

Exam 3 Review

P vs. NP : definitions

P
NP
NP-hard
NP-complete

examples

given a problem,
which does it fall into?

Reductions

2D dynamic programming

hint: make sure you understand 1D dynamic programming

① English subproblem def.

"Let $\text{MaxFoo}(i, j)$ be ..."

What subproblem gives final answer?
what vals of i, j ?

② Recursive subproblem def.

$$\text{MaxFoo}(i, j) = \begin{cases} \text{base cases} & \leftarrow \\ & \text{recursive case} \leftarrow \\ & \text{MaxFoo}(i, j+1) \\ & \text{MaxFoo}(i-1, j+1) \end{cases}$$

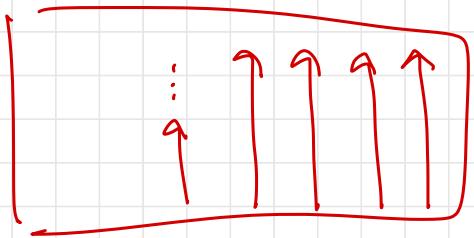
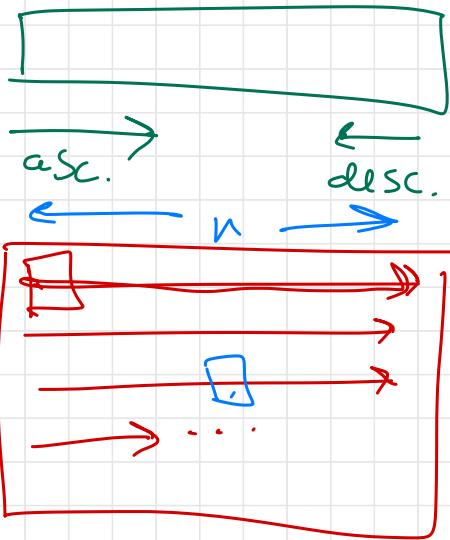
What are choices to be made at (i, j) ?
How to encode recursively (by calling MaxFoo)?

③ Memoization structure (2D array) and how to fill

"fill row by row, rows in a ascending order, columns in a ascending order"

Max Foo (m, n)

what do I need to have computed already in order to compute $A[i, j]$?



④ write iterative alg for loops filling an array returning correct array element YOU SHOULD NOT HAVE TO THINK!

Edit Distance

given two strings $A[1..m]$ and $B[1..n]$, what is the min. # of letter insertions, letter deletions, and letter substitutions to transform A into B.

$A = \text{CAT}$

$B = \text{CASE}$

CAT

CAST

insertion

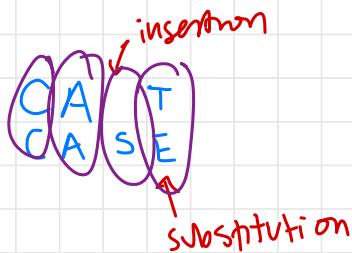
CASE

substitution

CASE

2

$$\text{edit}(\text{CAT}, \text{CASE}) = 2$$



$$\text{edit}(\text{FOOD}, \text{MONEY}) = 4$$

FOOD
MONEY
↑ ↑ ↑ ↑

If we have already aligned prefixes $A[1..i]$ and $B[1..j]$ optimally, we only need to align the remaining parts of A and B optimally.

① Let $\text{Edit}(i, j)$ be the edit distance between $A[1..i]$ and $B[1..j]$.

What is our final answer?

$\text{Edit}(m, n) = \text{edit dist b/w } A[1..m] \text{ and } B[1..n]$

②

$$\text{Edit}(i, j) = \left\{ \begin{array}{l} \dots \end{array} \right.$$

What choices do I need to make at (i, j) ?

align $A[1..i]$ with $B[1..j]$.

- insertion

$$\underline{\text{Edit}(i, j-1)} + 1$$

- deletion

$$\text{Edit}(i-1, j) + 1$$

- substitution

$$\begin{array}{c} A[i] \\ \rightarrow \\ \begin{matrix} X & * \\ * & Y \end{matrix} \end{array} \quad \text{Edit}(i, j) = \text{Edit}(i-1, j-1) + (A[\Sigma i] \neq A[\Sigma j])$$