

CBGL: Fast Monte Carlo Passive Global Localisation for 2D LIDAR Sensors

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Abstract—Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetur id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

CBGL leverages the relationships of (a) proportionality between the pose estimate error and the value of the Cumulative Absolute Error per Ray (CAER) metric for pose estimates in a neighbourhood of the sensor's pose, and (b) lack of disproportionality outside of that neighbourhood. The source code is available for download.

Index Terms—global localisation, 2D LIDAR, monte carlo, scan-to-map-scan matching

I. INTRODUCTION

This paper addresses the problem of Passive Global Localisation of a 2D LIDAR sensor, i.e. the estimation of its location and orientation within a given map, under complete locational and orientational uncertainty, without prescribing motion commands (to the mobile robot that the sensor is assumed mounted to) for further knowledge acquisition. The problem is formalised in Problem P:

Problem P. Let the unknown pose of an immobile 2D range sensor whose angular range is λ be $\mathbf{p}(\mathbf{l}, \theta)$, $\mathbf{l} = (x, y)$, with respect to the reference frame of map M . Let the range sensor measure range scan \mathcal{S}_R . The objective is the estimation of \mathbf{p} given M , λ , and \mathcal{S}_R .

II. DEFINITIONS

Let $\mathcal{A} = \{\alpha_i : \alpha_i \in \mathbb{R}\}$, $i \in \mathbb{I} = \langle 0, 1, \dots, n-1 \rangle$, denote a set of n elements, $\langle \cdot \rangle$ denote an ordered set, \mathcal{A}_\uparrow the set \mathcal{A} ordered in ascending order, the bracket notation $\mathcal{A}[\mathbb{I}] = \mathcal{A}$ denote indexing, and notation $\mathcal{A}_{k:l}$, $0 \leq k \leq l$, denote limited indexing: $\mathcal{A}_{k:l} = \{\mathcal{A}[k], \mathcal{A}[k+1], \dots, \mathcal{A}[l]\}$.

Definition I. *Range scan captured from a 2D LIDAR sensor.*—A conventional 2D LIDAR sensor provides a finite number of ranges, i.e. distances to objects within its range, on a horizontal cross-section of its environment, at regular angular and temporal intervals, over a defined angular range [1]. A range scan \mathcal{S} , consisting of N_s rays over an angular range λ , is an ordered map $\mathcal{S} : \Theta \rightarrow \mathbb{R}_{\geq 0}$, $\Theta = \{\theta_n \in$

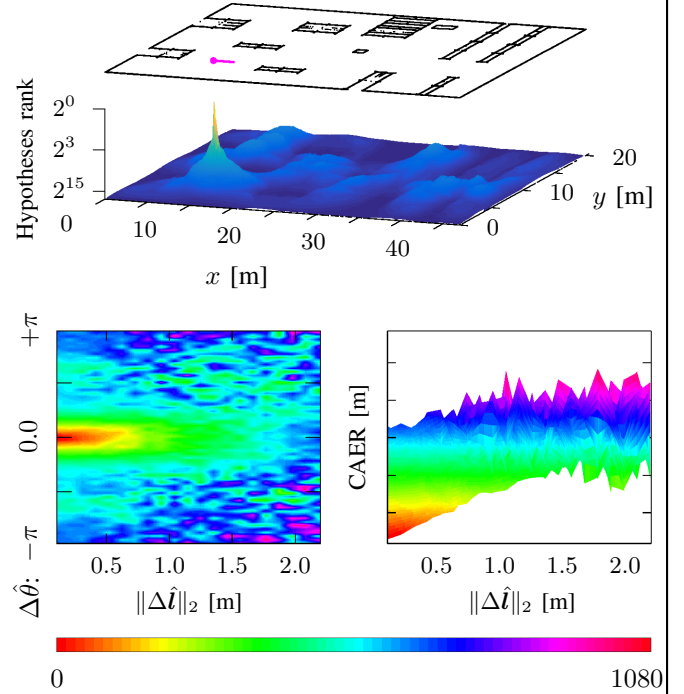


Fig. 1: Given a LIDAR sensor's 2D measurement, at its core, CBGL disperses pose hypotheses within the map and ranks them ascendingly according to the value of the CAER metric (Eq. (1)), whose inputs comprise the input measurement and the map-scan captured from each hypothesis. This produces a $\tau(\text{ank})$ -field which may be used to estimate the pose of the sensor (a) accurately due to the proportionality of estimate error and CAER, and (b) quickly due to the metric's low computational complexity. Top: a map of an environment, the pose of a panoramic 2D LIDAR sensor (magenta), and the corresponding CAER rank field below them. Bottom: distribution of CAER values by location $\Delta \hat{\mathbf{l}}$ and orientation error $\Delta \hat{\theta}$ of all sensor pose hypotheses corresponding to the rank field above, for estimate distances up to 2.0 m. In this example 10^6 hypotheses are dispersed randomly in the free space of a map with area 735 m², for 100 independent trials; CBGL's maximum location error and maximum execution time is, respectively, 0.062 m and 8.8 sec

$[-\frac{\lambda}{2}, +\frac{\lambda}{2}) : \theta_n = -\frac{\lambda}{2} + \lambda \frac{n}{N_s}, n = 0, 1, \dots, N_s-1\}$. Angles θ_n are expressed relative to the sensor's heading, in the sensor's frame of reference.

