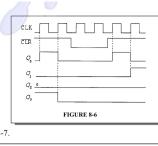


Each flip-flop is initially reset

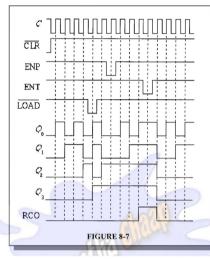
Lacii iiip	nop i	J IIIICIGI	ily rese					
CLK	$J_0K_0$	$J_1K_1$	$J_2K_2$	$J_3K_3$	$Q_0$	$Q_1$	$Q_2$	$Q_3$
1	1	0	0	0	1	0	0	0
2	1	1	0	0	0	1	0	0
3	1	0	0	0	1	1	0	0
4	1	1	1	0	0	0	1	0
5	1	0	0	0	1	0	1	0
6	1	1	0	0	0	1	1	0
7	1	0	0	0	1	1	1	0
8	1	1	1	1	0	0	0	1
9	1	0	0	0	1	0	0	1
10	1	0	0	1	0	0	0	0

FIGURE 8-4

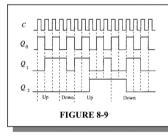


See Figure 8-7.

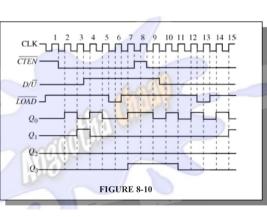
11. See Figure 8-6.



14. See Figure 8-9.



15 See Figure 8-10.



	$Q_2$	$Q_1$	$Q_0$	$D_2$	$D_1$	$D_0$
Initially	0	0	0	0	0	1
At CLK 1	0	0	1	0	1	1
At CLK 2	0	1	1	1	1	1
At CLK 3	1	1	1	1	1	0
At CLK 4	1	1	0	1	0	0
At CLK 5	1	0	0	0	0	1
At CLK 6	0	0	1	0	1	1

The sequence is 000 to 001 to 011 to 111 to 110 to 100 and back to 001, etc.

ı		
	1	

	FF3	FF2	FF1	FF0	$Q_3$	$Q_2$	$Q_1$	$Q_0$
Initially	Tog	Tog	Tog	Tog	0	0	0	0
After CLK 1	NC	NC	NC	Tog	1	1	1	1
After CLK 2	NC	NC	Tog	Tog	1	1	1	0
After CLK 3	NC	Tog	Tog	Tog	1	1	0	1
After CLK 4	Tog	Tog	Tog	Tog	1	0	1	0
After CLK 5	Tog	Tog	Tog	Tog	0	1	0	_1_

Tog = toggle, NC = no change

The counter locks up in the 1010 and 0101 states, alternating between them.



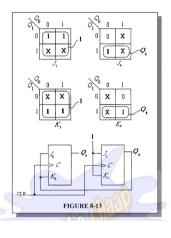
#### 18. NEXT-STATE TABLE

Preser	nt State	Next	State
$Q_1$	$Q_0$	$Q_1$	$Q_0$
0	0	1	0
1	0	0	1
0	1	1	1
1	1	0	0

### TRANSITION TABLE

	Transitions to next state)	Flip-Flop Inputs					
$Q_1$	$Q_0$	$J_1$	$K_1$	$J_0$	$K_0$		
0 to 1	0 to 0	[1]	X	0	X		
1 to 0	0 to 1	X	1	1	X		
0 to 1	1 to 1	1	X	X	0		
1 to 0	1 to 0	X	1	X	1		

See Figure 8-13.



