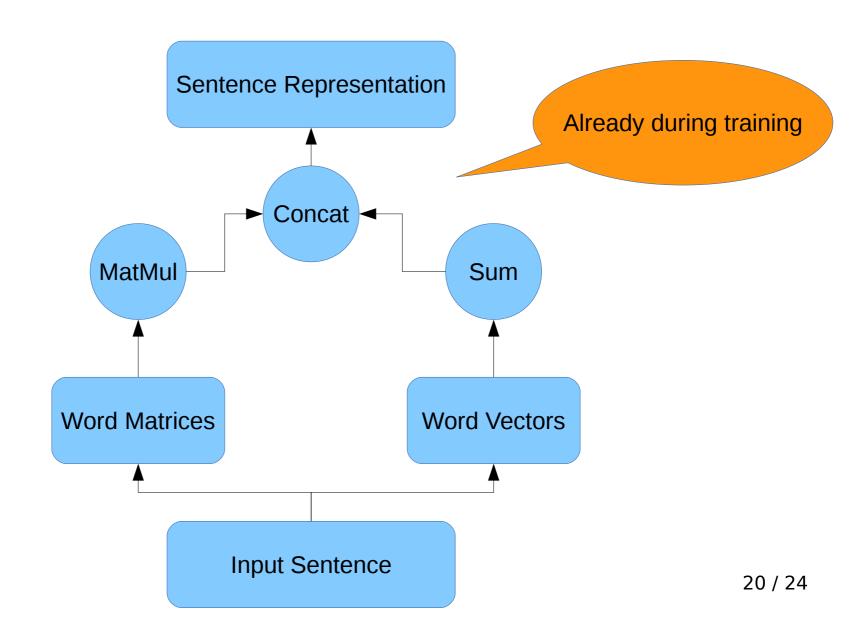
# Vector-based and matrix-based models are complementary

- Vector-based models succeed at word content memorization
- Matrix-based models are superior in all other linguistic probing task
- Idea: use both vectors and matrices

# **Hybrid CMOW-CBOW Approach**



# **Hybrid CMOW-CBOW Approach**



# **Results: Hybrid Approach**

#### **Linguistic Probing Tasks**

Method	Depth	BShift	SubjNum	Tense	Coord Inv	Length	Obj Num	TopConst	SOMO	WordContent
CBOW	33.0	49.6	79.3	78.4	53.6	74.5	78.6	72.0	49.6	89.5
CMOW	35.1	70.8	82.0	80.2	61.8	82.8	79.7	74.2	50.7	72.9
Hybrid	35.0	70.8	81.7	81.0	59.4	84.4	79.0	74.3	49.3	87.6

#### **Supervised Downstream Tasks**

Method	SUBJ	CR	MR	MPQA	MRPC	TREC	SICK-E	SST2	SST5	STS-B	SICK-R
CBOW	90.0	79.2	74.0	87.1	71.6	85.6	78.9	78.5	42.1	61.0	78.1
CMOW	87.5	73.4	70.6	87.3	69.6	88.0	77.2	74.7	37.9	56.5	76.2
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#### **Unsupervised Downstream Tasks**

Method	STS12	STS13	STS14	STS15	STS16
CBOW	43.5	50.0	57.7	63.2	61.0
CMOW	39.2	31.9	38.7	49.7	52.2
Hybrid	49.6	46.0	55.1	62.4	62.1

1.2% avg. improvement

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#### **Discussion**

#### Alternatives

- RNNs are weakly parallelizable, require O(n) sequential steps
- BERT (Devlin et al. 2018) and other
  Transformers are quadratic in sequence length
- 1D-Convolutions are similar, but wordorder might get lost during pooling

#### Our hybrid model

- Same #parameters as word embeddings
- Requires only O(log n) sequential steps
- Allows dynamic programming

#### Conclusion

- Matrix- and vector-based methods capture complementary properties
- Hybrid model achieves 1.2% improvement across 16 downstream tasks compared to CBOW
- First unsupervised training scheme for matrix-based embedding models
- Opens up new opportunities for order awareness

# Acknowledgment

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