

# The title of my thesis

*Any short subtitle*

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Master in Computational Science  
(Imaging and Biomedical Computing)  
60 credits

Departement of Informatics  
Departement of Physics  
Faculty of mathematics and natural sciences

UNIVERSITY OF OSLO

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Lucas Charpentier

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# Abstract





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# Preface





# **Chapter 1**

## **Introduction**

### **1.1 Background and Motivation**

### **1.2 Problem Statement**

### **1.3 Thesis Outline**





## Chapter 2

# Planning the project

### 2.1 Machine Learning

#### 2.1.1 Supervised Learning

#### 2.1.2 Unsupervised Learning

### 2.2 Artificial Neural Networks

#### 2.2.1 Perceptron

#### 2.2.2 Multilayer Perceptron

#### 2.2.3 Training a Neural Network

### 2.3 Convolutional Neural Network

#### 2.3.1 Convolutional Layers

#### 2.3.2 Pooling Layers

### 2.4 Neural Network Training Optimization

#### 2.4.1 Weight Initialization

#### 2.4.2 Training Batch Size

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### 2.5 Network Pruning

### 2.6 Datasets

#### 2.6.1 MNIST

#### 2.6.2 Fashion MNIST

#### 2.6.3 CIFAR-10

### 2.7 Architectures

#### 2.7.1 VGG-16

## Chapter 3

# Single Layer ANN

In this chapter we will start by analyzing how effective removing nodes at random is. For this section we will only consider a single hidden layer ANN. We will then try estimating the importance of each node by using the loss function and classifying them as important, zero or worse. An important node is one that when removed would increase the loss of the model. A zero node will not significantly affect the loss of the model when removed. Lastly, a worse node will improve the loss of the model when removed. At this point we will also consider a 3 hidden layer MLP and a CNN with 4 convolutional layers followed by a dense layer in addition to the single layer ANN. By using these estimated node importance's, we still prune the models. We will start by pruning the models based on the pre-calculated node importance's, this will be slightly too extreme. Therefore, we will prune the networks by re-calculating the node importance's after removing a node till no node improves the model when removed. Initially, we will do this exhaustively by finding the node when removed will improve the model the most and then removing it. This is very time-consuming and we will therefore consider a "greedy" method that removes the first node that improves or does not affect the model, we will also start ignoring nodes that are quite important for the model in subsequent removals. For the sections on the pruning.

TODO (Describe the datasets used, and the model we consider. Talk about the what we will keep the same during the whole project and what is kept the same for this chapter)

### 3.1 Pruning Nodes at Random

TODO - Describe the algorithms used to remove the nodes randomly

#### 3.1.1 MNIST

Artificial Neural Network with single hidden layer of 128 nodes, using ADAM as optimizer with a learning rate of 0.001 trained on 5 epochs, batch size of 32. Final Accuracy and Loss on test set are: Loss: 0.0879 Accuracy: 0.9724

---

**Algorithm 1:** Removing a user defined number of random nodes

---

```
1 def removeRandomNodes(n, weights, to_consider):  
    Input:  
        n is the number of nodes removed;  
        weights are the weights of the model;  
        to_consider is an array containing the nodes to consider in the  
        random choosing  
    Output: The weights with the nodes removed (set to zero) and  
        the positions of the nodes removed  
    /* Start of the code */  
2    to_drop  $\leftarrow$  choose n from to_consider without replacement  
3    for i in to_drop:  
4        weights[0][:,i] = 0 ;    /* weights going to the node */  
5        weights[1][i] = 0 ;      /* bias going to the node */  
6        weights[2][i,:] = 0 ;    /* weights outgoing the node */  
7    return weights, to_drop
```

