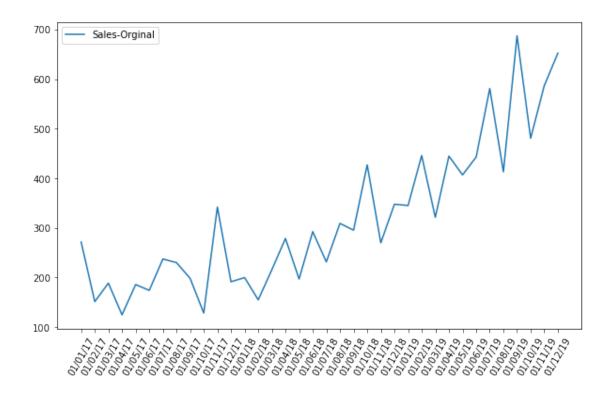
## chap8-signal\_time\_Processing

June 22, 2022

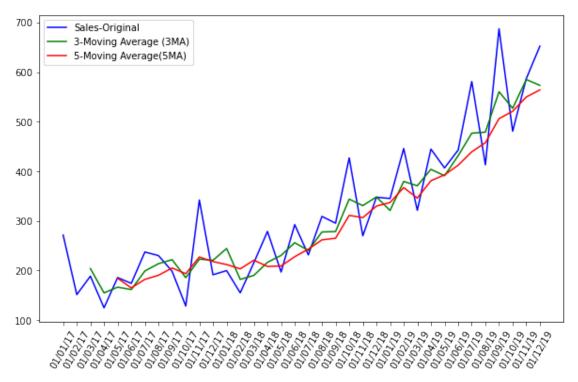
```
[3]: ## moving averages
     # import needful libs
     import pandas as pd
     import statsmodels.api as sm
     import matplotlib.pyplot as plt
     # read dataset
     sales_data = pd.read_csv('sales.csv')
     # setting figure size
     plt.figure(figsize=(10,6))
     # plot orginal sales data
     plt.plot(sales_data['Time'], sales_data['Sales'],
              label = "Sales-Orginal")
     # rotate xlabels
     plt.xticks(rotation=60)
     # add legends
     plt.legend()
     # display the plot
     plt.show()
```



```
[4]: # moving average with window 3
     sales_data['3MA'] = sales_data['Sales'].rolling(window=3).mean()
     # moving average with window 5
     sales_data['5MA'] = sales_data['Sales'].rolling(window=5).mean()
     # setting figure size
     plt.figure(figsize=(10,6))
     # plot orginal sales data
     plt.plot(sales_data['Time'], sales_data['Sales'],
             label="Sales-Original", color="blue")
     # plot 3-Moving Average of sales data
     plt.plot(sales_data['Time'], sales_data['3MA'],
              label="3-Moving Average (3MA)", color="green")
     # plot 5-Moving Average of sales data
     plt.plot(sales_data['Time'], sales_data['5MA'],
             label="5-Moving Average(5MA)", color="red")
     # rotate xlabels
     plt.xticks(rotation=60)
```

```
# add legends
plt.legend()

# display the plot
plt.show()
```



```
# window functions

# import needful libraries - loaded in first command
#import pandas as pd
#import statsmodels.api as sm
#import matplotlib.pyplot as plt

# read dataset
sales_data = pd.read_csv('sales.csv', index_col="Time")

# apply all the windows on given DataFrame
sales_data['boxcar'] = sales_data.Sales.rolling(3, win_type='boxcar').mean()
sales_data['triang'] = sales_data.Sales.rolling(3, win_type='triang').mean()
sales_data['hamming'] = sales_data.Sales.rolling(3, win_type='hamming').mean()
sales_data['blackman'] = sales_data.Sales.rolling(3, win_type='blackman').mean()
# plot the rolling mean of all the windows
```

```
sales_data.plot(kind='line', figsize=(10,6))
```

