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2) Does  $7 \mid 56$ ; yes,  $56 = 7 \cdot 8$

6) Is 29 a multiple of 3; No  $29/3 \neq \text{INT}$

7) Is -3 a factor of 66; yes  $-3 \cdot -22 = 66$

24) For all  $\text{INT } a, b, c$ ; if  $a \mid b$  and  $a \mid c$ , then  $a \mid (2b - 3c)$  True

Suppose  $a, b, c$  are any  $\text{INT}$  such that  $a \mid b$  &  $a \mid c$   
By def of divisibility, we know that  $b = am$   
and  $c = an$  for some  $\text{INT } m \text{ \& } n$

$$2b - 3c = 2(am) - 3(an) = a(2m - 3n)$$

Let  $t = 2m - 3n$ . Then  $t$  is an  $\text{INT}$ .

37) A) STD Form:  $1,176 = 2^3 \cdot 3 \cdot 7^2$

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3)  $n = dq + r$  and  $0 \leq r < d$

$$n = 36, d = 40 \quad q = 0 \quad r = 36$$

11) A) Day  $T = 6$  (Saturday) and  $h = 15$

If today is Sat, +15 days is 2 weeks = Sat + 1

$$= \text{Sunday}, \text{Day } N = 0 \quad \text{Day } N = (\text{Day } T + h) \bmod 7$$

$$= (6 + 15) \bmod 7$$

$$= 21 \bmod 7 = 0$$

13) On a Monday, a friend will meet you in 30 days

$$\text{What day is it? } 30 = 4 \cdot 7 + 2$$

2 days after Monday = Wed