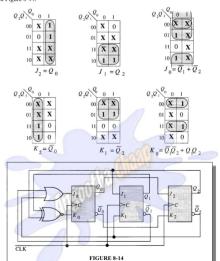
### ∖. NEXT-STATE TABLE

Pre	esent St	ate	Next State				
$Q_2$	$Q_1$	$Q_0$	$Q_2$	$Q_1$	$Q_0$		
0	0	1	1	0	0		
1	0	0	0	1	1		
0	1	1	1	0	1		
1	0	1	1	1	1		
1	1	1	1	1	0		
1	1	0	0	1	0		
0	1 /	0	0	0	1		

### TRANSITION TABLE

•	State Tra		Flip-flop Inputs								
$Q_2$	t state to no	$O_0$	$J_2$	$K_2$	$J_1$	$K_1$	$J_0$	$K_0$			
0 to 1	0 to 0	1 to 0	1	X	0	X	X	1			
1 to 0	0 to 1	0 to 1	X	1	1	X	1	X			
0 to 1	1 to 0	1 to 1	1	X	X	1	X	0			
1 to 1	0 to 1	1 to 1	X	0	1	X	X	0			
1 to 1	1 to 1	1 to 0	X	0	X	0	X	1			
0 to 0	1 to 0	0 to 1	0	X	X	1	1	X			
1 to 0	1 to 1	0 to 0	X	1	X	0	0	$\mathbf{X}$			

### See Figure 8-14.



## 2 NEXT-STATE TABLE

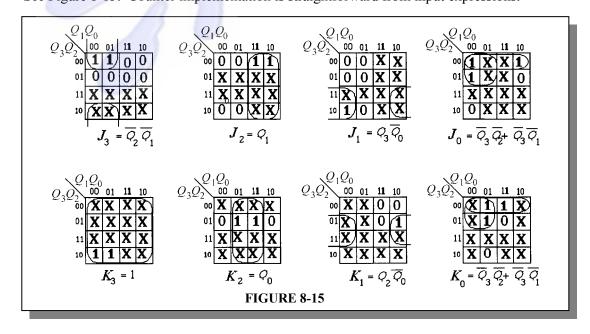
P	resen	t Sta	te	]	Next	State	
$Q_3$	$Q_2$	$Q_1$	$Q_0$	$Q_3$	$Q_2$	$Q_1$	$Q_0$
0	0	0	0	1	0	0	1
1	0	0	1	0	0	0	1
0	0	0	1	1	0	0	0
1	0	0	0	0	0	1	0
0	0	1	0	0	1	1	1
0	1	1	1	0	0	1	1
0	0	1	1	0	1	1	0
0	1	1	0	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	0	0	0

## TRANSITION TABLE

Out	put State	e Transi	tion			F	lip-fl	op Inputs		
(Pres	ent State	to next s	state)							
$Q_3$	$Q_2$	$Q_1$	$Q_0$	$J_3$	$K_3$	$J_2$	$K_2$	$J_1  K_1$	$J_0$	$K_0$
0 to 1	0 to 0	0 to 0	0 to 1	1	X	0	X	0 X	1	X
1 to 0	0 to 0	0 to 0	0 to 1	X	1	0	X	0 X	X	0
0 to 1	0 to 0	0 to 0	1 to 0	1	X	0	X	0 X	X	1
1 to 0	0 to 0	0 to 1	0 to 0	X	1	0	X	1 X	0	X
0 to 0	0 to 1	1 to 1	0 to 1	0	X	1	X	X 0	1	X
0 to 0	1 to 0	1 to 1	1 to 1	0	X	X	1	X 0	X	0
0 to 0	0 to 1	1 to 1	1 to 0	0	X	1	X	X 0	X	1
0 to 0	1 to 1	1 to 0	0 to 0	0	X	X	0	X 1	0	X
0 to 0	1 to 1	0 to 0	0 to 1	0	X	X	0	0 X	1	X
0 to 0	1 to 0	0 to 0	1 to 0	0	X	X	1	0 X	X	1

Binary states for 10, 11, 12, 13, 14, and 15 are unallowed and can be represented by don't cares.

See Figure 8-15. Counter implementation is straightforward from input expressions.