---

Trial text

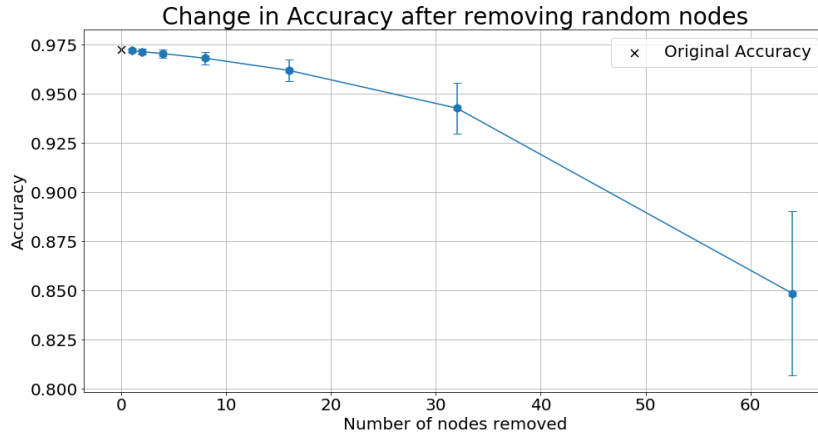


Figure 3.1: Testing

Trial text  
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Trial text  
Trial text  
Trial text

### 3.1.2 Fashion MNIST

Trial text

---

**Algorithm 2:** Shrinking the model by removing nodes randomly

---

```
1 def shrinkModelRandomly(model, acc, loss, weights, n, to_test, x_train,  
  y_train, v):  
    Input:  
        model is the TensorFlow model of the neural network used;  
        acc is the accuracy of the original model;  
        loss is the loss of the original model;  
        weights are the weights of the model;  
        n is the number of nodes removed at each step;  
        to_test is the number of times we try to remove nodes;  
        x_train is the training dataset used;  
        y_train is the labels of the training dataset used;  
        v defines whether are output should be verbose or not;  
    Output: The weights with the nodes removed (set to zero) and  
              the number of nodes removed  
  
    /* Start of the code                                     */  
2    best_loss  $\leftarrow$  loss  
3    best_acc  $\leftarrow$  acc  
4    best_weights  $\leftarrow$  copy(weights)  
5    num_removed  $\leftarrow$  0  
6    to_consider  $\leftarrow$  list from 0 to the number of nodes  
7    for _ in range(to_test):  
8        test_weights  $\leftarrow$  copy(best_weights)  
9        test_weights, dropped = removeRandomNodes(n, test_weights,  
            to_consider)  
10       new_loss, new_acc  $\leftarrow$  evaluate model on x_train and y_train  
11       score =  
           (1 - (new_loss/best_loss)) + ((new_acc/best_acc) - 1)  
12       if score > 0:  
13           best_loss  $\leftarrow$  new_loss  
14           best_acc  $\leftarrow$  new_acc  
15           best_weights  $\leftarrow$  copy(test_weights)  
16           increment num_removed by n  
17           for node in dropped:  
18               remove node from to_consider  
19 return best_weights, num_removed
```

---

	1	2	4	8	16	32	64
<b>mean</b>	0.9720	0.9714	0.9704	0.9681	0.9619	0.9427	0.8485
<b>std</b>	0.0009	0.0013	0.0020	0.0032	0.0056	0.0130	0.0417
<b>min</b>	0.9687	0.9624	0.9602	0.9523	0.9270	0.8861	0.6831
<b>25%</b>	0.9715	0.9708	0.9694	0.9664	0.9588	0.9364	0.8215
<b>50%</b>	0.9721	0.9717	0.9708	0.9685	0.9628	0.9448	0.8546
<b>75%</b>	0.9726	0.9724	0.9719	0.9704	0.9660	0.9526	0.8803
<b>max</b>	0.9736	0.9743	0.9744	0.9749	0.9724	0.9662	0.9328

