Assignment Solutions | Time and space complexity analysis | Week 8

1.Calculate the time complexity for the following code snippet.

```
for(int i = 0; i < n; i++) {
for(int j = 0; j * j < n; j++) {
cout << “PhysicsWallah ”;
}
}
```

Solution :

O(n * sqrt(n))

2.Calculate the time complexity for the following code snippet.

```
int c = 0;
for(int i = 0; i < n; i++) {
for(int j = 1; j < n; j *= 2) {
c++;
}
}
```

Solution :

O(n log n) as the first loop ‘i’ will be iterated n times and the inner loop will only traverse logn times so in total the overall time complexity becomes O(nlogn).

3.Calculate the time complexity for the following code snippet.

```
int c = 0;
for(int i = 0; i < n; i++) {
for(int j = 1; j * j < n; j *= 2) {
c++;
}
}
```

Solution :

Let us analyze how many times the inner loop will iterate. Let us see the values of j for that.
J = 1, 2, 4, ... 2k
So 2^k * 2^k < n
So 2^(k+1) < n
So Time complexity becomes logN.

4.Calculate the time complexity for the following code snippet.

```
int c = 0;
for(int i = n; i > 0; i /= 2) {
for(int j = 0; j < i; j ++) {
```

```
c++;
}
}
```
Solution :

Here the inner loop will be traversed ‘i’ times so let us see the values of ‘i’ here.
Values of ‘i’ will be n, n/2, n/4, n/8 and so on
So the total number of iterations in the above nested loop will be n + n/2 + n/4 + n/8 + ..
Which sums to 2n
So time complexity becomes O(2n) ~ O(n)

5.Calculate the time complexity for the following code snippet.

```
int c = 0;
for(int i = 1; i < n; i*=2) {
for(int j = n; j > i; j--) {
c++;
}
}
```
Solution :

Lets us calculate the number of iterations in the above nested loop here, we get
Values of ‘i’ will be 1,2,4,8, 2^k
So the total number of iterations will be
(n-1) + (n-2) + (n-4) + .. + (n-2^k)
This sum becomes n*k - (1+2+4+ .. + 2^k)
Which becomes n*k - (2^(k+1))
Here k is number of terms which is O(logN)

Hence the overall time complexity becomes nlogn - n
~ O(nlogn)