## **Computer Exercise 8.2.10**

The following program will determine the singular value decomposition of two different matrices such that  $\mathbf{A} = \mathbf{U}\mathbf{D}\mathbf{V}^T$ ; the built-in MATLAB function 'svd' will be used to accoplish this. The outputted matrices  $\mathbf{U}, \mathbf{D}$ , and  $\mathbf{V}$  will be used to check that  $\mathbf{U}\mathbf{D}\mathbf{V}^T$  returns  $\mathbf{A}$ .

$$\mathbf{a)} \ \mathbf{A} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \\ 1 & 0 \end{bmatrix}$$

```
A = [1, 1; 0, 1; 1, 0];
[U, D, V] = svd(A);
A
```

```
A = 3 \times 2

1 1

0 1
1 0
```

```
%round function is used
%because 'negative zeros' were
%being displayed; also the default
%(floating point) output is messy
round(U*D*V')
```

ans = 
$$3 \times 2$$

1 1
0 1
1 0

**b)** 
$$\mathbf{A} = \begin{bmatrix} 1 & 3 & -2 \\ 2 & 7 & 5 \\ -2 & -3 & 4 \\ 5 & -3 & -2 \end{bmatrix}$$

1

## round(U\*D\*V')

ans = 
$$4 \times 3$$

1 3 -2

2 7 5

-2 -3 4

5 -3 -2

In both parts  $\boldsymbol{a}$  and  $\boldsymbol{b}$ , we see that  $\mathbf{U}\mathbf{D}\mathbf{V}^T$  returns  $\mathbf{A}$ .