Table 3.1: Long

	1	2	4	8	16	32	64
<b>mean</b>	0.0895	0.0914	0.0948	0.1024	0.1216	0.1794	0.4466
<b>std</b>	0.0026	0.0038	0.0058	0.0095	0.0164	0.0361	0.1074
<b>min</b>	0.0848	0.0839	0.0838	0.0844	0.0901	0.1127	0.2306
<b>25%</b>	0.0877	0.0887	0.0907	0.0957	0.1101	0.1516	0.3662
<b>50%</b>	0.0890	0.0907	0.0937	0.1012	0.1186	0.1738	0.4313
<b>75%</b>	0.0908	0.0932	0.0981	0.1069	0.1305	0.1980	0.5112
<b>max</b>	0.0997	0.1245	0.1292	0.1489	0.2233	0.3409	0.9883

Table 3.2: Long

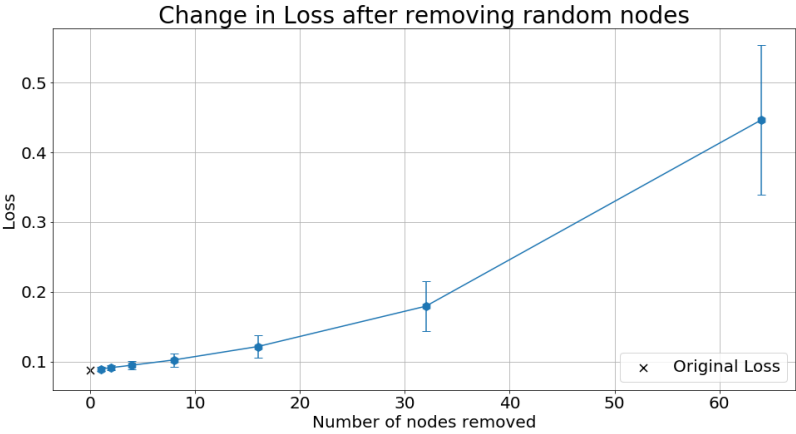


Figure 3.2: Testing

Trial text  
 Trial text  
 Trial text  
 There is trial text here  
 Trial text  
 Trial text  
 Trial text



	1	2	3	4	8
<b>mean</b>	7.4000	8.9000	8.2500	5.8000	2.4000
<b>std</b>	1.6983	2.7891	2.7314	3.3023	3.7613
<b>min</b>	5.0000	4.0000	3.0000	0.0000	0.0000
<b>25%</b>	6.0000	7.5000	6.0000	4.0000	0.0000
<b>50%</b>	7.0000	8.0000	9.0000	4.0000	0.0000
<b>75%</b>	8.2500	10.0000	9.7500	8.0000	8.0000
<b>max</b>	11.0000	16.0000	12.0000	12.0000	8.0000