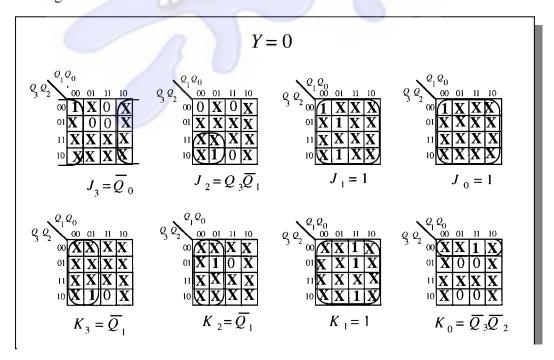
## NEXT-STATE TABLE

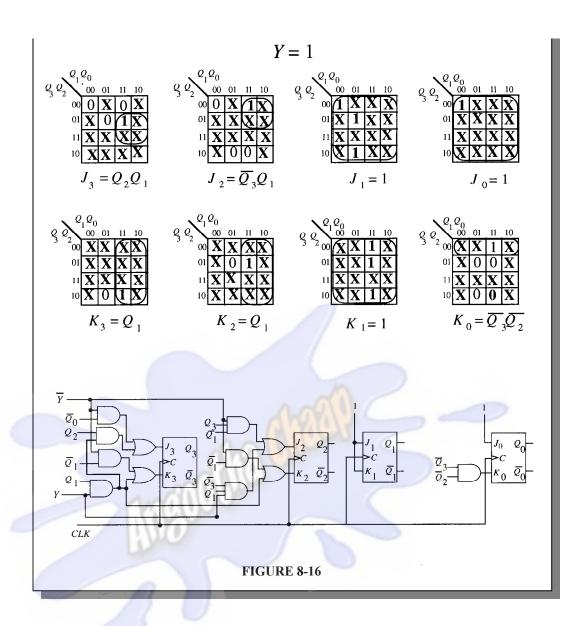
P	resen	nt State Next State						Next State				
				Y	T = 1 (U	Jp)		Y = 0 (Down)				
$Q_3$	$Q_2$	$Q_1$	$Q_0$	$Q_3$	$Q_2$	$Q_1$	$Q_0$	$Q_3$	$Q_2$	$Q_1$	$Q_0$	
0	0	0	0	0	0	1	1	1	0	1	1	
0	0	1	1	0	1	0	1	0	0	0	0	
0	1	0	1	0	1	1	1	0	0	1	1	
0	1	1	1	1	0	0	1	0	1	0	1	
1	0	0	1	1	0	1	1	0	1	1	1	
1	0	1	1	0	0	0	0	1	0	0	1	

## TRANSITION TABLE

Ou	tput State	Transit	ions	Y		Flip-flop	o Inputs	
(Pre	sent State	to next s	tate)					
$Q_3$	$Q_2$	$Q_1$	$Q_0$		$J_3K_3$	$J_2K_2$	$J_1K_1$	$J_0K_0$
0 to 1	0 to 0	0 to 1	0 to 1	0	1X	0X	1X	1X
0 to 0	0 to 0	0 to 1	0 to 1	1	0X	0X	1X	1X
0 to 0	0 to 0	1 to 0	1 to 0	0	0X	0X	X1	X1
0 to 0	0 to 1	1 to 0	1 to 1	1	0X	1X	X1	X0
0 to 0	1 to 0	0 to 1	1 to 1	0	0X	X1	1X	X0
0 to 0	1 to 1	0 to 1	1 to 1	1	0X	X0	1X	X0
0 to 0	1 to 1	1 to 0	1 to 1	0	0X	X0	X1	X0
0 to 1	1 to 0	1 to 0	1 to 1	1	1X	X1	X1	X0
1 to 0	0 to 1	0 to 1	1 to 1	0	X1	1X	1X	X0
1 to 1	0 to 0	0 to 1	1 to 1	1	X0	0X	1X	X0
1 to 1	0 to 0	1 to 0	1 to 1	0	X0	0X	X1	X0
1 to 0	0 to 0	1 to 0	1 to 0	1	X1	0X	X1	X1

See Figure 8-16.





