SHPECK - A Geochemical Speciation Modeling Software

Leonardo Hax Damiani^{a,*}, Marcos Antonio Klunk^b, Mara Abel^a, Anthony Jung Park^c, Carla Dal Sasso Freitas^a

^aInformatics Institute, UFRGS, Porto Alegre, RS, Brazil
^bInstitute of Geoscience, UFRGS, Porto Alegre, RS, Brazil
^cSienna Geodynamics and Consulting, Inc., 101 Kirkwood Avenue, Suite 222, Bloomington, Indiana 47404

Abstract

Geochemical speciation modeling software are used for calculating the distribution of dissolved solute and complex compound species between solutes and aqueous complexes, and also to compute saturation indices of minerals. In this work we introduce SHPECK, a software program developed to model geochemical speciation using the mass-balance conditions and the phase rule [Garrels and Christ 1965]. SHPECK can be used to model the chemical equilibrium interaction between elements and solutes. It provides an interactive and intuitive user interface, as well as the support of a relational database structure that handles the management of thermodynamic and material properties data used for the geochemical modeling. We present a thorough computer science based review about the available geochemical modeling software (only programs that provide speciation modeling), expressing relevant particularities as: input and output options; user interaction; file formats; and software environment and installation procedure. The software SHPECK is validated by modeling the diagenetic reactions observed in a siliciclastic geological system, and by performing a comparative study with other modeling software package. In addition to this, a database comparison was addressed and the results demonstrate a substantial improvement on the performance by the use of the SHPECK's relational database comparing to the existent approaches.

Keywords: Geochemical modeling, Chemical Equilibrium, Geochemistry, Multiphase System, Law of Mass-Action, Nonlinear simulation, Software Engineering, Computational simulation,

1. Introduction

Geochemical speciation modeling describes the process of simulating chemical reactions that occur between the water (solvent) and chemical elements. The motivation of this

^{*}Corresponding author

Email addresses: lhdamiani@inf.ufrgs.br (Leonardo Hax Damiani), marcos.klunk@ufrgs.br (Marcos Antonio Klunk), mara@inf.ufrgs.br (Mara Abel), ajpark@sienna-geo.com (Anthony Jung Park), carla@inf.ufrgs.br (Carla Dal Sasso Freitas)

URL: http://www.inf.ufrgs.br/~lhdamiani (Leonardo Hax Damiani)

study is to provide a better understanding of the diagenesis process of sediments during the burial process, especially the water-mineral chemical interaction. Applications of geochemical models are essential in several environmental problems, such as calculating compositions of natural ground or surface waters, and precipitation and/or dissolution of minerals. A geochemical speciation modeling software is responsible for calculating the distribution of dissolved species into solutes and aqueous complexes, and also for computing saturation indexes for different mineral.

In this work, a software system, named as *SHPECK*, is presented that simulates the chemical equilibrium reactions occurring in a geochemical system using the mass-balance approach and the phase rule set forth by Garrels and Christ [Garrels and Christ 1965]. The software system receives as input any general combination of chemical elements, species, and reactions, allowing the user to create several different environments, simulations and, therefore, and to fully control any aspect and configuration of the model. Moreover, the work shows a thorough analysis of the available existing solutions, making clear the uniqueness of the proposed computational approach for the geochemical modeling problem.

The software SHPECK also provides an interactive user interface that allows the users to more conveniently setup the simulations. The user interface used a relational database that further improves database archiving and managing, which is an option absent in any of the other alternatives. The flexibility of parameter configuration offered by the visual interface further extend the possibilities of experimentation with the software, and this is a unique characteristic among commercial software products for geochemical speciation. Limitations on the database structure and input capability strongly restricts the potential use of the the alternative geochemical packages. Therefore, SHPECK is unique among the geochemical speciation models by implementing modern computing technology, absent in other similarly tasked software, with efficient numerical method.