Table 3.3: Long

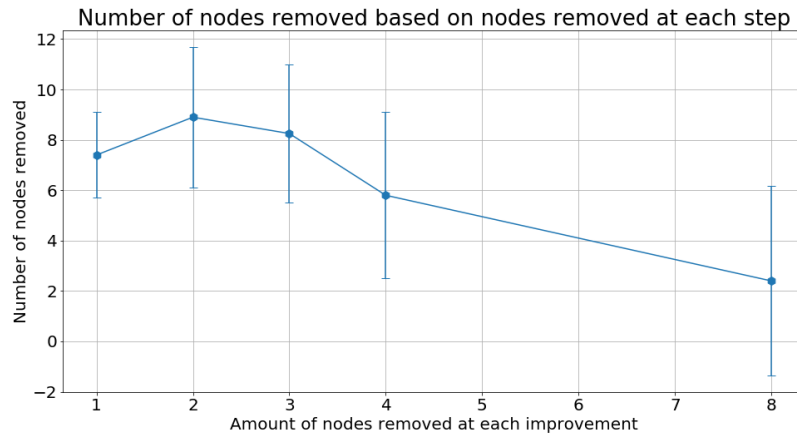


Figure 3.3: Testing

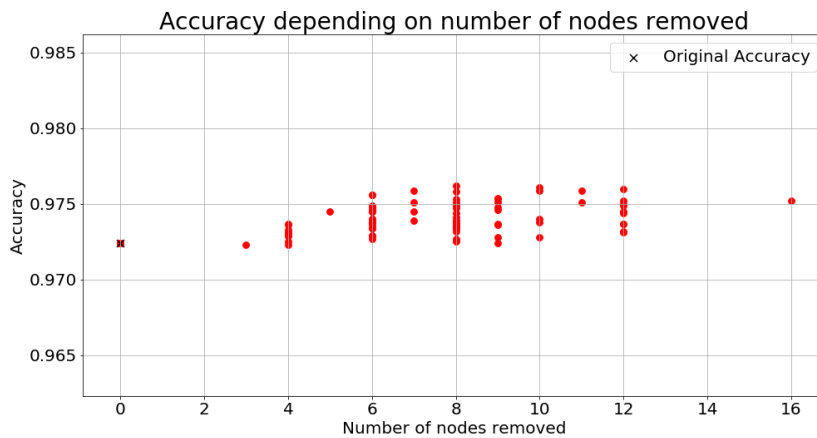


Figure 3.4: Testing

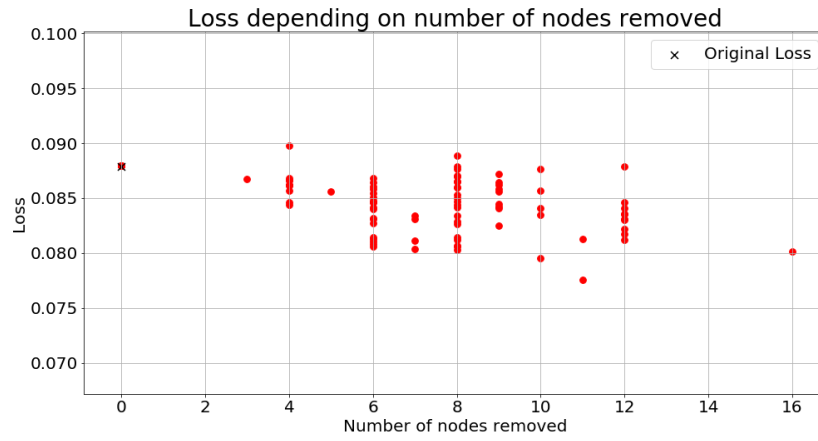


Figure 3.5: Testing

	1	2	4	8	16	32	64
<b>mean</b>	0.8677	0.8667	0.8652	0.8618	0.8543	0.8295	0.7394
<b>std</b>	0.0021	0.0030	0.0042	0.0059	0.0096	0.0200	0.0443
<b>min</b>	0.8578	0.8470	0.8470	0.8405	0.8050	0.7382	0.5493
<b>25%</b>	0.8670	0.8653	0.8632	0.8582	0.8491	0.8190	0.7171
<b>50%</b>	0.8684	0.8674	0.8659	0.8626	0.8558	0.8336	0.7437
<b>75%</b>	0.8686	0.8685	0.8681	0.8663	0.8611	0.8441	0.7698
<b>max</b>	0.8726	0.8735	0.8745	0.8767	0.8747	0.8656	0.8307

