

1. (15 points) Groundhog's Day is celebrated every February 1 and inspired a classic Bill Murray film. A groundhog (named Punxsutawney Phil) emerges from his winter burrow and if he "sees his shadow", supposedly there will be six more weeks of winter. Using data from 1898 - 2016, we want to examine whether the weather in March is actually different (on average) in years when Phil sees his shadow. The following sample statistics describe the results:

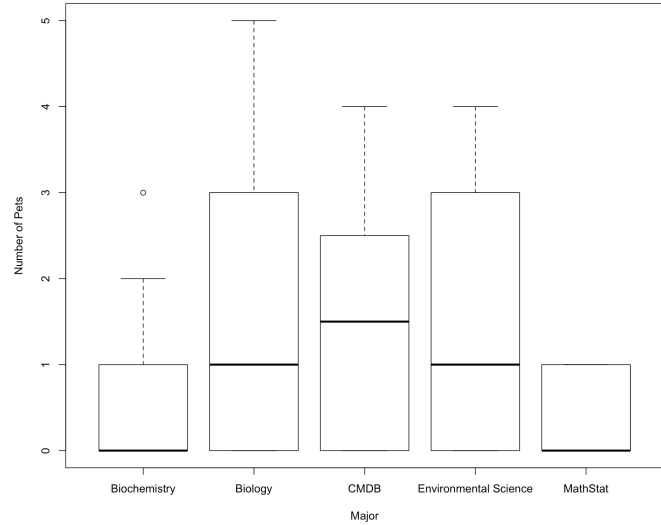
	n	Mean	Std Dev
Shadow	100	41.67°F	2.94
No Shadow	15	42.97°F	2.92

- (a) (10 points) Test at the $\alpha = 0.05$ level of significance if there is a difference in mean March temperature between years when Phil sees his shadow and years when Phil sees no shadow. Assume that any assumptions are satisfied.

- (b) (5 points) If we want to be able to detect a difference in temperature of 2°F (at the $\alpha = 0.05$ level), the power of this test is 65.33%. Explain what this means. How do we improve statistical power?

2. (15 points) After cleaning the start-of-term student survey data, the five most represented majors were biochemistry, biology, environmental science, mathematics/statistics, and CMDB. (Note: CMDB was not grouped with biology because it was so well represented!) We will examine whether a student's number of pets varies based on major. The following information may be useful:

Major	n	Mean	Std Dev
Biochem	17	0.7059	0.9852
Biology	38	1.4737	1.4656
CMDB	8	1.5000	1.5119
Enviro Sci	13	1.4615	1.4500
Math/Stats	15	0.4000	0.5071



- (a) (4 points) What are appropriate hypotheses for this test? You may use words or statistical notation.

- (b) (5 points) What are the ANOVA assumptions? Are they satisfied?

- (c) (2 points) Assume the ANOVA assumptions are satisfied. Use the following R output to test your hypotheses from part (a) at the $\alpha = 0.05$ level of significance.

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              Df Sum Sq Mean Sq F value Pr(>F)
survey$major    4  18.01   4.503    2.769 0.0323 *
Residuals      86 139.83   1.626
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Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

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- (d) (4 points) The following matrix gives the unadjusted p-values for comparisons for the differences in pets by major for the ANOVA in part (c). Use the Bonferonni approach to test which (if any) pairs differ significantly. Use $\alpha = 0.05$.

	Biochemistry	Biology	CMDB	Environmental Science
Biology	0.420	-	-	-
CMDB	0.150	0.958	-	-
Environmental Science	0.111	0.976	0.947	-
Math/Stat	0.500	0.007	0.052	0.031

3. (10 points) A random sample of 7 observations was selected from each of five populations (i.e., there are 7 observations in each of the five groups). A portion of the ANOVA table is shown below. Complete the missing entries.

Source	Degrees of Freedom	Sum of Squares	Mean Square	F
Group	_____	_____	370	_____
Error	_____	_____	_____	
Total	_____	1850		
