

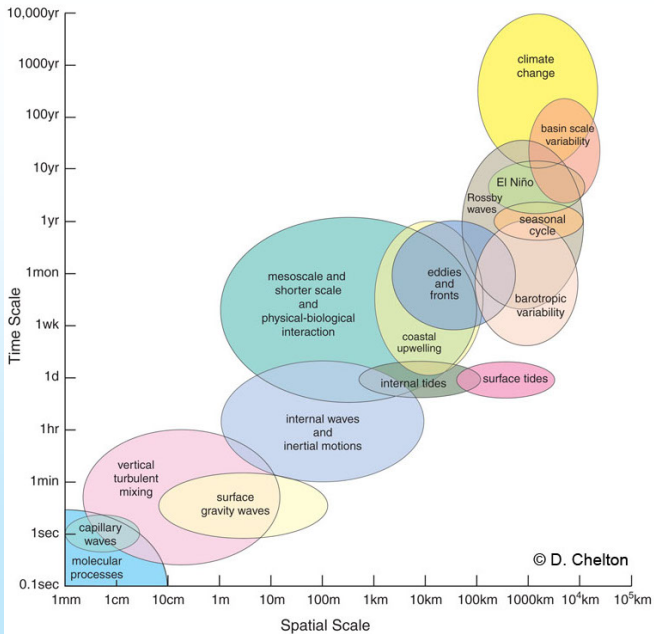
On the inversion of sub-mesoscale information to correct mesoscale velocity

Lucile Gaultier, Jacques Verron, Pierre Brasseur, Jean-Michel Brankart

April 12, 2011

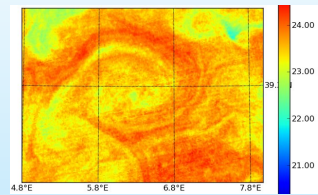
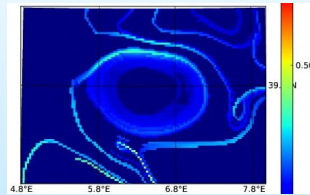
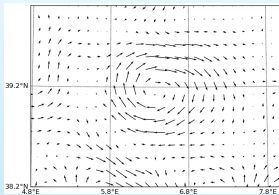


Mesoscale dynamics cascade into sub-mesoscale dynamics



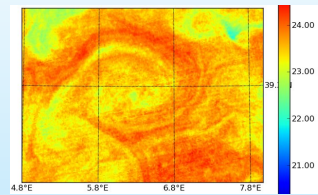
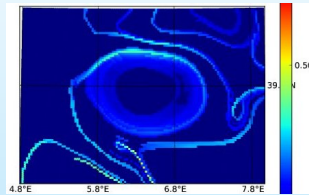
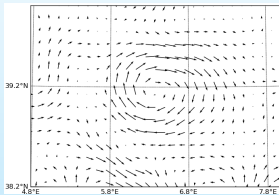
Context of this study

- Lyapunov exponents can be seen as a proxy for tracers (d'Ovidio & al (2004), Lehahn& al (2007)):



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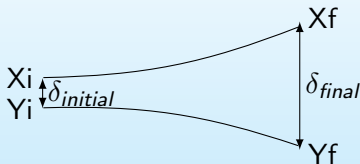
- Inversion of sub-mesoscale tracer information to correct mesoscale velocity

Outline

- 1 Lyapunov exponents
- 2 Methodology of the inversion
- 3 Test Case
- 4 Conclusion

Physical meaning of Lyapunov Exponents

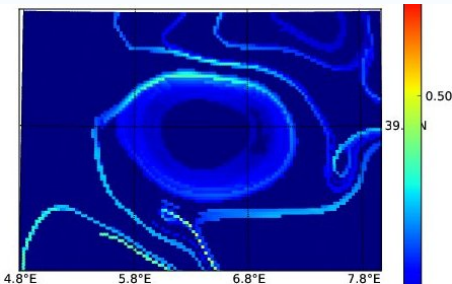
Lyapunov exponents are defined as the exponential rate of separation, averaged over time