2. Review of Available Geochemical modeling Software

Geochemical modeling software have been in use since the 70s to solve: speciation; determination of mineral saturation index; adjustment of equilibrium for minerals; mixing of compositionally distinct waters; calculation of stoichiometric reactions; mixing of solids, fluid and gas phases; calculation of equilibrium and kinetic reactions between solutes and minerals; and reactive transport. While a large number of computational models have been developed over the years, a number of them are particularly well known and available to general public. Thus, three models representing the large number of similar software have been identified and compared in this study: EQ3/6, PHREEQC and MINTEQ. We had given special attention to the geochemical modeling approaches and the computer-science related aspects of them, providing the comparison when the information is available.

EQ3/6 consists of two programs: EQ3 is a speciation code whose results EQ6 subsequently processes. It is a software package for geochemical modeling of aqueous systems written in FORTRAN77. EQ3/6 includes a speciation-solubility solver, which is useful for analyzing groundwater chemistry data, calculating solubility limits and determining whether certain reactions are in partial equilibrium or in state of disequilibrium. It also offers a reac-

tion path calculation that models water/rock interaction or fluid mixtures. EQ3/6 supports several thermodynamic data files. These data files also include supports for *Davies*, *B-dot*, *Debye Huckel* equations used to approximate activity of solutes in water, as well as data for standard-state properties of solutes. Currently available versions run under *UNIX-like* environments, and the full package distribution requires a paid license. Additional details of the software can be found in [Wolery 1979], [Wolery et al. 1990] and [Wolery 1992].

PHREEQC stands for PH REdox EQuilibrium in C language, and is largely used geo chemical modeling software obtainable from the USGS. Versions for Windows and UNIX-like are available. A detailed description of the package can be found in [Parkhurst 1995]. It was designed to perform a wide variety of low-temperature aqueous geochemical calculations based on an ion association aqueous model. It includes functionality for:

- Speciation and Saturation Index calculations;
- Batch reaction and one-dimensional (1D) transport calculations involving reversible reactions (including aqueous, minerals, gas, solid-solution, surface-complexation, and ion-exchange equilibrium) and irreversible reactions (including specified mole transfer of reactants, kinetically controlled reactions, mixing of solutions and temperature changes);
- Inverse modeling, which finds sets of mineral and gas mole transfers that takes into account differences in water composition.

MINTEQ [Felmy et al. 1983] is a geochemical program for modeling aqueous solutions and their interactions with hypothesized assemblages of solid phases. It has a particular inclination to calculate equilibrium composition of dilute aqueous solutions. The model is useful for calculating the equilibrium mass distribution among dissolved species, adsorbed species and multiple solid phases, limited by a simple treatment of the reactions. It was originally developed in FORTRAN77 by the Battelle Pacific Northwest Laboratories (BPNL) and continues to be maintained by the Environmental Protection Agency (EPA) to perform the necessary calculations regarding waste, sediments and ground water interaction. MINTEQ does not consider the kinetic reactions and works at fixed temperature (25 degrees Celcius). An extensive database is included in the software [Brown and Allison 1987] [Allison J. D. and Novo-Gradac 1991]. The latest update on MINTEQ dates from 1990. Limited improvements on the usability and calculations have been added since, and the new version is named MINTEQA2. The new version supports the thermodynamic database from the USGS. In this article only the MINTEQA2 is reviewed.

2.1. Input and Output Format

EQ3/6 and MINTEQA2 work with input files, more than one, that are generated manually and given to the program as arguments. It is important to note that they must be mutually consistent with the options and methods. Wrong chemical data or inconsistencies in the chosen algorithm will lead to erroneous results. PHREEQC works wot the same approach, however a visual plugin [Apello 2011] and a GUI [Post 2011] make it possible

to reduce the error. It is often very tedious and time consuming to generate input files for simulations. Output formats on the three software systems are similar: text files with blocks of information reporting input options, variables and results of the simulations.