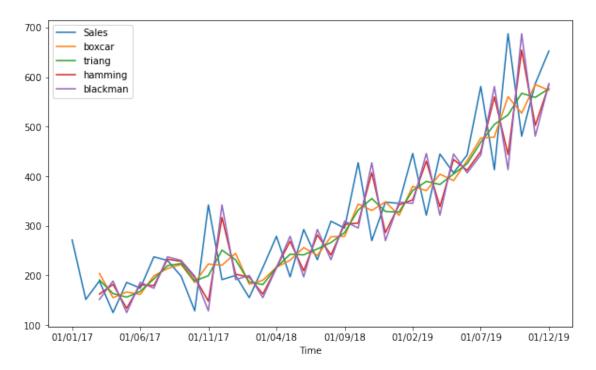
## [6]: <AxesSubplot:xlabel='Time'>

[9]: # create Sine wave and apply ADF test

sine = np.sin(np.sin(t))

t = np.linspace(-2 \* np.pi, 2 \* np.pi, N)

print("Self ADF", calc\_adf(sine, sine))



```
# defining cointegration

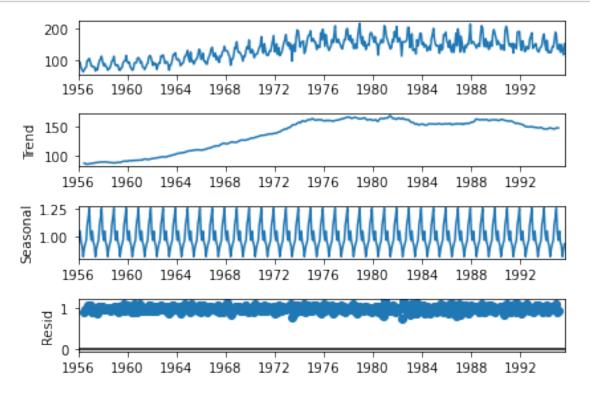
# import required libs
import pandas as pd
import statsmodels.api as sm
import statsmodels.tsa.stattools as ts
import numpy as np

# calculate ADF function
def calc_adf(x, y):
    result = sm.OLS(x, y).fit()
    return ts.adfuller(result.resid)

# read the Dataset
data = sm.datasets.sunspots.load_pandas().data.values
N = len(data)
```

```
Self ADF (3.956319476495162e-16, 0.958532086060056, 0, 308, {'1%':
     -3.45176116018037, 5\%': -2.870970093607691, 10\%': -2.571794416006072,
     -21598.896016765088)
[10]: # apply ADF test on Sine and Sine with noise
     noise = np.random.normal(0, .01, N)
      print("ADF sine with noise", calc_adf(sine, sine + noise))
     ADF sine with noise (-17.62552157029604, 3.8203908287165654e-30, 0, 308, {'1%':}
     -3.45176116018037, '5\%': -2.870970093607691, '10\%': -2.571794416006072},
     -1855.506811043978)
[11]: # apply ADF test on Sine and Cosine with noise
      cosine = 100 * np.cos(t) + 10
      print("ADF sine vs cosine with noise", calc_adf(sine, cosine + noise))
     ADF sine vs cosine with noise (-6.374451613018041, 2.302155686948863e-08, 16,
     292, {'1%': -3.4529449243622383, '5%': -2.871489553425686, '10%':
     -2.572071437887033}, -10037.933932666414)
[12]: | print("Sine vs sunspots", calc_adf(sine, data))
     Sine vs sunspots (-6.7242691810701, 3.4210811915549524e-09, 16, 292, {'1%':
