CBGL: Fast Passive Monte Carlo Global Localisation of 2D LIDAR Sensor

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Abstract-Navigation of a mobile robot is conditioned on the knowledge of its pose. In observer-based localisation configurations its initial pose may not be knowable in advance, leading to the need of its estimation. The Monte Carlo class of solutions disperse hypotheses in the environment's map, which gradually converge on an estimate. These methods are robust against noise but require motion and time, which may be economised on. Feature-based solutions require minimal estimation time but assume environmental structure, may be sensitive to noise, and require preprocessing and tuning. The method proposed in this article retains the positive qualities of the two main approaches to global localisation and avoids their pitfalls: it requires a single measurement from a 2D LIDAR sensor, assumes no motion, environmental structure, or parameter tuning in a perenvironment or sensor basis, and is robust against noise. A large number of tests, in real and simulated conditions, involving disparate environments and sensor properties, illustrate that the proposed method outperforms state-of-the-art methods of both classes in terms of pose discovery rate and execution time. The source code is available for download.

Index Terms—global localisation, 2D LIDAR, monte carlo, scan-to-map-scan matching

I. INTRODUCTION

In tasks involving navigation of a mobile robot the knowledge of its initial pose is a prerequisite, especially in contexts where an observer is used for pose tracking. However, not in all tasks is the robot's pose predictable or settable in advance, and this results in the need for its ad hoc estimation without priors. Various sensor and map modalities have been investigated in the literature; from 2D and 3D LIDAR sensors [1], [2], RGBD cameras [3], and RFID equipment [4], to keyframe-based submaps [5] and metric maps [6]. The latter combined with 2D LIDAR sensors have become the de facto means in mobile robot localisation and navigation due to the sensor's high measurement precision, high update frequency, almost no need for preprocessing, and low cost compared to 3D LIDAR sensors.

This article addresses the problem of Passive Global Localisation of a 2D LIDAR sensor in a metric map, i.e. the estimation of its location and orientation within the map, under complete locational and orientational uncertainty, without prescribing motion commands (to the mobile robot that the sensor is assumed mounted to) for further knowledge acquisition. The problem is formalised in Problem P:

Problem P. Let the unknown pose of an immobile 2D range sensor whose angular range is λ be $p(l, \theta)$, l = (x, y), with respect to the reference frame of map M. Let the

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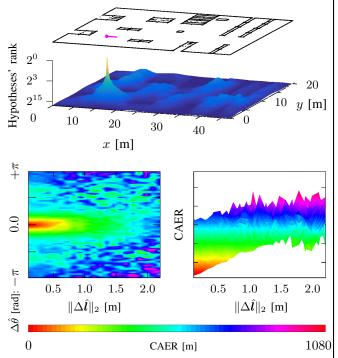


Fig. 1: Given a LIDAR sensor's 2D measurement, at its core, CBGL disperses pose hypotheses within the map and ranks them ascendingly according to the value of the Cumulative Absolute Error per Ray (CAER) metric. This produces a r(ank)-field which may be used to estimate the pose of the sensor (a) quickly due to the metric's low computational complexity, and (b) accurately due to (i) proportionality between the pose estimate error and the value of the metric for pose estimates in a neighbourhood of the sensor's pose, and (ii) lack of disproportionality outside of that neighbourhood. Top: a map of an environment, the pose of a panoramic 2D LIDAR sensor (magenta), and the corresponding CAER rank field below them. Bottom: distribution of CAER values by location $\Delta \hat{l}$ and orientation error $\Delta \hat{\theta}$ of all sensor pose hypotheses corresponding to the rank field above, for estimate position errors up to 2.0 m

range sensor measure range scan S_R . The objective is the estimation of p given M, λ , and S_R .

For the solution of Problem P this article introduces CBGL: a single-shot Monte Carlo method (a) which makes no assumptions regarding the structure or the particulars of the sensor's environment or the sensor's characteristics, (b) whose pose errors exhibit robustness to varying sensor angular range, and (c) which operates with three optionally-set and intuitive parameters, which trade accuracy for execution time. The central contributions of the article are:

• To the best of the author's knowledge the fastest Monte Carlo global localisation method that employs a 2D

LIDAR

- The extension and validation of the CAER metric's ability to infer pose error hierarchies solely from real and virtual range scans, extended from scan—to—mapscan matching (sm2) during pose-tracking (where pose errors are "small") to the context of global localisation, where hypotheses' errors may be arbitrarily large
- The thorough evaluation of the proposed method against

 (a) established state-of-the-art localisation methods,
 (b) real and publicly available benchmark conditions, and
 (c) varying characteristics of environments and sensors, which target real conditions that pose hindrances to global localisation methods

The rest of the paper is structured as follows: Section II provides necessary definitions and the notation employed. Section III gives a brief review of the literature of solutions to problem P, and the relation of the proposed method to them. The latter's methodology is presented in section IV, its evaluation in section V, and its limitations in section VI. Section VII concludes this study.