2.2. User Interaction

EQ3/6, MINTEQA2 and PHREEQC (UNIX-like distribution) develop all the interaction with users through the command line, since there is no graphical interaction. Once the simulation process starts, any change in the parameters requires to kill the process manually through the operating system and run the simulator again. The PHREEQC package provides a version for Windows [Post 2011], however it has not been updated since 2011. This version allows the user to generate input files, however there are no error verification or analysis capabilities.

2.3. File formats

All three software mentioned work with text input files (ASCII), which can be created and edited using any text editor.

2.4. Thermodynamic database

The three software use flat files as thermodynamic database. This mechanism has demonstrated along the years several potential issues: duplication of the information; non-unique records; difficulty updating and maintaining; inherently inefficient; rigid (difficult data format); and insecure; ??

2.5. Software environment and installation procedures

EQ3/6 has no self-extracting installer, and the installation process requires some level of proficiency with command prompts and DOS. Furthermore, EQ3/6 is available only for Windows; the UNIX distribution is no longer available. PHREEQC and MINTEQA2 have Windows installers available for download. MINTEQA2 distribution on UNIX environment consists of the source code, thus requiring the user to compile and link. EQ3/6 and MINTEQA2 were written in FORTRAN77 while PHREEQC is written in C

3. SHPECK

SHPECK is a geochemical speciation modeling software capable of calculating the distribution of dissolved species between free ions and aqueous complexes and also the saturation indexes for different mineral phases. SHPECK was developed using C++ and is modelled following the concept of Model-View-Controller (MVC) [Gamma et al. 1994]. The architecture is described in figure 1.

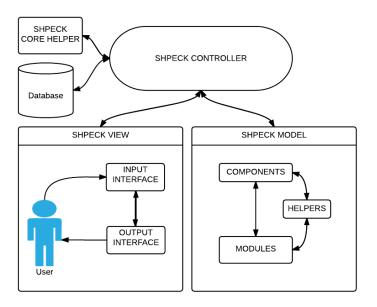


Figure 1: Architecture of the SHPECK software

3.1. Graphical User Interface

In existing geochemical modeling software systems, the *GUI* are either poorly implemented, or not implemented at all. The *GUI* of *SHPECK* enables a user to interactively construct a geochemical system for modeling. *SHPECK*'s *GUI* uses tabs to address different criteria and input types, as it is presented in detail below:

- Configurations tab: this panel allows users to view and manipulate basic system settings and to control temperature, activity coefficient calculation method, the number of iterations, solver options, and other numerical method parameters. It is presented in figure 2.
- Chemical phases in the water tab: this panel allows users to create and edit composition of waters that are used in the model. This section has access to the complete catalog of solutes database. The solutes in the tab with non-zero concentrations are included in the simulations. This tab is presented in figure 3.
- Tab of results: This panel allows users to examine input information and simulation results, such as temperature, ionic strength, pH of the solution, final concentration for the solutes, saturation indices, etc. It is presented in figure 4.

3.2. Database

Relational database is used in *SHPECK* to bypass the problems associated with the use of text files used as databases in other software, and to provide flexible and rapid, visually effective correlation between information required and available through the database enquiries. In addition, relational databases offer three important advantages:

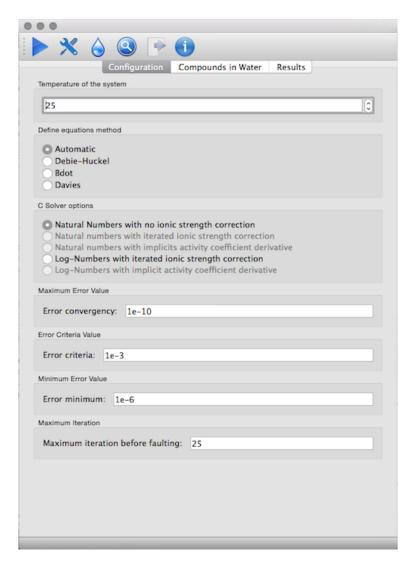


Figure 2: Configuration tab

- Memory saving, since it does not require the complete database to be fully load in main memory during the run time. The program fetches the information only when required by each module.
- Direct access to relevant information: SQL queries are used to fetch only the relevant information, whereas sequential search is required when text files are used. Database queries and concatenation of queries result in a faster and more efficient use of the available resources.

