

3.3

- 11) A)  $S$  = The set of students at your school  
 $M$  = The set of movies that have ever been released  
 $V(S, M)$  Students  $s$  has seen movie  $m$   
 There is a student at your school who has seen Casablanca

D) There is a movie that all students have seen  
 For every  $m \in M$  There exist  $s \in S$  such that  $V(s, m)$

- 15)  $\forall$  odd INT  $N$ ,  $\exists$  an INT  $K$  such that  $n = 2K + 1$   
 For every odd INT There exist a second INT such that twice the second plus one equals that odd INT

$\sim (\forall$  odd INT  $N, \exists$  an INT  $K$  such that  $n = 2K + 1)$   
 $\sim (\forall x \text{ in } D, \exists y \text{ in } E \text{ such that } P(x, y))$

- $\exists x \in D$  such that  $\forall y \in E, \sim P(x, y)$   
 $\exists$  an odd INT  $n$  such that  $\forall$  INT  $K, n \neq 2K + 1$   
 There is an odd INT that doesn't equal two times an INT plus one True

- 22) A) For every real number, there exist another real number such that the sum of these two numbers equal 0

B) There exist a real number such that when we add any other real number, the sum equals 0

- 41) C) False No 1 number is possible for all  $y$  values  
 d) True Can't divide by 0  
 E) False  $x \neq 0$   
 f) False  $-2 \in \mathbb{Z}^+$   
 g) True  $\mathbb{Z} = x - y$   
 h) True If  $0 < u < 1$  then  $\forall v \in \mathbb{R}^+ uv < v$



3.4  $\forall x \quad P(x) \rightarrow Q(x)$   
 16) If a number is even then twice that number is even  
 $Q(a)$  for a particular  $a$   
 The particular number  $2n$  is even  
 For a particular number  $n$   
 $\therefore$  The particular number  $n$  is even  
 $P(a)$  for particular  $a$

Invalid

19) B) No good car is cheap  
 A Simba is not cheap  
 $\therefore$  A Simba is a good car  
 $\forall$  cars, if car is good then car isn't cheap  
 $\forall x, \text{ if } P(x) \rightarrow \neg Q(x)$

A Simba isn't cheap  
 $\neg Q(a)$  for particular  $a$   
 $\therefore$  A Simba is a good car  
 $P(a)$  for particular  $a$

Let  $R(x) = \neg Q(x)$   $R(a) = \neg Q(a)$

$\forall x \text{ if } P(x) \rightarrow R(x)$

$\neg R(a)$  for particular  $a$

$\therefore P(a)$  for particular  $a$

25) No college cafeteria food is good (solid)  
 No good food is wasted (dash)  
 $\therefore$  No college cafeteria food is wasted

invalid good food

College cafeteria

Invalid good food

College Food

wasted food

Invalid good food

College Food  
 wasted