$$\hat{\rho}_{A} \longrightarrow \hat{U}_{A} \longrightarrow \\
\hat{\rho}_{B} \longrightarrow \hat{U}_{B} \longrightarrow \\
\hat{\rho}_{B} \longrightarrow \hat{U}_{B} \longrightarrow \\
\hat{\rho}' \iff \hat{\rho}' = (\hat{U}_{A} \otimes \hat{U}_{B})(\hat{\rho}_{A} \otimes \hat{\rho}_{B})(\hat{U}_{A} \otimes \hat{U}_{B})^{\dagger} \\
= \hat{U}_{A}\hat{\rho}_{A}\hat{U}_{A}^{\dagger} \otimes \hat{U}_{B}\hat{\rho}_{B}\hat{U}_{B}^{\dagger}$$