The database architecture, presented in details in figure 5, was defined after studying the algorithm and determining what would be the structure and the information requested. The relational database embraces all the important data required for a geochemical modeling software and the structure was defined to compact and organized structure, and to make



Figure 3: Water composition tab

the information access efficient.

The implementation was done with SQLite database [Hipp 2015], which is a software-library that implements a self-contained, transactional SQL open source database engine. Currently it is the most widely deployed SQL database engine in the world.

SHPECK's database is composed by the information about elements, solute species, compounds, reactions and thermodynamic constants from the $Lawrence\ Livermore\ National\ Laboratory\ (LLNL)$ thermodynamic dataset. A parser for LLNL flat file database was created to extract this information from text files and to populate the database tables. The same text files are used as database in EQ3/6, PHREEQC and other geochemical codes.

Once the structure and the technology of our database were defined, a parser was prepared to extract the information from the flat file database. The parser was generated carefully in order to ensure that all of the data and delimiters were identified and treated

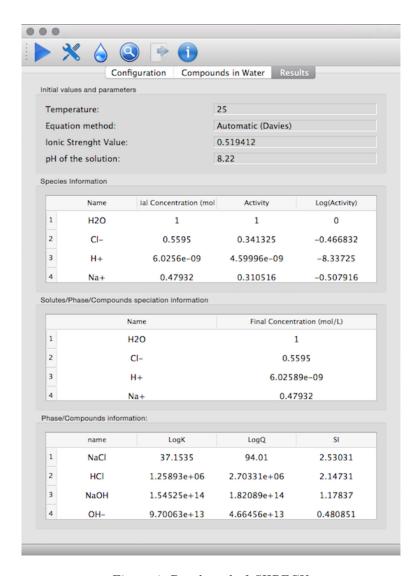


Figure 4: Results tabof SHPECK

properly. This task was extremely time-consuming because of irregularities found in the flat files (i.e. wrong tab or space formating, different encoding of the files, etc).

4. Verification and Validation

To test and validate the simulator, we model the diagenetic reactions observed in Snorre Field reservoir sandstones of Norwegian North Sea. The main reservoir horizons of the field are the fluvial sandstones in the upper member of the Upper Triassic Lunde Formation and the Upper Triassic to Lower Jurassic Statfjord Formation [Hollander]. The sandstones sampled for this study, according to Morad [Morad. S. 1990], belong to the upper member of the Lunde Formation. The sandstones are dominantly fine- to medium-grained and arkosic with framework constituents of quartz (40-80%), K-feldspar (5-12%), plagioclase (15-45%),

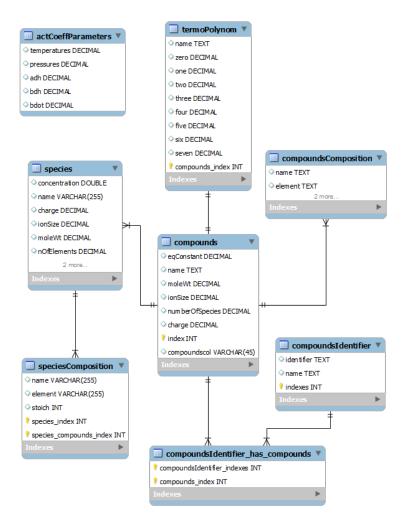


Figure 5: ER Diagram of the database

muscovite, biotite and clay minerals that include smectite, mixed-layer clay minerals, chlorite and subordinate amounts of kaolinite and illite. Subordinate rock fragments include intraformational mudstone and carbonate clasts and extrabasinal grains of quartz-feldsparmica aggregates that probably represent granitic rocks and/or schist or gneisses. Mica and detrittal clay minerals seldom make up more than 2% of the total mineral content in the sandstones. Diagenetic clay minerals include pore-filling kaolinite and pore-lining smectite, mixed-layer chlofite-smectite, and chlorite. Other cements include the carbonates (0.0-25%) which play a significant role in porosity reduction in some of the sandstones. Authigenic overgrowths are primarily quartz, anatase and minor albite, pyrite and barite. The modeling setup and results given in Morad [Morad. S. 1990], which also describes the texture, origin, chemistry of the sandstones reservoirs in terms of the water composition and temperature. Against this SHPECKs results were examined.