     -3.4529449243622383, '5\%': -2.871489553425686, '10\%': -2.572071437887033},
     -1102.5867415291168)
 [1]: # STL decomposition
      # import needful libraries
      import pandas as pd
      import matplotlib.pyplot as plt
      from statsmodels.tsa.seasonal import seasonal_decompose
      # read the data dataset
      data = pd.read_csv('beer_production.csv')
      data.columns = ['date', 'data']
      # change datatype to pandas datetime
      data['date'] = pd.to_datetime(data['date'])
      data = data.set_index('date')
      # decompose the data
      decomposed_data = seasonal_decompose(data, model='multiplicative')
      # plot decomposed data
      decomposed_data.plot()
```

```
# display the plot
plt.show()
```



```
# autocorrelation
# import needful libraries
import pandas as pd
import numpy as np
import statsmodels.api as sm
import matplotlib.pyplot as plt

# read the dataset
data = sm.datasets.sunspots.load_pandas().data

# calculate autocorrelation using numpy
dy = data.SUNACTIVITY - np.mean(data.SUNACTIVITY)
dy_square = np.sum(dy ** 2)

# cross-correlation
sun_correlated = np.correlate(dy, dy, mode='full') / dy_square
result = sun_correlated[int(len(sun_correlated)/2):]

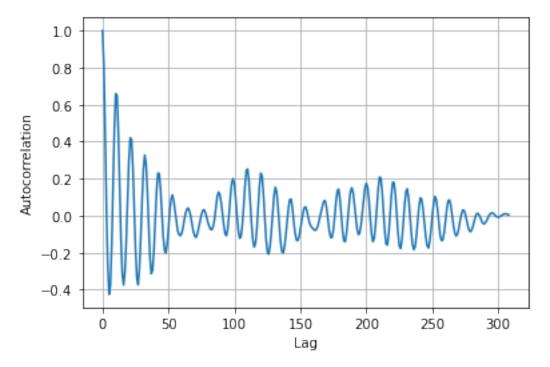
# display the chart
```

```
plt.plot(result)

# display grid
plt.grid(True)

# add labels
plt.xlabel("Lag")
plt.ylabel("Autocorrelation")

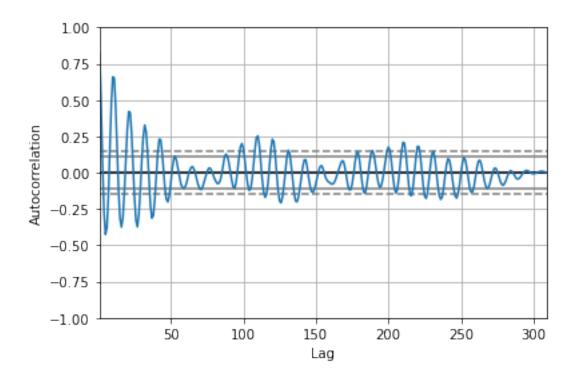
# display the chart
plt.show()
```



```
[5]: from pandas.plotting import autocorrelation_plot

# plot using pandas function
autocorrelation_plot(data.SUNACTIVITY)
```

