

$$np = 400 \times 0.15 = 60 > 10$$

$$P(X \leq 42) \text{ binomial}$$

$$n(1-p) = 400 \times 0.85 = 340 > 10$$

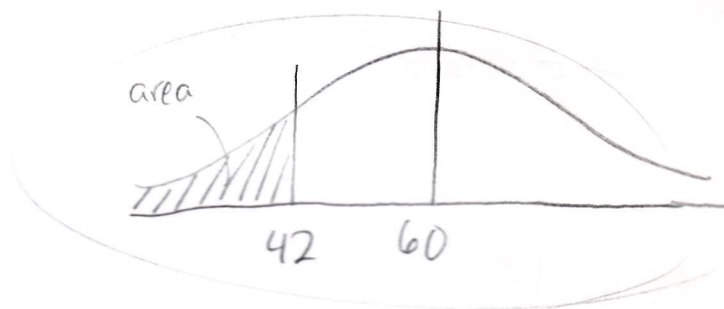
$$\mu = np = 60$$

$$\sigma = \sqrt{np(1-p)} = \sqrt{400 \times 0.15 \times 0.85} = 7.14$$

$$\text{Normal}(\mu=60, \sigma=7.14) \sim \star$$

$$P(X < 42) = 0.0059$$

$$Z = \frac{X - \mu}{\sigma} = \frac{42 - 60}{7.14} = -2.52$$



$$P(Z < -2.52) = 0.0059$$

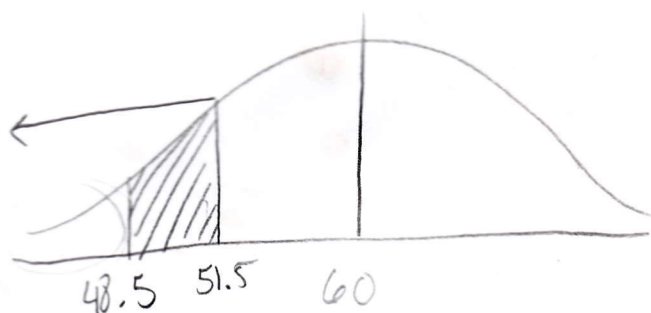
$$\text{True binomial probability} = 0.0054.$$

$$P(X = 49, 50, \text{ or } 51) = P(49 \leq X \leq 51) \text{ binomial}$$

$$\text{Normal}(\mu=60, \sigma=7.14)$$

$$P(49 - 0.5 < X < 51 + 0.5)$$

$$P(48.5 < X < 51.5)$$



$$Z_L = \frac{48.5 - 60}{7.14} = -1.61$$

$$Z_U = \frac{51.5 - 60}{7.14} = -1.19$$

$$P(X < 51.5) - P(X < 48.5)$$

$$P(Z < -1.19) - P(Z < -1.61)$$

$$= 0.1170 - 0.0537$$

$$= 0.0633$$