Definition II. *Map-scan.*—A map-scan is a virtual scan that encapsulates the same pieces of information as a scan derived from a physical sensor. Only their underlying operating principle is different due to the fact the map-scan refers to distances to the boundaries of a point-set, referred to as the map, rather than within a real environment. A map-scan $\mathcal{S}_V^M(\hat{\mathbf{p}})$ is derived by means of locating intersections of rays

emanating from the estimate of the sensor's pose estimate \hat{p} and the boundaries of the map M .

Definition III. CAER as metric.—Let S_p and S_q be two range scans, equal in angular range λ and size N_s . The value of the Cumulative Absolute Error per Ray (CAER) metric $\psi \in \mathbb{R}_{\geq 0}$ between S_p and S_q is given by

$$\psi(S_p, S_q) \triangleq \sum_{n=0}^{N_s-1} |S_p[n] - S_q[n]| \quad (1)$$

Definition IV. CAER as field.—A ψ -field on map M $f_\psi^M : \mathbb{R}^2 \times [-\pi, +\pi) \rightarrow \mathbb{R}_{\geq 0}$ is a mapping of 3D pose configurations $\hat{p}(\hat{x}, \hat{y}, \hat{\theta})$ to CAER values (def. III) such that if $\psi(S_R, S_V^M(\hat{p})) = c$ then $f_\psi^M(\hat{p}) = c$. In other words a CAER field is produced by computing the value of the CAER metric between a range scan S_R (def. I) and a map-scan $S_V^M(\hat{p})$ captured from pose configuration \hat{p} within map M (def. II).

Definition V. Rank field.—Let f_ψ^M be a ψ -field on map M and $\mathcal{P} = \{\hat{p}_i\}$, $i \in \mathbb{I} = \langle 0, 1, \dots, |\mathcal{P}| - 1 \rangle$, be a set of 3D pose configurations within map M , such that $f_\psi^M(\mathcal{P}) = \Psi$. Let \mathbb{I}^* be the set of indices such that $\Psi[\mathbb{I}^*] = \Psi_\uparrow$. A r -field on map M $f_r^M : \mathbb{R}^2 \times [-\pi, +\pi) \rightarrow \mathbb{Z}_{\geq 0}$ is a mapping of 3D pose configurations \mathcal{P} to non-negative integers such that if $f_\psi^M(\mathcal{P}) = f_\psi^M(\mathcal{P}[\mathbb{I}]) = \Psi$ then $f_r^M(\mathcal{P}[\mathbb{I}^*]) = \mathbb{I}$. In other words a rank field maps the elements of pose estimate set $\{\hat{p}_i\}$ to the ranks \mathbb{I}^* of their corresponding CAER values in hierarchy Ψ_\uparrow .

Definition VI. Field densities.—The locational and angular density, d_l and d_α respectively, of a ψ - or r -field express, correspondingly, the number of pose estimates per unit area of space and per angular unit, where $d_l, d_\alpha \in \mathbb{N}$.

Definition VII. Admissibility of solution.—A pose estimate $\hat{p}(\hat{x}, \hat{y}, \hat{\theta}) \in \mathbb{R}^2 \times [-\pi, +\pi)$ may be deemed an admissible solution to Problem P iff $\|\hat{l} - \hat{l}\|_2 \leq \delta_l$ and $|\hat{\theta} - \hat{\theta}| \leq \delta_\theta$ and $\|\mathbf{p} - \hat{\mathbf{p}}\|_2 \leq \delta$, where $\delta_l, \delta_\theta, \delta \in \mathbb{R}_{>0}$: $\delta_l^2 + \delta_\theta^2 = \delta^2$.

III. RELATED WORK

IV. THE CBGL METHOD

A. Motivation

The proposed method's motivation lies in the simple but powerful fact that, in general, is exhibited through figure 1: Assume a pose estimate residing in a neighbourhood of a 2D LIDAR sensor's pose within a given map; then the CAER metric between the scan measured by the sensor and the map-scan captured from the estimate within the map—the CAER metric is simultaneously proportional to both the estimate's location error and orientation error. Formally the proposed method's foundations rest on Observation O:

Observation O. It may be observed that there are conditions such that Hypothesis H stands true.

