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CS-225: Discrete Structures in CS

Homework Assignment 2, Part 1

Exercise Set 3.1: Question # 16, 17, 18, 23, 24, 28    Set 3.2: Question # 2, 4

● Set 3.1 – Q#16, 17

- 16.a.  $\forall$  dinosaurs  $x$ ,  $x$  is extinct.
- 16.b.  $\forall$  real number  $x$ ,  $x$  is positive, negative, or zero.
- 16.c.  $\forall$  irrational number  $x$ ,  $x$  is not integers.
- 16.d.  $\forall$  logician  $x$ ,  $x$  is not lazy.
- 16.e.  $\forall$  integer  $x$ ,  $x^2$  is not equal to the number 2,147,581,953.
- 16.f.  $\forall$  real number  $x$ ,  $x^2$  is not equal to the number -1.
- 17.a.  $\exists$  an exercise  $x$  such that  $x$  has an answer.
- 17.b.  $\exists$  a real number  $x$  such that  $x$  is rational.

● Set 3.1 – Q#18

Let  $D$  be the set of all students at your school, and let  $M(s)$  be “ $s$  is a math major”, let  $C(s)$  be “ $s$  is a computer science student”, and let  $E(s)$  be “ $s$  is an engineering student”.

- a.  $\exists s \in D$  such that  $E(s) \wedge M(s)$ .
- b.  $\exists s \in D$ , if  $C(s)$  then  $E(s)$ .
- c.  $\exists s \in D$ , if  $C(s)$  then  $\sim E(s)$ .
- d.  $\exists s \in D$  such that  $C(s) \wedge M(s)$ .
- e.  $(\exists s \in D \text{ such that } C(s) \wedge E(s)) \wedge (\exists s \in D \text{ such that } C(s) \wedge \sim E(s))$

● Set 3.1 – Q#23, 24

- 23.a.  $\forall x$ , if  $x$  is an equilateral triangle, then  $x$  is isosceles.  
     $\forall$  equilateral triangle  $x$ ,  $x$  is isosceles.
- b.  $\forall x$ , if  $x$  is a computer science student, then  $x$  needs to take data structures.  
     $\forall$  computer science student  $x$ ,  $x$  needs to take data structures.
- 24.a.  $\exists$  a hatter  $x$  such that  $x$  is mad.  
     $\exists x$  such that  $x$  is a hatter and  $x$  is mad.
- b.  $\exists$  a question  $x$  such that  $x$  is easy.  
     $\exists x$  such that  $x$  is a question and  $x$  is easy.

● Set 3.1 – Q#28

- a. 0 is a positive real number.
- b. If a real number is negative, then its opposite number is a positive real number.
- c. All integers are real numbers.
- d. There exists a real number that is not an integer.

Set 3.2 – Q#2

a. b. c. f.

● Set 3.2 – Q#4

- a. Some dogs are not friendly.
- b. Some people are not happy.
- c. All suspicions were unsubstantiated.
- d. No estimates are accurate.