

## ▼ CS224N Assignment 1: Exploring Word Vectors (25 Points)

Due 4:30pm, Tue Jan 17

Welcome to CS224N!

Before you start, make sure you read the README.txt in the same directory as this notebook for important setup information. A lot of code is provided in this notebook, and we highly encourage you to read and understand it as part of the learning :)

If you aren't super familiar with Python, Numpy, or Matplotlib, we recommend you check out the review session on Friday. The session will be recorded and the material will be made available on our [website](#). The CS231N Python/Numpy [tutorial](#) is also a great resource.

**Assignment Notes:** Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

```
# All Import Statements Defined Here
# Note: Do not add to this list.
# -----

import sys
assert sys.version_info[0]==3
assert sys.version_info[1] >= 5

from platform import python_version
assert int(python_version().split(".")[1]) >= 5, "Please upgrade your Python version following
    the README.txt file found in the same directory as this notebook. Your Python version is

from gensim.models import KeyedVectors
from gensim.test.utils import datapath
import pprint
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = [10, 5]

import nltk
nltk.download('reuters') #to specify download location, optionally add the argument: download
from nltk.corpus import reuters

import numpy as np
import random
import scipy as sp
from sklearn.decomposition import TruncatedSVD
from sklearn.decomposition import PCA

START_TOKEN = '<START>'
```

```
END_TOKEN = '<END>'
```

```
np.random.seed(0)
```

```
random.seed(0)
```

```
# -----
```

```
[nltk_data] Downloading package reuters to /root/nltk_data...
```

## Word Vectors

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from *co-occurrence matrices*, and those derived via *GloVe*.

**Note on Terminology:** The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As [Wikipedia](#) states, "*conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension*".

### ▼ Part 1: Count-Based Word Vectors (10 points)

Most word vector models start from the following idea:

*You shall know a word by the company it keeps* ([Firth, J. R. 1957:11](#))

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, *co-occurrence matrices* (for more information, see [here](#) or [here](#)).

## Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word  $w_i$  occurring in the document, we consider the *context window* surrounding  $w_i$ . Supposing our fixed window size is  $n$ , then this is the  $n$  preceding and  $n$  subsequent words in that document, i.e. words  $w_{i-n} \dots w_{i-1}$  and  $w_{i+1} \dots w_{i+n}$ . We build a *co-occurrence matrix*  $M$ , which is a symmetric word-by-word matrix in which  $M_{ij}$  is the number of times  $w_j$  appears inside  $w_i$ 's window among all documents.

**Example: Co-Occurrence with Fixed Window of  $n=1$ :**

Document 1: "all that glitters is not gold"

Document 2: "all is well that ends well"

*	<START>	all	that	glitters	is	not	gold	well	ends	<END>
<START>	0	2	0	0	0	0	0	0	0	0
all	2	0	1	0	1	0	0	0	0	0
that	0	1	0	1	0	0	0	1	1	0
glitters	0	0	1	0	1	0	0	0	0	0
is	0	1	0	1	0	1	0	1	0	0
not	0	0	0	0	1	0	1	0	0	0
gold	0	0	0	0	0	1	0	0	0	1
well	0	0	1	0	1	0	0	0	1	1
ends	0	0	1	0	0	0	0	1	0	0
<END>	0	0	0	0	0	0	1	1	0	0

**Note:** In NLP, we often add <START> and <END> tokens to represent the beginning and end of sentences, paragraphs or documents. In this case we imagine <START> and <END> tokens encapsulating each document, e.g., "<START> All that glitters is not gold <END>", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on word-word co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run *dimensionality reduction*. In particular, we will run *SVD* (*Singular Value Decomposition*), which is a kind of generalized *PCA* (*Principal Components Analysis*) to select the top  $k$  principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is  $A$  with  $n$  rows corresponding to  $n$  words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal  $S$  matrix, and our new, shorter length- $k$  word vectors in  $U_k$ .

 Picture of an SVD

This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. *doctor* and *hospital* will be closer than *doctor* and *dog*.

**Notes:** If you can barely remember what an eigenvalue is, here's [a slow, friendly introduction to SVD](#). If you want to learn more thoroughly about PCA or SVD, feel free to check out lectures [7](#), [8](#), and [9](#) of CS168. These course notes provide a great high-level treatment of these general purpose algorithms. Though, for the purpose of this class, you only need to know how to extract the  $k$ -dimensional embeddings by utilizing pre-programmed implementations of these algorithms from the numpy, scipy, or sklearn python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top  $k$

vector components for relatively small  $k$  – known as [Truncated SVD](#) – then there are reasonably scalable techniques to compute those iteratively.

## ▼ Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see <https://www.nltk.org/book/ch02.html>. We provide a `read_corpus` function below that pulls out only articles from the "gold" (i.e. news articles about gold, mining, etc.) category. The function also adds `<START>` and `<END>` tokens to each of the documents, and lowercases words. You do **not** have to perform any other kind of pre-processing.

```
def read_corpus(category="gold"):
    """ Read files from the specified Reuter's category.
        Params:
            category (string): category name
        Return:
            list of lists, with words from each of the processed files
    """
    files = reuters.fileids(category)
    return [[START_TOKEN] + [w.lower() for w in list(reuters.words(f))] + [END_TOKEN] for f in files]
```