Hypothesis H. There exists $\hat{p} \in \mathbb{R}^2 \times [-\pi, +\pi)$ such that $\hat{p} \in \mathcal{V} : \|\mathbf{p} - \hat{\mathbf{p}}\|_2 \leq \delta \leq \delta_0$ is an admissible pose estimate

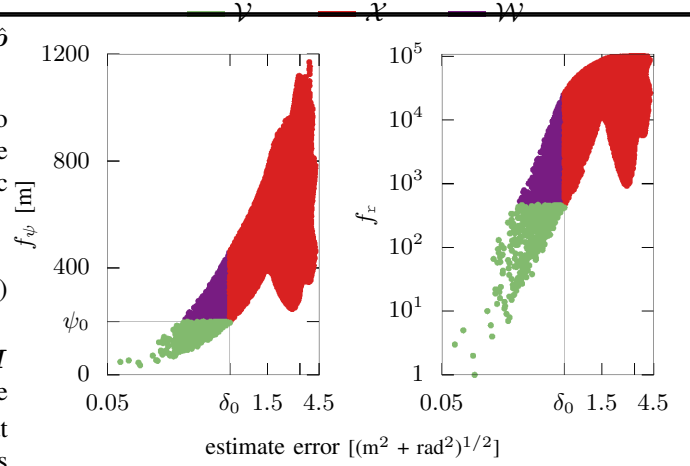


Fig. 2: The ψ -field (left) and r -field (right) of a configuration where Observation O can be made for $\delta \leq \delta_0$

solution to Problem P (def. VII), where set \mathcal{V} and δ_0 are defined by Conjecture C.

Conjecture C. Let the unknown pose of a 2D range sensor measuring range scan S_R (def. I) be $p(x, y, \theta)$ with respect to the reference frame of map M . Let \mathcal{H} be a set of pose hypotheses within the free (i.e. traversable) space of M : $\mathcal{H} = \{\hat{p}_i(\hat{x}_i, \hat{y}_i, \hat{\theta}_i)\} \subseteq \text{free}(M)$, $i \in \mathbb{I} = \langle 0, 1, \dots, |\mathcal{H}| - 1 \rangle$. Let f_ψ^M be the ψ -field on M (def. IV) such that $f_\psi^M(\mathcal{H}) = \Psi$. Let the field's locational and orientational densities be d_l and d_α . Let $\hat{p}_\omega \in \mathcal{H}$ and $\psi_0, \delta_0 \in \mathbb{R}_{>0}$ such that $f_\psi^M(\hat{p}_\omega) = \psi_0$ and $\|\mathbf{p} - \hat{\mathbf{p}}_j\|_2 \leq \delta_0$ for all $\hat{p}_j \in \mathcal{H} : f_\psi^M(\hat{p}_j) \leq \psi_0$. Let now $\mathcal{V} = \{\hat{p}_i \in \mathcal{H} : f_\psi^M(\hat{p}_i) \leq \psi_0, \|\mathbf{p} - \hat{\mathbf{p}}_i\|_2 \leq \delta_0\}$. Without loss of generality there exist d_l, d_α , and ψ_0, δ_0 such that for all $\hat{p}_\nu \in \mathcal{V}$:

$$f_\psi^M(\hat{p}_\nu) < f_\psi^M(\hat{p}) \Leftrightarrow \|\mathbf{p} - \hat{\mathbf{p}}_\nu\|_2 < \|\mathbf{p} - \hat{\mathbf{p}}\|_2$$

for any $\hat{p} \in \mathcal{X} = \mathcal{H} \setminus \mathcal{V} : \|\mathbf{p} - \hat{\mathbf{p}}\|_2 > \delta_0$.

Remark I. The composition of $\mathcal{H} = \mathcal{V} \cup \mathcal{X} \cup \mathcal{W}$, where $\mathcal{W} = \{\hat{p} \in \mathcal{H} \setminus \mathcal{V} : \|\mathbf{p} - \hat{\mathbf{p}}\|_2 \leq \delta_0\}$. With regard to the elements of set \mathcal{W} : if a global localisation system's output was pose $\hat{p}_\mathcal{W} \in \mathcal{W}$ then, in the language of classification, $\hat{p}_\mathcal{W}$ would constitute a false negative: it may be that $f_\psi^M(\hat{p}_\mathcal{W}) > f_\psi^M(\hat{p}_\mathcal{X})$ but with regard to the pose error: $\|\mathbf{p} - \hat{\mathbf{p}}_\mathcal{X}\|_2 \leq \delta_0$ and $\|\mathbf{p} - \hat{\mathbf{p}}_\mathcal{W}\|_2 \leq \delta_0$.

In simple terms Conjecture C states that, in general, given a dense enough set of pose hypotheses \mathcal{H} over a map M , it is possible to partition \mathcal{H} into such (non-empty) sets \mathcal{V} , \mathcal{X} , and \mathcal{W} that the error of pose estimates in set \mathcal{V} and their corresponding CAER values are simultaneously lower than those of estimates in set \mathcal{X} . Hypothesis H restrictingly states that \mathcal{V} is populated by a pose estimate whose error is such that it is deemed an admissible solution to Problem P.

