# Intoduction to Data Analysis by "Nafiseh Sedaghat"

# Missing values

There are two types of missing data:

- MCAR: missing completely at random. This is the desirable scenario in case of missing data.
- MNAR: missing not at random. Missing not at random data is a more serious issue and in this case it might be wise to check the data gathering process further and try to understand why the information is missing.
   For instance, if most of the people in a survey did not answer a certain question, why did they do that? Was the question unclear?

#### Loading data:

```
data <- airquality
dim(data)

## [1] 153 6</pre>
head(data)
```

```
Ozone Solar.R Wind Temp Month Day
## 1
        41
              190 7.4
                         67
## 2
        36
              118 8.0
                         72
## 3
       12
              149 12.6
                                    3
## 4
       18
              313 11.5
                         62
                                 5
                                    4
## 5
       NA
               NA 14.3
                         56
                                 5
                                    5
## 6
               NA 14.9
                         66
        28
```

Checking for features (columns) and samples (rows) to see how amount of data is missing

```
pMiss <- function(x){sum(is.na(x))/length(x)*100}
print("Amount of missing values in features:")</pre>
```

```
## [1] "Amount of missing values in features:"
```

```
apply(data,2,pMiss)
```

```
## Ozone Solar.R Wind Temp Month Day
## 24.183007 4.575163 0.000000 0.000000 0.0000000
```

```
cat("\n") # blank line
```

```
print("Amount of missing values in samples:")
## [1] "Amount of missing values in samples:"
apply(data,1,pMiss)
##
          0.00000
                   0.00000
                             0.00000
     [1]
                                      0.00000 33.33333 16.66667
                                                                  0.00000
##
     [8]
          0.00000
                   0.00000 16.66667 16.66667
                                               0.00000
                                                         0.00000
                                                                  0.00000
##
    [15]
          0.00000
                   0.00000
                             0.00000
                                      0.00000
                                               0.00000
                                                         0.00000
                                                                  0.00000
##
    [22]
          0.00000
                   0.00000
                             0.00000 16.66667 16.66667 33.33333
                                                                  0.00000
##
    [29]
          0.00000
                   0.00000
                             0.00000 16.66667 16.66667 16.66667
##
    [36] 16.66667 16.66667
                             0.00000 16.66667
                                                0.00000
                                                         0.00000 16.66667
    [43] 16.66667
##
                   0.00000 16.66667 16.66667
                                               0.00000
                                                         0.00000
                                                                  0.00000
##
    [50]
          0.00000
                   0.00000 16.66667 16.66667 16.66667 16.66667
    [57]
##
         16.66667 16.66667 16.66667 16.66667
                                                         0.00000
                                                                  0.00000
##
                             0.00000
    [64]
          0.00000 16.66667
                                      0.00000
                                               0.00000
                                                         0.00000
                                                                  0.00000
    [71]
                             0.00000
##
          0.00000 16.66667
                                      0.00000 16.66667
                                                         0.00000
                                                                  0.00000
    [78]
                   0.00000
##
          0.00000
                             0.00000
                                      0.00000
                                               0.00000 16.66667 16.66667
    [85]
          0.00000
                   0.00000
                             0.00000
##
                                      0.00000
                                               0.00000
                                                         0.00000
                                                                  0.00000
##
    [92]
          0.00000
                   0.00000
                             0.00000
                                      0.00000 16.66667 16.66667 16.66667
##
    [99]
          0.00000
                   0.00000
                             0.00000 16.66667 16.66667
                                                         0.00000
                                                                  0.00000
  [106]
          0.00000 16.66667
                             0.00000
                                      0.00000
                                                0.00000
                                                         0.00000
##
                                                                  0.00000
##
   [113]
          0.00000
                   0.00000 16.66667
                                      0.00000
                                                0.00000
                                                         0.00000 16.66667
                                      0.00000
##
  [120]
          0.00000
                   0.00000
                             0.00000
                                                0.00000
                                                         0.00000
                                                                  0.00000
##
  [127]
          0.00000
                   0.00000
                             0.00000
                                      0.00000
                                                0.00000
                                                         0.00000
                                                                  0.00000
##
  [134]
          0.00000
                   0.00000
                             0.00000
                                      0.00000
                                               0.00000
                                                         0.00000
                                                                  0.00000
## [141]
          0.00000
                   0.00000
                             0.00000
                                      0.00000
                                                0.00000
                                                         0.00000
                                                                  0.00000
## [148]
          0.00000
                   0.00000 16.66667
                                      0.00000
                                               0.00000
                                                         0.00000
```

Here, we are going to omit or impute missing values using a the airquality dataset (available in R).