II. DEFINITIONS AND NOTATION

Let $\mathcal{A} = \{\alpha_i : \alpha_i \in \mathbb{R}\}, i \in \mathbb{I} = \langle 0, 1, \dots, n-1 \rangle$, denote a set of n elements, $\langle \cdot \rangle$ denote an ordered set, \mathcal{A}_{\uparrow} the set \mathcal{A} ordered in ascending order, the bracket notation $\mathcal{A}[\mathbb{I}] = \mathcal{A}$ denote indexing, and notation $\mathcal{A}_{k:l}$, $0 \leq k \leq l$, denote limited indexing: $\mathcal{A}_{k:l} = \{\mathcal{A}[k], \mathcal{A}[k+1], \dots, \mathcal{A}[l]\}$.

Definition I. Range scan captured from a 2D LIDAR sensor.—A range scan \mathcal{S} , measured by a 2D LIDAR sensor, consisting of N_s rays over an angular range λ , is an ordered map of angles to distances to objects within its range r_{\max} : $\mathcal{S}:\Theta\to\mathbb{R}_{\geq 0},\ \Theta=\{\theta_n\in[-\frac{\lambda}{2},+\frac{\lambda}{2}):\theta_n=-\frac{\lambda}{2}+\lambda\frac{n}{N_s},\ n=0,1,\ldots,N_s-1\}.$ Angles θ_n are expressed relative to the sensor's heading, in the sensor's frame of reference [7].

Definition II. Map-scan.—A map-scan is a virtual scan that encapsulates the same pieces of information as a scan derived from a physical sensor (Def. I). Contrary to the latter it refers to distances within a map rather than within a real environment. A map-scan $\mathcal{S}_V^M(\hat{p})$ is derived by locating intersections of rays emanating from the estimate of the sensor's pose estimate \hat{p} and the boundaries of map M.

Definition III. CAER as metric.—Let S_p and S_q be two range scans, equal in angular range λ and size N_s . The value of the Cumulative Absolute Error per Ray (CAER) metric $\psi \in \mathbb{R}_{>0}$ between S_p and S_q is given by

$$\psi(\mathcal{S}_p, \mathcal{S}_q) \triangleq \sum_{n=0}^{N_s - 1} \left| \mathcal{S}_p[n] - \mathcal{S}_q[n] \right| \tag{1}$$

Definition IV. CAER as field.—A ψ -field on map M $f_{\psi}^{M}: \mathbb{R}^{2} \times [-\pi, +\pi) \to \mathbb{R}_{\geq 0}$ is a mapping of 3D pose configurations $\hat{p}(\hat{x}, \hat{y}, \hat{\theta})$ to CAER values (Def. III) such that if $\psi(\mathcal{S}_{R}, \mathcal{S}_{V}^{M}(\hat{p})) = c$ then $f_{\psi}^{M}(\hat{p}) = c$.

Definition V. Rank field.—Let f_{ψ}^{M} be a ψ -field on map M and $\mathcal{P} = \{\hat{p}_{i}\}, i \in \mathbb{I} = \langle 0, 1, \dots, |\mathcal{P}| - 1 \rangle$, be a set of 3D

pose configurations within M, such that $f_{\psi}^{M}(\mathcal{P}) = \Psi$. Let \mathbb{I}^{*} be the set of indices such that $\Psi[\mathbb{I}^{*}] = \Psi_{\uparrow}$. A r-field on map M $f_{r}^{M}: \mathbb{R}^{2} \times [-\pi, +\pi) \to \mathbb{Z}_{\geq 0}$ is a mapping of 3D pose configurations \mathcal{P} to non-negative integers such that if $f_{\psi}^{M}(\mathcal{P}) = f_{\psi}^{M}(\mathcal{P}[\mathbb{I}]) = \Psi$ then $f_{r}^{M}(\mathcal{P}[\mathbb{I}^{*}]) = \mathbb{I}$. A rank field maps the elements of set $\{\hat{p}_{i}\}$ to the ranks \mathbb{I}^{*} of their corresponding CAER values in hierarchy Ψ_{\uparrow} .

