

$$\frac{15\%}{25\%} \quad \frac{3}{17}$$

$$14. P(AB) = 5\%, P(A\bar{B}) = 15\%, P(\bar{A}B) = 10\% \\ P(\bar{A}\bar{B}) = 70\%$$

$$(1) P(A) = P(AB) + P(A\bar{B}) = 20\%$$

$$P(B) = P(AB) + P(\bar{A}B) = 15\%$$

$$(2) P(B|A) = \frac{P(AB)}{P(A)} = 25\%$$

$$(3) P(B|\bar{A}) = \frac{P(\bar{A}B)}{P(\bar{A})} = 12.5\%$$

$$(4) P(A|\bar{B}) = \frac{P(A\bar{B})}{P(\bar{B})} = \frac{3}{17}$$

$$(5) P(A|B) = \frac{P(AB)}{P(B)} = \frac{1}{3}$$

$$16. (1) \frac{1}{C_{n-k+1}^1} = \frac{1}{n-k+1}$$

$$(2) P = \frac{n-1}{n} \cdot \frac{n-2}{n-1} \cdot \dots \cdot \frac{1}{n-k+1} = \frac{1}{n}$$

$$\frac{146}{200} \quad 73\% \\ \frac{27}{100} + \frac{17}{200} + \frac{15}{300}$$

19. 设 A 为选的人进入, B 为选到一级, C 为选到二级, D 为选到三级

$$P(A) = P(B)P(A|B) + P(C)P(A|C) + P(D)P(A|D)$$

$$= \frac{3}{10} \times \frac{9}{10} + \frac{11}{20} \times \frac{7}{10} + \frac{3}{20} \times \frac{1}{2} = 73\%$$

23. (1) 设  $A_i$  为有  $i$  件次品, B 为取出的是正品

$$P(B) = \sum_{i=0}^4 P(A_i)P(B|A_i) = \frac{1}{5} \left( 1 + \frac{3}{4} + \frac{2}{4} + \frac{1}{4} + 0 \right) = \frac{1}{2}$$

$$(2) P(A_0|B) = \frac{P(A_0B)}{P(B)} = \frac{P(B|A_0) \cdot P(A_0)}{\frac{1}{2}} = \frac{1 \times \frac{1}{5}}{\frac{1}{2}} = \frac{2}{5}$$

$$\begin{aligned} 27. P &= 0.5 \times (0.7 \times 0.2 + 0.8 \times 0.3) + 0.8 \times 0.7 \times 0.8 \\ &= 0.638 \end{aligned}$$

≈ 63.8%

补充是题:  $AB \cup \bar{A}$  与  $(C \cup D)$  独立

$$P[(AB \cup \bar{A}) \cap (C \cup D)] = P[(\bar{A} \cup B) \cap (C \cup D)]$$

$$= 1 - P[(A\bar{B}) \cup (\bar{C}\bar{D})] = 1 - P(A\bar{B}) - P(\bar{C}\bar{D}) + P(A\bar{B}\bar{C}\bar{D})$$

$$= P(\bar{A} \cup B) + 1 - P(\bar{C}\bar{D}) - (1 - P(A\bar{B}\bar{C}\bar{D}))$$

$$= P(\bar{A} \cup B) + P(C \cup D) - P[(\bar{A} \cup B) \cup (C \cup D)]$$

$$= P(\bar{A} \cup B) + P(C \cup D) - P(\bar{A} \cup B) - P(C \cup D) + P(\bar{A} \cup B) \cdot P(C \cup D)$$

$$= P(\bar{A} \cup B)P(C \cup D) = P(AB \cup \bar{A}) \cdot P(C \cup D)$$

得证