

homework 7 4.6

- 3) Use proof by contradiction to show that for all INT n , $3n+2 \not\equiv 3$

Suppose not; there is an INT such that $3n+2 \equiv 3$ by 3. By def of divisibility, $3n+2=3k$ for some INT k . Subtracting $3n$ from both sides gives that $2=3k-3n=3(k-n)=3 \cdot 2 \neq 3 \cdot 2$

- 5) Formulate negation; prove by contradiction
There is a greatest even int, N
 N is even & $N \geq N$ for every INT N
Let $m=N+2$ then m is an even INT
Since it has the sum of two INT, even
 $m > m$ since $m=N+2$

- 14) Prove by contraposition
Suppose r and s are positive real numbers, $r \leq 10$ and $s \leq 10$, $rs \leq 100$