Definition VI. Field densities.—The locational and angular density, d_l and d_{α} respectively, of a ψ - or r-field express, correspondingly, the number of pose estimates per unit area of space and per angular cycle, where $d_l, d_{\alpha} \in \mathbb{N}$.

Definition VII. Admissibility of solution.—A pose estimate $\hat{p}(\hat{x}, \hat{y}, \hat{\theta}) \in \mathbb{R}^2 \times [-\pi, +\pi)$ may be deemed an admissible solution to Problem P iff $\|\boldsymbol{l} - \hat{\boldsymbol{l}}\|_2 \leq \delta_l$ and $\|\boldsymbol{p} - \hat{\boldsymbol{p}}\|_2 \leq \delta$, where $\delta_l, \delta_\theta, \delta \in \mathbb{R}_{>0}$: $\delta_l^2 + \delta_\theta^2 = \delta^2$.

III. RELATED WORK

The literature concerning the solution to the problem of global localisation with the use of a 2D LIDAR sensor is rich. A recent and comprehensive survey on global localisation may be found in [8], while a brief overview is given below.

In broad terms global localisation approaches may be divided into two categories: (a) approaches that operate in feature space, that is, methods that extract features from measurements and the map and then establishing correspondences between them, and (b) approaches that directly exploit only raw measurements.

In the latter category a number of global localisation methods solve the problem in an iterative Bayesian Monte Carlo fashion, i.e. by dispersing hypotheses within the map and updating the belief of the robot's pose by incorporating new measurements as it moves until estimate convergence [9]–[13]. However, the requirement of motion (a) may give rise to safety concerns (the robot may not even be visible), and (b) increases estimation time. The Monte Carlo method proposed in this article operates directly in measurement space as well but, in contrast, it does not require motion or more than one measurement. As a result CBGL is a single-shot global localisation approach that is executable in less time compared to previous Monte Carlo approaches.

Research on the former category has been more extensive due to the richness, appropriateness, adaptability, and efficacy of methods originated in the computer vision field. Relevant methods mainly perform detection of keypoints in a measurement, followed by the calculation of a distinctive signature, which is then matched to similarly- and pre-computed place-signatures [1], [14]–[20]. In principle, however, unstructured environments cannot be relied upon for the existence of features, due to their complete absence or their sparse and fortuitous distribution (although Deep Neural Network approaches have demonstrated increased performance in place recognition with the use of 3D LI-DARs [21]–[23]). Structured environments on the other hand manifest different features depending on the particularities of the environment, and features may be present but not in

a sufficiently undisturbed state by sensor noise or map-toenvironment mismatch. Furthermore, feature-based methods require the tuning of parameters in a per-environment basis, which hinders the degree of their applicability and efficacy. In contrast CBGL uses three parameters, whose optional setting is intuitive.

The motivation of the proposed method originates from seeking to achieve a greater degree of universality, reliability, and portability across multiple and disparate environments, by (a) not making a priori assumptions on environment structure, and (b) aiming to minimise requirements on resources (number, type, and cost of sensors; number of measurements; time). The proposed method is most akin to the two tested methods in [24]: all three are single-shot 2D LIDAR-based Monte Carlo approaches, but CBGL computes a measure of the alignment of (a) the measurement to (b) the virtual scan captured from each hypothesis before scan-tomap-scan matching a subset of the most-aligned poses to the measurement. So far this alignment measure (Def. III) has been used only in the context of sm2, i.e. for pose hypotheses in a neighbourhood of the sensor's true pose [25], [26], and its computational complexity is low. As a consequence CBGL is able to process more hypotheses in less time, resulting in an improvement in (a) the number of correctly estimated locations and (b) execution time, making it able to compete against (traditionally faster) feature-based approaches.

IV. THE CBGL METHOD

A. Motivation

The proposed method's motivation lies in the simple but powerful fact that is, in general, exhibited through figure 1: Assume a pose estimate residing in a neighbourhood of a 2D LIDAR sensor's pose within a given map; then the value of the CAER metric between the scan measured by the sensor and the map-scan captured from the estimate within the map is simultaneously proportional to both the estimate's location error and orientation error. Formally the proposed method's foundations rest on Observation O:

Observation O. It may be observed that there are conditions such that Hypothesis H stands true.