B. The CBGL System

In the same vein as Hypothesis H assume the r -field $f_r^M(\mathcal{H})$ corresponding to the ψ -field $f_\psi^M(\mathcal{H})$ on a given map

Algorithm III: sm2

Input: $\mathcal{S}_R, M, \hat{p}$

Output: $\hat{p} + \text{correction}$ that aligns $\mathcal{S}_V^M(\hat{p})$ to \mathcal{S}_R

- 1: $\mathcal{S}_V \leftarrow \text{scan_map}(M, \hat{p})$
 - 2: $\Delta p \leftarrow \text{scan-match}(\mathcal{S}_R, \mathcal{S}_V)$ (e.g. ICP [4], FSM [5])
 - 3: **return** $\hat{p} + \Delta p$
-

M (def. V) such that $\Psi[\mathbb{I}^*] = \Psi_{\uparrow}$, and $f_{\mathbf{r}}^M(\mathcal{H}[\mathbb{I}^*]) = \mathbb{I}$. Then the top $k \ll |\mathcal{H}|$ ranked pose hypotheses $\mathcal{H}[\mathbb{I}^*]_{0:k-1}$ define set \mathcal{V} such that $\psi_0 = \max f_{\psi}^M(\mathcal{H}[\mathbb{I}^*]_{0:k-1})$, and for all $\hat{p}_{\mathcal{V}} \in \mathcal{V}$ and any $\hat{p}_{\mathcal{X}} \in \mathcal{X}$: $f_{\mathbf{r}}^M(\hat{p}_{\mathcal{V}}) < f_{\mathbf{r}}^M(\hat{p}_{\mathcal{X}}) \Leftrightarrow f_{\psi}^M(\hat{p}_{\mathcal{V}}) < f_{\psi}^M(\hat{p}_{\mathcal{X}}) \Leftrightarrow \|\mathbf{p} - \hat{p}_{\mathcal{V}}\|_2 < \|\mathbf{p} - \hat{p}_{\mathcal{X}}\|_2$. By identifying the pose estimates that correspond to the bottom k CAER values, this rationale attempts to recover the identity of the pose hypotheses with the bottom k pose errors across \mathcal{H} . It constitutes the core of the proposed passive global localisation method, termed CBGL, and is described in block diagram form in figure 4 and in pseudocode in algorithm II.

Assuming the satisfaction of Observation O, the challenge is choosing such k , d_l , and d_{α} that, given pose estimate error requirements δ_l , δ_{θ} (def. VII; hyp. H), CBGL produces admissible pose estimates while being executed in timely manner. Given the rank field's Monte Carlo nature, optimistically, the only option for increasing the accuracy of the final pose estimate by a factor of two is doubling the densities of the \mathbf{r} -field; instead of doing that—and thereby doubling the method's execution time—subsequent to the estimation of the pose estimates with the k lowest CAER values, CBGL utilises scan-to-map-scan matching [2], [3], followed by the estimation of the one pose estimate with the lowest CAER value within the group of matched estimates.

Matching allows for (a) the correction of the pose of true positive estimates by scan-matching the map-scan captured within the map from the pose of a pose estimate against the range scan measured by the real sensor, (b) by the same token the potential divergence of spurious, false positive, pose estimates, and hence their elimination as pose estimate candidates, (c) the production of finer pose estimates without excessive increase in execution time, and (d) the decoupling of the final pose estimate's error from the field's density. Selecting among all matched estimates the one with the minimum (updated) CAER allows for the system's delivery of one pose estimate response. Figure 3 and algorithm I present the proposed method of CBGL in block diagram and algorithmic forms respectively.

V. EXPERIMENTAL EVALUATION

This section serves the testing of Hypothesis H under state of the global localisation art methods and CBGL, in varying environmental conditions and sensor configurations. With regard to CBGL its three required parameters are set to $(d_l, d_{\alpha}, k) = (40, 2^5, 10)$ after preparatory tests with the dataset tested against in subsection V-A. The rationale of choosing appropriate d_l, d_{α} is depicted in figure 5, and k was

Algorithm I: CBGL

Input: $\mathcal{S}_R, M, (d_l, d_{\alpha}), k$

Output: Pose estimate of sensor measuring range scan \mathcal{S}_R

- 1: $A \leftarrow \text{calculate_area}(\text{free}(M))$
 - 2: $\mathcal{H} \leftarrow \{\emptyset\}$
 - 3: **for** $i \leftarrow 0, 1, \dots, d_l \cdot A - 1$ **do**
 - 4: $(\hat{x}, \hat{y}, \hat{\theta}) \leftarrow \text{rand}(): (x, y) \in \text{free}(M), \hat{\theta} \in [-\pi, +\pi]$
 - 5: **for** $j \leftarrow 0, 1, \dots, d_{\alpha} - 1$ **do**
 - 6: $\mathcal{H} \leftarrow \{\mathcal{H}, (\hat{x}, \hat{y}, \hat{\theta} + j \cdot 2\pi/d_{\alpha})\}$
 - 7: **end for**
 - 8: **end for**
 - 9: $\mathcal{H}_1 \leftarrow \text{bottom_k_poses}(\mathcal{S}_R, M, \mathcal{H}, k)$ (Alg. II)
 - 10: $\mathcal{H}_2 \leftarrow \{\emptyset\}$
 - 11: **for** $k \leftarrow 0, 1, \dots, |\mathcal{H}_1| - 1$ **do**
 - 12: $\hat{h}' \leftarrow \text{sm2}(\mathcal{S}_R, M, \mathcal{H}_1[k])$ (Alg. III or e.g. x1 [3])
 - 13: $\mathcal{H}_2 \leftarrow \{\mathcal{H}_2, \hat{h}'\}$
 - 14: **end for**
 - 15: **return** $\text{bottom_k_poses}(\mathcal{S}_R, M, \mathcal{H}_2, 1)$
-