[5]: <AxesSubplot:xlabel='Lag', ylabel='Autocorrelation'>



```
[17]: # autoregressive models
      # import needful libs
      \# library change from from statsmodels.tsa.ar_model import AR
      from statsmodels.tsa.ar_model import AutoReg
      from sklearn.metrics import mean_absolute_error
      from sklearn.metrics import mean_squared_error
      import matplotlib.pyplot as plt
      import statsmodels.api as sm
      from math import sqrt
      # read the dataset
      data = sm.datasets.sunspots.load_pandas().data
      # split data into train and test set
      train_ratio = 0.8
      train = data[:int(train_ratio*len(data))]
      test = data[int(train_ratio*len(data)):]
      # autoregression Model training
      ar_model = AutoReg(train.SUNACTIVITY, 20)
      ar_model = ar_model.fit()
```

```
# print lags and model coefficients
      print("Number of Lars: ", ar_model.summary)
      print("Model Coefficients:\n", ar_model.params)
     Number of Lars: <bound method AutoRegResults.summary of
     <statsmodels.tsa.ar_model.AutoRegResults object at 0x000002046E41F220>>
     Model Coefficients:
      const
                         12.189240
     SUNACTIVITY.L1
                         1.193347
                        -0.487991
     SUNACTIVITY.L2
     SUNACTIVITY.L3
                        -0.132572
     SUNACTIVITY.L4
                         0.200282
     SUNACTIVITY.L5
                        -0.189088
     SUNACTIVITY.L6
                         0.063540
     SUNACTIVITY.L7
                        -0.027693
     SUNACTIVITY.L8
                         0.099539
     SUNACTIVITY.L9
                         0.147040
     SUNACTIVITY.L10
                        -0.104183
     SUNACTIVITY.L11
                         0.197207
     SUNACTIVITY.L12
                        -0.075315
     SUNACTIVITY.L13
                        -0.135734
     SUNACTIVITY.L14
                         0.181400
     SUNACTIVITY.L15
                        -0.108997
     SUNACTIVITY.L16
                         0.002903
     SUNACTIVITY.L17
                         0.099517
     SUNACTIVITY.L18
                        -0.205439
     SUNACTIVITY.L19
                         0.042356
     SUNACTIVITY.L20
                        -0.023225
     dtype: float64
[19]: # make predictions
      start_point = len(train)
      end_point = start_point + len(test) - 1
      pred = ar_model.predict(start=start_point, end=end_point, dynamic=False)
      # calculate errors
      mae = mean_absolute_error(test.SUNACTIVITY, pred)
      mse = mean_squared_error(test.SUNACTIVITY, pred)
      rmse = sqrt(mse)
      print("MAE: ", mae)
      print("MSE: ", mse)
      print("RMSE: ", rmse)
     MAE: 36.36004069801688
```