The descriptions presented in [Morad. S. 1990] of the diagenetic reactions that take place in the Snorre Field allows us to generate results to carry out a computationally comparative

Table 1: Chemical composition of the solution in the sea water at 25° in mM/LC									
Al^{3+}	K^{+}	Na ⁺	Ca^{2+}	Mg^{2+}	Fe^{2+}	SiO_2	SO_4^{2-}	Cl^-	рН
7.59e-5	10.45	479.32	10.53	54.39	3.66e-5	0.073	28.893	559.5	8.22

study. We model and compare the same diagenetic environment using SHPECK, PHREEQC and MINTEQA2. The water composition is detailed in [Nordstrom 1979].

As stated in [Morad. S. 1990], the model presented in [Egeberg and Aagaard 1988] calculates activities of the various ions of formations waters using the ion association model (originally described in [Wigley 1977]). The thermodynamics data used are given in [Helgeson and Kirkham 1966], [Walter and Helgeson 1977], [Helgeson H. C. and Flowers 1981].

The activity diagram generated for a known temperature and log activity ratio of Potassium to Sodium ions of [Aagaard 1990] is provided as input to *SHPECK* model (Figure 6). The results show a consistent pattern: as the temperature rises the potassium activity becomes higher than sodiums, which means that the phases associated to the ion potassium (i.e. K-feldspar, Illite, etc) are dissolving.

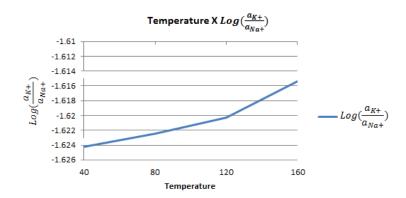


Figure 6: Log activity ratio of Potassium to Sodium ions using the results from SHPECK

4.1. Computational comparative study

By modeling the same environment using three distinct software packages, we attain a relevant comparison among the numerical methods and algorithms. Chemical composition of the water adopted in the models is taken from [Nordstrom 1979] which provides the chemical composition of the seawater (table 1). The comparative study tested temperatures from 25°C to 100°C. In MINTEQA2, due to limitations of its thermodynamics equilibrium database, the maximum temperature available is 100°C.

We aim to model the diagenetic processes that best represent the behavior of ions in the water-rock interactions. Figures 7, 8, 9 and 10 present the most representative ions of the solution.

The results of SHPECK are similar to those from both PHREEQC and MINTEQA2 in most of the cases, especially for temperatures under 100° C. Discrepancies occur in SHPECK and PHREEQC results when temperatures are higher than 100° C. This discrepancy is due to incomplete equilibrium constant K defined in the MINTEQA2 database.

This is a known issue from *LLNL* thermodynamic dataset: sometimes equilibrium constants have no measures in literature and are treated as unknown. *SHPECK* adopts the nearest equilibrium constant known value. Unfortunately we do not have access to the whole softwares details in order to describe how they treat this issue.

