$$\begin{array}{c}
\hat{U} \\
 & \hat{A} \\
 & \iff \hat{U} = (\hat{A} \otimes \hat{I})(\hat{I} \otimes \hat{B}) \\
 & = \hat{A} \otimes \hat{B}
\end{array}$$