Detecting missing values:

```
complete.cases(data)
```

```
TRUE
                                                        TRUE
##
     [1]
          TRUE
                 TRUE
                       TRUE
                              TRUE FALSE FALSE
                                                              TRUE FALSE FALSE
##
    [12]
          TRUE
                 TRUE
                       TRUE
                              TRUE
                                    TRUE
                                           TRUE
                                                  TRUE
                                                        TRUE
                                                               TRUE
                                                                     TRUE
                                                                           TRUE
                                                  TRUE
##
    [23]
          TRUE
                 TRUE FALSE FALSE FALSE
                                           TRUE
                                                        TRUE
                                                               TRUE FALSE FALSE
##
    [34] FALSE FALSE FALSE
                                    TRUE FALSE
                                                  TRUE
                                                        TRUE FALSE FALSE
                                                                            TRUE
    [45] FALSE FALSE
                       TRUE
                              TRUE
                                    TRUE
                                           TRUE
                                                  TRUE FALSE FALSE FALSE
##
                                                  TRUE
##
    [56] FALSE FALSE FALSE FALSE FALSE
                                                        TRUE
                                                              TRUE FALSE
                                                                            TRUE
##
    [67]
          TRUE
                 TRUE
                       TRUE
                              TRUE
                                    TRUE FALSE
                                                 TRUE
                                                        TRUE FALSE
                                                                     TRUE
                                                                            TRUE
                 TRUE
                       TRUE
                              TRUE
                                    TRUE FALSE FALSE
                                                        TRUE
                                                              TRUE
                                                                     TRUE
##
    [78]
          TRUE
                                                                            TRUE
                              TRUE
##
    [89]
          TRUE
                 TRUE
                       TRUE
                                    TRUE
                                           TRUE
                                                  TRUE FALSE FALSE FALSE
                                                                            TRUE
                 TRUE FALSE FALSE
                                    TRUE
                                           TRUE
                                                                     TRUE
##
   [100]
          TRUE
                                                  TRUE FALSE
                                                              TRUE
                                                                            TRUE
##
   [111]
          TRUE
                 TRUE
                       TRUE
                              TRUE FALSE
                                           TRUE
                                                  TRUE
                                                        TRUE FALSE
                                                                     TRUE
                                                                            TRUE
##
   [122]
          TRUE
                 TRUE
                       TRUE
                              TRUE
                                    TRUE
                                           TRUE
                                                  TRUE
                                                        TRUE
                                                               TRUE
                                                                     TRUE
                                                                            TRUE
   [133]
          TRUE
                 TRUE
                       TRUE
                              TRUE
                                    TRUE
                                           TRUE
                                                  TRUE
                                                        TRUE
                                                               TRUE
                                                                     TRUE
                                                                            TRUE
##
                 TRUE
                       TRUE
                              TRUE
                                    TRUE
                                           TRUE FALSE
                                                        TRUE
                                                              TRUE
                                                                     TRUE
## [144]
          TRUE
```

## Omitting missing values

- The resulting logical can be used to remove incomplete records from the matrix/data.frame.
- Alternatively the na.omit function, does the same.

```
ind <- complete.cases(data)
newData <- data[ind,]
dim(data)

## [1] 153 6

dim(newData)

## [1] 111 6</pre>
```