Let's have a look what these documents are like....

```
reuters_corpus = read_corpus()
pprint.pprint(reuters_corpus[:3], compact=True, width=100)

[['<START>', 'western', 'mining', 'to', 'open', 'new', 'gold', 'mine', 'in', 'australia',
  'mining', 'corp', 'holdings', 'ltd', '&', 'lt', ';', 'wmng', '.', 's', '>', '(', 'wmc',
  'said', 'it', 'will', 'establish', 'a', 'new', 'joint', 'venture', 'gold', 'mine', 'in',
  'northern', 'territory', 'at', 'a', 'cost', 'of', 'about', '21', 'mln', 'dlrs', '.',
  'mine', ',', 'to', 'be', 'known', 'as', 'the', 'goodall', 'project', ',', 'will', 'be',
  '60', 'pct', 'by', 'wmc', 'and', '40', 'pct', 'by', 'a', 'local', 'w', '.', 'r', '.',
  'and', 'co', '&', 'lt', ';', 'gra', '>', 'unit', '.', 'it', 'is', 'located', '30', 'km',
  'of', 'the', 'adelaide', 'river', 'at', 'mt', '.', 'bundey', ',', 'wmc', 'said', 'in',
  'statement', 'it', 'said', 'the', 'open', '-', 'pit', 'mine', ',', 'with', 'a', 'conve',
  'leach', 'treatment', 'plant', ',', 'is', 'expected', 'to', 'produce', 'about', '50',
  'ounces', 'of', 'gold', 'in', 'its', 'first', 'year', 'of', 'production', 'from', 'mid',
  '1988', '.', 'annual', 'ore', 'capacity', 'will', 'be', 'about', '750', ',', '000', 't',
  '<END>'],
 ['<START>', 'belgium', 'to', 'issue', 'gold', 'warrants', ',', 'sources', 'say', 'belgi',
  'plans', 'to', 'issue', 'swiss', 'franc', 'warrants', 'to', 'buy', 'gold', ',', 'with',
  'suisse', 'as', 'lead', 'manager', ',', 'market', 'sources', 'said', '.', 'no', 'confi
```

```
'or', 'further', 'details', 'were', 'immediately', 'available', '.', '<END>'],
['<START>', 'belgium', 'launches', 'bonds', 'with', 'gold', 'warrants', 'the', 'kingdom',
'belgium', 'is', 'launching', '100', 'mln', 'swiss', 'francs', 'of', 'seven', 'year',
'with', 'warrants', 'attached', 'to', 'buy', 'gold', ',', 'lead', 'manager', 'credit',
'said', '.', 'the', 'notes', 'themselves', 'have', 'a', '3', '-', '3', '/', '8', 'pct',
'and', 'are', 'priced', 'at', 'par', '.', 'payment', 'is', 'due', 'april', '30', ',', ', ',
'and', 'final', 'maturity', 'april', '30', ',', ', ', '1994', '.', 'each', '50', ',', ', ', '000',
'note', 'carries', '15', 'warrants', '.', 'two', 'warrants', 'are', 'required', 'to',
'the', 'holder', 'to', 'buy', '100', 'grammes', 'of', 'gold', 'at', 'a', 'price', 'of',
'450', 'francs', ',', ', ', 'during', 'the', 'entire', 'life', 'of', 'the', 'bond', '.', 'the',
'latest', 'gold', 'price', 'in', 'zurich', 'was', '2', ',', ', ', '045', '/', '2', ',', ', ', '076',
'per', '100', 'grammes', '.', '<END>']]
```

### ▼ Question 1.1: Implement `distinct_words` [code] (2 points)

Write a method to work out the distinct words (word types) that occur in the corpus. You can do this with `for` loops, but it's more efficient to do it with Python list comprehensions. In particular, [this](#) may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's [more information](#).

Your returned `corpus_words` should be sorted. You can use python's `sorted` function for this.

You may find it useful to use [Python sets](#) to remove duplicate words.

```
def distinct_words(corpus):
    """ Determine a list of distinct words for the corpus.
        Params:
            corpus (list of list of strings): corpus of documents
        Return:
            corpus_words (list of strings): sorted list of distinct words across the corpus
            n_corpus_words (integer): number of distinct words across the corpus
    """
    corpus_words = []
    n_corpus_words = -1

    ### SOLUTION BEGIN
    temp_set = set()
    for s in corpus:
        for w in s:
            temp_set.add(w)

    corpus_words = sorted(list(temp_set))
    n_corpus_words = len(corpus_words)
    ### SOLUTION END

    return corpus_words, n_corpus_words
```

```
# -----
# Run this sanity check
# Note that this not an exhaustive check for correctness.
# -----

# Define toy corpus
test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN, END_TOKEN).split(" ")
test_corpus_words, num_corpus_words = distinct_words(test_corpus)

# Correct answers
ans_test_corpus_words = sorted([START_TOKEN, "All", "ends", "that", "gold", "All's", "glitter
ans_num_corpus_words = len(ans_test_corpus_words)

# Test correct number of words
assert(num_corpus_words == ans_num_corpus_words), "Incorrect number of distinct words. Correc

# Test correct words
assert (test_corpus_words == ans_test_corpus_words), "Incorrect corpus_words.\nCorrect: {} \nY

# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
```

```
-----
Passed All Tests!
-----
```

## ▼ Question 1.2: Implement `compute_co_occurrence_matrix` [code] (3 points)

Write a method that constructs a co-occurrence matrix for a certain window-size  $n$  (with a default of 4), considering words  $n$  before and  $n$  after the word in the center of the window. Here, we start to use `numpy` (`np`) to represent vectors, matrices, and tensors. If you're not familiar with NumPy, there's a NumPy tutorial in the second half of this cs231n [Python NumPy tutorial](#).

```
def compute_co_occurrence_matrix(corpus, window_size=4):
    """ Compute co-occurrence matrix for the given corpus and window_size (default of 4).
```

Note: Each word in a document should be at the center of a window. Words near edges w  
number of co-occurring words.

For example, if we take the document "<START> All that glitters is not gold <EN  
"All" will co-occur with "<START>", "that", "glitters", "is", and "not".

Params:

corpus (list of list of strings): corpus of documents

window\_size (int): size of context window

Return:

M (a symmetric numpy matrix of shape (number of unique words in the corpus , number of unique words in the corpus))  
 Co-occurrence matrix of word counts.