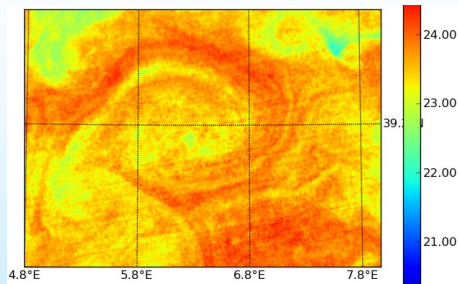
$$\lambda = \frac{1}{T} \times \log\left(\frac{\delta_{final}}{\delta_{initial}}\right)$$

Lyapunov exponents constitute Lagrangian transport barriers between different regions (Lehahn & al (2007)).

Are Lyapunov exponents a reliable proxy/image?



FSLE, June 30, 2004



Sea Surface Temperature, July 03, 2004

Maximum lines of Lyapunov exponents and frontal tracer structures present similar patterns (d'Ovidio & al (2004)).

An exploratory study

- **Step 1:** Inversion of synthetic sub-mesoscale images to larger scale ocean circulation (twin experiment approach)
- **Step 2:** Inversion of sub-mesoscale ocean color or sea surface temperature to larger scale ocean circulation

Methodology

- Velocity panel using Principal Component Analysis with all velocity fields available

$$\mathbf{u}_k = \bar{\mathbf{u}} + \sum_{i=0}^n \underbrace{a_k^i}_{\text{Eigenvalue}} \underbrace{\mathbf{u}^i}_{\text{EOF}}$$

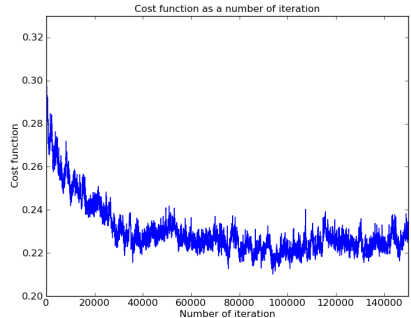
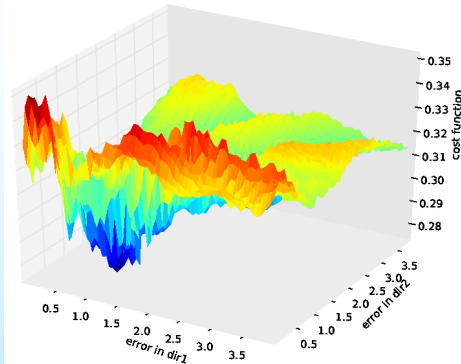
The number of degrees of freedom is reduced using only 100 or less EOFs.

- Assumption of the gaussianity of the velocity error panel: The velocity errors are normally distributed with 0 mean and covariance \mathbf{P} (the covariance of the time sequence) $\delta\mathbf{u} \simeq \mathcal{N}(0, \mathbf{P})$
- Integration of trajectories to derive Lyapunov exponents: $\lambda = \frac{1}{T} \times \log\left(\frac{\delta_f}{\delta_i}\right)$
- The Cost function is the distance between the model and the observation

$$J(u) = \|\lambda(u) - \lambda_{obs}\| + \textit{background term}$$

Minimization of this cost function complex because of many local minima

Methodology



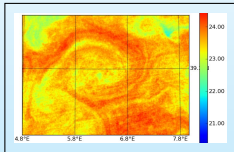
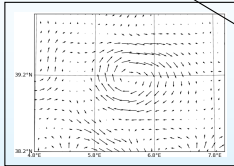
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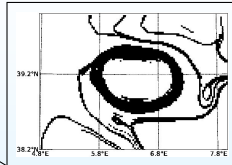
Minimization of this cost function complex because of many local minima

Inversion algorithm

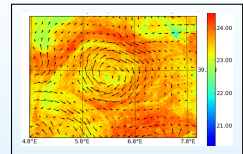
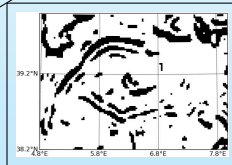
Mesoscale Velocity