Table 3.4: Long

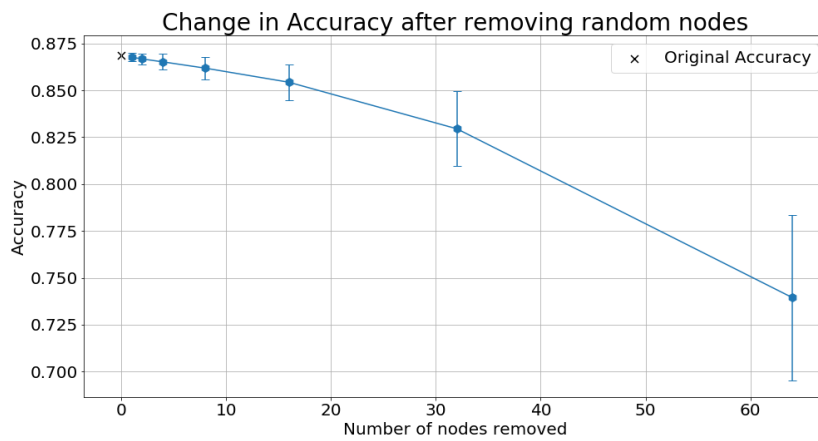


Figure 3.6: Testing

Trial text

	1	2	4	8	16	32	64
<b>mean</b>	0.3578	0.3601	0.3643	0.3730	0.3939	0.4607	0.7062
<b>std</b>	0.0049	0.0070	0.0098	0.0137	0.0228	0.0495	0.1182
<b>min</b>	0.3459	0.3452	0.3434	0.3448	0.3515	0.3725	0.4730
<b>25%</b>	0.3557	0.3559	0.3576	0.3629	0.3772	0.4245	0.6235
<b>50%</b>	0.3564	0.3584	0.3625	0.3711	0.3900	0.4504	0.6867
<b>75%</b>	0.3591	0.3632	0.3693	0.3811	0.4060	0.4857	0.7619
<b>max</b>	0.3791	0.4055	0.4035	0.4297	0.5106	0.7079	1.3649

Table 3.5: Long

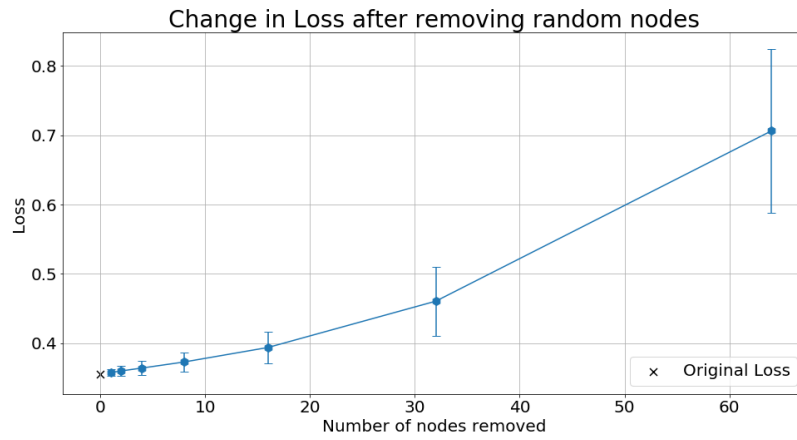


Figure 3.7: Testing

	1	2	3	4	8
<b>mean</b>	5.5000	8.6000	10.6500	8.400	5.6000
<b>std</b>	1.5728	1.8468	3.1502	3.409	3.7613
<b>min</b>	2.0000	6.0000	3.0000	4.000	0.0000
<b>25%</b>	5.0000	8.0000	9.0000	7.000	0.0000
<b>50%</b>	5.5000	8.0000	12.0000	8.000	8.0000
<b>75%</b>	6.2500	10.0000	12.0000	12.000	8.0000
<b>max</b>	8.0000	12.0000	18.0000	16.000	8.0000