The ordering of the words in the rows/columns should be the same as the order  
 word2ind (dict): dictionary that maps word to index (i.e. row/column number) for

```
"""
```

```
words, n_words = distinct_words(corpus)
```

```
M = np.zeros((n_words, n_words))
```

```
word2ind = {}
```

```
### SOLUTION BEGIN
```

```
for i, w in enumerate(words):
```

```
    word2ind[w] = i
```

```
for s in corpus:
```

```
    for i, w in enumerate(s):
```

```
        l = len(s)
```

```
        center_word = w
```

```
        left = i - window_size
```

```
        right = i + window_size + 1
```

```
        if(left < 0):
```

```
            left = 0
```

```
        if(right > l):
```

```
            right = l - 1
```

```
        context_words = s[left:i] + s[i+1:right]
```

```
        for centext_word in context_words:
```

```
            M[word2ind[center_word], word2ind[centext_word]] += 1
```

```
### SOLUTION END
```

```
return M, word2ind
```

```
# -----
```

```
# Run this sanity check
```

```
# Note that this is not an exhaustive check for correctness.
```

```
# -----
```

```
# Define toy corpus and get student's co-occurrence matrix
```

```
test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN, END_TOKEN).split(" ")]
```

```
M_test, word2ind_test = compute_co_occurrence_matrix(test_corpus, window_size=1)
```

```
# Correct M and word2ind
```

```
M_test_ans = np.array(
```

```
    [[0., 0., 0., 0., 0., 0., 1., 0., 0., 1.],
```

```
    [0., 0., 1., 1., 0., 0., 0., 0., 0., 0.],
```

```
    [0., 1., 0., 0., 0., 0., 0., 0., 1., 0.],
```

```
    [0., 1., 0., 0., 0., 0., 0., 0., 0., 1.],
```

```
    [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.],
```

```
    [0., 0., 0., 0., 0., 0., 0., 1., 1., 0.],
```

```
    [1., 0., 0., 0., 0., 0., 0., 1., 0., 0.],
```

```
    [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.],
```

```
    [0., 0., 1., 0., 1., 1., 0., 0., 0., 1.]
```

```

    [1., 0., 0., 1., 1., 0., 0., 0., 1., 0.,]]
)
ans_test_corpus_words = sorted([START_TOKEN, "All", "ends", "that", "gold", "All's", "glitter
word2ind_ans = dict(zip(ans_test_corpus_words, range(len(ans_test_corpus_words))))

# Test correct word2ind
assert (word2ind_ans == word2ind_test), "Your word2ind is incorrect:\nCorrect: {}\nYours: {}"

# Test correct M shape
assert (M_test.shape == M_test_ans.shape), "M matrix has incorrect shape.\nCorrect: {}\nYours

# Test correct M values
for w1 in word2ind_ans.keys():
    idx1 = word2ind_ans[w1]
    for w2 in word2ind_ans.keys():
        idx2 = word2ind_ans[w2]
        student = M_test[idx1, idx2]
        correct = M_test_ans[idx1, idx2]
        if student != correct:
            print("Correct M:")
            print(M_test_ans)
            print("Your M: ")
            print(M_test)
            raise AssertionError("Incorrect count at index ({}, {})=({}, {}) in matrix M. You

# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)

```

```

-----
Passed All Tests!
-----

```

### ▼ Question 1.3: Implement `reduce_to_k_dim` [code] (1 point)

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

**Note:** All of numpy, scipy, and scikit-learn ( `sklearn` ) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use [sklearn.decomposition.TruncatedSVD](http://scikit-learn.org/stable/modules/generated/sklearn.decomposition.TruncatedSVD).

```

def reduce_to_k_dim(M, k=2):
    """ Reduce a co-occurrence count matrix of dimensionality (num_corpus_words, num_corpus_wo
        to a matrix of dimensionality (num_corpus_words, k) using the following SVD function
        - http://scikit-learn.org/stable/modules/generated/sklearn.decomposition.Truncate

```



```

Params:
    M (numpy matrix of shape (number of unique words in the corpus , number of unique
    k (int): embedding size of each word after dimension reduction
Return:
    M_reduced (numpy matrix of shape (number of corpus words, k)): matrix of k-dimens
        In terms of the SVD from math class, this actually returns U * S
"""
n_iters = 10      # Use this parameter in your call to `TruncatedSVD`
M_reduced = None
print("Running Truncated SVD over %i words..." % (M.shape[0]))

### SOLUTION BEGIN
svd = TruncatedSVD(n_components=k, n_iter=n_iters)
M_reduced = svd.fit_transform(M)
### SOLUTION END

print("Done.")
return M_reduced

# -----
# Run this sanity check
# Note that this is not an exhaustive check for correctness
# In fact we only check that your M_reduced has the right dimensions.
# -----

# Define toy corpus and run student code
test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN, END_TOKEN).split(" ")
M_test, word2ind_test = compute_co_occurrence_matrix(test_corpus, window_size=1)
M_test_reduced = reduce_to_k_dim(M_test, k=2)

# Test proper dimensions
assert (M_test_reduced.shape[0] == 10), "M_reduced has {} rows; should have {}".format(M_test
assert (M_test_reduced.shape[1] == 2), "M_reduced has {} columns; should have {}".format(M_te

# Print Success
print("-" * 80)
print("Passed All Tests!")
print("-" * 80)

Running Truncated SVD over 10 words...
Done.
-----
Passed All Tests!
-----

```

### ▼ Question 1.4: Implement `plot_embeddings` [code] (1 point)

Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (`plt`).

