

$$\rho^\dagger = \rho \iff \text{tr}_1[(I \otimes \rho)(\cdot \cdot)]$$