Hypothesis H. There exists $\hat{p} \in \mathbb{R}^2 \times [-\pi, +\pi)$ such that $\hat{p} \in \mathcal{V} : \|p - \hat{p}\|_2 \le \delta \le \delta_0$ is an admissible pose estimate solution to Problem P (Def. VII), where set \mathcal{V} and δ_0 are defined by Conjecture C.

Conjecture C. Let the unknown pose of a 2D range sensor measuring range scan \mathcal{S}_R (Def. I) be $p(x,y,\theta)$ with respect to the reference frame of map M. Let \mathcal{H} be a set of pose hypotheses within the free (i.e. traversable) space of M: $\mathcal{H} = \{\hat{p}_i(\hat{x}_i, \hat{y}_i, \hat{\theta}_i)\} \subseteq \mathtt{free}(M), i \in \mathtt{I} = \langle 0, 1, \dots, |\mathcal{H}| - 1 \rangle$. Let f_{ψ}^M be the ψ -field on M (Def. IV) such that $f_{\psi}^M(\mathcal{H}) = \Psi$. Let the field's locational and orientational densities be d_l and d_{α} . Let $\hat{p}_{\omega} \in \mathcal{H}$ and $\psi_0, \delta_0 \in \mathbb{R}_{>0}$ such that $f_{\psi}^M(\hat{p}_{\omega}) = \psi_0$ and $\|p - \hat{p}_j\|_2 \leq \delta_0$ for all $\hat{p}_j \in \mathcal{H} : f_{\psi}^M(\hat{p}_j) \leq \psi_0$. Let now $\mathcal{V} = \{\hat{p}_i \in \mathcal{H} : f_{\psi}^M(\hat{p}_i) \leq \psi_0\}$

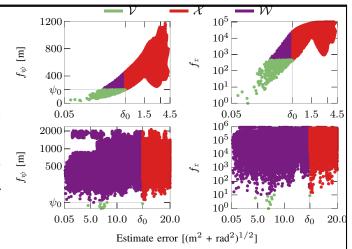


Fig. 2: The ψ -field (left) and r-field (right) of a configuration where Observation O may (top) and may not (bottom) be made for $\delta \leq \delta_0$. Bottom: in contrast to the top row, set $\mathcal V$ is empty of admissible pose estimates for $\delta < 4.5~(\text{m}^2+\text{rad}^2)^{1/2}$. The effect is produced in environment WILLOWGARAGE (pose p_i^G ; subsection V-B) due to (a) the repetition of the immediate environment of the sensor more than once in the given map, and (b) the non-panoramic angular range of the sensor

 $\psi_0, \|\mathbf{p} - \hat{\mathbf{p}}_i\|_2 \leq \delta_0$. Without loss of generality there exist d_l, d_{α} , and ψ_0, δ_0 such that for all $\hat{\mathbf{p}}_{\mathcal{V}} \in \mathcal{V}$:

$$\begin{split} f_{\psi}^{\pmb{M}}(\hat{\pmb{p}}_{\mathcal{V}}) < f_{\psi}^{\pmb{M}}(\hat{\pmb{p}}) & \Leftrightarrow & \|\pmb{p} - \hat{\pmb{p}}_{\mathcal{V}}\|_2 < \|\pmb{p} - \hat{\pmb{p}}\|_2 \\ \text{for any } \hat{\pmb{p}} \in \mathcal{X} = \mathcal{H} \setminus \mathcal{V} : \|\pmb{p} - \hat{\pmb{p}}\|_2 > \delta_0. \end{split}$$

Remark I. The composition of $\mathcal{H} = \mathcal{V} \cup \mathcal{X} \cup \mathcal{W}$, where $\mathcal{W} = \hat{\boldsymbol{p}} \in \mathcal{H} \setminus \mathcal{V} : \|\boldsymbol{p} - \hat{\boldsymbol{p}}\|_2 \leq \delta_0$. With regard to the elements of set \mathcal{W} : if a global localisation system's output was pose $\hat{\boldsymbol{p}}_{\mathcal{W}} \in \mathcal{W}$, then $\hat{\boldsymbol{p}}_{\mathcal{W}}$ would constitute a false negative: it may be that $f_{\psi}^{\boldsymbol{M}}(\hat{\boldsymbol{p}}_{\mathcal{W}}) > f_{\psi}^{\boldsymbol{M}}(\hat{\boldsymbol{p}}_{\mathcal{X}})$ but with regard to the pose error: $\|\boldsymbol{p} - \hat{\boldsymbol{p}}_{\mathcal{X}}\|_2 \leq \delta_0$ and $\|\boldsymbol{p} - \hat{\boldsymbol{p}}_{\mathcal{W}}\|_2 \leq \delta_0$.