# Handling missing values usin mice R package

```
library(mice)

## Loading required package: lattice

## ## Attaching package: 'mice'

## The following objects are masked from 'package:base':
## ## cbind, rbind

mice.obj <- mice(data, m=3, maxit=10, meth='pmm', seed=500)</pre>
```

```
##
##
    iter imp variable
##
           Ozone Solar.R
                   Solar.R
##
            0zone
##
     1
         3
            Ozone
                   Solar.R
##
     2
            Ozone
                   Solar.R
     2
         2
            Ozone Solar.R
##
     2
         3
##
            Ozone
                   Solar.R
     3
         1
                   Solar.R
##
            0zone
     3
         2
            Ozone Solar.R
##
         3
##
     3
            0zone
                   Solar.R
         1
                   Solar.R
##
            0zone
         2
##
     4
            0zone
                   Solar.R
##
         3
            Ozone
                  Solar.R
##
     5
         1
            Ozone
                   Solar.R
##
     5
         2
            Ozone
                  Solar.R
     5
         3
##
            Ozone
                   Solar.R
##
     6
         1
            0zone
                   Solar.R
         2
     6
                   Solar.R
##
            0zone
     6
         3
##
            0zone
                   Solar.R
     7
         1
                   Solar.R
##
            0zone
##
            0zone
                   Solar.R
     7
         3
##
            Ozone
                   Solar.R
     8
         1
            Ozone Solar.R
##
##
     8
         2
            Ozone Solar.R
     8
         3
                   Solar.R
##
            0zone
##
     9
         1
            Ozone
                   Solar.R
     9
         2
##
            Ozone Solar.R
         3
##
     9
            Ozone
                   Solar.R
     10
          1 Ozone
                   Solar.R
##
##
     10
          2 Ozone
                    Solar.R
##
     10
          3 Ozone Solar.R
newData <- complete(mice.obj)</pre>
dim(data)
## [1] 153
dim(newData)
## [1] 153
anyNA(data)
## [1] TRUE
anyNA(newData)
```

```
## [1] FALSE
```

For more information about imputation using `mice' package please see: https://datascienceplus.com/imputing-missing-data-with-r-mice-package/ (https://datascienceplus.com/imputing-missing-data-with-r-mice-package/)

# Handling missing values using caret R package

The caret package (short for Classification And REgression Training) contains functions to streamline the model training process for complex regression and classification problems.

Create the knn imputation model on the data:

```
library(caret)
## Loading required package: ggplot2
preProcess_missingdata_model <- preProcess(data, method='knnImpute')</pre>
preProcess_missingdata_model
## Created from 111 samples and 6 variables
##
## Pre-processing:
##
   - centered (6)
##
   - ignored (0)
    - 5 nearest neighbor imputation (6)
##
##
     - scaled (6)
# Use the imputation model to predict the values of missing data points
library(RANN) # required for knnInpute
newData <- predict(preProcess_missingdata_model, newdata = data)</pre>
anyNA(newData)
## [1] FALSE
dim(newData)
## [1] 153
             6
```

#### **Feature Selection**

Contains functions for the data analysis with the emphasis on biological data, including several algorithms for feature ranking, feature selection, classification algorithms with the embedded validation procedures.

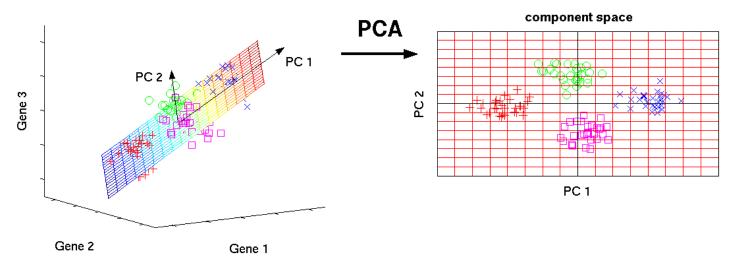
The functions can deal with numerical as well as with nominal features.

```
set.seed(7)
# load the library
library(mlbench)
library(Biocomb)
## Loading required package: gtools
## Loading required package: Rcpp
# Load the data
data(PimaIndiansDiabetes)
dim(PimaIndiansDiabetes)
## [1] 768
            9
head(PimaIndiansDiabetes)
##
    pregnant glucose pressure triceps insulin mass pedigree age diabetes
## 1
           6
                 148
                           72
                                   35
                                            0 33.6
                                                      0.627 50
## 2
           1
                  85
                           66
                                   29
                                            0 26.6
                                                     0.351 31
                                                                    neg
## 3
                 183
                           64
                                  0
                                            0 23.3
                                                     0.672 32
                                                                    pos
                                       94 28.1
              89
## 4
           1
                           66
                                   23
                                                     0.167 21
                                                                    neg
## 5
         0
                 137
                           40
                                   35
                                        168 43.1
                                                     2.288 33
                                                                    pos
                                            0 25.6
## 6
                 116
                           74
                                    0
                                                     0.201 30
                                                                    neg
cat("\n")
print("The selected features are:")
## [1] "The selected features are:"
select.cfs(PimaIndiansDiabetes)
          Biomarker Index
##
## glucose
            glucose
## mass
               mass
                        6
## age
                age
                        8
```

