

$$|\phi\rangle \longrightarrow \boxed{\hat{U}} \longrightarrow |\phi'\rangle \Longleftrightarrow \rho = |\phi\rangle\langle\phi| = \hat{U}|\phi\rangle\langle\phi|\hat{U}^\dagger$$