In simple terms Conjecture C states that, in general, given a dense enough set of pose hypotheses $\mathcal H$ over a map M, it is possible to partition $\mathcal H$ into such (non-empty) sets $\mathcal V$, $\mathcal X$, and $\mathcal W$ that the error of pose estimates in set $\mathcal V$ and their corresponding CAER values are simultaneously lower than those of estimates in set $\mathcal X$. Hypothesis H restrictingly states that $\mathcal V$ contains a pose estimate whose error is such that it is deemed an admissible solution to Problem P. Figure 2 (top) shows an example configuration where Hypothesis H stands true for some $\delta \leq \delta_0 = 0.50 \ (\text{m}^2 + \text{rad}^2)^{1/2}$.

B. The CBGL System

In the same vein as Hypothesis H assume the r-field $f_{\rm r}^M(\mathcal{H})$ corresponding to the ψ -field $f_{\psi}^M(\mathcal{H})$ on a given map M (Def. V) such that $\Psi[\mathtt{I}^*] = \Psi_{\uparrow}$, and $f_{\rm r}^M(\mathcal{H}[\mathtt{I}^*]) = \mathtt{I}$. Then the top $k \ll |\mathcal{H}|$ ranked pose hypotheses $\mathcal{H}[\mathtt{I}^*]_{0:k-1}$ define set \mathcal{V} such that $\psi_0 = \max f_{\psi}^M(\mathcal{H}[\mathtt{I}^*]_{0:k-1})$, and for all $\hat{p}_{\mathcal{V}} \in \mathcal{V}$ and any $\hat{p}_{\mathcal{X}} \in \mathcal{X}$: $f_{\rm r}^M(\hat{p}_{\mathcal{V}}) < f_{\rm r}^M(\hat{p}_{\mathcal{X}}) \Leftrightarrow f_{\psi}^M(\hat{p}_{\mathcal{V}}) < f_{\psi}^M(\hat{p}_{\mathcal{X}}) \Leftrightarrow \|p - \hat{p}_{\mathcal{V}}\|_2 < \|p - \hat{p}_{\mathcal{X}}\|_2$. By identifying the pose estimates that correspond to the bottom k CAER values, this rationale attempts to recover the identity of the pose hypotheses with the bottom k pose errors across

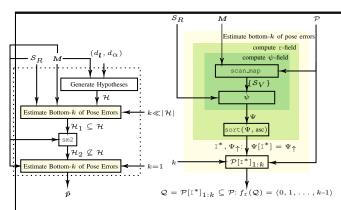


Fig. 3: CBGL in block diagram form. Left: Given a LIDAR's 2D measurement S_R and a map M, CBGL generates a set of pose hypotheses \mathcal{H} and estimates the k hypotheses with the least pose error (right; alg. ??). Then it scan-to-map-scan matches those to S_R for finer estimation (sm2; alg. ??). CBGL's output pose estimate is that with the least CAER among the k matched estimates. Right: CBGL's core method. Given S_R , M, and pose estimates \mathcal{P} , it (a) computes and ranks the CAER values between S_R and map-scans captured from \mathcal{P} within M, and (b) outputs the hypotheses with the k lowest CAER values

H. It constitutes the core of the proposed passive global localisation method, termed CBGL, and is described in block diagram form in figure 3 (right) and in pseudocode in Algorithm ??.

Assuming the satisfaction of Observation O, the challenge is choosing such k, d_l , and d_α that, given pose estimate error requirements δ_l , δ_θ (Def. VII; Hyp. H), CBGL produces admissible pose estimates while being executed in timely manner. Given the rank field's Monte Carlo nature, optimistically, the only option for increasing the accuracy of the final pose estimate by a factor of two is doubling the densities of the r-field; instead of doing that—and thereby doubling the method's execution time—subsequent to the estimation of the pose estimates with the k lowest CAER values, CBGL utilises scan—to—map-scan matching [26], [27], followed by the estimation of the one pose estimate with the lowest CAER value within the group of matched estimates.