#### **Feature Extraction**

One of the well-known methods to extract features is Principal Component Analysis (PCA). \*\*\*

#### original data space

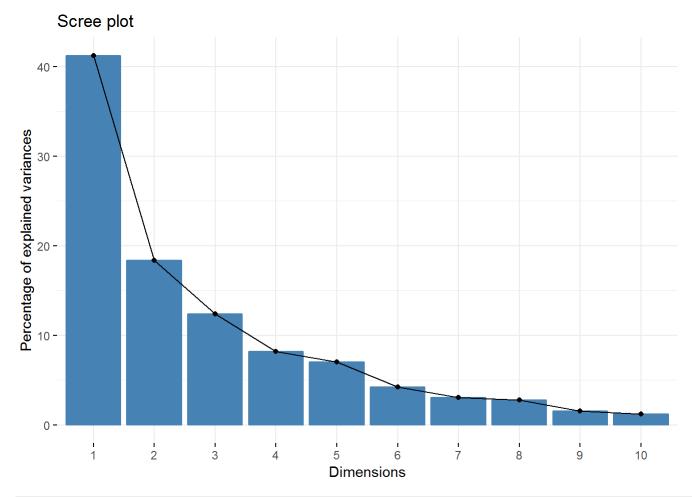


For more information please see: http://www.sthda.com/english/articles/31-principal-component-methods-in-r-practical-guide/118-principal-component-analysis-in-r-prcomp-vs-princomp/ (http://www.sthda.com/english/articles/31-principal-component-methods-in-r-practical-guide/118-principal-component-analysis-in-r-prcomp-vs-princomp/)

```
library("factoextra")
data(decathlon2)
decathlon2.active <- decathlon2[1:23, 1:10]
head(decathlon2.active[, 1:6])</pre>
```

##		X100m	Long.jump	Shot.put	High.jump	X400m	X110m.hurdle
##	SEBRLE	11.04	7.58	14.83	2.07	49.81	14.69
##	CLAY	10.76	7.40	14.26	1.86	49.37	14.05
##	BERNARD	11.02	7.23	14.25	1.92	48.93	14.99
##	YURKOV	11.34	7.09	15.19	2.10	50.42	15.31
##	ZSIVOCZKY	11.13	7.30	13.48	2.01	48.62	14.17
##	McMULLEN	10.83	7.31	13.76	2.13	49.91	14.38

```
res.pca <- prcomp(decathlon2.active, scale = TRUE)
fviz_eig(res.pca)</pre>
```



```
# Results for variables
res.var <- get_pca_var(res.pca)
head(res.var$coord)  # Coordinates</pre>
```

```
Dim.1
                              Dim.2
                                        Dim.3
                                                  Dim.4
##
                                                            Dim.5
## X100m
              -0.8506257
                         0.17939806 -0.3015564 0.03357320 -0.1944440
## Long.jump
               0.7941806 -0.28085695 0.1905465 -0.11538956 0.2331567
## Shot.put
               0.7339127 -0.08540412 -0.5175978 0.12846837 -0.2488129
## High.jump
               0.6100840 0.46521415 -0.3300852 0.14455012
                                                         0.4027002
## X400m
              -0.7016034 -0.29017826 -0.2835329 0.43082552
                                                        0.1039085
## X110m.hurdle -0.7641252 0.02474081 -0.4488873 -0.01689589 0.2242200
##
                    Dim.6
                                Dim.7
                                            Dim.8
                                                       Dim.9
## X100m
               0.035374780 -0.091336386 -0.104716925 -0.30306448
## Long.jump
              -0.033727883 -0.154330810 -0.397380703 -0.05158951
## Shot.put
              -0.239789034 -0.009886612 0.024359049 0.04778655
## High.jump
              ## X400m
              ## X110m.hurdle 0.002632395 -0.370072158 -0.008344682 0.16176025
##
                   Dim. 10
## X100m
               0.04441797
## Long.jump
               0.02971945
## Shot.put
               0.21745195
## High.jump
              -0.13356677
## X400m
              -0.03417067
## X110m.hurdle -0.01562991
```

