

$M_{\min}$  calculation, Fengt 2015, are the units correct? /

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Fengt 2015 quoted

$$M_{\min} \approx (0.0164 M_{\text{Jup}}) \left( \frac{\tau}{\text{yr}} \right)^{4/3} \left| \frac{\dot{\gamma}}{\text{ms}^{-1} \text{yr}^{-1}} \right| \left( \frac{M_{\star}}{M_{\odot}} \right)^{2/3}$$

where the surprising thing is that  $\dot{\gamma}$  is typically given in  $\text{ms}^{-1} \text{day}^{-1}$ .  
the origin of this eqn is stated by Fengt 15 to be the mass function,  
assuming  $e \approx 0.5$ ,  $p = 1.25 \tau$ ,  $K \sim \tau \dot{\gamma}$ , & they cite

Wright & Howard 2008.

Looking at Wright & Howard 2008, Eq 11 is the mass function:

$$K^3 = \frac{2\pi G}{p(1-e^2)^{3/2}} \frac{m^3 \sin^3 i}{(m_{\star} + m)^2}$$

$$m^3 \sin^3 i = \frac{p(1-e^2)^{3/2}}{2\pi G} (m_{\star} + m)^2 K^3$$

$$m \sin i = \left( \frac{p}{2\pi G} \right)^{1/3} (1-e^2)^{1/2} (m_{\star} + m)^{2/3} K$$

$$\approx \left( \frac{1.25 \tau}{2\pi G} \right)^{1/3} (1-e^2)^{1/2} (M_{\star})^{2/3} (\tau \dot{\gamma})$$

$$= \left( \frac{1.25}{2\pi G} \right)^{1/3} (1-e^2)^{1/2} M_{\star}^{2/3} \tau^{4/3} \dot{\gamma}$$

$$= \left( \frac{1.25}{2\pi G} \right)^{1/3} (1-e^2)^{1/2} (M_{\odot}^{2/3} 1 \text{ms}^{-1} \text{yr}^{-1} \cdot (1 \text{yr})^{4/3})$$

$$\cdot \left( \frac{\tau}{\text{yr}} \right)^{4/3} \left| \frac{\dot{\gamma}}{\text{ms}^{-1} \text{yr}^{-1}} \right| \left( \frac{M_{\star}}{M_{\odot}} \right)^{2/3}$$

$$m \sin i \approx (0.03281 M_{\text{Jup}}) \cdot \left( \frac{\tau}{\text{yr}} \right)^{4/3} \left| \frac{\dot{\gamma}}{\text{ms}^{-1} \text{yr}^{-1}} \right| \left( \frac{M_{\star}}{M_{\odot}} \right)^{2/3}$$

# factor of half presumably comes from assuming  $K = \frac{1}{2} \tau \dot{\gamma}$ .