For this example, you may find it useful to adapt [this code](#). In the future, a good way to make a plot is to look at [the Matplotlib gallery](#), find a plot that looks somewhat like what you want, and adapt the code they give.

```
def plot_embeddings(M_reduced, word2ind, words):
    """ Plot in a scatterplot the embeddings of the words specified in the list "words".
        NOTE: do not plot all the words listed in M_reduced / word2ind.
        Include a label next to each point.

        Params:
            M_reduced (numpy matrix of shape (number of unique words in the corpus , 2)): mat
            word2ind (dict): dictionary that maps word to indices for matrix M
            words (list of strings): words whose embeddings we want to visualize
    """

    ### SOLUTION BEGIN
    for w in words:
        i = word2ind[w]
        x, y = M_reduced[i]
        plt.scatter(x, y, marker='x', color='red')
        plt.text(x, y, w, fontsize=9)
    plt.show()
    ### SOLUTION END

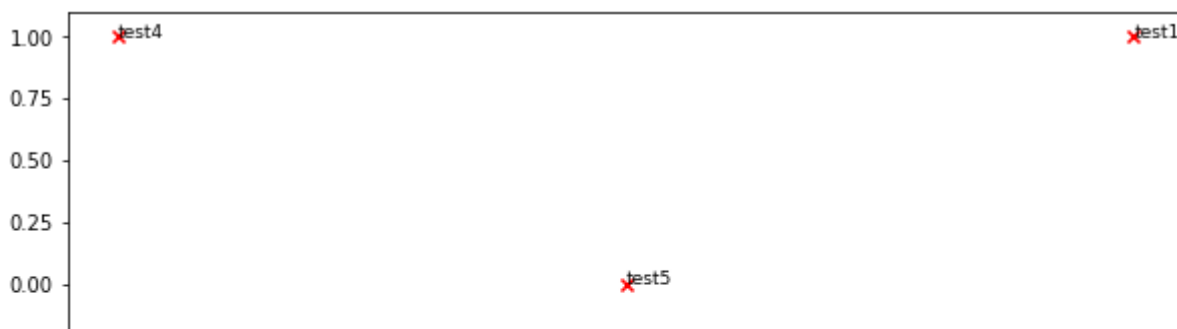
# -----
# Run this sanity check
# Note that this is not an exhaustive check for correctness.
# The plot produced should look like the "test solution plot" depicted below.
# -----

print("-" * 80)
print("Outputted Plot:")

M_reduced_plot_test = np.array([[1, 1], [-1, -1], [1, -1], [-1, 1], [0, 0]])
word2ind_plot_test = {'test1': 0, 'test2': 1, 'test3': 2, 'test4': 3, 'test5': 4}
words = ['test1', 'test2', 'test3', 'test4', 'test5']
plot_embeddings(M_reduced_plot_test, word2ind_plot_test, words)

print("-" * 80)
```

-----  
 Outputted Plot:



### ▼ Question 1.5: Co-Occurrence Plot Analysis [written] (3 points)

Now we will put together all the parts you have written! We will compute the co-occurrence matrix with fixed window of 4 (the default window size), over the Reuters "gold" corpus. Then we will use TruncatedSVD to compute 2-dimensional embeddings of each word. TruncatedSVD returns  $U \cdot S$ , so we need to normalize the returned vectors, so that all the vectors will appear around the unit circle (therefore closeness is directional closeness). **Note:** The line of code below that does the normalizing uses the NumPy concept of *broadcasting*. If you don't know about broadcasting, check out [Computation on Arrays: Broadcasting by Jake VanderPlas](#).

Run the below cell to produce the plot. It'll probably take a few seconds to run.

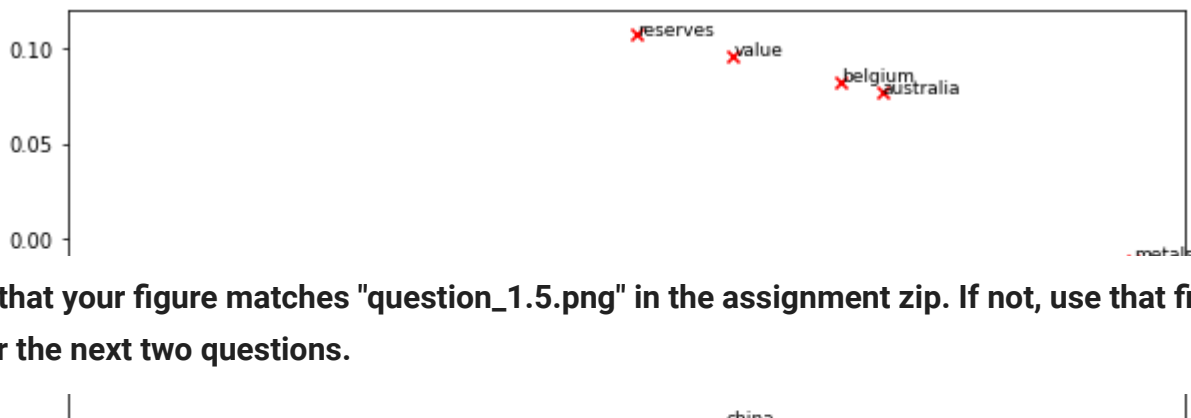
```
# -----
# Run This Cell to Produce Your Plot
# -----
reuters_corpus = read_corpus()
M_co_occurrence, word2ind_co_occurrence = compute_co_occurrence_matrix(reuters_corpus)
M_reduced_co_occurrence = reduce_to_k_dim(M_co_occurrence, k=2)

# Rescale (normalize) the rows to make them each of unit-length
M_lengths = np.linalg.norm(M_reduced_co_occurrence, axis=1)
M_normalized = M_reduced_co_occurrence / M_lengths[:, np.newaxis] # broadcasting

words = ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', 'belgium', 'a

plot_embeddings(M_normalized, word2ind_co_occurrence, words)
```

Running Truncated SVD over 2830 words...  
Done.



**Verify that your figure matches "question\_1.5.png" in the assignment zip. If not, use that figure to answer the next two questions.**

a. Find at least two groups of words that cluster together in 2-dimensional embedding space. Give an explanation for each cluster you observe.

#### ▼ G1 : belgium, australia

These two countries are close together, but I expected china to be next to them!

