

7.1

2) Let $X = \{1, 3, 5\}$ and $Y = \{a, b, c, d\}$

Define $g: X \rightarrow Y$

x	y
1	a
3	b
5	c
	d

a) Domain of g $X = \{1, 3, 5\}$

co domain of g $Y = \{a, b, c, d\}$

b) $g(1) = a$ $g(3) = b$ $g(5) = c$

c) range of $g = \{a, b, c\}$

d) 3 is not an inverse of a

1 is an inverse of a

e) $\{1, 3, 5\}$ is the inverse of b ; c doesn't exist

f) g as ordered pairs: $\{(1, a), (3, b), (5, c)\}$

3) Define a function of $S: \mathbb{Z}^+ \rightarrow \mathbb{Z}^+$ as follows
For each positive INT n

$S(n) =$ the sum of the positive divisors of n

d) $S(5) = 1 + 5 = 6$

e) $S(18) = 1 + 2 + 3 + 6 + 9 + 18 = 39$

f) $S(21) = 1 + 3 + 7 + 21 = 32$

14) Let $J_5 = \{0, 1, 2, 3, 4\}$ and define functions $h: J_5 \rightarrow J_5$ and $k: J_5 \rightarrow J_5$ as follows for each $x \in J_5$

$h(x) = (x+3)^3 \pmod{5}$ and $k(x) = (x^3 + 4x^2 + 2x + 2) \pmod{5}$ Is $h = k$? yes, they give same output

Element	h	k
0	2	2
1	4	4
2	0	0
3	1	1
4	3	3

19) Use the def of log to prove that for any positive real number b with $b \neq 1$, $\log_b b = 1$

$$\log_b x = y \Leftrightarrow b^y = x$$

$$\log_b b = 1 \Leftrightarrow b^1 = b$$

29) Find $H(00110, 1011)$ = 2
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