



# ENDURANCE LIMIT MODIFYING FACTORS

MET 4501

LEAH GINSBERG, PH.D.

## ROAD MAP FOR THE STRESS-LIFE METHOD – FULLY REVERSED SIMPLE LOADING

1. Determine  $S'_e$  either from test data or

$$S'_e = \begin{cases} 0.5 S_{ut} & S_{ut} \leq 200 \text{ kpsi (1400 MPa)} \\ 100 \text{ kpsi} & S_{ut} > 200 \text{ kpsi} \\ 700 \text{ MPa} & S_{ut} > 1400 \text{ MPa} \end{cases} \quad (6-10)$$

2. Modify  $S'_e$  to determine  $S_e$ .

$$S_e = k_a k_b k_c k_d k_e S'_e \quad (6-17)$$

- a. Surface factor,  $k_a$

$$k_a = a S_{ut}^b \quad (6-18)$$

**Table 6–2** Curve Fit Parameters for Surface Factor, Equation (6–18)

Surface Finish	Factor $a$		Exponent $b$
	$S_{ut}$ , kpsi	$S_{ut}$ , MPa	
Ground	1.21	1.38	–0.067
Machined or cold-drawn	2.00	3.04	–0.217
Hot-rolled	11.0	38.6	–0.650
As-forged	12.7	54.9	–0.758

## ROAD MAP FOR THE STRESS-LIFE METHOD – FULLY REVERSED SIMPLE LOADING

- b. Size factor,  $k_b$

**Rotating shaft.** For bending or torsion,

$$k_b = \begin{cases} (d/0.3)^{-0.107} = 0.879d^{-0.107} & 0.3 \leq d \leq 2 \text{ in} \\ 0.91d^{-0.157} & 2 < d \leq 10 \text{ in} \\ (d/7.62)^{-0.107} = 1.24d^{-0.107} & 7.62 \leq d \leq 51 \text{ mm} \\ 1.51d^{-0.157} & 51 < d \leq 254 \text{ mm} \end{cases} \quad (6-19)$$

For axial,

$$k_b = 1 \quad (6-20)$$

**Nonrotating member.** For bending, use Table 6-3 for  $d_e$  and substitute into Equation (6-19) for  $d$ .

- c. Load factor,  $k_c$

$$k_c = \begin{cases} 1 & \text{bending} \\ 0.85 & \text{axial} \\ 0.59 & \text{torsion} \end{cases} \quad (6-25)$$

## ROAD MAP FOR THE STRESS-LIFE METHOD – FULLY REVERSED SIMPLE LOADING

- b. Temperature factor,  $k_d$

$$\begin{aligned} S_T/S_{RT} &= 0.98 + 3.5(10^{-4})T_F - 6.3(10^{-7})T_F^2 \\ S_T/S_{RT} &= 0.99 + 5.9(10^{-4})T_C - 2.1(10^{-6})T_C^2 \end{aligned} \quad (6-26)$$

Either use the ultimate strength from Equation (6-26) to estimate  $S_e$  at the operating temperature, with  $k_d = 1$ , or use the known  $S_e$  at room temperature with  $k_d = S_T/S_{RT}$  from Equation (6-26).

- c. Reliability factor,  $k_e$

**Table 6-4** Reliability Factor  $k_e$  Corresponding to 8 Percent Standard Deviation of the Endurance Limit

Reliability, %	Transformation Variate $z_d$	Reliability Factor $k_e$
50	0	1.000
90	1.288	0.897
95	1.645	0.868
99	2.326	0.814
99.9	3.091	0.753
99.99	3.719	0.702

## ROAD MAP FOR THE STRESS-LIFE METHOD – FULLY REVERSED SIMPLE LOADING

3. Determine fatigue stress-concentration factor,  $K_f$  or  $K_{fs}$ .

[TO BE COVERED NEXT TIME]

4. Apply  $K_f$  to the nominal completely reversed stress,  $\sigma_a = K_f \sigma_{a0}$ .

[TO BE COVERED NEXT TIME]

5. Determine  $f$  from Figure 6-23 or Equation (6-11). For  $S_{ut}$  lower than the range, use  $f = 0.9$ .

$$\begin{aligned} f &= 1.06 - 2.8(10^{-3})S_{ut} + 6.9(10^{-6})S_{ut}^2 & 70 < S_{ut} < 200 \text{ kpsi} & (6-11) \\ f &= 1.06 - 4.1(10^{-4})S_{ut} + 1.5(10^{-7})S_{ut}^2 & 500 < S_{ut} < 1400 \text{ MPa} \end{aligned}$$

$$a = (f S_{ut})^2 / S_e \quad (6-13)$$

$$b = -[\log (f S_{ut} / S_e)] / 3 \quad (6-14)$$

6. Determine fatigue strength  $S_f$  at  $N$  cycles, or,  $N$  cycles to failure at a reversing stress  $\sigma_{ar}$ .

(Note: This only applies to purely reversing stresses where  $\sigma_m = 0$ .)

$$S_f = aN^b \quad (6-12)$$

$$N = (\sigma_{ar} / a)^{1/b} \quad (6-15)$$

# EXAMPLE PROBLEM

1080 HR steel bar

$$S_{ut} = 770 \text{ MPa} @ T_c = 20^\circ\text{C}$$

**Table A-20**

Deterministic ASTM Minimum Tensile and Yield Strengths for Some Hot-Rolled (HR) and Cold-Drawn (CD) Steels [The strengths listed are estimated ASTM minimum values in the size range 18 to 32 mm ( $\frac{3}{4}$  to  $1\frac{1}{4}$  in). These strengths are suitable for use with the design factor defined in Sec. 1–10, provided the materials conform to ASTM A6 or A568 requirements or are required in the purchase specifications. Remember that a numbering system is not a specification.] *Source:* 1986 SAE Handbook, p. 2.15.

1 UNS No.	2 SAE and/or AISI No.	3 Process- ing	4 Tensile Strength, MPa (kpsi)	5 Yield Strength, MPa (kpsi)	6 Elongation in 2 in, %	7 Reduction in Area, %	8 Brinell Hardness
G10060	1006	HR	300 (43)	170 (24)	30	55	86
		CD	330 (48)	280 (41)	20	45	95
G10100	1010	HR	320 (47)	180 (26)	28	50	95
		CD	370 (53)	300 (44)	20	40	105
G10150	1015	HR	340 (50)	190 (27.5)	28	50	101
		CD	390 (56)	320 (47)	18	40	111
G10180	1018	HR	400 (58)	220 (32)	25	50	116
		CD	440 (64)	370 (54)	15	40	126
G10200	1020	HR	380 (55)	210 (30)	25	50	111
		CD	470 (68)	390 (57)	15	40	131
G10300	1030	HR	470 (68)	260 (37.5)	20	42	137
		CD	520 (76)	440 (64)	12	35	149
G10350	1035	HR	500 (72)	270 (39.5)	18	40	143
		CD	550 (80)	460 (67)	12	35	163
G10400	1040	HR	520 (76)	290 (42)	18	40	149
		CD	590 (85)	490 (71)	12	35	170
G10450	1045	HR	570 (82)	310 (45)	16	40	163
		CD	630 (91)	530 (77)	12	35	179
G10500	1050	HR	620 (90)	340 (49.5)	15	35	179
		CD	690 (100)	580 (84)	10	30	197
G10600	1060	HR	680 (98)	370 (54)	12	30	201
G10800	1080	HR	770 (112)	420 (61.5)	10	25	229
G10950	1095	HR	830 (120)	460 (66)	10	25	248