Matching allows for (a) the correction of the pose of true positive estimates by scan-matching the map-scan from of a pose estimate against the range scan measured by the real sensor, (b) by the same token the potential divergence of spurious, false positive, pose estimates, and hence their elimination as pose estimate candidates, (c) the production of finer pose estimates without excessive increase in execution time, and (d) the decoupling of the final pose estimate's error from the field's density. Figure 3 (left) and algorithm?? present the proposed method of CBGL in block diagram and algorithmic forms respectively.

V. EXPERIMENTAL EVALUATION

This section serves the testing of Hypothesis H with state of the global localisation art methods and CBGL, in varying environmental conditions and sensor configurations. With regard to CBGL its three required parameters are set to $(d_{l}, d_{c}, k) = (40, 2^{5}, 10)$ after initial tests with the dataset

used in subsection V-A. The rationale of choosing appropriate d_l , d_{α} is depicted in figure 4, and k is chosen as such in order to retain a high-enough true positive discovery rate without significant increase in execution time. References to sets \mathcal{H}_* are made to fig. 3 (left) and lines ??, ??, and ?? of Algorithm ??. All tests are performed with a processor of 12 threads and a clock speed of 4.00 GHz.

A. Experiments in real conditions

The first type of test is conducted using a Hokuyo UTM-30LX sensor, whose angular range is $\lambda = 3\pi/2$ rad and radial range $r_{\rm max}=30.0$ m, in the Electrical and Computer Engineering Department's Laboratory of Computer Systems Architecture (CSAL), Aristotle University of Thessaloniki a map of which is depicted in figure 5. The sensor was mounted on a Robotnik RB1 robot, which was teleoperated within the environment while scans were being recorded This resulted in $N_S = 6669$ range scans, whose number of rays are downsampled by a factor of four before being inputted to CBGL and ALS [29]. The latter implements Free-Space Features [1]. Other global localisation methods are not to tested for this type of experiment due to their infeasible execution time with respect to the range dataset's volume (see fig. 8). CBGL's internal sm2 method is chosen to be PLICP [30] due to its low execution time and the sensor's non-panoramic field of view. The top of figure 6 depicts the proportion of output pose estimates from each method whose position and orientation error is lower than outlier thresholds δ_{I} , δ_{θ} ; at the bottom they are depicted exclusively for CBGL's output and its internal pose sets. The mean and standard deviation of the two methods' execution times are $(\mu_t^{\text{ALS}}, \sigma_t^{\text{ALS}}) = (6.15, 5.32)$ sec, and $(\mu_t^{\text{CBGL}}, \sigma_t^{\text{CBGL}}) =$ (1.61, 0.06) sec. From the experimental evidence it is clear that (a) Hypothesis H is observed to be true 991 times out of a thousand for an outliers' locational threshold $\delta_l = 0.5$ m when an angular threshold is δ_{θ} is not considered, and (b) CBGL outperforms ALS in terms of (i) number of pose estimates within all locational and angular thresholds and (ii) execution time.

B. Simulations against sources of uncertainty

The second type of test concerns the main limiting factor of global localisation methods, i.e. uncertainty—: arising e.g. from spurious measurements, repeatability of surroundings missing range information, or their combinations. For this reason the experimental procedure of [24] is extended here for the two methods tested therein, i.e. PGL-FMIC and PGL-PLICP, and then for CBGL, ALS, MCL [9], and GMCL [12]. Specifically these methods are tested against the two most challenging environments, i.e. WAREHOUSE and WILLOWGARAGE, in which a panoramic range sensor is placed at 16 different poses, respectively p_*^W and p_*^G , for N=100 independent attempts at global localisation per pose. The tests are conducted with the use of a sensor whose number of rays $N_s = 360$, maximum range $r_{\text{max}} = 10.0$ m, and noise $\mathcal{N}(0, 0.05^2)$ [m,m²]. CBGL's internal sm2 method is chosen to be x1 [26] due to the periodicity of the range

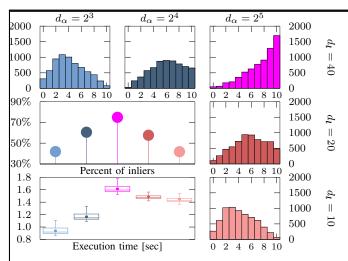


Fig. 4: Top row and right column: histograms of the number of times when exactly $n \in [0,k] = [0,10]$ pose estimates belonging to set \mathcal{H}_1 exhibited pose errors lower than $\delta = (\delta_t^2 + \delta_\theta^2)^{1/2} = (0.3^2 + 0.4^2)^{1/2} = 0.5 \text{ (m}^2 + \text{rad}^2)^{1/2}$. For densities $(d_t, d_\alpha) = (40, 2^5)$ this number is strictly increasing with n. Middle block: percent proportion of pose estimates whose pose error is lower than δ for varying field densities. Bottom block: the distribution of corresponding execution times