head(res.var\$contrib) # Contributions to the PCs

```
##
                  Dim.1
                             Dim.2
                                      Dim.3
                                                 Dim.4
                                                           Dim.5
              17.544293 1.7505098 7.338659 0.13755240 5.389252
## X100m
## Long.jump 15.293168 4.2904162 2.930094 1.62485936 7.748815
## Shot.put
               13.060137 0.3967224 21.620432 2.01407269 8.824401
## High.jump
              9.024811 11.7715838 8.792888 2.54987951 23.115504
## X400m
               11.935544 4.5799296 6.487636 22.65090599 1.539012
## X110m.hurdle 14.157544 0.0332933 16.261261 0.03483735 7.166193
##
                     Dim.6
                                Dim.7
                                           Dim.8
                                                     Dim.9
                                                               Dim. 10
## X100m
              0.295915322 2.75705260 3.99520353 59.174001 1.6175614
## Long.jump
              0.269003613 7.87159392 57.53322220 1.714683 0.7241439
## Shot.put 13.596858744 0.03230371 0.21618512 1.471201 38.7676858
## High.jump
            19.159607001 0.26202607 2.59565787 8.101552 14.6264909
## X400m
               0.574509906 27.05274658 19.87344405 4.348967 0.9573050
## X110m.hurdle 0.001638634 45.26163460 0.02537025 16.857939 0.2002887
```

## Model Training and evaluation

The function createDataPartition can be used to create a stratified random sample of the data into training and test sets:

```
library(mlbench)
data(Sonar)
library(caret)
set.seed(998)
inTraining <- createDataPartition(Sonar$Class, p = .75, list = FALSE)
training <- Sonar[ inTraining,]
testing <- Sonar[-inTraining,]</pre>
```

Here, we train a random forest model and evaluate its performance using 5-fold cross-validation.

```
## Random Forest
##
## 157 samples
   60 predictor
##
##
   2 classes: 'M', 'R'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 126, 125, 125, 127, 125
## Resampling results across tuning parameters:
##
##
    mtry Accuracy
                      Kappa
##
     2
           0.8279704 0.6498436
##
    31
           0.7965188 0.5892971
##
     60
           0.7771505 0.5498401
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was mtry = 2.
```

```
print(rf_model$finalModel)
```

```
##
## Call:
   randomForest(x = x, y = y, mtry = param$mtry)
##
##
                  Type of random forest: classification
                        Number of trees: 500
##
## No. of variables tried at each split: 2
##
           OOB estimate of error rate: 15.29%
##
## Confusion matrix:
##
      M R class.error
## M 78 6 0.07142857
## R 18 55 0.24657534
```

Evaluating trained model on test data that is independent from training data.

```
# predict the outcome on a test data
rf_pred <- predict(rf_model, testing)
# compare predicted outcome and true outcome
confusionMatrix(rf_pred, testing[,'Class'])</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction M R
##
            M 26 5
            R 1 19
##
##
##
                  Accuracy : 0.8824
                    95% CI: (0.7613, 0.9556)
##
      No Information Rate : 0.5294
##
       P-Value [Acc > NIR] : 8.488e-08
##
##
##
                     Kappa : 0.7617
##
   Mcnemar's Test P-Value: 0.2207
##
##
               Sensitivity: 0.9630
               Specificity: 0.7917
##
##
            Pos Pred Value: 0.8387
            Neg Pred Value: 0.9500
##
                Prevalence: 0.5294
##
            Detection Rate: 0.5098
##
##
      Detection Prevalence: 0.6078
##
         Balanced Accuracy: 0.8773
##
##
          'Positive' Class : M
##
```