Table 3.6: Long

## 3.2 Estimating Node Importance based on Loss

TODO - Describe the algorithms used

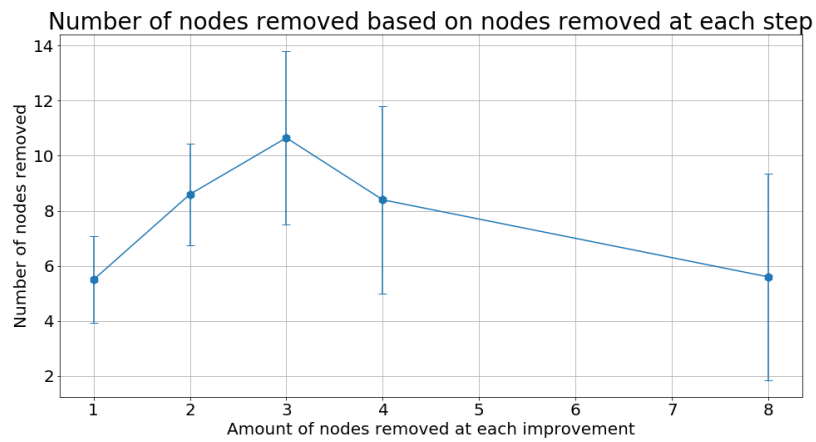


Figure 3.8: Testing

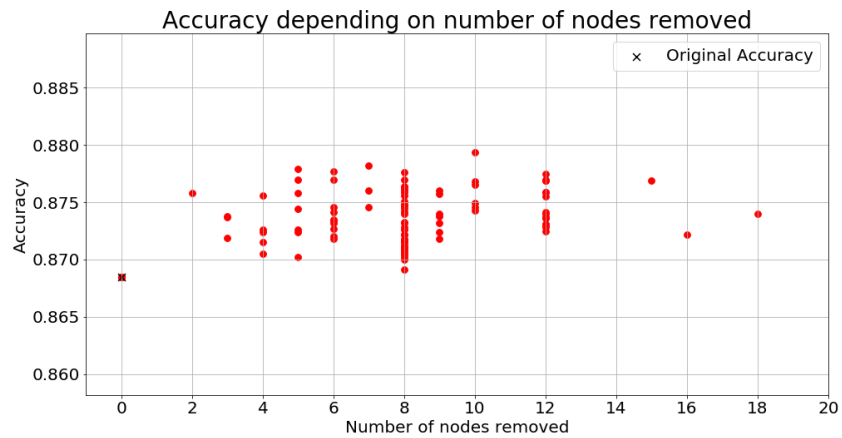


Figure 3.9: Testing

### 3.3 Pruning network with pre-calculated importance

TODO - Describe the algorithms used

### 3.4 Pruning Nodes based on the Loss

TODO - Describe the algorithms used

### 3.5 Greedy approach to pruning instead of Exhaustive approach

TODO - Describe the algorithms used

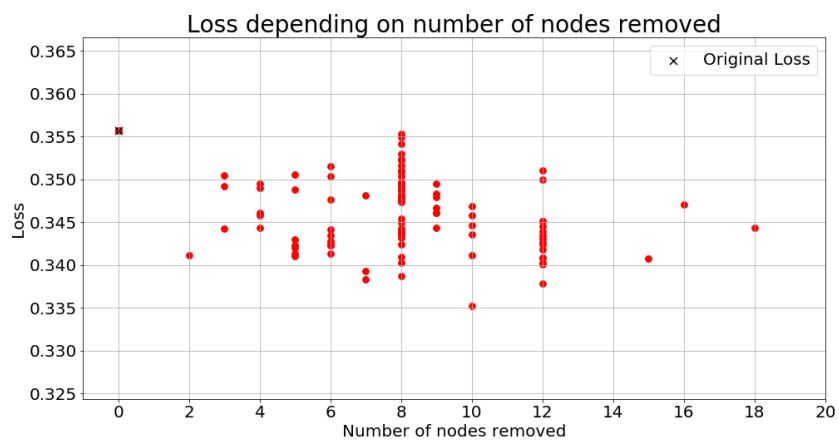


Figure 3.10: Testing



## **Chapter 4**

# **Multi-Layer Perceptron**

- 4.1 Effects of Changing Training Batch Size on Node Importance**
- 4.2 Effects of Using Dropout**
- 4.3 Iterative weight initialization using Node importance**





## **Chapter 5**

# **Convolutional Neural Network**

**5.1 Looking at effects of per class accuracy after pruning**

**5.2 Pruning based on class accuracy**



## **Chapter 6**

### **Case study: Reducing a VGG-16 model trained on X dataset**



## **Chapter 7**

# **Conclusion**

### **7.1 Summary**

### **7.2 Future Works**