Algorithm II: bottom_k_poses

Input: $\mathcal{S}_R, M, \mathcal{H}, k$

Output: \mathcal{H}_{∇}

- 1: $\Psi \leftarrow \{\emptyset\}$
 - 2: **for** $h \leftarrow 0, 1, \dots, |\mathcal{H}| - 1$ **do**
 - 3: $\mathcal{S}_V^h \leftarrow \text{scan_map}(M, \mathcal{H}[h])$
 - 4: $\psi \leftarrow 0$
 - 5: **for** $n \leftarrow 0, 1, \dots, |\mathcal{S}_R| - 1$ **do**
 - 6: $\psi \leftarrow \psi + |\mathcal{S}_R[n] - \mathcal{S}_V^h[n]|$ (Eq. (1))
 - 7: **end for**
 - 8: $\Psi \leftarrow \{\Psi, \psi\}$
 - 9: **end for**
 - 10: $[\Psi_{\uparrow}, \mathbb{I}^*] \leftarrow \text{sort}(\Psi, \text{asc})$
 - 11: $\mathcal{H}_{\nabla} \leftarrow \{\emptyset\}$
 - 12: **for** $h \leftarrow 0, 1, \dots, k - 1$ **do**
 - 13: $\mathcal{H}_{\nabla} \leftarrow \{\mathcal{H}_{\nabla}, \mathcal{H}[\mathbb{I}^*[h]]\}$
 - 14: **end for**
 - 15: **return** \mathcal{H}_{∇}
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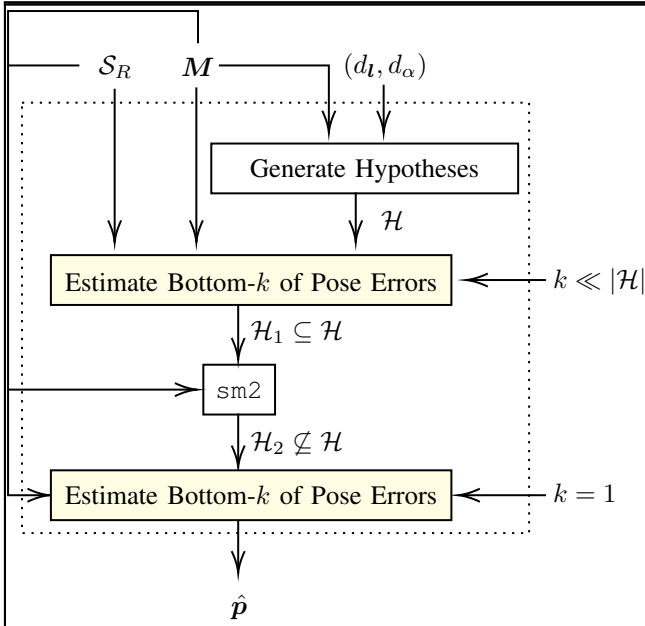


Fig. 3: CBGL in block diagram form. Given a LIDAR's 2D measurement S_R and the map M that represents the environment in which the sensor is posed, CBGL generates a set of pose hypotheses \mathcal{H} and invokes the estimation of the k hypotheses with the least pose error (fig. 4; alg. II). Then it scan-to-map-scan matches those to the measurement for finer estimation and outlier rejection (alg. III). CBGL's output pose estimate is that with the least CAER among matched estimates

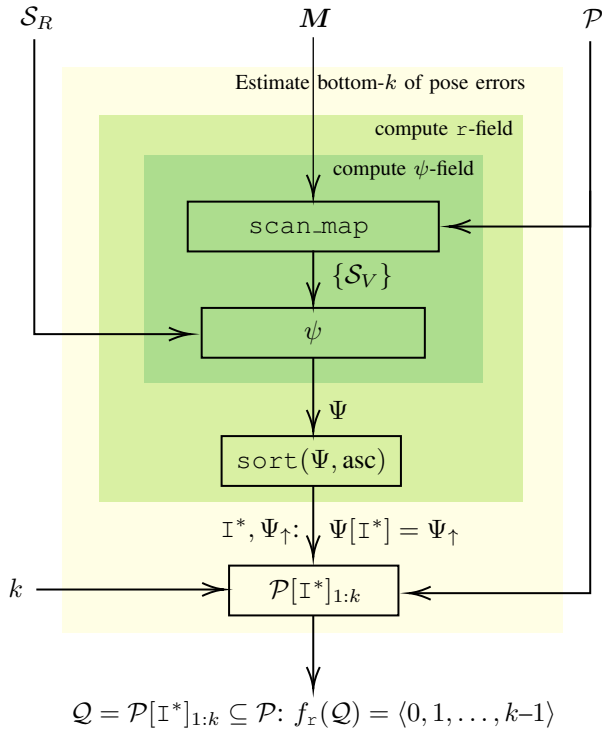


Fig. 4: CBGL's core method. Given a LIDAR's 2D measurement S_R , the map M that represents the environment in which the sensor is posed, and a set of pose hypotheses \mathcal{H} , CBGL (a) computes and ranks the CAER values between the measurement and map-scans captured from the hypotheses within the map, and (b) outputs the hypotheses with the k lowest CAER values

chosen as such in order to retain a high-enough true positive discovery rate without significant increase in execution time (due to the application of scan-to-map-scan matching on k pose estimates).

