$$h = -16 + 2$$
 (1) (6)

b)
$$V = h'$$

= -32t + 6

c)
$$0 = -32t + 6$$

 $t = \frac{6}{32}$

$$a = v' = -32$$

$$0 = 7t^{2} - 32t + 6$$

$$-\frac{5 \pm \sqrt{b^{2} - 4ac}}{2a} = \frac{32 \pm \sqrt{32^{2} - 4 \times 7 \times 6}}{2(7)}$$

$$\frac{-6 \pm \sqrt{6^2 - 4 \times (-16) \times 66}}{2(-16)} \rightarrow t = -1.752, t = 2.227$$

Must touch pool bottom after surface of water - use
$$t=4.376$$

At $t=4.376$, $h=-214.134$ so 214.13 feet deep!

2.
$$f(x) = \frac{1}{\chi^{2}+2}$$

$$f'(x) = \lim_{\Delta x \to 0} \frac{f(x+\Delta x) - f(x)}{\Delta x}$$

$$= \lim_{\Delta x \to 0} \frac{1}{(x^{2}+\Delta x)^{2}+2} - \frac{1}{\chi^{2}+2}$$

$$= \lim_{\Delta x \to 0} \frac{1}{(x^{2}+\Delta x)^{2}+2} - \frac{1}{\chi^{2}+2}$$

$$= \lim_{\Delta x \to 0} \frac{(x^2 + 2) - [(x + \Delta x)^2 + 2]}{\Delta x (x^2 + 2) [(x + \Delta x)^2 + 2]}$$

$$= \lim_{\Delta x \to 0} \frac{x^2 + 2 - (x^2 + 2x\Delta x + (\Delta x)^2 + 2)}{\Delta x (x^2 + 2)(x^2 + 2x\Delta x + (\Delta x)^2 + 2)}$$

$$= \lim_{\Delta x \to 0} \frac{-2x\Delta x - (\Delta x)^2}{\Delta x (x^2 + 2)(x^2 + 2x\Delta x + (\Delta x)^2 + 2)}$$

=
$$\lim_{\Delta x \to 0} \frac{-2x - (\Delta x)^2}{(x^2 + 2)(x^2 + 2x\Delta x + (\Delta x)^2 + 2)}$$

$$= \frac{\lim_{\Delta x \to 0} \left[-2x - (\Delta x)^2 \right]}{\lim_{\Delta x \to 0} \left[(x^2 + 2)(x^2 + 2x\Delta x + (\Delta x)^2 + 2) \right]}$$

$$= \frac{\lim_{\Delta x \to 0} \left[-2x - (\Delta x)^2 \right]}{\lim_{\Delta x \to 0} \left[x^2 + 2 \right] \lim_{\Delta x \to 0} \left[x^2 + 2x \Delta x + (\Delta x)^2 + 2 \right]}$$

$$= \frac{-2x}{(x^2+2)(x^2+2)}$$

$$= \frac{-2x}{(x^2+2)^2}$$

3.
$$h(x) = \frac{(x^{2}+1)(\sqrt{3}x-2)}{x^{2}+2}$$

$$h'(x) = \frac{(x^{3}+2)}{dx} \frac{d}{dx} [(x^{2}+1)\sqrt{3}x-2] - (x^{2}+1)\sqrt{3}x-2 \frac{d}{dx} [(x^{3}+2)]}{(x^{3}+2)^{2}}$$
Then
$$\frac{d}{dx} [x^{3}+2] = 3x^{2} + 0 = 3x^{2}$$
And
$$\frac{d}{dx} [(x^{2}+1)\sqrt{3}x-2] = (x^{2}+1) \frac{d}{dx} [(3x-2)^{1/2}] + (3x-2) \frac{d}{dx} [x^{2}+1]$$

$$= (x^{2}+1) \left[\frac{1}{2} (3x-2) (3) \right] + (3x-2) \frac{d}{dx} [x^{2}+1]$$

$$= \frac{3(x^{2}+1)}{2(3x-2)^{1/2}} + \frac{2x(3x-2)^{1/2}}{2(3x-2)^{1/2}}$$

$$= \frac{3(x^{2}+1)}{2(3x-2)^{1/2}} + \frac{4x(3x-2)^{1/2}}{2(3x-2)^{1/2}}$$

$$= \frac{3(x^{2}+1)}{2\sqrt{3}x-2}$$

$$= \frac{3x^{2}+3+12x^{2}-8x}{2\sqrt{3}x-2}$$

$$= \frac{15x^{2}-8x+3}{2\sqrt{3}x-2}$$

Then
$$h'(x) = (x^3+2)\left(\frac{15x^2-8x+3}{2\sqrt{3}x-2}\right) - (x^2+1)\sqrt{3}x-2^{-1}(3x^2)$$

$$(x^3+2)^2$$

 $h'(x) = \frac{(x^3+2)(15x^2-8x+3) - (x^2+1)(3x-2)^{1/2}(3x^2)[2(3x-2)^{1/2}]}{2(3x-2)^{1/2}(x^3+2)^2}$ $= \frac{(x^3+2)(15x^2-8x+3) - (6x^2(x^2+1)(3x-2))}{2(x^3+2)^2\sqrt{3}x-2}$