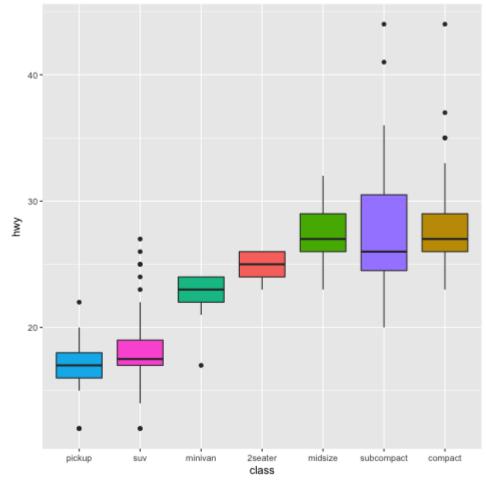
### If we still have time...

Let's talk about outliers.

### **Outliers**

A general definition:

- An outlier in a data set is an observation (or set of observations) which appear to be inconsistent with that set of data.
- Outliers do not equal errors. They should be detected, but not necessarily removed. Their inclusion in the analysis is a statistical decision.



Outliers in a sample box-plot

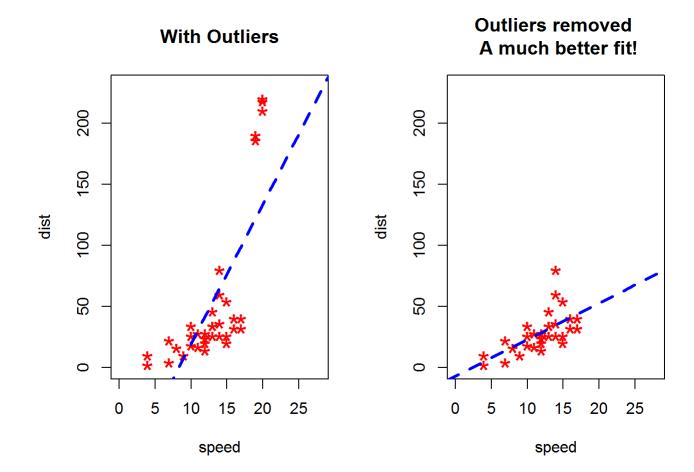
```
x <- c(1:10, 20, 30)
boxplot.stats(x)$out
```

## [1] 20 30

# Inject outliers into data

```
# Inject outliers into data.
cars1 <- cars[1:30, ] # original data
cars_outliers <- data.frame(speed=c(19,19,20,20,20), dist=c(190, 186, 210, 220, 218)) # introdu
ce outliers.
cars2 <- rbind(cars1, cars_outliers) # data with outliers.</pre>
```

See the ablines in these plots:



### Outlier detection

The ``outliers" package provides a number of useful functions to systematically extract outliers. One of these functions is outlier().

```
library(outliers)
set.seed(1234)
y <- rnorm(16)
print("Vector y is:")

## [1] "Vector y is:"

cat("\n")

y

## [1] -1.20706575 0.27742924 1.08444118 -2.34569770 0.42912469
## [6] 0.50605589 -0.57473996 -0.54663186 -0.56445200 -0.89003783
## [11] -0.47719270 -0.99838644 -0.77625389 0.06445882 0.95949406
## [16] -0.11028549
```

```
cat("\n")
print("The outlier in y is:")
## [1] "The outlier in y is:"
outlier(y)
## [1] -2.345698
cat("\n")
print("Removing the outlier from y:")
## [1] "Removing the outlier from y:"
rm.outlier(y)
## [1] -1.20706575 0.27742924 1.08444118 0.42912469 0.50605589
## [6] -0.57473996 -0.54663186 -0.56445200 -0.89003783 -0.47719270
## [11] -0.99838644 -0.77625389  0.06445882  0.95949406 -0.11028549
```