A. Experiments in real conditions

The first type of tests are conducted with the use of a Hokuyo UTM-30LX sensor, whose angular range is $\lambda = 3\pi/2$ rad and maximum range $r_{\max} = 30.0$ m, in the Electrical and Computer Engineering Department's Laboratory of Computer Systems Architecture (CSAL), Aristotle University of Thessaloniki, Greece, a map of which is depicted in figure 6. The sensor was mounted on a Robotnik RB1 robot, which was teleoperated to move within the environment while range scans were being captured. This resulted in $N_S = 6669$ range scans, whose number of rays are downsampled by a factor of four before being inputted to CBGL and ALS [6], an algorithm which implements Free-Space Features [7]. CBGL's internal scan-to-map-scan matching method is chosen to be PLICP [8] due to its low execution time and the scans' non-panoramic field of view. Other global localisation methods ?? were not to tested for this type of experiment due to their infeasible execution time with respect to the range dataset's volume. The top of figure 7 depicts the proportion of output pose estimates from each method whose position and orientation error is lower than varying values of outlier thresholds δ_l , δ_θ ; at the bottom they are depicted exclusively with regard to CBGL's output and its internal pose sets. The mean and standard deviation of the two methods' execution times are $(\mu_t^{\text{ALS}}, \sigma_t^{\text{ALS}}) = (6.15, 5.32)$ sec, and $(\mu_t^{\text{CBGL}}, \sigma_t^{\text{CBGL}}) = (1.61, 0.06)$ sec. From the experimental evidence it is clear that (a) hypothesis H is observed to be true 991 times out of a thousand for an outliers' locational threshold $\delta_l = 0.5$ m when an angular threshold is δ_θ is not considered, and (b) CBGL outperforms ALS in terms of number of pose estimates within all locational and angular thresholds and in terms of execution time.

B. Simulations against sources of uncertainty

The second type of tests concerns the main limiting factors of global localisation methods, i.e. uncertainty—arising e.g. from spurious measurements, repeatability of surroundings, missing range information, or their combinations. For this reason the experimental procedure of [9] is repeated here for the two methods tested therein, PGL-FMIC and PGL-PLICP, and CBGL, ALS, MCL [10], and GMCL [11]. Specifically these methods are tested against the two most challenging environments, i.e. WAREHOUSE and WILLOWGARAGE, in which a panoramic range sensor is placed at 16 different poses for $N = 100$ independent attempts at global localisation per tested method. The tests are conducted with the use of a sensor whose number of rays $N_s = 360$ and maximum range $r_{\max} = 10.0$ m. CBGL's internal scan-to-map-scan matching method is chosen to be $\times 1$ [3] exactly due to the periodicity of the range signal, $\times 1$'s improved results over scan-to-map-scan matching state of the art

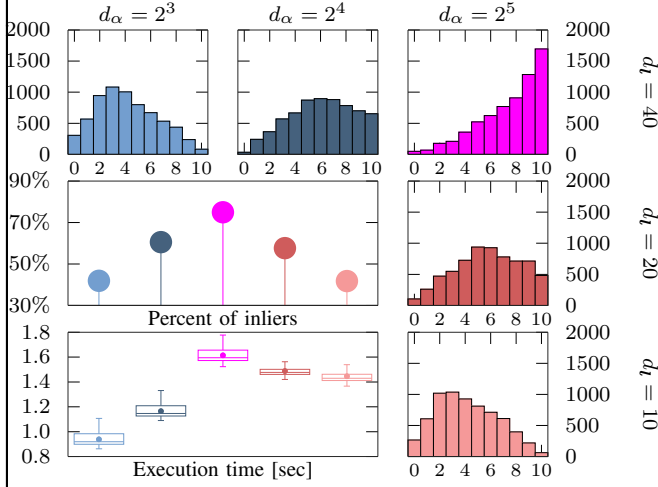


Fig. 5: Top row and right column: histograms of the number of times when exactly $n \in [0, k] = [0, 10]$ pose estimates belonging to set \mathcal{H}_1 exhibited pose errors lower than $\delta = (\delta_l^2 + \delta_\theta^2)^{1/2} = (0.3^2 + 0.4^2)^{1/2} = 0.5 \text{ (m}^2 + \text{rad}^2)^{1/2}$. For densities $(d_l, d_\alpha) = (40, 2^5)$ this number is strictly increasing with n . Middle block: percent proportion of pose estimates whose pose error is lower than δ for varying field densities. Bottom block: the corresponding execution times