MSE: 2416.2348267095017 RMSE: 49.15521159256159

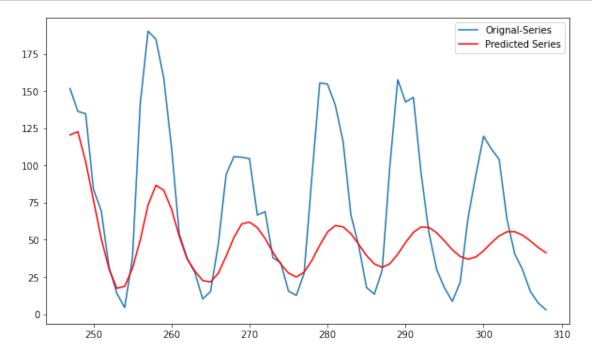
```
[20]: # setting figure size
plt.figure(figsize=(10, 6))

# plot test data
plt.plot(test.SUNACTIVITY, label='Orignal-Series')

# plot predictions
plt.plot(pred, color='red', label='Predicted Series')

# add legends
plt.legend()

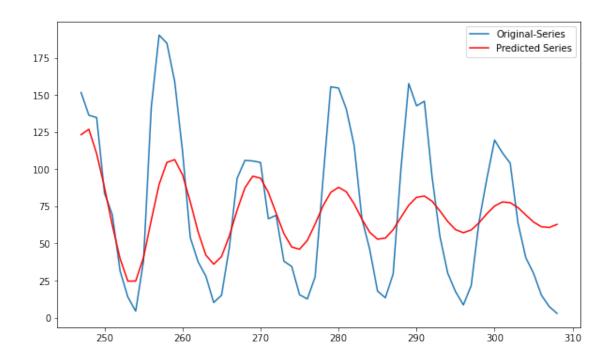
# display the plot
plt.show()
```



```
[35]: # ARMA models

# import needful libraries
import statsmodels.api as sm
# removed: from statsmodels.tsa.arima_model import ARIMA
# replaced on:
from statsmodels.tsa.api import ARIMA
from sklearn.metrics import mean_absolute_error
from sklearn.metrics import mean_squared_error
import matplotlib.pyplot as plt
```

```
from math import sqrt
      # read the dataset
      data = sm.datasets.sunspots.load_pandas().data
      data.drop('YEAR', axis=1, inplace=True)
      # split data into train and test set
      train_ratio = 0.8
      train = data[:int(train_ratio*len(data))]
      test = data[int(train_ratio*len(data)):]
      # AutoRegression Model training
      arma_model = ARIMA(train, order=(7,1,2))
      arma_model = arma_model.fit()
      # make predictions
      start_point = len(train)
      end_point = start_point + len(test) - 1
      pred = arma_model.predict(start_point, end_point)
      # calculate errors
      mae = mean_absolute_error(test.SUNACTIVITY, pred)
      mse = mean_squared_error(test.SUNACTIVITY, pred)
      rmse = sqrt(mse)
      print("MAE: ", mae)
      print("MSE: ", mse)
      print("EMSE: ", rmse)
     MAE: 31.27864467599967
     MSE: 1482.6106300479853
     EMSE: 38.50468322227811
[36]: # setting figure size
      plt.figure(figsize=(10,6))
      # plot test data
      plt.plot(test, label='Original-Series')
      # plot predictions
      plt.plot(pred, color='red', label='Predicted Series')
      # add legends
      plt.legend()
      # display the plot
      plt.show()
```



```
[38]: # generating periodic signals
      # import required libs
      import numpy as np
      import statsmodels.api as sm
      from scipy.optimize import leastsq
      import matplotlib.pyplot as plt
      # create model function
      def model(p, t):
          C, p1, f1, phi1, p2, f2, phi2, p3, f3, phi3 = p
          return C + p1 * np.sin(f1 * t + phi1) + p2 * np.<math>sin(f2 * t + phi2) + p3 *_{\sqcup}
       \rightarrownp.sin(f3 * t + phi3)
      # create error function
      def error(p, y, t):
          return y - model(p,t)
      # create fit function
      def fit(y, t):
          p0 = [y.mean(), 0, 2 * np.pi/11, 0, 0, 2 * np.pi/22, 0, 0, 2 * np.pi/100, 0]
          params = leastsq(error, p0, args = (y, t))[0]
          return params
      # load the dataset
```

```
data_loader = sm.datasets.sunspots.load_pandas()
sunspots = data_loader.data["SUNACTIVITY"].values
years = data_loader.data["YEAR"].values

# apply and fit the model
cutoff = int(.9 * len(sunspots))
params = fit(sunspots[:cutoff], years[:cutoff])
print("Params", params)

pred = model(params, years[cutoff:])
actual = sunspots[cutoff:]
```