#### G2: metal, grammes, gold, mine

These are about mine and elements, but again I expected copper or silver to be next to them.

#### G3: reserves, value

These are about resources.

And words like copper, platinum, silver and china each one in the different clusters because of distance.

b. What doesn't cluster together that you might think should have? Describe at least two examples.

As I mentioned above, I think copper, silver and platinum should be placed next to G2 words and the word China should be near G1 words.

#### ▼ Part 2: Prediction-Based Word Vectors (15 points)

As discussed in class, more recently prediction-based word vectors have demonstrated better performance, such as word2vec and GloVe (which also utilizes the benefit of counts). Here, we shall explore the embeddings produced by GloVe. Please revisit the class notes and lecture slides for

more details on the word2vec and GloVe algorithms. If you're feeling adventurous, challenge yourself and try reading [GloVe's original paper](#).

Then run the following cells to load the GloVe vectors into memory. **Note:** If this is your first time to run these cells, i.e. download the embedding model, it will take a couple minutes to run. If you've run these cells before, rerunning them will load the model without redownloading it, which will take about 1 to 2 minutes.

```
def load_embedding_model():
    """ Load GloVe Vectors
        Return:
            wv_from_bin: All 400000 embeddings, each length 200
    """
    import gensim.downloader as api
    wv_from_bin = api.load("glove-wiki-gigaword-200")
    print("Loaded vocab size %i" % len(list(wv_from_bin.vocab.keys()))) # index_to_key doesn't
    return wv_from_bin

# -----
# Run Cell to Load Word Vectors
# Note: This will take a couple minutes
# -----
wv_from_bin = load_embedding_model()

[=====] 100.0% 252.1/252.1MB downloaded
Loaded vocab size 400000
```

Note: If you are receiving a "reset by peer" error, rerun the cell to restart the download. If you run into an "attribute" error, you may need to update to the most recent version of gensim and numpy. You can upgrade them inline by uncommenting and running the below cell:

```
!pip install gensim --upgrade
!pip install numpy --upgrade
```

```

Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-wheels/public
Requirement already satisfied: gensim in /usr/local/lib/python3.8/dist-packages (4.3.0)
Requirement already satisfied: numpy>=1.18.5 in /usr/local/lib/python3.8/dist-packages (1.22.4)
Requirement already satisfied: FuzzyTM>=0.4.0 in /usr/local/lib/python3.8/dist-packages (0.4.0)
Requirement already satisfied: smart-open>=1.8.1 in /usr/local/lib/python3.8/dist-packages (1.8.1)
Requirement already satisfied: scipy>=1.7.0 in /usr/local/lib/python3.8/dist-packages (1.7.0)
Requirement already satisfied: pyfume in /usr/local/lib/python3.8/dist-packages (from FuzzyTM) (0.4.0)
Requirement already satisfied: pandas in /usr/local/lib/python3.8/dist-packages (from FuzzyTM) (1.3.4)
Collecting numpy>=1.18.5
  Downloading numpy-1.22.4-cp38-cp38-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (16.9 MB)
    16.9/16.9 MB 59.6 MB/s eta 0:00:00
Requirement already satisfied: pytz>=2017.3 in /usr/local/lib/python3.8/dist-packages (from pandas) (2022.1)
Requirement already satisfied: python-dateutil>=2.7.3 in /usr/local/lib/python3.8/dist-packages (from pandas) (2.8.2)
Requirement already satisfied: fasttext-py in /usr/local/lib/python3.8/dist-packages (from FuzzyTM) (0.9.0)
Requirement already satisfied: simpy in /usr/local/lib/python3.8/dist-packages (from FuzzyTM) (4.0.1)
Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.8/dist-packages (from fasttext-py) (1.16.0)
Requirement already satisfied: miniflow in /usr/local/lib/python3.8/dist-packages (from fasttext-py) (0.10.0)
Requirement already satisfied: requests in /usr/local/lib/python3.8/dist-packages (from fasttext-py) (2.28.1)
Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/python3.8/dist-packages (from requests) (2022.9.24)
Requirement already satisfied: chardet<5,>=3.0.2 in /usr/local/lib/python3.8/dist-packages (from requests) (3.0.4)
Requirement already satisfied: urllib3<1.27,>=1.21.1 in /usr/local/lib/python3.8/dist-packages (from requests) (1.26.13)
Requirement already satisfied: idna<3,>=2.5 in /usr/local/lib/python3.8/dist-packages (from requests) (3.3)
Installing collected packages: numpy
  Attempting uninstall: numpy
    Found existing installation: numpy 1.24.2
    Uninstalling numpy-1.24.2:
      Successfully uninstalled numpy-1.24.2
Successfully installed numpy-1.22.4
Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-wheels/public
Requirement already satisfied: numpy in /usr/local/lib/python3.8/dist-packages (1.22.4)
Collecting numpy
  Using cached numpy-1.24.2-cp38-cp38-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (17.1 MB)
Installing collected packages: numpy
  Attempting uninstall: numpy
    Found existing installation: numpy 1.22.4
    Uninstalling numpy-1.22.4:
      Successfully uninstalled numpy-1.22.4

```

## ▼ Reducing dimensionality of Word Embeddings

Let's directly compare the GloVe embeddings to those of the co-occurrence matrix. In order to avoid running out of memory, we will work with a sample of 10000 GloVe vectors instead. Run the following cells to:

1. Put 10000 Glove vectors into a matrix M
2. Run `reduce_to_k_dim` (your Truncated SVD function) to reduce the vectors from 200-dimensional to 2-dimensional.

```

def get_matrix_of_vectors(wv_from_bin, required_words):
    """ Put the GloVe vectors into a matrix M.
    Param:

```

wv\_from\_bin: KeyedVectors object; the 400000 GloVe vectors loaded from file

Return:

M: numpy matrix shape (num words, 200) containing the vectors  
word2ind: dictionary mapping each word to its row number in M

