

4.3

~~9) For all $\text{INT } n$ and d , $d \mid n$ if, and only if~~

11) Does 3 divide $(3k+1)(3k+2)(3k+3)$

yes; $(3k+1)(3k+2)(3)(k+1)$

$$= 3(3k+1)(3k+2)(k+1)$$

$$\therefore 3 \mid (3k+1)(3k+2)(3k+3)$$

By definition of divisibility

15) Prove From def. of divisibility

For all $\text{INT } a, b$, and c

If $a \mid b$ and $a \mid c$ then $a \mid (b+c)$

Let a, b, c be particular but arbitrary INT
We are given that $a \mid b$ and $a \mid c$.

We must show $a \mid (b+c)$

25) For all $\text{INT } a, b, c$ if a is a factor
of c then ab is a factor of c
false; counter ex: $a=3, b=7, c=9$

42) A) 6! in standard factored form

$$6! = 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1$$

$$= 2 \cdot 3 \cdot 5 \cdot 2 \cdot 2 \cdot 3 \cdot 2 \cdot 1$$

$$= 2^4 \cdot 3^2 \cdot 5$$