Params [ 47.18800335 28.89947427 0.56827284 6.51168781 4.55215008 0.29372074 -14.30920341 -18.16523992 0.06574835 -4.37789699]

```
print("Params", params)
print("Root mean square error", np.sqrt(np.mean(actual - pred) **2))
print("Mean absolute error", np.mean(np.abs(actual - pred)))
print("Mean absolute percentage error", 100 * np.mean(np.abs(actual - pred)/
actual))
mid = (actual + pred) / 2
print("Symmetric Mean absolute percentage error", 100 * np.mean(np.abs(actual -
pred)/mid))
print("Coefficient of determination", 1 - ((actual - pred) ** 2). sum() /
a((actual - actual.mean()) ** 2).sum())
```

Params [ 47.18800335 28.89947427 0.56827284 6.51168781 4.55215008 0.29372074 -14.30920341 -18.16523992 0.06574835 -4.37789699]

Root mean square error 35.83089088049339

Mean absolute error 44.581468315714496

Mean absolute percentage error 65.16404904506578

Symmetric Mean absolute percentage error 78.44776724314043

Coefficient of determination -0.36352579271706853

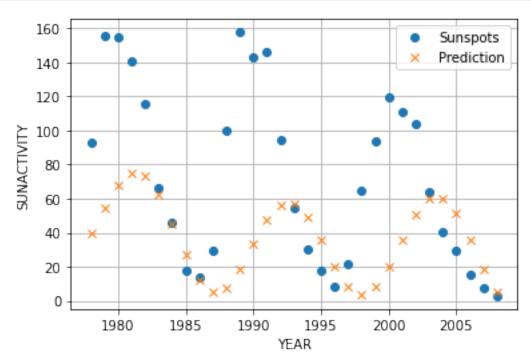
```
[42]: year_range = data_loader.data["YEAR"].values[cutoff:]

# plot the actual and predicted data points
plt.plot(year_range, actual, 'o', label="Sunspots")
plt.plot(year_range, pred, 'x', label="Prediction")
plt.grid(True)

# Add labels
plt.xlabel("YEAR")
plt.ylabel("SUNACTIVITY")

# add legend
plt.legend()
```

```
# display the chart
plt.show()
```



```
[5]: # fourier analysis
     # import required library
     import numpy as np
     import statsmodels.api as sm
     import matplotlib.pyplot as plt
     from scipy.fftpack import rfft
     from scipy.fftpack import fftshift
     # read the dataset
     data = sm.datasets.sunspots.load_pandas().data
     # create Sine wave
     t = np.linspace(-2 * np.pi, 2 * np.pi, len(data.SUNACTIVITY.values))
     mid = np.ptp(data.SUNACTIVITY.values) / 2
     sine = mid + mid * np.sin(np.sin(t))
     # compute FFT for Sine wave
     sine_fft = np.abs(fftshift(rfft(sine)))
     print("Index of max sine FFT", np.argsort(sine_fft)[-5:])
```

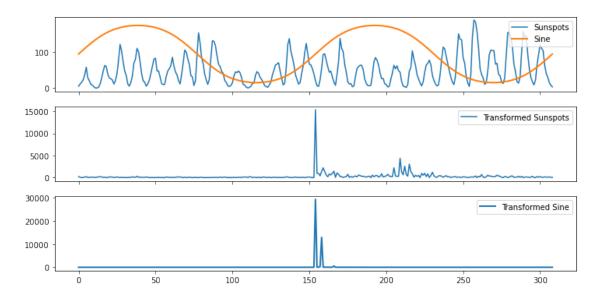
```
# compute FFT for sunsports dataset
transformed = np.abs(fftshift(rfft(data.SUNACTIVITY.values)))
print("Indices of max sunspots FFT", np.argsort(transformed)[-5:])

# create subplots
fig, axs = plt.subplots(3, figsize=(12, 6), sharex=True)
fig.suptitle('Power Spectrum')
axs[0].plot(data.SUNACTIVITY.values, label="Sunspots")
axs[0].plot(sine, lw=2, label="Sine")
axs[0].legend() # set legends
axs[1].plot(transformed, label="Transformed Sunspots")
axs[1].legend() # set legends
axs[2].plot(sine_fft, lw=2, label="Transformed Sine")
axs[2].legend() # set legends

# display the chart
plt.show()
```

Index of max sine FFT [160 157 166 158 154]
Indices of max sunspots FFT [205 212 215 209 154]

Power Spectrum

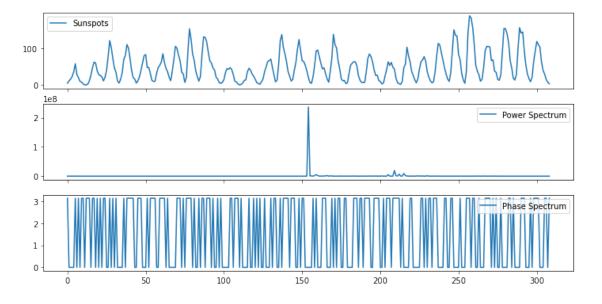


```
[6]: # spectral analysis filtering

# import required library
import numpy as np
import statsmodels.api as sm
```

```
from scipy.fftpack import rfft
from scipy.fftpack import fftshift
import matplotlib.pyplot as plt
# read the dataset
data = sm.datasets.sunspots.load_pandas().data
# compute FFT
transformed = fftshift(rfft(data.SUNACTIVITY.values))
# compute Power Spectrum
power = transformed ** 2
# compute Phase
phase = np.angle(transformed)
# create subplots
fig, axs = plt.subplots(3, figsize=(12,6), sharex=True)
fig.suptitle('Power Spectrum')
axs[0].plot(data.SUNACTIVITY.values, label="Sunspots")
axs[0].legend() # set legends
axs[1].plot(power, label="Power Spectrum")
axs[1].legend() # set legends
axs[2].plot(phase, label="Phase Spectrum")
axs[2].legend() # set legends
# display the chart
plt.show()
```

Power Spectrum



[]:[