"""

```
import random
words = list(wv_from_bin.vocab.keys()) # index_to_key doesn't work --
print("Shuffling words ...")
random.seed(225)
random.shuffle(words)
words = words[:10000]
print("Putting %i words into word2ind and matrix M..." % len(words))
word2ind = {}
M = []
curInd = 0
for w in words:
    try:
        M.append(wv_from_bin.get_vector(w))
        word2ind[w] = curInd
        curInd += 1
    except KeyError:
        continue
for w in required_words:
    if w in words:
        continue
    try:
        M.append(wv_from_bin.get_vector(w))
        word2ind[w] = curInd
        curInd += 1
    except KeyError:
        continue
M = np.stack(M)
print("Done.")
return M, word2ind
```

```
# -----
# Run Cell to Reduce 200-Dimensional Word Embeddings to k Dimensions
# Note: This should be quick to run
# -----
```

```
M, word2ind = get_matrix_of_vectors(wv_from_bin, words)
M_reduced = reduce_to_k_dim(M, k=2)
```

```
# Rescale (normalize) the rows to make them each of unit-length
M_lengths = np.linalg.norm(M_reduced, axis=1)
M_reduced_normalized = M_reduced / M_lengths[:, np.newaxis] # broadcasting
```

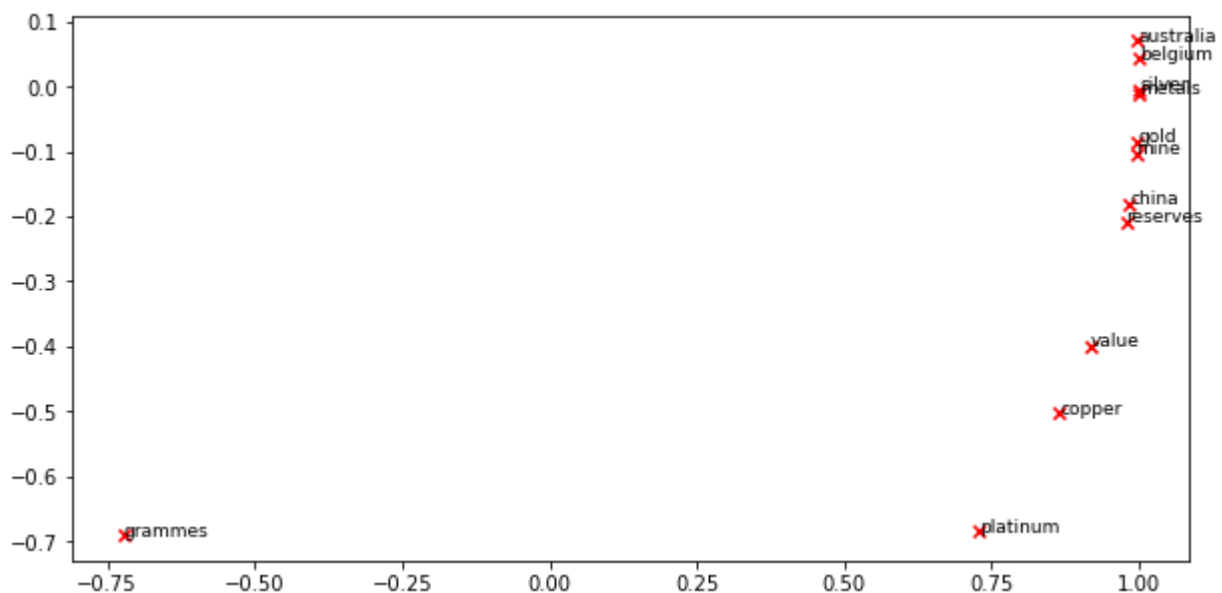
```
Shuffling words ...
Putting 10000 words into word2ind and matrix M...
Done.
Running Truncated SVD over 10012 words...
Done.
```

**Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly. If you still have problems with loading the embeddings onto your local machine after this, please go to office hours or contact course staff.**

### ▼ Question 2.1: GloVe Plot Analysis [written] (3 points)

Run the cell below to plot the 2D GloVe embeddings for ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', 'belgium', 'australia', 'china', 'grammes', 'mine'].

```
words = ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', 'belgium', 'australia', 'china', 'grammes', 'mine']
plot_embeddings(M_reduced_normalized, word2ind, words)
```



a. What is one way the plot is different from the one generated earlier from the co-occurrence matrix? What is one way it's similar?

### ▼ The word "grammes" has become separated from other words.

The words "value" and "reserves" have gone lower.

The word "china" has gone higher.

The word "silver" is close to "metal" and "gold".



The pairs "australia" and "belgium", "gold" and "mine" are still next to each other.

b. What is a possible cause for the difference?

Glove model is based on global word to word co-occurrence counts the entire corpus but the first one is based on the other co-occurrence within local context (neighbouring words). In practice, however, both these models give similar results for many tasks.

## Cosine Similarity

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective [L1](#) and [L2](#) Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:



Instead of computing the actual angle, we can leave the similarity in terms of  $similarity = \cos(\Theta)$ . Formally the [Cosine Similarity](#)  $s$  between two vectors  $p$  and  $q$  is defined as:

$$s = \frac{p \cdot q}{||p|| ||q||}, \text{ where } s \in [-1, 1]$$

### ▼ Question 2.2: Words with Multiple Meanings (1.5 points) [code + written]

Polysemes and homonyms are words that have more than one meaning (see this [wiki page](#) to learn more about the difference between polysemes and homonyms ). Find a word with *at least two different meanings* such that the top-10 most similar words (according to cosine similarity) contain related words from *both* meanings. For example, "leaves" has both "go\_away" and "a\_structure\_of\_a\_plant" meaning in the top 10, and "scoop" has both "handed\_waffle\_cone" and "lowdown". You will probably need to try several polysemous or homonymic words before you find one.

