$$\boxed{\hat{X}} \quad\Longleftrightarrow\quad \hat{\sigma}_x = |0\rangle\langle 1| + |1\rangle\langle 0|$$