

$$8. H_0: \sigma^2 = 1.2^2, H_1: \sigma^2 \neq 1.2^2$$

$$\chi^2 = \frac{(n-1) \cdot S^2}{\sigma_0^2} \stackrel{H_0}{\sim} \chi^2(n-1)$$

$$\text{代入 } S = 2.1, n = 15: \chi_{0.025}(14) = 26.119, \chi_{0.975}(14) = 5.629$$

$$\therefore W = \{ \chi^2 > \chi_{0.025}^2(14) \} \cup \{ \chi^2 < \chi_{0.975}^2(14) \}$$

$$\text{而 } \hat{\chi}^2 = \frac{14 \times 2.1^2}{1.2^2} = 42.875, \text{ 在拒绝域}$$

接受 H_1 , 拒绝 H_0 , 有显著变化

9. 对于标准差:

$$H_0: \sigma^2 \leq 0.3^2, H_1: \sigma^2 > 0.3^2$$

$$\chi^2 = \frac{(n-1) \cdot S^2}{\sigma_0^2} \stackrel{H_0}{\sim} \chi^2(n-1)$$

$$W: \{ \chi^2 > \chi_{0.05}^2(n-1) \}$$

$$n = 9: \chi_{0.05}^2(8) = 15.507$$

$$\text{代入数据 } \hat{\chi}^2 = \frac{8 \times 0.55}{0.3^2} = 48.889$$

落在拒绝域, 接受 H_1 , 拒绝 H_0 , 有显著差异

对于均值:

$$H_0: \mu = 18, H_1: \mu \neq 18$$

$$T = \frac{\bar{X} - \mu_0}{S / \sqrt{n}} \stackrel{H_0}{\sim} t(n-1)$$

$$W: \{ |T| > t_{0.025}(n-1) \}$$

$$n = 9, t_{0.025}(8) = 2.306$$

$$\hat{T} = \frac{\bar{X} - \mu_0}{S / \sqrt{n}} = \frac{17.5 - 18}{\sqrt{0.55/9}} = 2.0226$$

不在拒绝域, 接受 H_0 , 拒绝 H_1 , 无明显差异

综上, 存在质量问题