Please state the word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous or homonymic words you tried didn't work (i.e. the top-10 most similar words only contain **one** of the meanings of the words)?

**Note:** You should use the `wv_from_bin.most_similar(word)` function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance, please check the [GenSim documentation](#).

```
### SOLUTION BEGIN
```

```
wv_from_bin.most_similar("bank")
```

```
### SOLUTION END
```

```
[('banks', 0.7625691890716553),  
 ('banking', 0.6818838119506836),  
 ('central', 0.6283639669418335),  
 ('financial', 0.6166563034057617),  
 ('credit', 0.6049750447273254),  
 ('lending', 0.5980608463287354),  
 ('monetary', 0.5963002443313599),  
 ('bankers', 0.5913101434707642),  
 ('loans', 0.5802938938140869),  
 ('investment', 0.5740202069282532)]
```

selected word = "bank"

Because one meaning may come more than the other meanings and remove them and generally it depends on the corpus. The other reason might be that we have one vector for each word so it would be difficult to discover a word with multiple meanings.

### ▼ Question 2.3: Synonyms & Antonyms (2 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply  $1 - \text{Cosine Similarity}$ .

Find three words  $(w_1, w_2, w_3)$  where  $w_1$  and  $w_2$  are synonyms and  $w_1$  and  $w_3$  are antonyms, but  $\text{Cosine Distance}(w_1, w_3) < \text{Cosine Distance}(w_1, w_2)$ .

As an example,  $w_1 = \text{"happy"}$  is closer to  $w_3 = \text{"sad"}$  than to  $w_2 = \text{"cheerful"}$ . Please find a different example that satisfies the above. Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the `wv_from_bin.distance(w1, w2)` function here in order to compute the cosine distance between two words. Please see the [GenSim documentation](#) for further assistance.

```
#### SOLUTION BEGIN
```

```
w1 = "tired"
w2 = "bored"
w3 = "fresh"
w1_w2_dist = wv_from_bin.distance(w1, w2)
w1_w3_dist = wv_from_bin.distance(w1, w3)

print("Synonyms {}, {} have cosine distance: {}".format(w1, w2, w1_w2_dist))
print("Antonyms {}, {} have cosine distance: {}".format(w1, w3, w1_w3_dist))
```

```
#### SOLUTION END
```

```
Synonyms tired, bored have cosine distance: 0.34196406602859497
Antonyms tired, fresh have cosine distance: 0.7548569738864899
```

Again, according to the corpus, the second pair of words may have come together more often. Because we considered the co-occurrence of the words and not the closeness of the meanings.

### ▼ Question 2.4: Analogies with Word Vectors [written] (1.5 points)

Word vectors have been shown to *sometimes* exhibit the ability to solve analogies.

As an example, for the analogy "man : grandfather :: woman : x" (read: man is to grandfather as woman is to x), what is x?

In the cell below, we show you how to use word vectors to find x using the `most_similar` function from the [GenSim documentation](#). The function finds words that are most similar to the words in the

positive list and most dissimilar from the words in the negative list (while omitting the input words, which are often the most similar; see [this paper](#)). The answer to the analogy will have the highest cosine similarity (largest returned numerical value).

```
# Run this cell to answer the analogy -- man : grandfather :: woman : x
pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'grandfather'], negative=['man']))

[('grandmother', 0.7608444690704346),
 ('granddaughter', 0.7200808525085449),
 ('daughter', 0.7168302536010742),
 ('mother', 0.7151535749435425),
 ('niece', 0.7005682587623596),
 ('father', 0.6659887433052063),
 ('aunt', 0.6623408794403076),
 ('grandson', 0.6618767976760864),
 ('grandparents', 0.6446609497070312),
 ('wife', 0.6445354223251343)]
```

Let  $m$ ,  $g$ ,  $w$ , and  $x$  denote the word vectors for man, grandfather, woman, and the answer, respectively. Using **only** vectors  $m$ ,  $g$ ,  $w$ , and the vector arithmetic operators  $+$  and  $-$  in your answer, to what expression are we maximizing  $x$ 's cosine similarity?

Hint: Recall that word vectors are simply multi-dimensional vectors that represent a word. It might help to draw out a 2D example using arbitrary locations of each vector. Where would man and woman lie in the coordinate plane relative to grandfather and the answer?

$$x = g - m + w$$

$x$  and grandfather would lie in same distance between man and woman.

## Question 2.5: Finding Analogies [code + written] (1.5 points)

a. For the previous example, it's clear that "grandmother" completes the analogy. But give an intuitive explanation as to why the `most_similar` function gives us words like "granddaughter", "daughter", or "mother?"

▼ Because these words are close to each other in our vector space.

b. Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form  $x:y :: a:b$ . If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

**Note:** You may have to try many analogies to find one that works!

```
### SOLUTION BEGIN
```

```
x, y, a, b = "north", "south", "east", "west"
wv_from_bin.most_similar(positive=[a, y], negative=[x])[0][0]
```

```
### SOLUTION END
```

```
'west'
```

north:south :: east:west

As I expected, the relation between "north" and "south" is similar to relation between "east" and "west", and They are easy pairs that most of the time use.