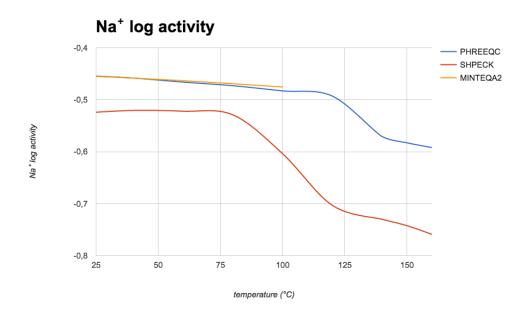


Figure 7: Na⁺ log activity comparative study

4.2. Database Evaluation

All geochemical models used for comparison studies use text files as the database. The goal of this section is to make clear the difference and, more importantly, the benefits of SHPECKs relational database. Most of the information inside a geochemical database is related to each other (i.e. a mineral phase is described by a reaction, a reaction is composed by solute species, and a solute species is composed of chemical elements). Relational databases sophisticated built-in query and sorting statements make the organization of the data convenient, and this significantly improves the performance and robustness of the application. On SQLite databases, the data can be accessed using SQL queries that reduce the complexity and increase the speed on information retrieval. Code 1 shows a typical query issued from SHPECKs SQLite query. The options and the flexibility afforded by the use of relational database cannot be compared to the options available when text file based databases are used.

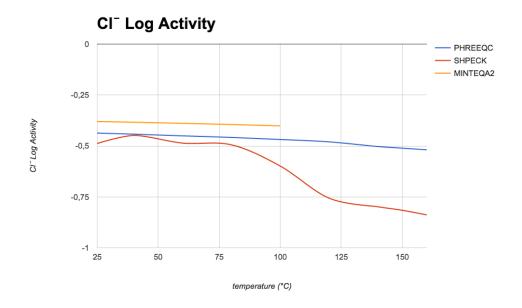


Figure 8: Cl⁻ log activity comparative study

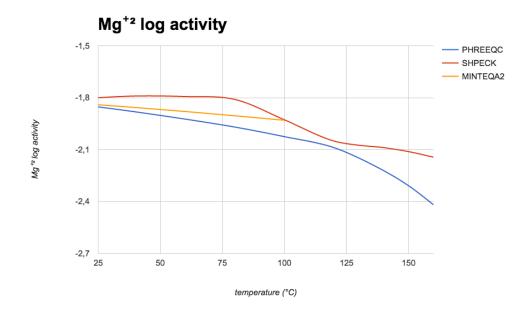


Figure 9: Mg⁺² log activity comparative study

Code 1: SHPECK's SQLite example query

SELECT compoundsComposition.element, compoundsComposition.name, compoundsComposition.stoich, compounds.eqConstant, termoPolynom.zero, termoPolynom.one, termoPolynom.two, termoPolynom.three, termoPolynom.four, termoPolynom.five, termoPolynom.six, termoPolynom.seven FROM termoPolynom, compoundsComposition, compounds WHERE compoundsComposition.name = compounds.hame AND termoPolynom.name = compounds.name AND compounds.name = XXXXXX;

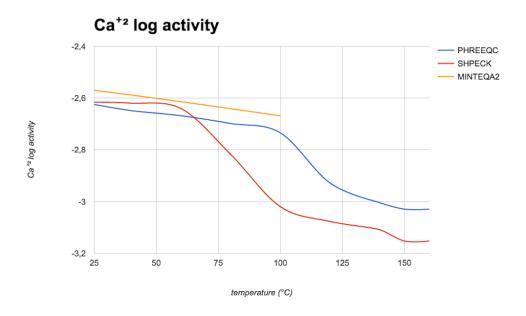


Figure 10: Ca⁺² log activity comparative study

Important to note that at each simulation the value XXXX in code 1 is updated to the simulations solute name. Also interesting to point that the information fetched with this query comes from three different tables and many relevant information for the simulation is fetched at once.

4.3. Time analysis

The response time is considered as the sum of the processing time and the time waiting for the availability of the resource. It is necessary to understand that until the software has received all the information requested from the database it is inactive and in a standby mode. To analyze the response time within a geochemical analysis point of view, we discuss not only the access time, but also the implications of that information.

When fetching any information from a thermodynamic database, it is important to take into consideration additional allied data will also have to be retrieved. For example, when fetching a reaction data, the basic information consists of the compounds that take part in this reaction and the related stoichiometric values. Behind this action, the database must also provide information about the compounds (i.e. charge, ion size, molecular weight, elements in that species, formula, and molar volume), as well as the reaction (i.e., thermodynamic equilibrium constant coefficients, etc).