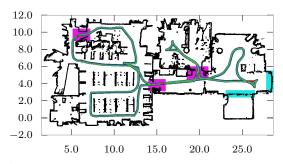


Fig. 5: The map of the CSAL environment (black), the trajectory of the sensor (blue), and CBGL's estimated positions of the sensor (green). Sensor poses for which CBGL's output exhibits position error larger than $\delta_l=0.5$ m are marked with red, sources of great range noise with cyan, and regions around doors with purple. A total of $N_S=6669$ pose estimations take place. Estimation is performed for each sensor pose independently of previous estimates and measurements

signal, x1's improved results over sm2 matching state of the art methods, and its ability in matching scans captured from greater initial locational distances than ICP alternatives. The latter translates to the need for smaller initial hypothesis sets: for each environment the locational density is set to 3e+04 divided by the free space area of each environment. For Monte Carlo approaches MCL and GMCL the number of initial hypotheses is also set to 3e+04.

The maximum range of the sensor is such that the geometry of environment WAREHOUSE causes (disorderly) extended lack of sampling of the sensor's surrounding environment, which limits available information and may therefore produce spurious measurements and increase ambiguities between candidate estimates. In WILLOWGARAGE on the other hand, almost all sensor placements result in complete sampling of its surroundings, but the sensor is purposefully

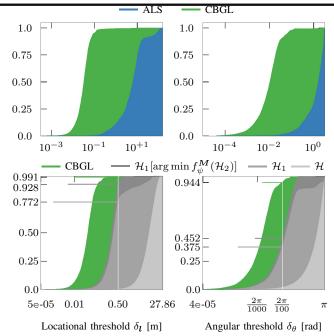


Fig. 6: Proportions of pose estimates whose position and orientation error is lower than corresponding thresholds δ_l and δ_θ . Top: ALS vs CBGL. Bottom: CBGL and internal pose estimate sets. Approximately 77% of all bottom-k pose estimates—the contents of \mathcal{H}_1 sets, populated via rank fields as described in sections II and IV—exhibit position errors lower than $\delta_l=0.5$ m for k=10, and so do over 99% of CBGL's final pose estimates. The improvement in position and orientation induced by scan—to—mapscan matching is captured by the difference between the output (i.e. $\mathcal{H}_2[\arg\min f_\psi^M(\mathcal{H}_2)])$ and $\mathcal{H}_1[\arg\min f_\psi^M(\mathcal{H}_2)]$

posed in such conditions as to challenge the localisation methods' ability to perform fine distinctions between similar surroundings. Figure 7 depicts the percentage of outputs whose position error is lower than $\delta_l=0.5$ m per tested pose, and figure 8 depicts the overall distribution of execution times per tested environment and algorithm. CBGL's mean execution time in environment WAREHOUSE is $\mu_t^W=7.98$ sec and in WILLOWGARAGE $\mu_t^G=3.59$ sec. Although the cardinality of set \mathcal{H} is equal for both environments CBGL's execution times are uneven due to x1's increased execution time when dealing with scans with missing range information. Notwithstanding the aforementioned sources of uncertainty, CBGL manages to exhibit the highest number of inliers in each environment tested.

C. Simulations against environmental and sm2 algorithmic disparity

The third type of test aims to inquire how the performance of CBGL scales with respect to increasing environment area (and therefore to increased number of hypotheses), environment diversity, sensor angular range, and choice of overlying sm2 method. CBGL is tested once in each of $N_E \simeq 4.5 \text{e} + 0.4$ environments, generated via the evaluation procedure of [26], which utilises five established and publicly available benchmark datasets provided courtesy of the Department of Computer Science, University of Freiburg [31]. Each

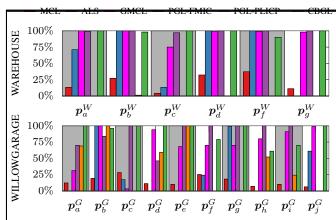


Fig. 7: Percent proportions of pose outputs whose position error is lower than $\delta_l = 0.5$ m per tested environment, pose, and method. Overall CBGL (green) features the highest number of inlier poses