Tracer Image



Osmium



Corrected Velocity

Choice of a Study area

Required by Lyapunov exponent

- Being far from any coast : Problem with particules advection in the presence of land
- Being far from any upwelling or downwelling : Vertical velocity is not taken into account in the calculation of Lyapunov exponent

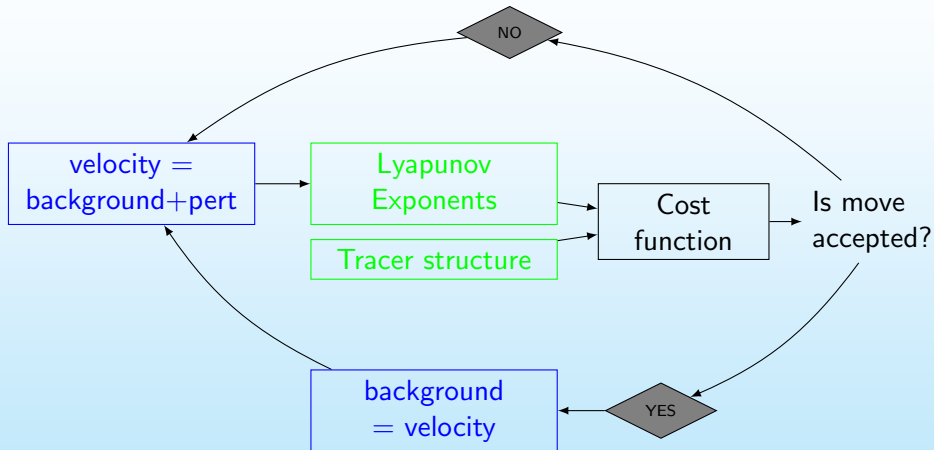
Required by tracer

- Presence of heterogeneity in the tracer to detect filament
- Low cloud cover: Visible and Near IR wavelength do not go through clouds
- Presence of an unstable manifold

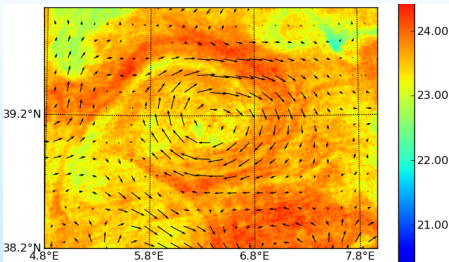
Test case : Mediterranean Sea

- **Region:** Mediterranean Sea, from $4.8^{\circ}E$ to $8^{\circ}E$, from $38.2^{\circ}N$ to $40.0^{\circ}N$
- **Time Range:** from 1998 to June 2009, 595 velocity maps
- **Velocity fields:** AVISO altimeter data
- **Resolution:** $1/8^{\circ}$, grid points: 26×17
- **FSLE Resolution:** $1/48^{\circ}$, grid points: 119×86
- **SST field:** Data from MODIS captor, L2 product
- **Resolution needed to detect filament:** $1/100^{\circ}$

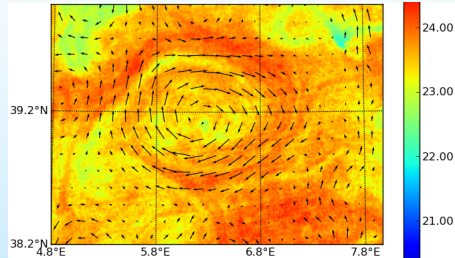
Inversion algorithm



Results



*Aviso velocity, June 30, 2004,
cost function: 0.33*



*Corrected velocity, cost function: 0.23,
number of iterations: 30000*

Conclusion

Sub-mesoscale tracers invertible to larger scales

- Sub-mesoscale tracers inversion to mesoscale velocity is feasible using Lyapunov exponents as a proxy.
- High resolution Sea Surface Temperature or Ocean Color data are useful to control ocean physics.

Next

- Quantify the error made on the estimated velocity
- Avoid the degradation of the corrected velocity with the number of iterations

Prospects

- Assimilation of image in a coupled physico-biogeochemical model
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Thank you for your attention