Figure 11 indicates the time elapsed (in seconds) that it takes to retrieve all necessary information related to a chemical reaction from the database. In this example, we simulated from 20 to 580 randomly selected reactions in the database. It is possible to see that SHPECK's database has improved approximately 40% in the average time elapsed to fetch the information when compared to the procedure used by other models.

Time x Reactions 8,00E+00 Others* (Flat File) SHPECK 6,00E+00 (SQLite) Time Elapsed 4,00E+00 2,00E+00 0.00E+00 100 200 400 300 500 Number of reactions fetched

Figure 11: Time elapsed in seconds X Reactions Accessed

5. Concluding remarks

This work provides details of *SHPECK*, a modeling software package intended to raise the quality of available geochemical speciation. The program innovates by including a visual user interface that allows to parametrize the reaction simulation, as well as a relational database architecture component. The user interface implements a dynamic tool that facilitates the simulation case preparation. *SHPECK* accepts any general combination of chemical elements, mineral species and chemical reactions, along with definitions of boundary contour conditions of temperature, pH, pressure, etc. *SHPECK* calculates the distribution of dissolved solutes in the water and saturation indices of various mineral phases. *SHPECK* calculates the speciation of a solution based on a set of mass-balance equations, which are solved iteratively using the Newton-Raphson numerical method. *SHPECK* was built with considerations for computer sciences priorities and theories.

The completed software was tested and its results compared with the results obtained through the alternative software. The results produced by SHPECK were found to be consistent with those of the alternative models.

SHPECK's results accuracy is equivalent and inside the expect range to the study case developed in this work. The results show that all the three software compared have nearly the same results with the same inputs. Slight differences are found when simulating with temperatures higher than 100°C, which appear to arise from discrepancies in the thermodynamic properties of the equilibrium constant.

We plan to improve SHPECK by adding kinetic reactions to the processing core - it is a delicate topic since adding kinetic reactions implies not only working with mass balance equations but also with chemical elemental mass evolution. The elemental mass evolution

describes mass change through mass transfer and kinetic reactions of solids and solute-solute interaction - described in details in [Park 2014]. Moreover, a distribution platform where users can register, interact, collaborate in forums, indicate bugs, and download SHPECK is projected.