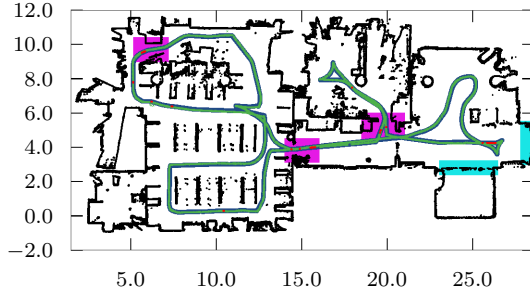


Fig. 6: The map of the CSAL environment (black), the trajectory of the sensor (blue), CBGL's estimated positions of the sensor (green), sensor poses for which CBGL estimated positions with error larger than $\delta_l = 0.5 \text{ m}$ (red), sources of great range noise (cyan), and doors (purple). Estimation is performed for each sensor pose independently of previous estimates or measurements

methods, and its ability in matching scans captured from greater initial locational distances than ICP alternatives. The latter translates to the need for smaller initial hypothesis sets: for each environment the locational density is set to $3\text{e}+04$ divided by the free space area of each environment.

The geometry of environment WAREHOUSE is such that the maximum range of the sensor causes (disorderly) lack of sampling of the sensor's surrounding environment, which may therefore produce spurious measurements and increase ambiguities. In WILLOWGARAGE on the other hand, almost all sensor placements result in complete sampling of its surroundings, but the sensor is purposefully posed in such conditions as to challenge the localisation methods' ability to perform fine distinctions between similar

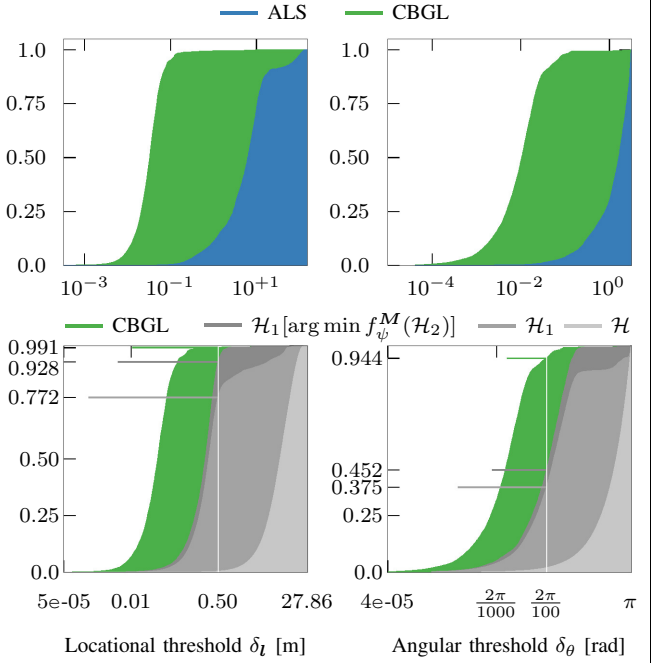


Fig. 7: Proportions of pose estimates whose position and orientation error is lower than corresponding thresholds δ_l and δ_θ . Top: ALS vs CBGL. Bottom: CBGL and internal pose estimate sets; the improvement in position and orientation induced by scan-to-map-scan matching is captured by the difference between the output (i.e. $\mathcal{H}_2[\arg \min f_\psi^M(\mathcal{H}_2)]$) and $\mathcal{H}_1[\arg \min f_\psi^M(\mathcal{H}_2)]$. Approximately 99% of CBGL's pose estimates exhibit position errors equal to or lower than $\delta_l = 0.5 \text{ m}$

surroundings. Figure 8 depicts the percentage of cases where the output pose's position error is lower than $\delta_l = 1.0 \text{ m}$, and figure 9 depicts the distribution of execution times per tested environment and algorithm. CBGL's mean execution time in environment WAREHOUSE is $\mu_t^W = 7.98 \text{ sec}$ and in WILLOWGARAGE $\mu_t^G = 3.59 \text{ sec}$. Although the cardinality of set \mathcal{H} is equal for both environments CBGL's execution times are reversed due to $\times 1$'s increased execution time when dealing with scans with missing range information. Notwithstanding, CBGL manages to overall exhibit the highest inlier rate for each pose in WAREHOUSE, and consistently high inlier rates in WILLOWGARAGE.

C. Simulations against environment disparity and choice of scan-to-map-scan matching methods

VI. CHARACTERISATION & LIMITATIONS

sources of great range error: causing corrupted CAERs: trajectory and map figure, purple and cyan regions

VII. CONCLUSION

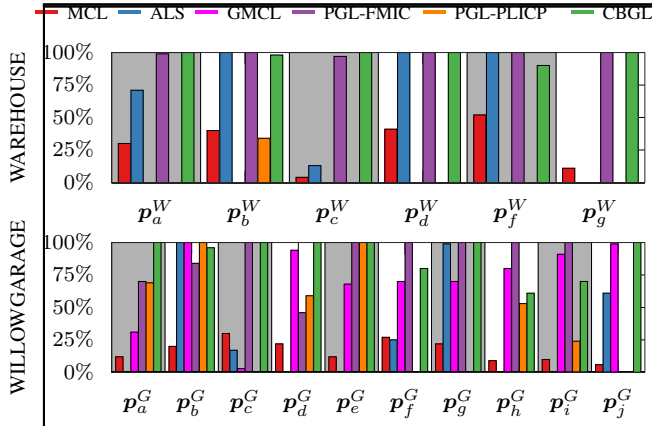


Fig. 8: Percent proportions of pose outputs whose position error is lower than $\delta_l = 1.0$ per tested environment, pose, and method. Overall CBGL features the highest number of inlier poses

