

X is random variable $\mu = 15$ $\sigma = 10$ $n = 100$

$n = 100 \geq 30 \rightarrow$ Central Limit Theorem.

\bar{X} will Normal($\mu, \sigma/\sqrt{n}$)

Normal($\mu_{\bar{x}} = 15, \sigma_{\bar{x}} = 10/\sqrt{100}$)

Normal($15, 1$)

How often should \bar{x} be within 2 units of $\mu = 15$?

$$15 \pm 2 \times 1$$

$\mu_{\bar{x}} \pm 2\sigma_{\bar{x}} \rightarrow$ empirical rule! 95% of observations
(\bar{x}) will fall within 2 std dev
of the mean!