References

- [Aagaard 1990]AAGAARD, P. E. A. Diagenetic albitization of detrital k-feldspars in jurassic, lower cretaceous and tertiary elastic reservoir rocks from offshore norway. if. formation water chemistry and kinetic considerations. *Jour. Sed. Petrology*, 1990.
- [Allison J. D. and Novo-Gradac 1991] ALLISON J. D., B. D. S.; NOVO-GRADAC, K. J. Minteqa2/prodefa2, a geochemical assessment model for environmental systems: version 3.0. Environmental Research Laboratory, Office of research and development, U.S. Environmental Protection Agency, 1991.
- [Apello 2011] APELLO, C. NotPHREEQC Notepad++ with PHREEQC Plugin. 2011. Available from Internet: <www.hydrochemistry.eu/ph3>.
- [Brown and Allison 1987]BROWN, D. S.; ALLISON, J. D. MINTEQA1, an equilibrium metal speciation model: user's manual. [S.l.]: Environmental Research Laboratory, Office of research and development, U.S. Environmental Protection Agency, 1987.
- [Egeberg and Aagaard 1988] EGEBERG, P. K.; AAGAARD, P. Formation water chemistry in relation to the stability ofdetrital and authigenic minerals in elastic reservoirs from offshore norway of oslo. *University of OSLO*, 1988.
- [Felmy et al. 1983] FELMY, A. R. et al. Minteq: A computer program for calculating aquoues geochemical equilibria. Environmental Research Laboratory, Office of research and development, U.S. Environmental Protection Agency, 1983.
- [Gamma et al. 1994]GAMMA, E. et al. Design Patterns. Elements of Reusable Object-Oriented Software. [S.l.: s.n.], 1994.
- [Garrels and Christ 1965] GARRELS, R. M.; CHRIST, C. M. Solutions, Minerals, and Equilibria. [S.l.]: Harpers' Geoscience Series, 1965.
- [Helgeson and Kirkham 1974]HELGESON, H. C.; KIRKHAM, D. H. Theoretical prediction of the thermodyanmic behavior of aqueous electrolytes at high pressures and temperatures: Ii. deby-hiickel parameters for activity coefficients and relative partial molal properties. *Am. Jour. Science*, 1974.
- [Helgeson and Kirkham 1974]HELGESON, H. C.; KIRKHAM, D. H. Theoretical prediction of the thermodynamic behavior of aqueous electrolytes at high pressures and temperatures: 1. summary of the thermodynamic/electrostatic properties of the solvent. *Am. Jour. Science*, 1974.
- [Helgeson and Kirkham 1976]HELGESON, H. C.; KIRKHAM, D. H. Theoretical prediction of the thermodynamic behavior of aqueous electrolytes at high pressures and temperatures: Iii. equations of state for aqueous species at inifinite dilution. *Am. Jour. Science*, 1976.
- [Helgeson H. C. and Bird 1978] HELGESON H. C., D. W. J. N. H. W.; BIRD, D. K. Summary and critique of the thermodynamic properties of rock-forming minerals. *Am. Jour. Science*, 1978.
- [Helgeson H. C. and Flowers 1981]HELGESON H. C., K. D. H.; FLOWERS, G. C. Theoretical prediction of the thermodynamic behavior of aqueous electrolytes at high pressures and temperatures: Iv. calculation of activity coefficients, osmotic coefficients, and apparent molal and standard and relative partial molal properties science. *Am. Jour. Science*, 1981.
- [Hipp 2015] HIPP, D. R. SQLite. 2015. Available from Internet: https://www.sqlite.org. [Hollander] HOLLANDER, N. B.
- [Morad. S. 1990] MORAD. S., E. A. Albitization of detrital plagioclase in triassic reservoir sandstones from the snorre field, norwegian north sea. j. sediment. *U.S. Geological Survery Books and Open-File Reports*, 1990.
- [Nordstrom 1979]NORDSTROM, D. K. e. a. A comparison of computerized chemical models for equilibrium calculations in aqueous systems. *American Chemical Society*, 1979.
- [Park 2014]PARK, A. J. Water-rock interaction and reactive-transport modeling using elemental mass-balance approach: I. the methodology. *American Journal of Science*, 2014.
- [Parkhurst 1995]PARKHURST, D. L. User's guide to phreeqc a computer program for speciation, reaction-path, advective-transport, and inverse geochemical calculations. *U.S. Geological Survey Water-Resources Investigations Report*, 1995.
- [Post 2011] POST, V. PHREEQC for Windows. 2011. Available from Internet: http://pfw.antipodes.nl/>.

- [Walter and Helgeson 1977] WALTER, T. E.; HELGESON, H. C. Calculations of the thermodynamic properties of aqueous silica and the solubility of quartz and its polymorphs at high pressures and temperatures. *American Journal of Science*, 1977.
- [Wigley 1977] WIGLEY, T. M. L. A computer program for determining the equilibrium speciation of aqueous solutions. *Technical Bulletin No. 20, Climatic Research Unit, Univ. East Anglia, U.K*, 1977.
- [Wolery 1979] WOLERY, T. J. Calculation of chemical equilibrium between aqueous solution and minerals: the eq3/6 software package. Lawrence Livermore National Laboratory, Livermore CA, U.S.A., 1979.
- [Wolery 1992] WOLERY, T. J. Eq3/6, a software package for geochemical modeling of aqueous systems: package overview and installation guide (version 7.0). American Chemical Society Symposium series, No 416, 1992.
- [Wolery et al. 1990] WOLERY, T. J. et al. Current status of the eq3/6 software package for geochemical modeling in chemical modeling of aqueous system. *American Chemical Society Symposium series, No* 416, p. 104–116, 1990.