

10. $X Y=1$	0	1
$P(X Y=1)$	$\frac{1}{4}$	$\frac{3}{4}$

$X Y \neq 1$	0	1
$P(X Y \neq 1)$	$\frac{1}{2}$	$\frac{1}{2}$

$$\frac{(n-1)!}{(n-1)! \cdot 0! \cdot 1!}$$

$$-\frac{x^3}{2} e^{-x-xy}$$

$$11. P(X_i=1 | X_1+X_2+\dots+X_n=r) = \frac{p \cdot C_{n-1}^{r-1} \cdot p^{r-1} \cdot (1-p)^{n-r}}{C_n^r p^r (1-p)^{n-r}} = \frac{r}{n}$$

$$\therefore P(X_i=0 | X_1+X_2+\dots+X_n=r) = 1 - \frac{r}{n}$$

$X_i X_1+X_2+\dots+X_n=r$	0	1
$P(X_i X_1+X_2+\dots+X_n=r)$	$1 - \frac{r}{n}$	$\frac{r}{n}$

$$14. (1) f_X(x) = \int_0^\infty \frac{x^3}{2} e^{-x-xy} dy = \frac{x^2}{2} e^{-x}, x > 0$$

$$f_X(x) = 0, x \leq 0$$

$$(2) f_{Y|X}(y|x) = \frac{f(x,y)}{f_X(x)} = \begin{cases} x e^{-xy}, & x, y > 0 \\ 0, & \text{其它} \end{cases}$$

$$f_{Y|X}(y|x=0.5) = \begin{cases} 0.5 e^{-0.5y}, & y > 0 \\ 0, & \text{其它} \end{cases}$$

$$-e^{-0.5y}$$

$$(3) P(Y \geq 1 | X=0.5) = \int_1^\infty f_{Y|X}(y|x=0.5) dy = e^{-0.5}$$

$$15. (1) f(x,y) = f_X(x) \cdot f_{Y|X}(y|x) = \frac{1+xy}{3}, 0 < x < 2, 0 < y < 1$$

$$f(x,y) = 0, \text{其它}$$

$$(2) f_Y(y) = \int_0^2 \frac{1+xy}{3} dx = \frac{2}{3} + \frac{2}{3}y, 0 < y < 1$$

$$f_Y(y) = 0, \text{其它}$$

$$(3) f_{X|Y}(x|y) = \frac{f(x,y)}{f_Y(y)} = \frac{1+xy}{2+2y}, 0 < x < 2, 0 < y < 1$$

$$f_{X|Y}(x|y) = 0, \text{其它}$$

$$\frac{4}{5}x + \frac{6}{5}y$$

$$\frac{3}{5}y^2 + \frac{4}{5}xy$$

$$\frac{3}{5}x + \frac{2}{5}x^2$$

$$0.6 - 0.48 = 0.12$$

$$16. (1) \int f_X(x) = \int_0^1 f(x,y) dy = \frac{3}{5} + \frac{4}{5}x, 0 \leq x \leq 1$$

$$f_X(x) = 0, \text{其他}$$

$$P(X > 0.8) = \int_{0.8}^1 \left(\frac{3}{5} + \frac{4}{5}x \right) dx = 0.264$$

$$(2) f_{X|Y}(X|Y) = \frac{f(x,y)}{f_Y(y)} = \frac{2x+3y}{3y+1}, 0 \leq y \leq 1$$

$$\int f_Y(y) = \int_0^1 f(x,y) dx = \frac{6}{5}y + \frac{2}{5}, 0 \leq y \leq 1$$

$$f_Y(y) = 0, \text{其他}$$

$$(3) P(0.6 \leq X \leq 0.8 | Y=0.3) = \int_{0.6}^{0.8} \frac{19}{10} \cdot \left(2x + \frac{9}{10} \right) dx = 0.874$$

$$\text{补: } (X,Y) \sim N(1,2; 3,4; -0.3)$$

$$\text{则 } X \sim N(1,2), P(X < 2) = \Phi\left(\frac{2-1}{\sqrt{2}}\right) = \Phi(0.707) = 0.7194$$

$$Y|X=2 \sim N(3 - 0.3 \cdot \sqrt{2} \cdot (2-1), 0.91 \times 4) = N(2.576, 3.64)$$

$$P(Y < 4 | X=2) = \Phi\left(\frac{4 - 2.576}{\sqrt{3.64}}\right) = 0.773$$