### ▼ Question 2.6: Incorrect Analogy [code + written] (1.5 points)

a. Below, we expect to see the intended analogy "hand : glove :: foot : **sock**", but we see an unexpected result instead. Give a potential reason as to why this particular analogy turned out the way it did?

```
pprint.pprint(wv_from_bin.most_similar(positive=['foot', 'glove'], negative=['hand']))
```

```
[('45,000-square', 0.4922032356262207),
 ('15,000-square', 0.4649604558944702),
 ('10,000-square', 0.45447561144828796),
 ('6,000-square', 0.44975775480270386),
 ('3,500-square', 0.4441334009170532),
 ('700-square', 0.44257503747940063),
 ('50,000-square', 0.4356396794319153),
 ('3,000-square', 0.43486517667770386),
 ('30,000-square', 0.4330596923828125),
 ('footed', 0.43236875534057617)]
```

▼ Our vector space doesn't work very well sometimes and I think It's depends on corpus. Maybe the word "sock" is rare in the corpus or it hasn't come at all.

b. Find another example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form  $x:y :: a:b$ , and state the **incorrect** value of  $b$  according to the word vectors (in the previous example, this would be '**45,000-square**').

```
### SOLUTION BEGIN
```

```
x, y, a, b = "white", "black", "sun", "moon"
pprint.pprint(wv_from_bin.most_similar(positive=[a, y], negative=[x]))
```

```
### SOLUTION END
```

```
[('sky', 0.5087384581565857),
 ('bright', 0.4660125970840454),
 ('moon', 0.4504569172859192),
 ('jiazheng', 0.4423024654388428),
 ('shine', 0.43356406688690186),
 ('shines', 0.43294209241867065),
 ('earth', 0.4307621419429779),
 ('solar', 0.4234520196914673),
 ('blue', 0.420571506023407),
 ('light', 0.41411280632019043)]
```

white:black :: sun:moon

I expected the model to notice the contrast in the first pair and return the word "moon" instead of "sky"!

### ▼ Question 2.7: Guided Analysis of Bias in Word Vectors [written] (1 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit in our word embeddings. Bias can be dangerous because it can reinforce stereotypes through applications that employ these models.

Run the cell below, to examine (a) which terms are most similar to "woman" and "profession" and most dissimilar to "man", and (b) which terms are most similar to "man" and "profession" and most dissimilar to "woman". Point out the difference between the list of female-associated words and the list of male-associated words, and explain how it is reflecting gender bias.

```
# Run this cell
# Here `positive` indicates the list of words to be similar to and `negative` indicates the 1
# most dissimilar from.
```

```
pprint.pprint(wv_from_bin.most_similar(positive=['man', 'profession'], negative=['woman']))
print()
pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'profession'], negative=['man']))
```

```
[('reputation', 0.5250176191329956),
 ('professions', 0.5178038477897644),
 ('skill', 0.49046966433525085),
 ('skills', 0.49005505442619324),
 ('ethic', 0.4897659420967102),
```

```
(('business', 0.4875851273536682),
 ('respected', 0.4859202802181244),
 ('practice', 0.4821045994758606),
 ('regarded', 0.47785723209381104),
 ('life', 0.4760662317276001])

[(('professions', 0.5957458019256592),
 ('practitioner', 0.498841255903244),
 ('teaching', 0.48292142152786255),
 ('nursing', 0.4821180999279022),
 ('vocation', 0.4788966178894043),
 ('teacher', 0.47160351276397705),
 ('practicing', 0.46937811374664307),
 ('educator', 0.46524325013160706),
 ('physicians', 0.4628995358943939),
 ('professionals', 0.4601394236087799))]
```

Most similar word to man is "reputation"! and the most similar word to woman is "professions". The words similar to man are more abstract like skill, regarded while the words similar to woman are more practical like teacher, nursing.

### Question 2.8: Independent Analysis of Bias in Word Vectors [code + written] (1 point)

Use the `most_similar` function to find another pair of analogies that demonstrates some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

### SOLUTION BEGIN

```
A = "man"
B = "woman"
word = "worker"
pprint.pprint(wv_from_bin.most_similar(positive=[A, word], negative=[B]))
print()
pprint.pprint(wv_from_bin.most_similar(positive=[B, word], negative=[A]))
```

### SOLUTION END

```
(('workers', 0.6113258004188538),
 ('employee', 0.5983108282089233),
 ('working', 0.5615328550338745),
 ('laborer', 0.5442320108413696),
 ('unemployed', 0.5368517637252808),
 ('job', 0.5278826951980591),
 ('work', 0.5223963260650635),
 ('mechanic', 0.5088937282562256),
 ('worked', 0.505452036857605),
```

```
('factory', 0.4940453767776489)]  
  
[('employee', 0.6375863552093506),  
 ('workers', 0.6068919897079468),  
 ('nurse', 0.5837947726249695),  
 ('pregnant', 0.5363885164260864),  
 ('mother', 0.5321309566497803),  
 ('employer', 0.5127025842666626),  
 ('teacher', 0.5099576711654663),  
 ('child', 0.5096741914749146),  
 ('homemaker', 0.5019454956054688),  
 ('nurses', 0.4970572590827942)]
```

The words that relate to man are all about work and job while the words relate to woman has some words like pregnant, child and homemaker in the concept of job!

### Question 2.9: Thinking About Bias [written] (2 points)

a. Give one explanation of how bias gets into the word vectors. Briefly describe a real-world example that demonstrates this source of bias.

- ▼ The bias here is picked up from the text on which these algorithms are trained.

For example the word "homemaker" often comes with the word "woman".

[source](#)

b. What is one method you can use to mitigate bias exhibited by word vectors? Briefly describe a real-world example that demonstrates this method.

1. Cleaning the corpus itself

2. Hard Debiasing

3. Soft Debiasing

For example, the word doctor seems like a word we should neutralize to make it non-gender-specific or non-ethnicity-specific. Whereas the words grandmother and grandfather or beard should not be made non-gender-specific.

[source](#)



## Submission Instructions

1. Click the Save button at the top of the Jupyter Notebook.
2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).
3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
4. Once you've rerun everything, select File -> Download as -> PDF via LaTeX (If you have trouble using "PDF via LaTeX", you can also save the webpage as pdf. **Make sure all your solutions especially the coding parts are displayed in the pdf**, it's okay if the provided codes get cut off because lines are not wrapped in code cells).
5. Look at the PDF file and make sure all your solutions are there, displayed correctly. The PDF is the only thing your graders will see!
6. Submit your PDF on Gradescope.