# Section 8-5 Cascaded Counters

**24** (a) Modulus = 
$$4 \times 8 \times 2 = 64$$

$$f_1 = \frac{1 \text{ kHz}}{4} = 250 \text{ Hz}$$
  
 $f_2 = \frac{250 \text{ Hz}}{8} = 31.25 \text{ Hz}$   
 $f_3 = \frac{31.25 \text{ Hz}}{2} = 15.625 \text{ Hz}$ 

(b) Modulus = 
$$10 \times 10 \times 10 \times 2 = 2000$$
  
$$f_1 = \frac{100 \text{ k}}{10}$$

(c)

(d)

$$f_1 = \frac{100 \text{ kHz}}{10} = 10 \text{ kHz}$$

$$f_2 = \frac{10 \text{ kHz}}{10} = 1 \text{ kHz}$$

$$f_3 = \frac{1 \text{ kHz}}{10} = 100 \text{ Hz}$$
  
 $f_4 = \frac{100 \text{ Hz}}{2} = 50 \text{ Hz}$ 

(c) Modulus = 
$$3 \times 6 \times 8 \times 10 \times 10 = 14400$$

$$f_1 = \frac{21\,\mathrm{MHz}}{3} = 7\,\mathrm{MHz}$$

$$f_2 = \frac{7 \text{ MHz}}{6} = 1.167 \text{ MHz}$$

$$f_3 = \frac{1.167 \text{ MHz}}{8} = 145.875 \text{ kHz}$$
  
 $f_3 = \frac{145.875 \text{ kHz}}{8} = 145.875 \text{ kHz}$ 

$$f_4 = \frac{145.875 \text{ kHz}}{10} = 14.588 \text{ kHz}$$
  
 $f_5 = \frac{14.588 \text{ kHz}}{10} = 1.459 \text{ kHz}$ 

$$Modulus = 2 \times 4 \times 6 \times 8 \times 16 = 6144$$

$$f_1 = \frac{39.4 \text{ kHz}}{2} = 19.7 \text{ kHz}$$

$$f_2 = \frac{19.7 \text{ kHz}}{4} = 4.925 \text{ kHz}$$

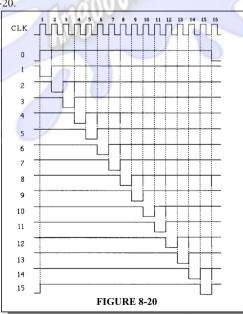
$$f_2 = \frac{19.7 \text{ kHz}}{4} = 4.925 \text{ kHz}$$

$$f_3 = \frac{4.925 \text{ kHz}}{6} = 820.83 \text{ Hz}$$

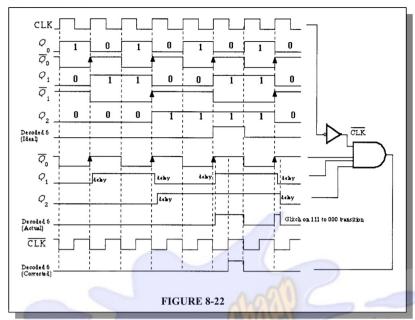
$$f_4 = \frac{820.683}{8} = 102.6 \text{ Hz}$$

$$f_4 = \frac{820.683}{8} = 102.6 \text{ Hz}$$

$$f_5 = \frac{8}{102.6 \,\mathrm{Hz}} = 6.41 \,\mathrm{Hz}$$



3 , See Figure 8-22.



3 ψ. For the digital clock, the counter output frequencies are: **Divide-by-60 input counter:** 

$$\frac{60\,\mathrm{Hz}}{60} = 1\,\mathrm{Hz}$$

## **Seconds counter:**

$$\frac{1 \, Hz}{60} = 16.7 \text{ mHz}$$

## **Minutes counter:**

$$\frac{16.7 \text{ mHz}}{60} = 278 \text{ } \mu\text{Hz}$$

## **Hours counter:**

$$\frac{278 \,\mu\text{Hz}}{12} = 23.1 \,\mu\text{Hz}$$

$$35.53 + 37 - 22 = 68$$