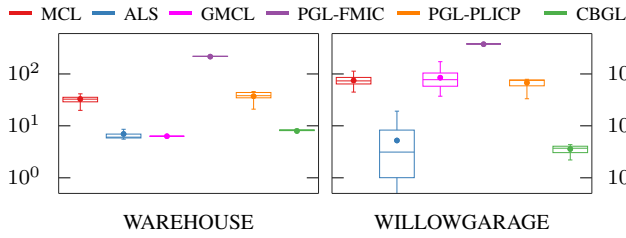


Fig. 9: Distribution of execution times per tested environment and algorithm for $N_s = 360$ rays. CBGL's execution time is at least eighteen times lower than other Monte Carlo approaches in WILLOWGARAGE and four times lower in WARHOUSE

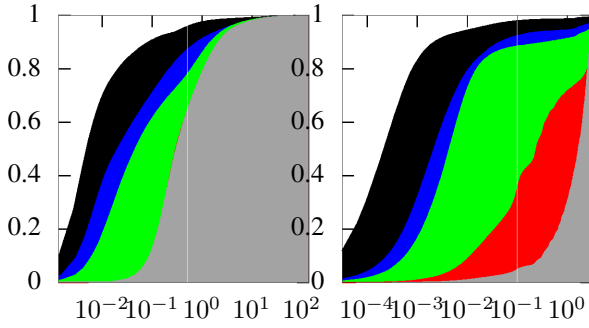


Fig. 10:

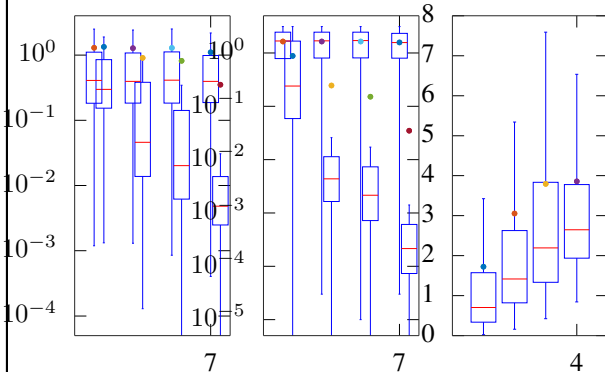


Fig. 11:

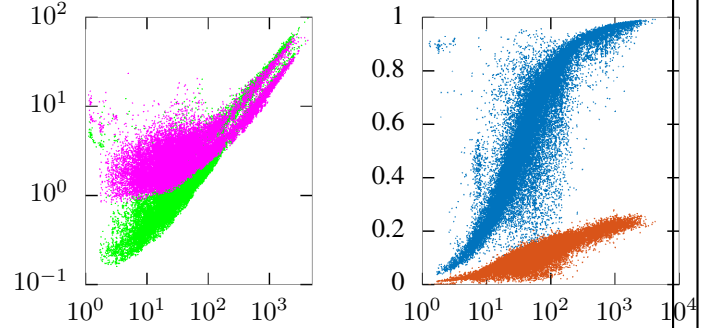


Fig. 12:

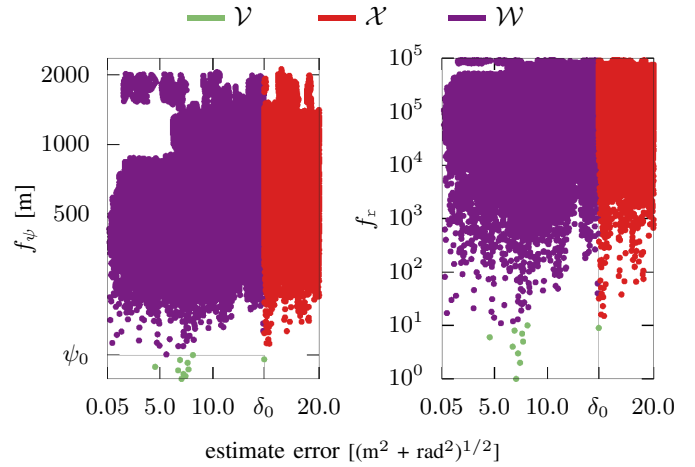


Fig. 13: Contrary to fig. 2: the ψ -field (left) and τ -field (right) of a configuration where Observation O cannot be made: set \mathcal{V} is empty of admissible pose estimates for $\delta < 4.5 \text{ (m}^2 + \text{rad}^2)^{1/2}$. The effect is in fact produced due to the repetition of the immediate environment of the sensor more than once in the given map and its apparent dissimilarity to its corresponding portion of the map

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