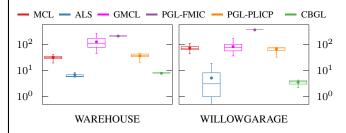


Fig. 8: Distribution of execution times per tested environment and algorithm in seconds for $N_s = 360$ rays. CBGL's execution time is at least eighteen times lower than other Monte Carlo approaches in WILLOWGARAGE and four times lower in WAREHOUSE

coordinate of the map corresponding to each environment is corrupted by noise $\mathcal{N}(0,0.05^2)$ [m, m²]. The angular range of the range sensor varies according to the overlying sm2 method used: for NDT [32], FastGICP [33], and FastVGICP [34]: $\lambda = 3\pi/2$ rad; for x1: $\lambda = 2\pi$ rad. Measurement noise is $\mathcal{N}(0,0.03^2)$ [m,m²]. As in subsection V-A the choice of field densities and k is $(d_l, d_{\alpha}, k) = (40, 2^5, 10)$.

Figure 9 illustrates that, with the exception of NDT, all versions of CBGL exhibit mean positional errors less than 1.0 m; its combination with $\times 1$ exhibits a mean error of approximately 0.5 m. The evidence support the claim that CBGL is robust to sensor angular range, as the distributions of errors are indistinguishable between bottom-k (\mathcal{H}_1) sets for k=10. Figure 10 shows the execution time of CBGL combined with FastVGICP and $\times 1$ as a function of environmental area, and that with $\times 1$'s timing breakdown with respect to (a) CBGL's total time minus scan—to—map-scan matching time and (b) computing map-scans, as proportions of total execution time.

VI. CHARACTERISATION & LIMITATIONS

Rank-fields produced by panoramic angular ranges induce fewer pose ambiguities than those produced by non-panoramic ones. In the latter case this means that, given the evidence of subsections V-A and V-C where $\lambda = 3\pi/2$ rad, the choice of k=10 largely inhibits the propagation of ambiguities to the output (fig. 9). However, non-panoramic angular ranges coupled with repeated environment struc-

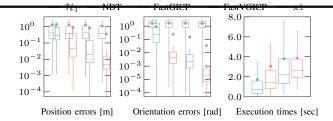


Fig. 9: Distributions of positional and orientational errors and of execution time of CBGL for varying choices of scan-to-mapscan matching methods. The errors of CBGL's internal \mathcal{H}_1 set are virtually unaffected by the decrease in angular range λ ($\lambda_{\text{NDT}} = \lambda_{\text{FastGICP}} = \lambda_{\text{FastVGICP}} = 3\pi/2 \neq \lambda_{\text{x}1} = 2\pi$)

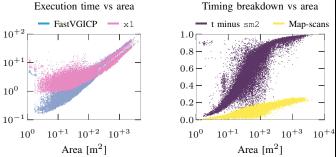


Fig. 10: Left: CBGL's execution time with respect to environment area for two choices of overlying scan-to-map-scan matching methods. In rough terms $time_{CBGL}$ [sec] = $10^{-3} \cdot area$ [m²] for areas larger than 200 m². Right: Proportion of CBGL \circ x1's total execution time spent on (a) all operations up to and except for matching, and (b) computing map-scans, with respect to area

tures may give rise to the conditions of figure 2 (bottom). Other sources of potential, large pose errors for CBGL are portrayed in figure 5: (a) regions encoded with cyan indicate closed glass doors, wherein great discrepancy with respect to map-derived virtual ranges may be observed, which is subsequently propagated to ψ -fields and hence r-fields, and (b) regions encoded with purple indicate vicinities around doors, wherein the amount of environment and map information is restricted.

VII. CONCLUSIONS AND FUTURE STEPS

This article has presented a single-shot Monte Carlo approach to the solution of the passive version of the global localisation problem with the use of a 2D LIDAR sensor, titled CBGL. CBGL allows for the fast estimation of the sensor's pose within a metric map by first dispersing hypotheses in it and then leveraging the proportionality of values of the Cumulative Absolute Error per Ray (CAER) metric to the pose errors of the hypotheses, for estimates in a neighbourhood of the sensor's pose. CBGL was evaluated in various real and simulated conditions and environments; it was found to be superior to Monte Carlo and feature-based approaches in terms of number of inlier pose estimates and execution time. Future steps will aim at the extension of the CAER metric for the use with 3D LIDAR sensors in service to a solution of the problem of their global localisation in 6DoF. The C++ ROS code of the proposed method is available at https://github.com/li9i/cbgl.

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